

# A Novel $\mu \rightarrow eee$ Experiment



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# Shifting Stones in the Sierra Nevada



# Shifting Stones in the Sierra Nevada

A photograph of a dry, cracked earth surface in a desert landscape, with mountains in the background.

**Shifts were never directly seen  
(like charged lepton flavor violation)**

# History

G.Feinberg, P.Kabir, S.Weinberg, PRL 3 527 (1959)

„Absence of:

- $\text{Br}(\mu \rightarrow e \gamma)$
- $\text{Br}(\mu \rightarrow eee)$
- $\text{Br}(\mu N \rightarrow e N)$

does not constitute a paradox there being no compelling reason why muons should transform into electrons, but it seems a **mystery** that processes which are allowed energetically and in every other known respect do not occur...“

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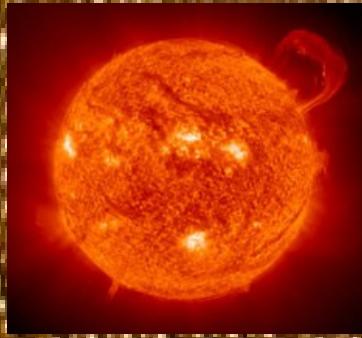
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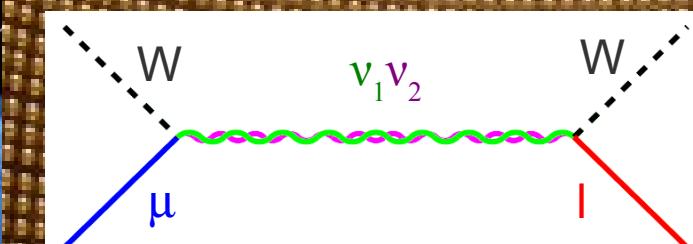
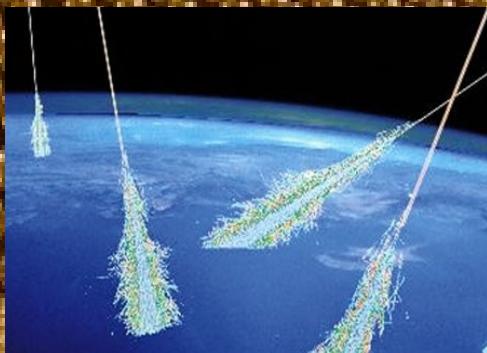
→ **Introduction of lepton flavor quantum number**

Standard Model:  $\mu \rightarrow e \bar{\nu}_e \nu_\mu$

# Discovery of Neutrino Oscillations

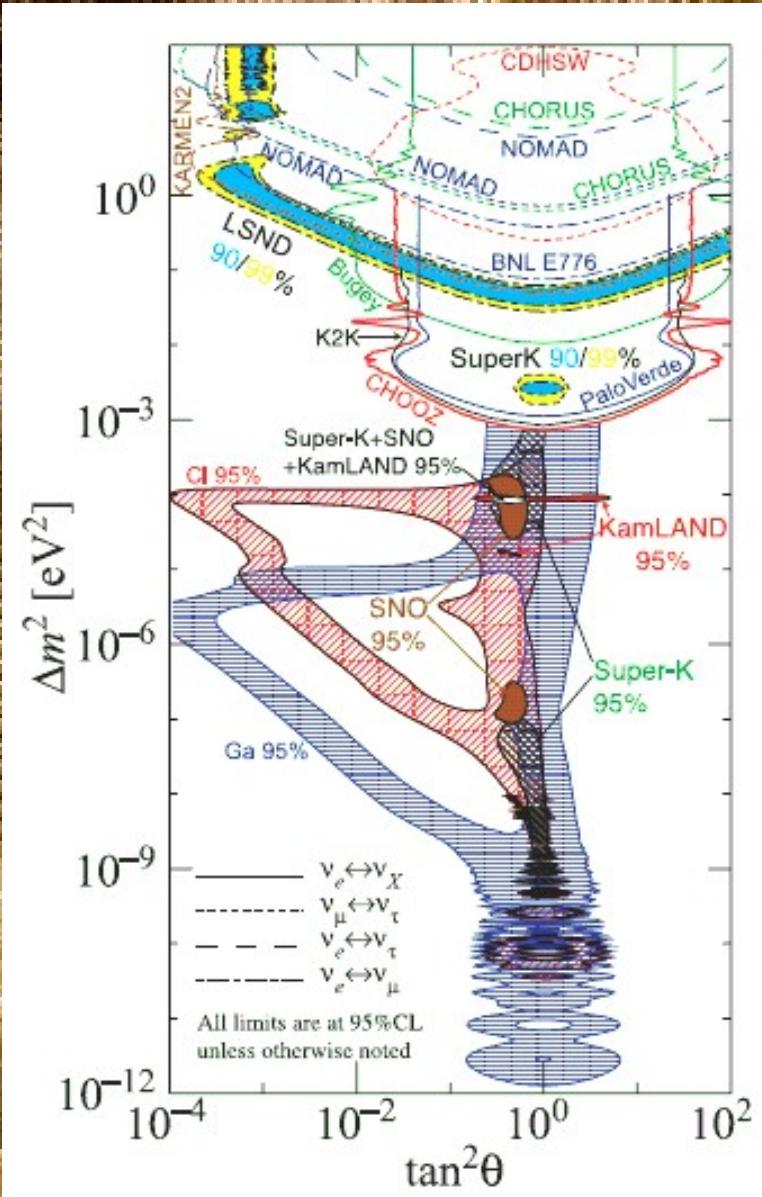


- Neutrino Oscillations:
  - solar neutrinos
  - reactor neutrinos
  - atmospheric neutrinos
  - neutrino beams



$$P(\nu_\alpha \rightarrow \nu_\beta) = \sin^2(2\theta) \sin^2(1.2 \Delta m_{\alpha\beta}^2 \frac{L}{E})$$

“Feinberg Kabir and Weinberg were wrong!”



# Overview

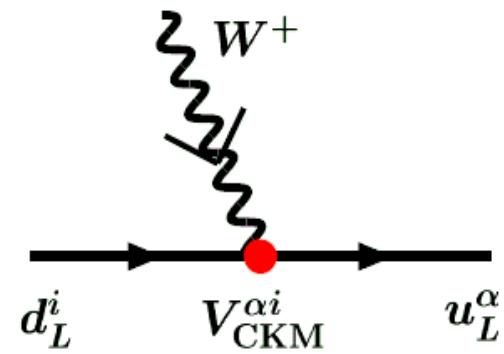
- **Introduction to Lepton Flavor Violation**
- **Motivation to Search for  $\mu \rightarrow eee$**
- **Backgrounds and Past Experiments**
- **(Novel) Detector Concept and Design**
- **Simulation Studies**
- **Summary**

# Fermion Mixing

Quarks

Cabibbo Kobayashi Maskawa (CKM)

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$



# Fermion Mixing

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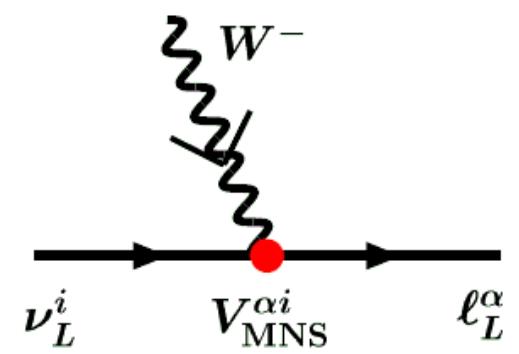
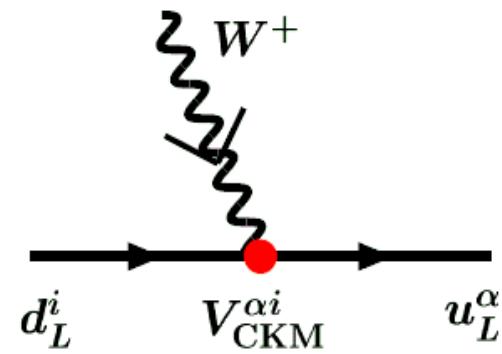
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Leptons

Pontecorvo Maki Nakagawa Sakata (PMNS)

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} V_{e1} & V_{e2} & V_{e3} \\ V_{\mu 1} & V_{\mu 2} & V_{\mu 3} \\ V_{\tau 1} & V_{\tau 2} & V_{\tau 3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$



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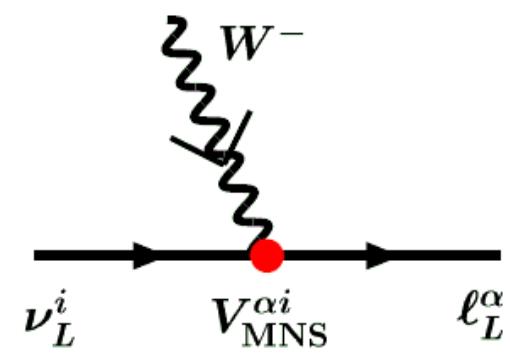
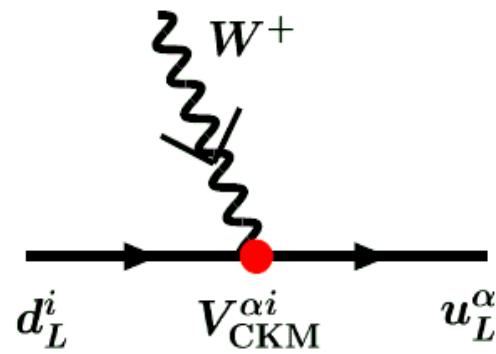
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- **W bosons smell different flavors!**
- other gauge bosons ( $\gamma, Z, g$ ) do not ( $\rightarrow$  no FCNC)

# Fermion Mixing

Quarks

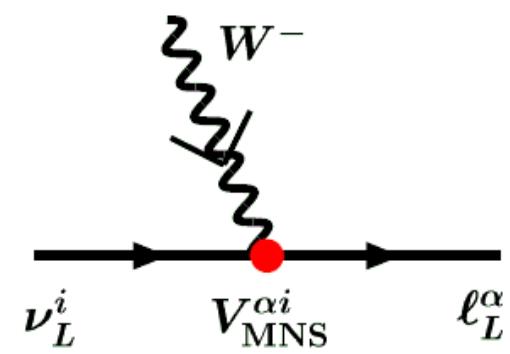
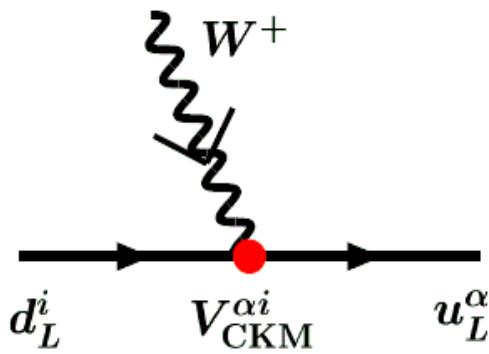
Cabibbo Kobayashi Maskawa (CKM)

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} 0.974 & 0.225 & 0.003 \\ 0.225 & 0.973 & 0.041 \\ 0.009 & 0.040 & 0.999 \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

Leptons

Pontecorvo Maki Nakagawa Sakata (PMNS)

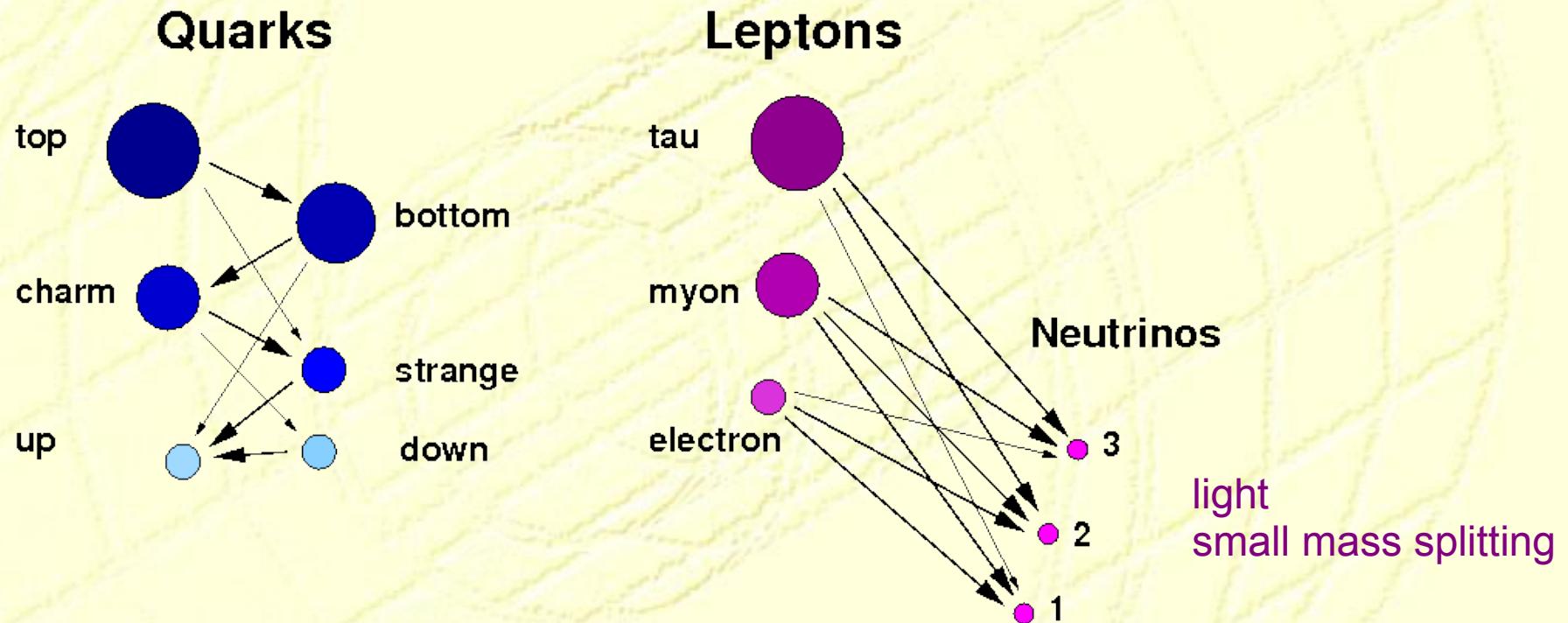
$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} \approx \begin{pmatrix} 0.816 & 0.577 & < 0.2 \\ 0.408 & 0.577 & 0.707 \\ 0.408 & 0.577 & 0.707 \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$



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# Family Number Violation

- Flavor Changing neutral currents are forbidden!
- Lepton Flavor Number in Charged Currents is an “adhoc” concept



quark flavor not conserved  
(family number changes)

lepton flavor not conserved  
but difficult to observe!

(concept of families right?)

# Lepton Mixing, LFV and FCNC

## $U$ = Neutrino Mixing Matrix

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} u_{e1} & u_{e2} & u_{e3} \\ u_{\mu 1} & u_{\mu 2} & u_{\mu 3} \\ u_{\tau 1} & u_{\tau 2} & u_{\tau 3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

weak eigenstates mass

## $W$ = Ch. Lepton Mixing Matrix

$$\begin{pmatrix} e \\ \mu \\ \tau \end{pmatrix} = \begin{pmatrix} w_{e1} & w_{e2} & w_{e3} \\ w_{\mu 1} & w_{\mu 2} & w_{\mu 3} \\ w_{\tau 1} & w_{\tau 2} & w_{\tau 3} \end{pmatrix} \begin{pmatrix} l_1 \\ l_2 \\ l_3 \end{pmatrix}$$

weak eigenstates mass

- **Charged Current:**

PMNS matrix:  $V_{ki} = \sum_{\alpha=1}^3 W_{\alpha k}^{l^*} U_{\alpha i}^\nu$  only product measurable

→ product of lepton and neutrino mixing matrices (→ **flavor changing**)

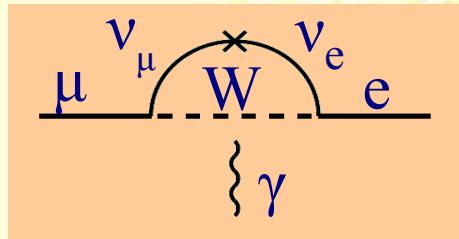
- **Neutral Current:**

unit matrix:  $1 = \sum_{\alpha=1}^3 U_{\alpha k}^{\nu^*} U_{\alpha i}^\nu = \sum_{\alpha=1}^3 W_{\alpha k}^{l^*} W_{\alpha i}^l$

→ unitary lepton and neutrino mixing matrices (→ **flavor conserving**)

# Lepton Flavor Violation in the SM

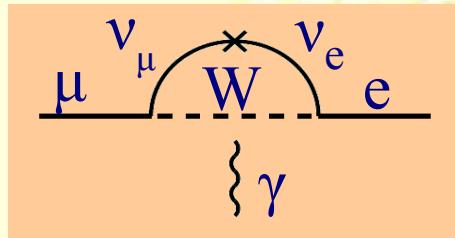
Higher Order!



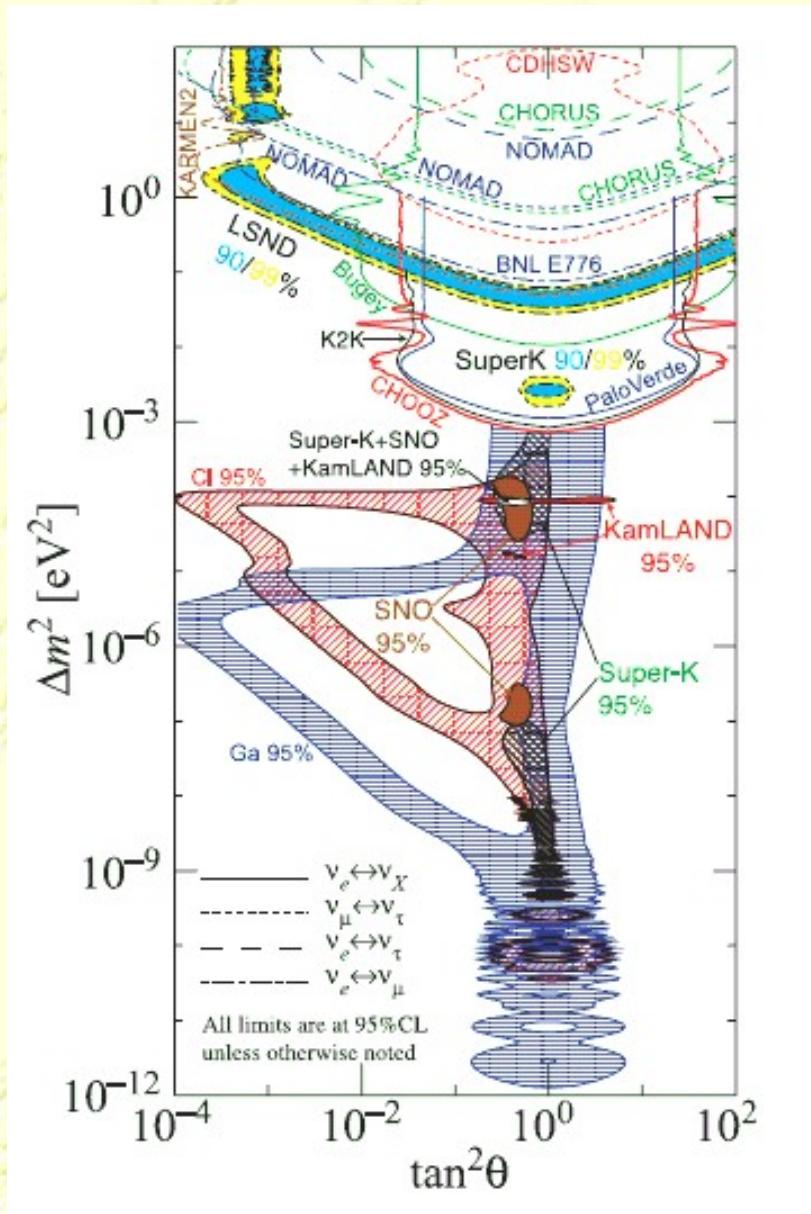
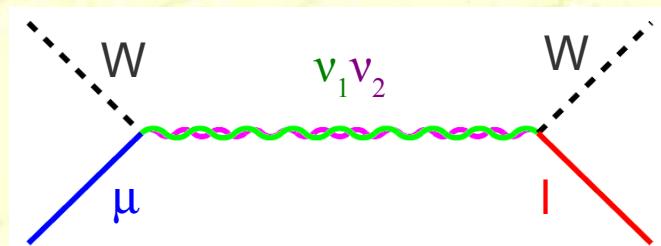
$$\mu \rightarrow e \gamma$$

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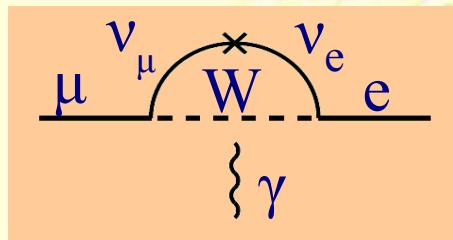


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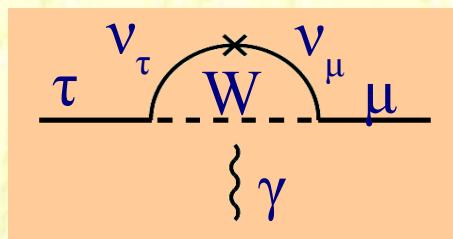


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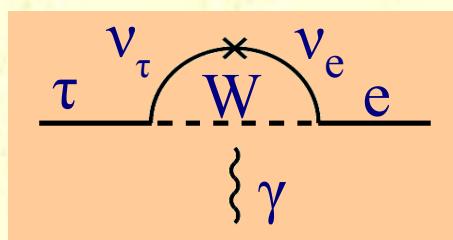
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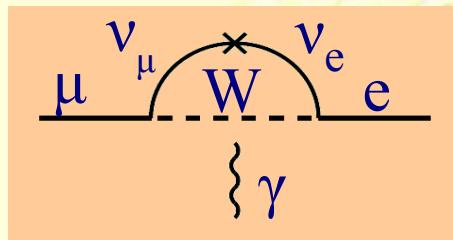
$$\tau \rightarrow \mu \gamma$$



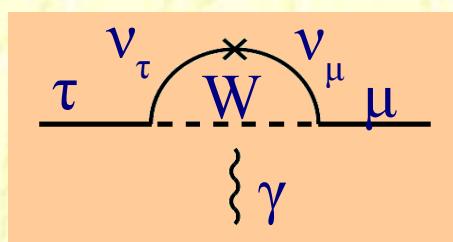
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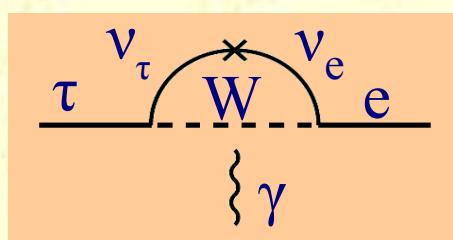
Higher Order!



$$\mu \rightarrow e \gamma$$



$$\tau \rightarrow \mu \gamma$$



$$\tau \rightarrow e \gamma$$

LFV is generated from lepton mixing:

$$BR(l_j \rightarrow l_k \gamma) \propto \left( \sum_i V_{ij} V_{jk}^* \frac{m_{\nu_i}^2}{M_W^2} \right)^2 \sim \left( \frac{\Delta m_{\nu_{jk}}^2}{M_W^2} \right)^2$$

GIM – like suppression:

$$\sim 10^{-50}$$

→ unobservable

→ high sensitivity to new physics!!!

c.t. quark mixing:

→ FCNC in SM  $\sim 10^{-10}$

$$\left( \frac{\Delta m_{c-u}^2}{M_W^2} \right)^2 \sim 10^{-7}$$

# Searches of Lepton $\pm$ Flavor Violation

## Lepton Decays:

- $\mu \rightarrow e \gamma$
- $\mu \rightarrow eee$
- $\tau \rightarrow e(\mu) \gamma$
- $\tau \rightarrow lll$  ( $l=e,\mu$ )
- $\tau \rightarrow lh$

## Meson Decays:

- $\Phi, K \rightarrow ll'$
- $D, J/\psi \rightarrow ll'$
- $B, Y \rightarrow ll'$

## Conversion ( $\mu$ -Capture):

- $\mu N \rightarrow e N$

**LFV**

## Fixed Target Experiments:

- $\mu N \rightarrow \tau N$  proposed
- $e N \rightarrow \mu(\tau) N$  proposed

## Collider Experiments:

- $e p \rightarrow \mu(\tau) X$  HERA
- $Z' \rightarrow ll'$  LHC
- $\chi^{0,\pm} \rightarrow ll' X$

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**LFV**

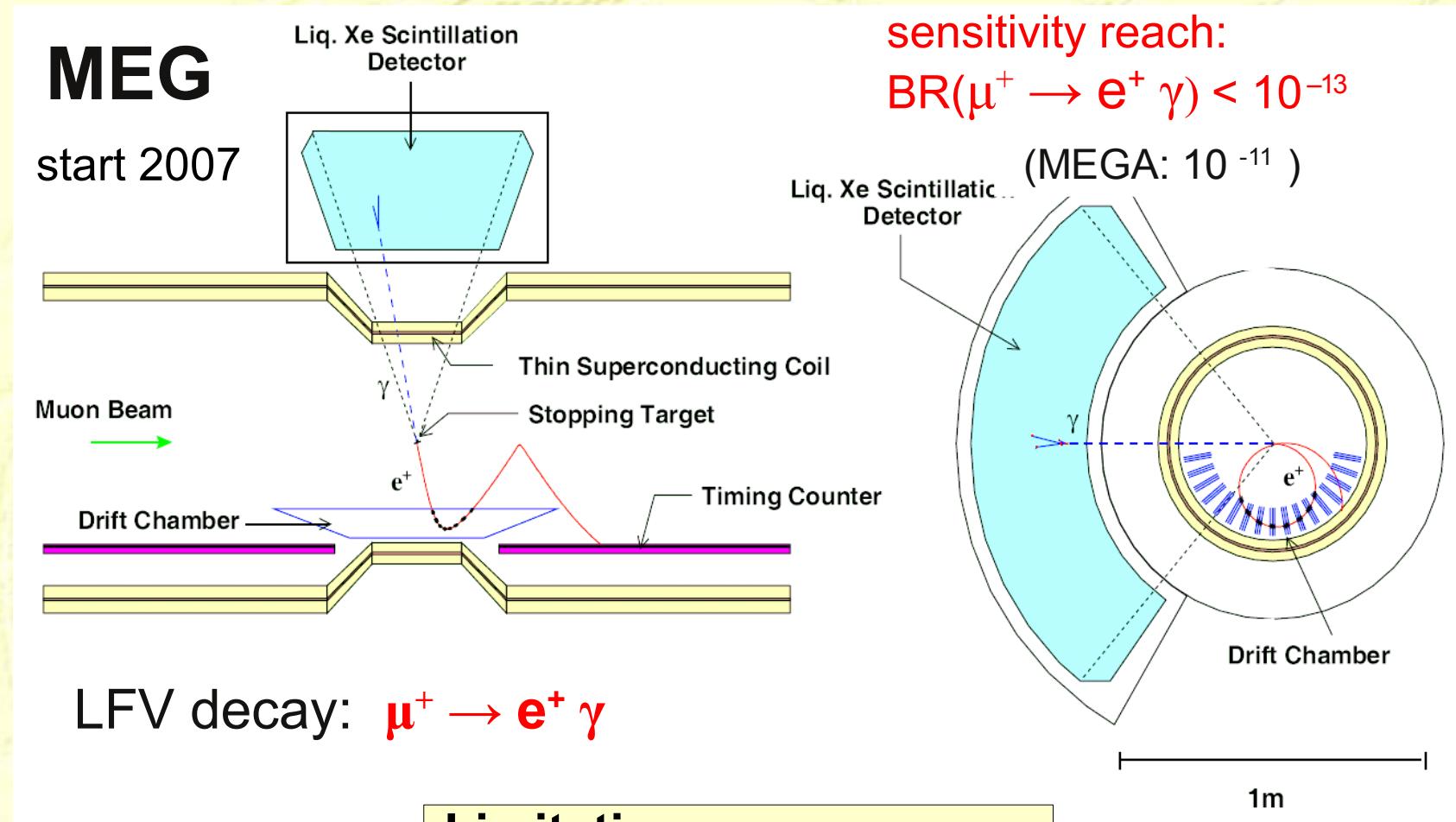
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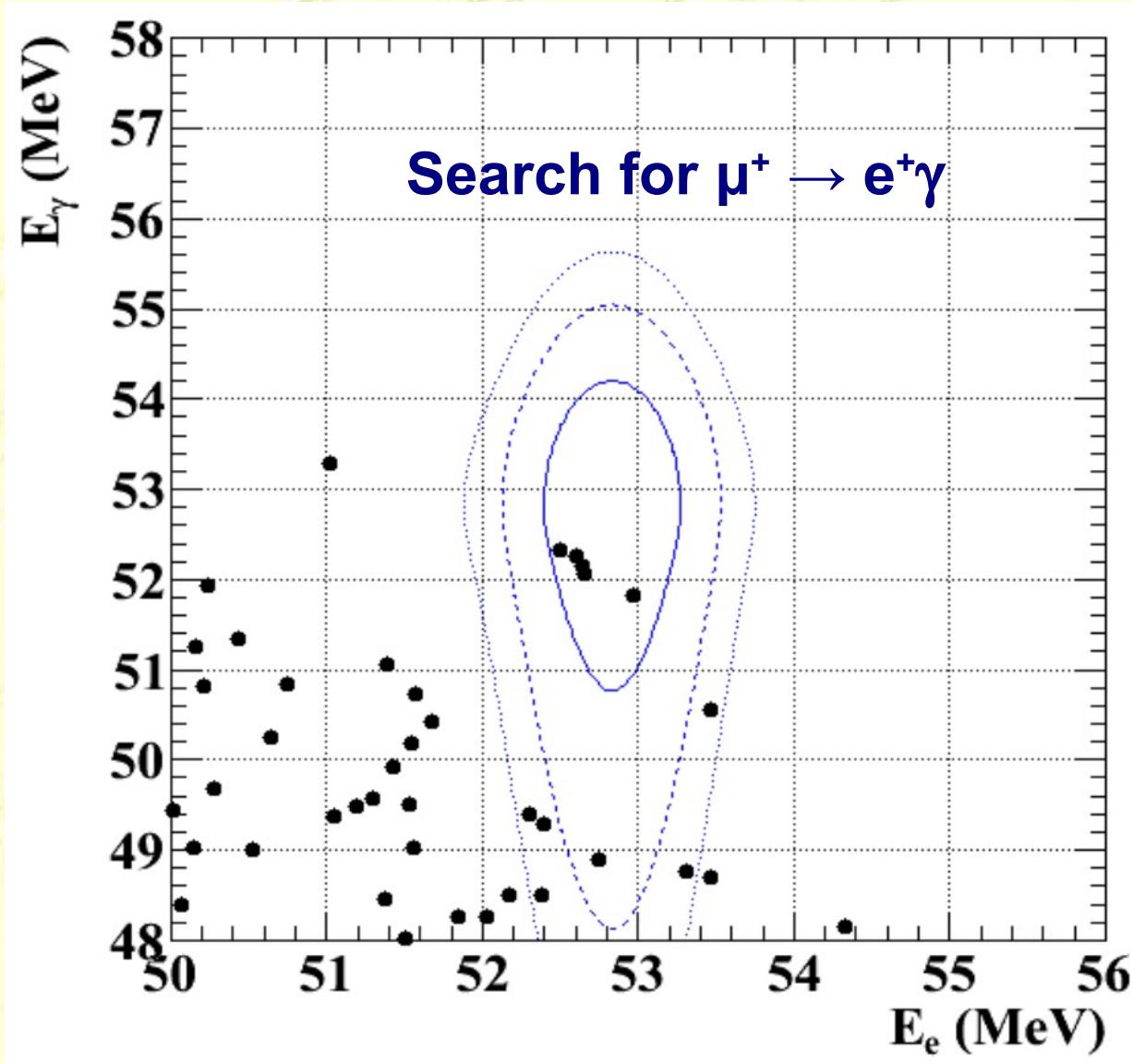
# The MEG Experiment



## Limitation:

- accidental background
  - better space resolution
  - improve tracking

# MEG Preliminary



MEG, ICHEP 2010

first indication of  
lepton flavor violation  
in muon decays?

# Experimental LFV Results

## Purely Leptonic LFV:

- $\text{Br}(\mu \rightarrow e \gamma) < 10^{-11}$  [MEGA]  
→  $10^{-13}$  MEG
- $\text{Br}(\tau \rightarrow \mu(e) \gamma) < \sim 4 \cdot 10^{-8}$  (B-factories)
- $\text{Br}(\mu \rightarrow eee) < 10^{-12}$  [SINDRUM]  
→  $10^{-16}$  this talk
- $\text{Br}(Z \rightarrow e\mu) < 10^{-6}$  [LEP]

## Semihadronic LFV:

- $\text{Br}(K \rightarrow \pi \mu e) < \approx 10^{-11}$
- $\text{Br}(\mu_{\text{capt}} N \rightarrow e N) < \sim 10^{-12}$  [SINDRUM2]  
→  $10^{-17}$  Mu2e, Prism
- $\mu N \rightarrow e N'$  or  $e N \rightarrow \mu(\tau) N'$  (DIS HERA):

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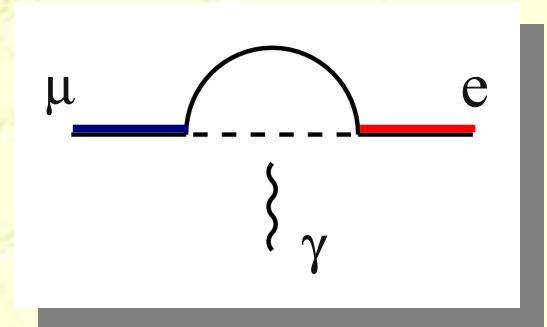
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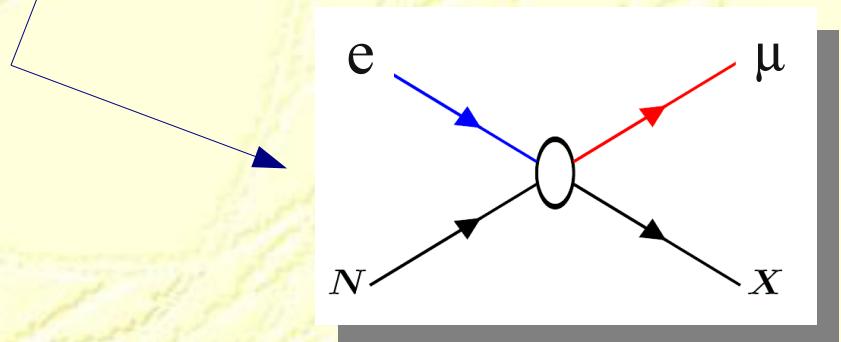
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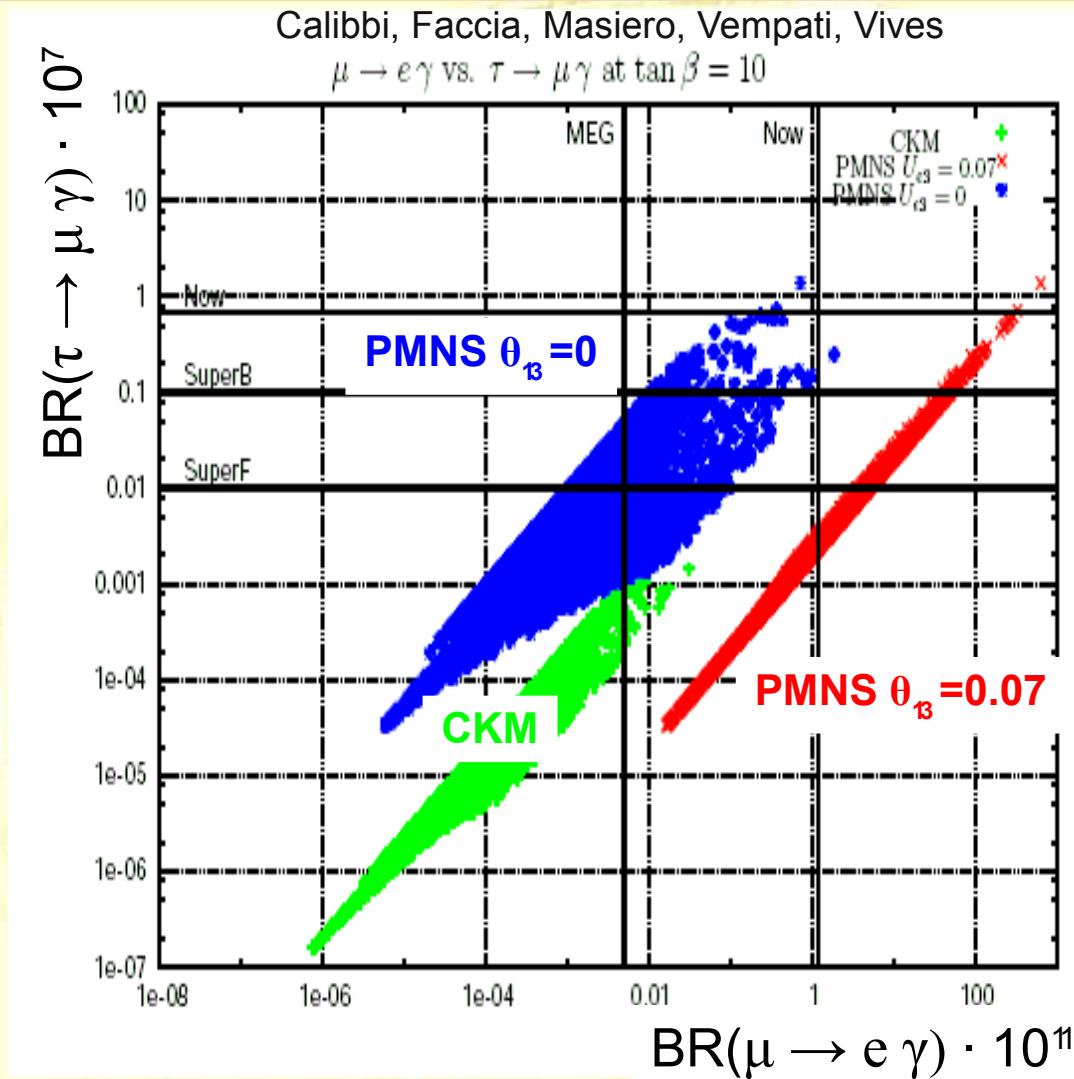


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# LFV in SUSY SO(10) GUT



points = SUSY LHC parameters

Yukawa couplings to neutrinos

$$h_\nu = h_u \quad (\text{CKM-case})$$

$$h_\nu = U_{PMNS} h_u^{diag} \quad (\text{PMNS-case})$$

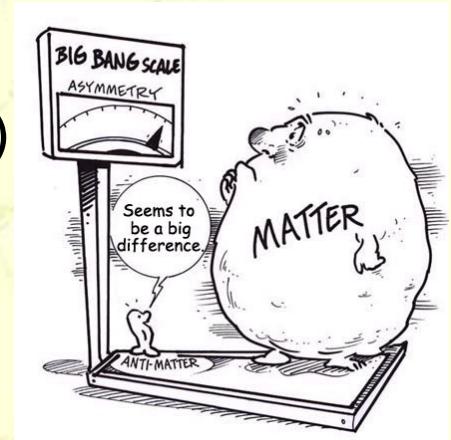
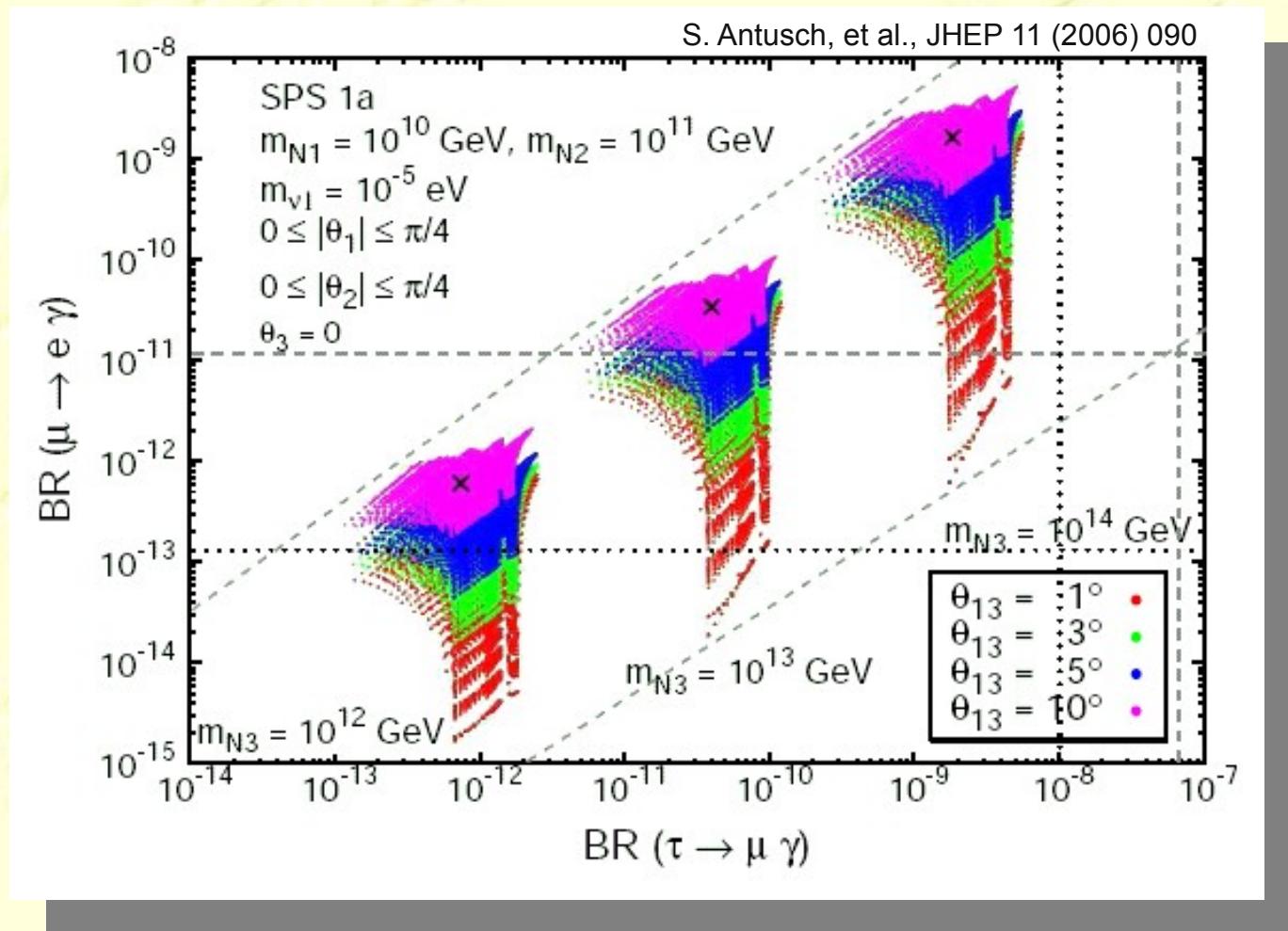
→ quasi model-dependent predictions: (G. Isidori et al.)

CKM:  $\text{BR}(\tau \rightarrow \mu\gamma) : \text{BR}(\tau \rightarrow e\gamma) : \text{BR}(\mu \rightarrow e\gamma) : \sim 10^4 : 500 : 1$

PMNS:  $\text{BR}(\tau \rightarrow \mu\gamma) : \text{BR}(\tau \rightarrow e\gamma) : \text{BR}(\mu \rightarrow e\gamma) : \sim 500-10 : 1 : 1$

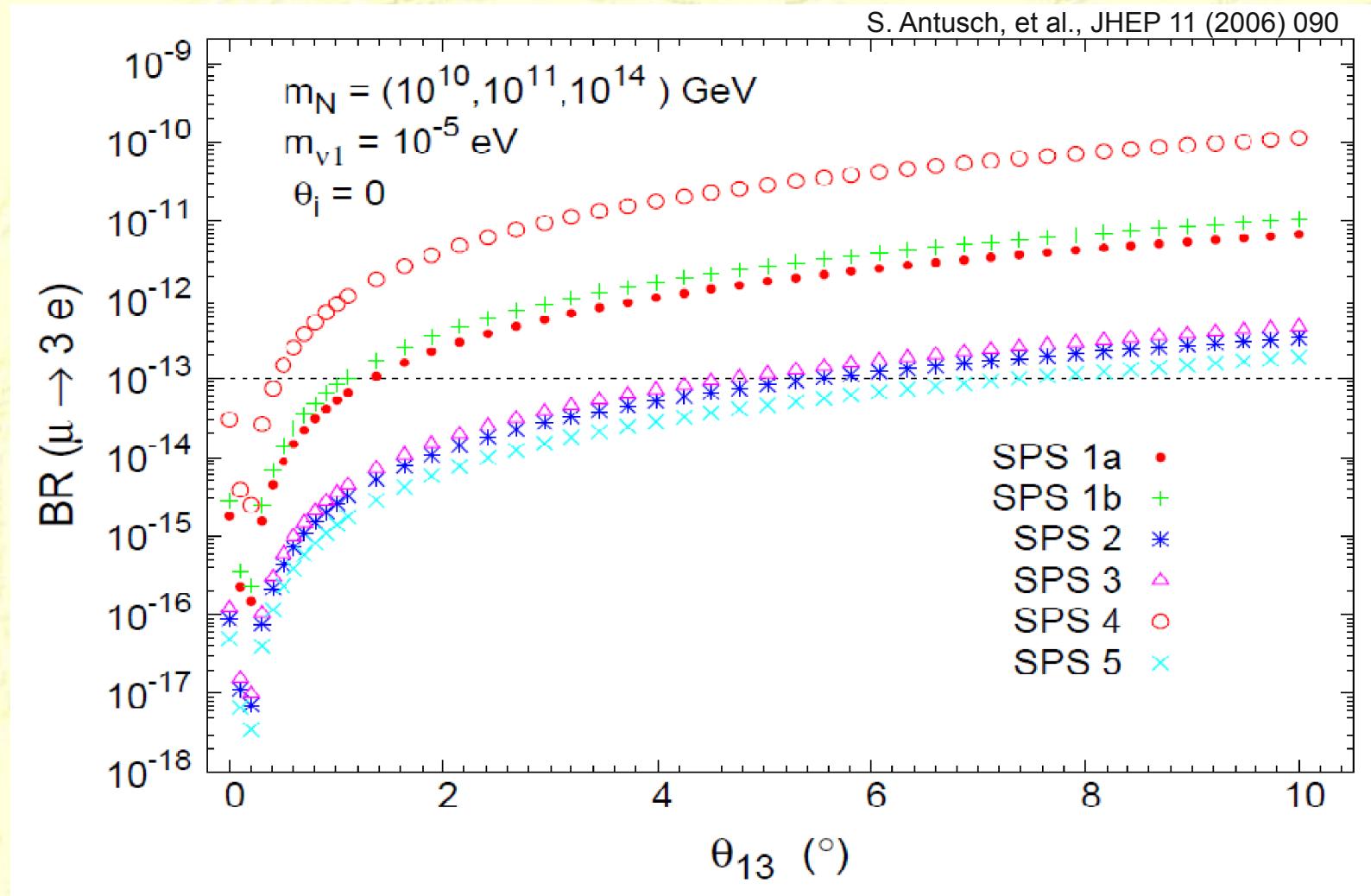
# cMSSM Seesaw with Leptogenesis

- SUSY SPS 1a
- require successfull BAU (baryon asymmetry in universe)



→ sensitivity to heavy Majorana Neutrino Masses

# cMSSM Seesaw with Leptogenesis



$$\sin^2 \Theta_\beta < 0.057 \text{ (PDG)}$$

# Motivation to Search for $\mu^+ \rightarrow e^+e^+e^-$

# Effective Model for $\mu^+ \rightarrow e^+e^+e^-$

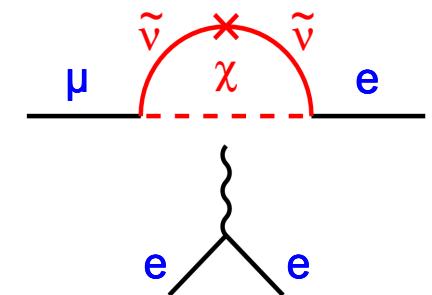
Effective charged LFV Lagrangian (Y. Kuno and Y Okada):

Tensor terms (dipole)

$$L_{\mu \rightarrow eee} = \frac{4G_F}{2} [m_\mu A_R \bar{\mu}_R \sigma^{\mu\nu} e_L F_{\mu\nu} + m_\mu A_L \bar{\mu}_L \sigma^{\mu\nu} e_R F_{\mu\nu}]$$

e.g. Supersymmetry

dipole coupling



# Effective Model for $\mu^+ \rightarrow e^+e^+e^-$

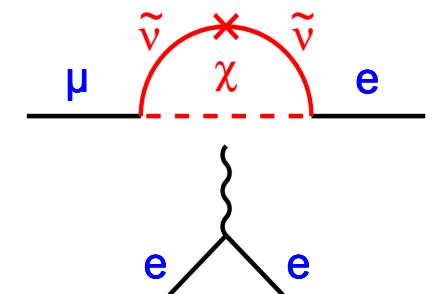
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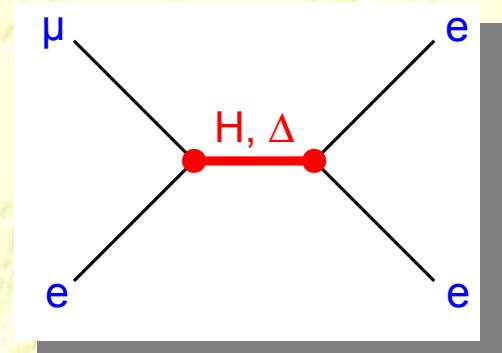


Four-fermion terms

$$\begin{aligned} &+ g_1 (\bar{\mu}_R e_L) (\bar{e}_R e_L) + g_2 (\bar{\mu}_L e_R) (\bar{e}_L e_R) && \text{(scalar)} \\ &+ g_3 (\bar{\mu}_R \gamma^\mu e_R) (\bar{e}_R \gamma_\mu e_R) + g_4 (\bar{\mu}_L \gamma^\mu e_L) (\bar{e}_L \gamma_\mu e_L) && \text{(vector)} \\ &+ g_5 (\bar{\mu}_R \gamma^\mu e_R) (\bar{e}_L \gamma_\mu e_L) + g_6 (\bar{\mu}_L \gamma^\mu e_L) (\bar{e}_R \gamma_\mu e_R) + H.c. \end{aligned}$$

e.g. Higgs, Z', Doubly Charged Higgs

tree diagram

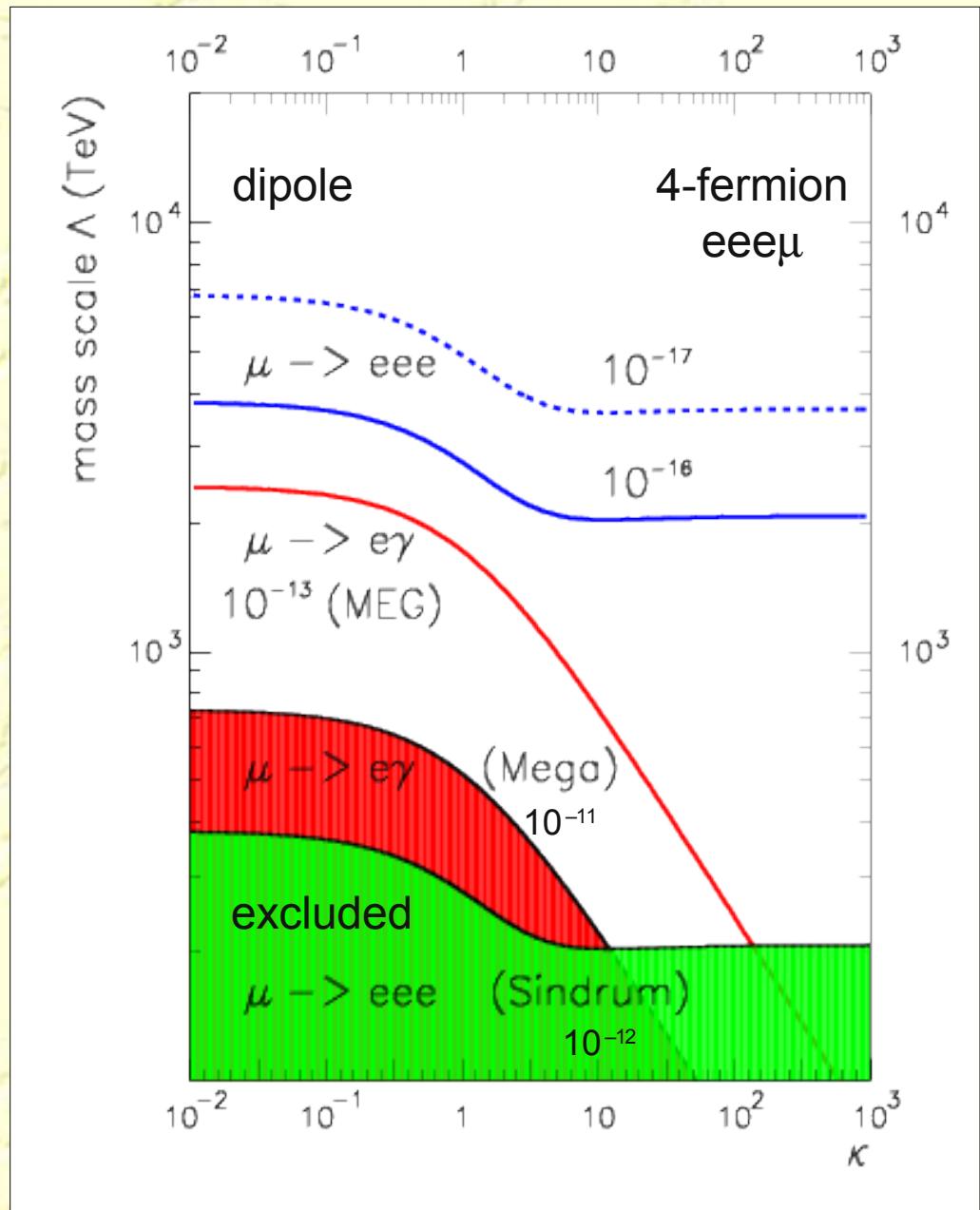


# Testing new Mass Scales

Effective cLFV Lagrangian:

$$L = \frac{m_\mu}{\Lambda^2 (1+\kappa)} H^{dipole} + \frac{\kappa}{\Lambda^2 (1+\kappa)} J_\nu^{e\mu} J^{\nu, ee}$$

“André de Gouvêa”  
plot for  $\mu eee$



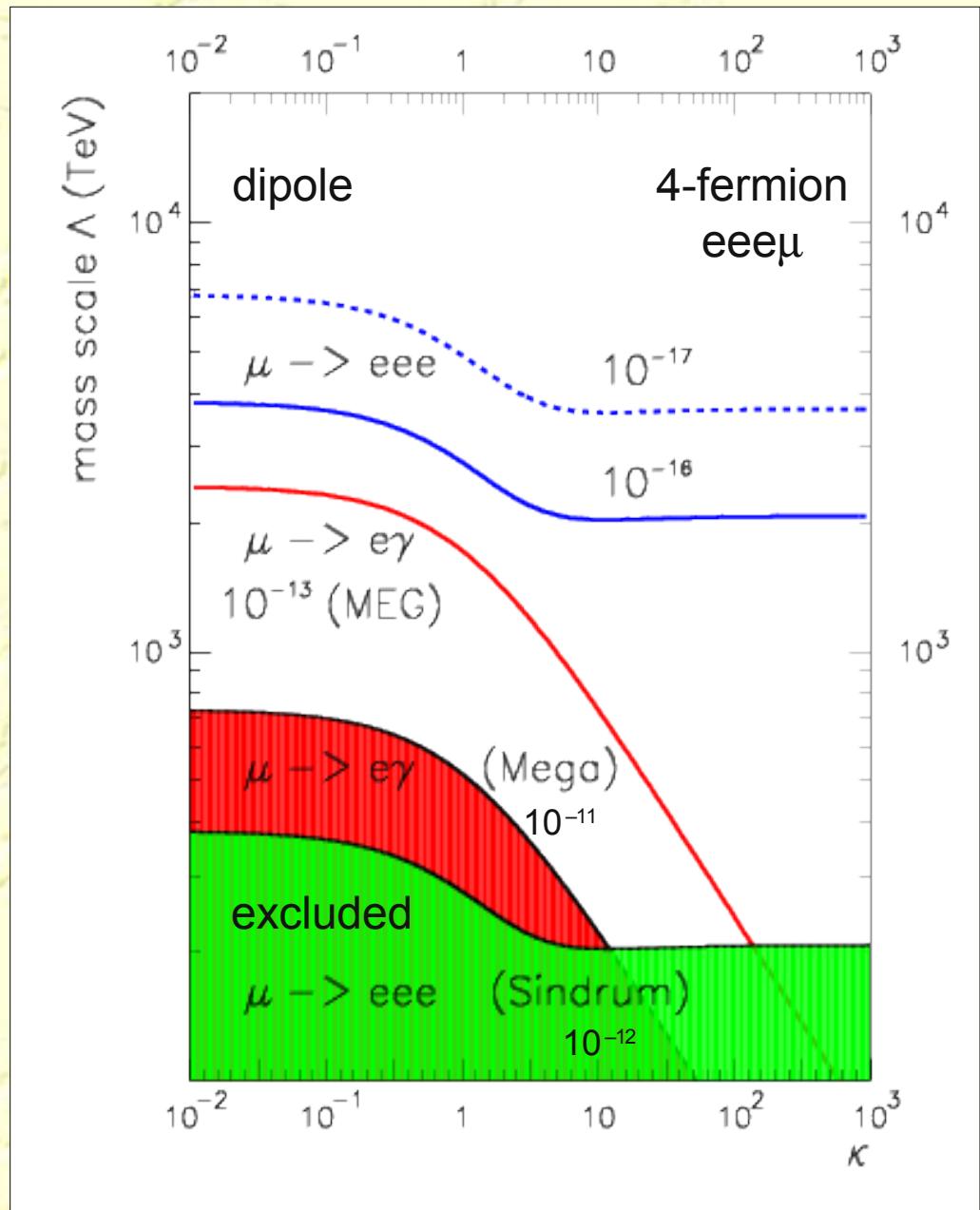
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- Almost factor 2 higher mass reach beyond MEG for LFV dipole couplings ( $\Lambda = 4 \cdot 10^3$  TeV)

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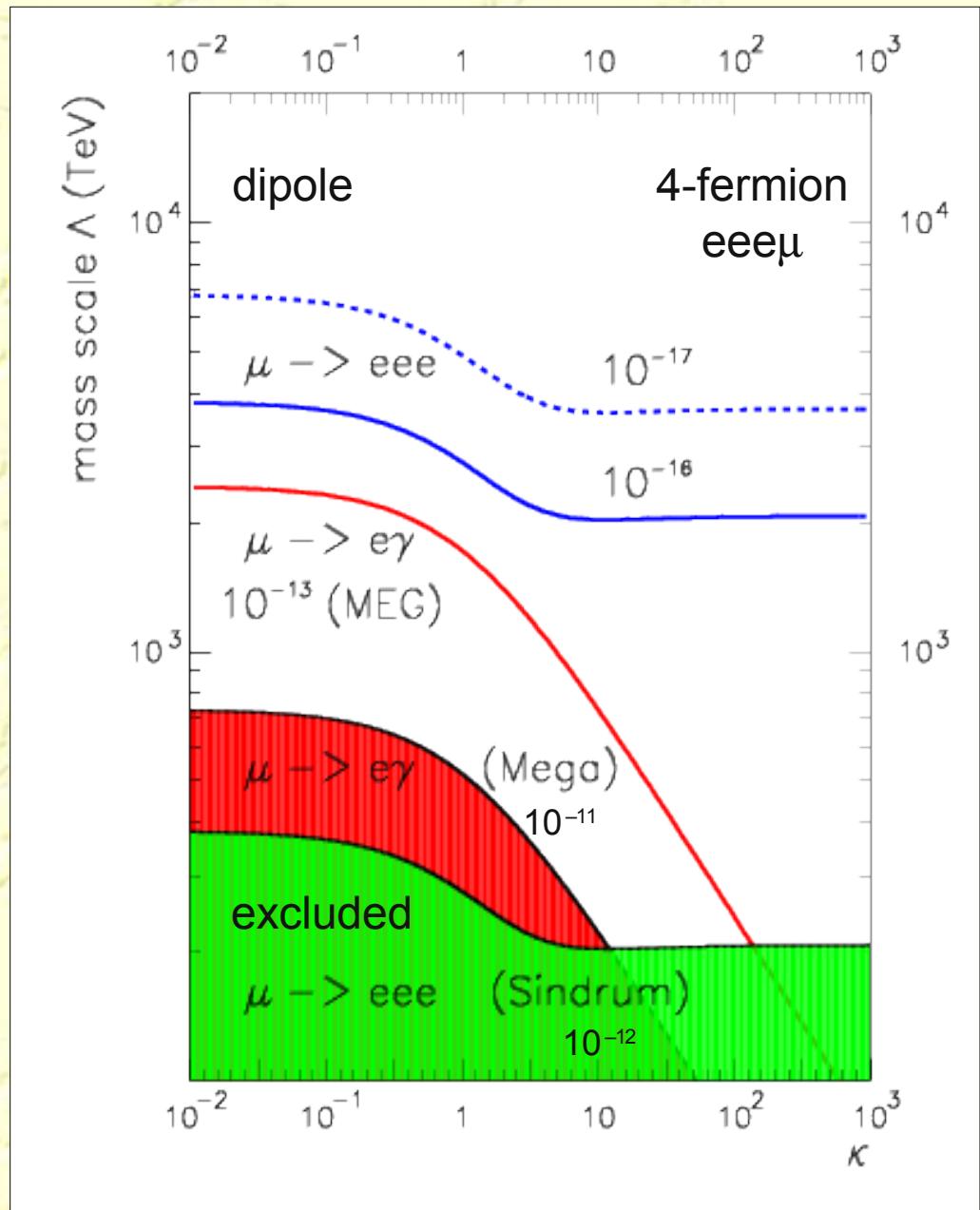
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- Almost factor 2 higher mass reach beyond MEG for LFV dipole couplings ( $\Lambda = 4 \cdot 10^3$  TeV)
- x 10 mass reach beyond SINDRUM for LFV four-fermion couplings ( $\Lambda = 2 \cdot 10^3$  TeV)

“André de Gouvêa”  
plot for  $\mu eee$



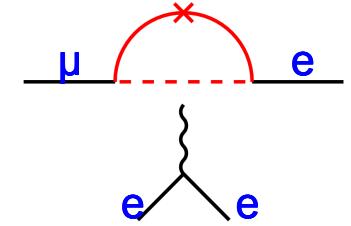
# Predictions: $\mu \rightarrow eee$ versus $\mu \rightarrow e\gamma$

- In case of dominating LFV dipole couplings  $\kappa = 0$  ( $A_{LR} \gg g_i$ )

$$\frac{B(\mu \rightarrow eee)}{B(\mu \rightarrow e\gamma)} \approx 0.006$$

$B(\mu \rightarrow eee) = 10^{-15}$  corresponds to  $B(\mu \rightarrow e\gamma) \sim 10^{-13}$   
 $B(\mu \rightarrow eee) = 10^{-16}$  corresponds to  $B(\mu \rightarrow e\gamma) \sim 10^{-14}$

dipole coupling



# Predictions: $\mu \rightarrow eee$ versus $\mu \rightarrow e\gamma$

- In case of dominating LFV dipole couplings  $\kappa = 0$  ( $A_{LR} \gg g_i$ )

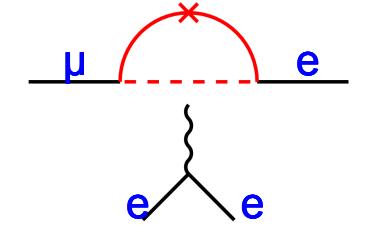
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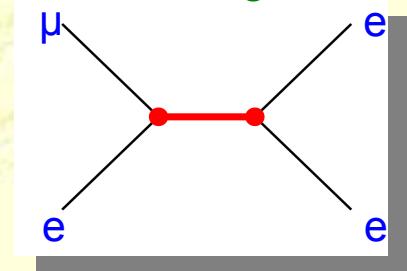
- Specific Models

Predictions	$B(\mu \rightarrow eee) / B(\mu \rightarrow e\gamma)$	$B(\mu \rightarrow eee)$
mSUGRA + seesaw	$\sim 10^{-2}$	$< 10^{-13}$
SUSY + SO(10)	$\sim 10^{-2}$	$< 10^{-13}$
SUSY + Higgs	$\sim 10^{-2}$	$< 10^{-13}$
Z', Kaluzza Klein	$> 1$	
Little Higgs	$0.1 - 1$	$< 10^{-13}$
Higgs Triplet	$10^{-3} - 10^{+3}$	$< 10^{-12}$

dipole coupling

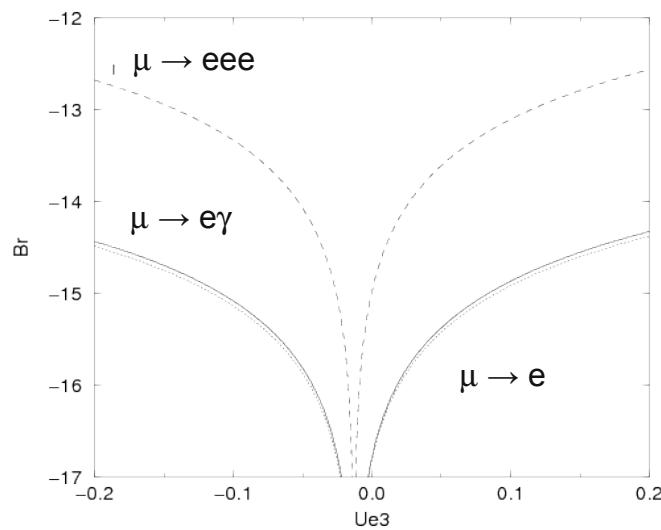


tree diagram

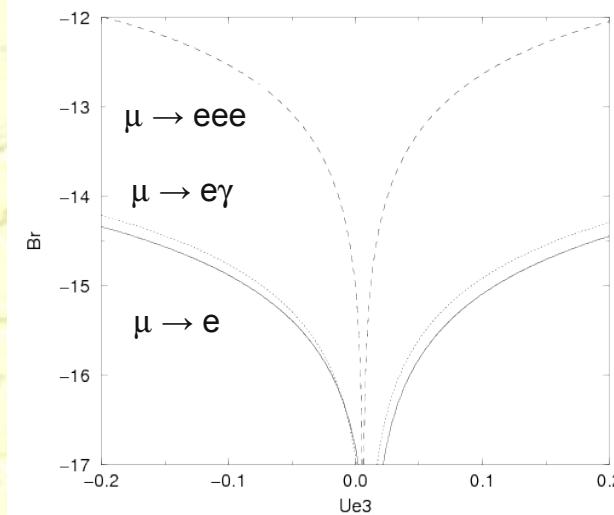


# Higgs Triplet Models

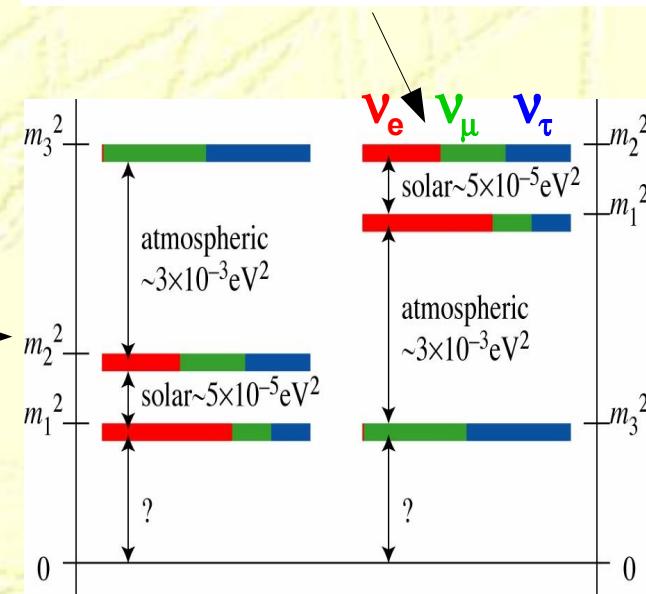
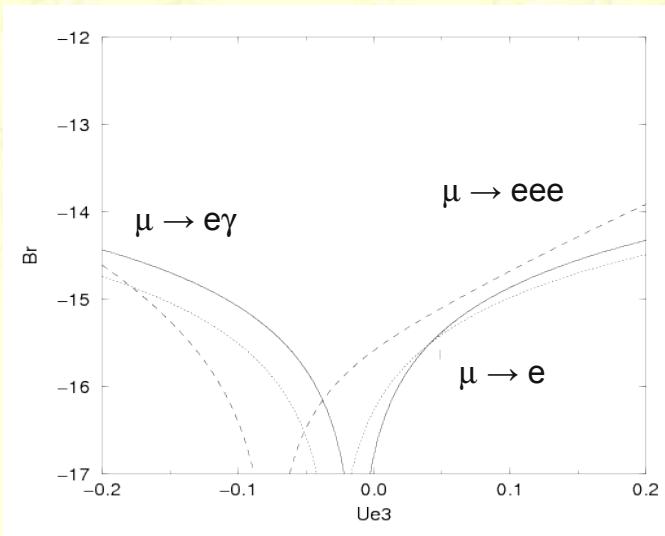
degenerate case



M. Kakizaki et al., Phys. Lett. B 566 (2003) 210  
inverted case

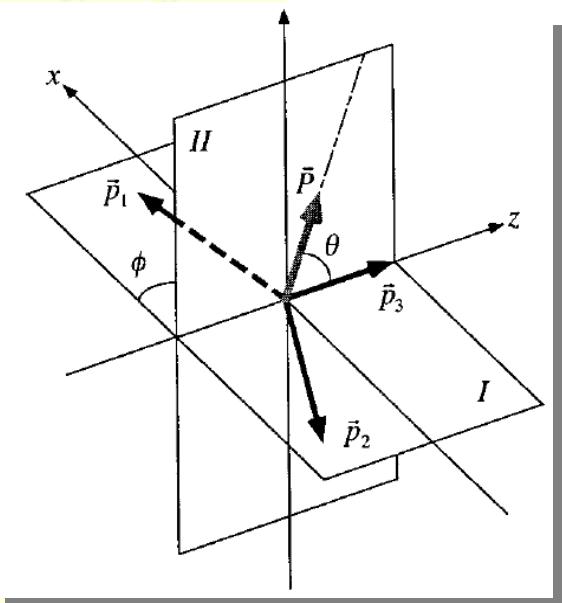


hierarchical case



# CP Violation in $\mu \rightarrow eee$

- Measurement of CP violation requires interference of diagrams
- 3-body decay kinematics allows for study of discrete symmetries!

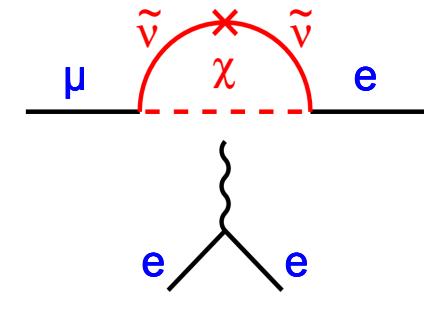


$$\frac{dB}{dx_1 dx_2 d\cos \theta d\varphi} = \frac{3}{2\pi} [ C_1 \alpha_1(x_1, x_2) (1 + P \cos \theta) + C_2 \alpha_1(x_1, x_2) (1 - P \cos \theta) + C_3 \{ \alpha_2(x_1, x_2) + P \beta_1(x_1, x_2) \cos \theta + P \gamma_1(x_1, x_2) \sin \theta \cos \varphi \} + C_4 \{ \alpha_2(x_1, x_2) - P \beta_1(x_1, x_2) \cos \theta - P \gamma_1(x_1, x_2) \sin \theta \cos \varphi \} + C_5 \{ \alpha_3(x_1, x_2) + P \beta_2(x_1, x_2) \cos \theta + P \gamma_2(x_1, x_2) \sin \theta \cos \varphi \} + C_6 \{ \alpha_3(x_1, x_2) - P \beta_2(x_1, x_2) \cos \theta - P \gamma_2(x_1, x_2) \sin \theta \cos \varphi \} + C_7 \{ \alpha_4(x_1, x_2) (1 - P \cos \theta) + P \gamma_3(x_1, x_2) \sin \theta \cos \varphi \} + C_8 \{ \alpha_4(x_1, x_2) (1 + P \cos \theta) - P \gamma_3(x_1, x_2) \sin \theta \cos \varphi \} + C_9 \{ \alpha_5(x_1, x_2) (1 + P \cos \theta) - P \gamma_4(x_1, x_2) \sin \theta \cos \varphi \} + C_{10} \{ \alpha_5(x_1, x_2) (1 - P \cos \theta) + P \gamma_4(x_1, x_2) \sin \theta \cos \varphi \} + C_{11} P \gamma_3(x_1, x_2) \sin \theta \sin \varphi - C_{12} P \gamma_4(x_1, x_2) \sin \theta \sin \varphi ],$$

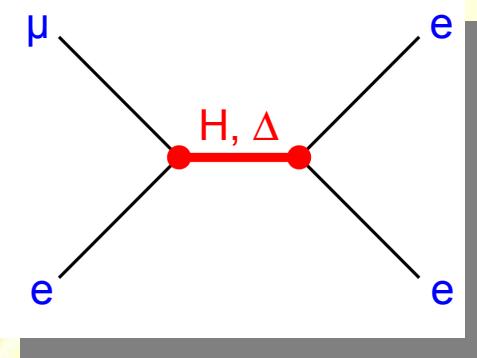
**T-odd**

(can also distinguish e.g. SU(5) from SO(10) models)

dipole coupling



tree diagram



# Motivation for $\mu^+ \rightarrow e^+e^+e^-$ Search I

- New Particles at the “Terascale” naturally induce LFV

$$\left| \frac{\Delta_M}{M} \right|^2$$

- Search  $\mu^+ \rightarrow e^+e^+e^-$  is complementary to other LFV searches

# Motivation for $\mu^+ \rightarrow e^+e^+e^-$ Search II

- Advances in detector technologies allow for high rate / high precision experiments at low energies
- Plans to improve PSI beamlines and targets: >  $10^9$  muon stops/s
  - would allow to test muon decay branching ratios at  $10^{-16}$
  - current exp. limit  $B(\mu^+ \rightarrow e^+e^+e^-) = 10^{-12}$  (Bellgard 1988)

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- A search for  $B(\mu^+ \rightarrow e^+e^+e^-) > 10^{-16}$  has a large potential to find LFV signal or to set very stringent bounds on new physics

# **Backgrounds and Previous Experiments**

# Backgrounds for $\mu^+ \rightarrow e^+e^+e^-$

- **Combinatorial Background (Pile up):**

- Two muon decays  $2 \times (\mu^+ \rightarrow e^+ \nu\nu)$  and one fake  $e^-$  (wrong charge: reconstruction, Bhabha, back-curling  $e^+ \rightarrow e^-$ )
- Radiative decay with internal conversion  $\mu \rightarrow (e^+) e^+e^- \nu\nu$  and muon decay  $\mu^+ \rightarrow e^+ \nu\nu$

- **Combinatorial BG can be largely reduced by imposing**

- timing vetos
- kinematic constraints
- vertex requirements

# Backgrounds for $\mu^+ \rightarrow e^+e^+e^-$

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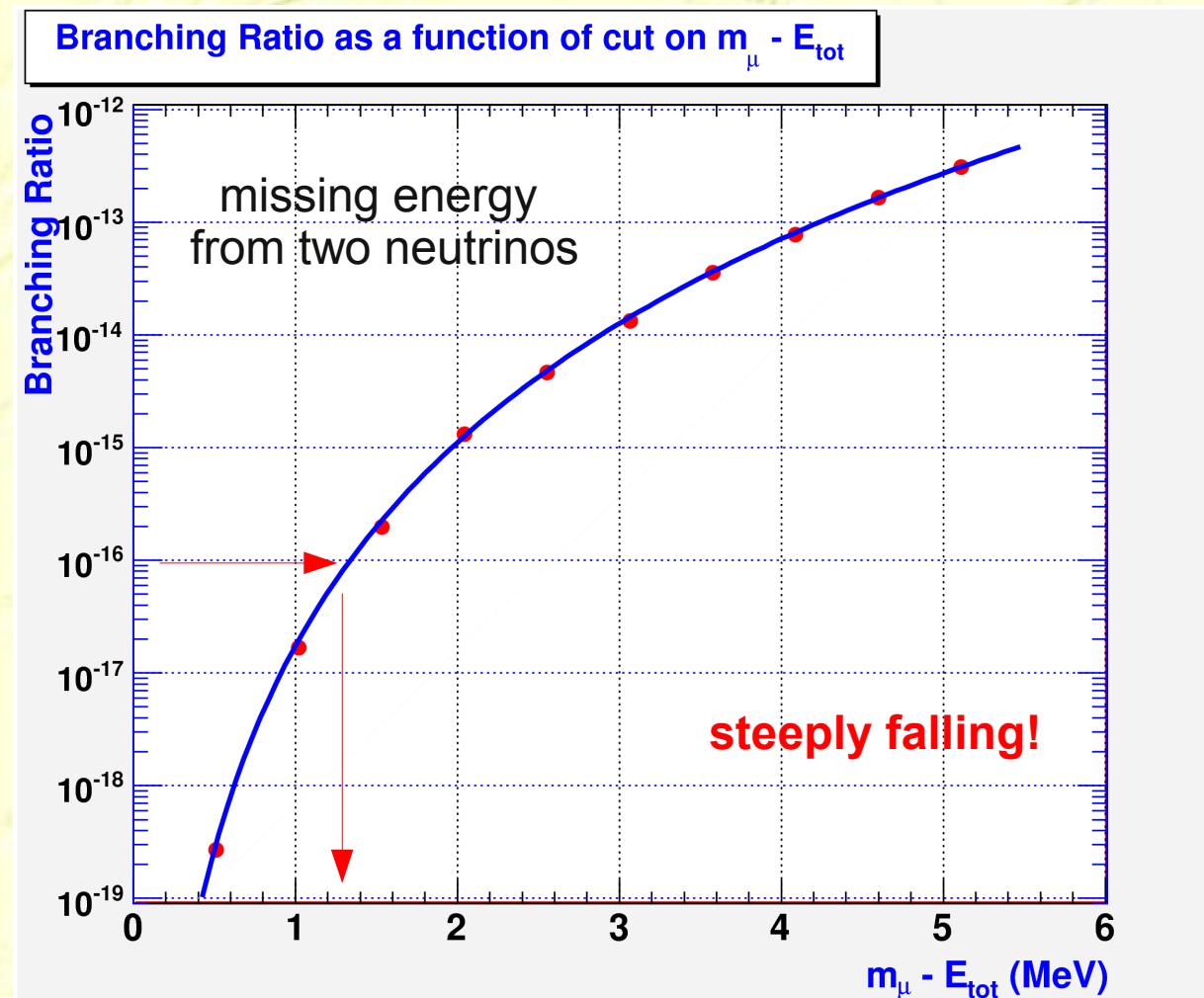
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- **Combinatorial BG can be largely reduced by imposing**
  - ◆ timing vetos
  - ◆ kinematic constraints
  - ◆ vertex requirements

- **Radiative decay with internal conversion  $\mu^+ \rightarrow e^+e^+e^- \nu\nu$**

irreducible background  $BR(\mu^+ \rightarrow e^+e^+e^- \nu\nu) = 3.4 \cdot 10^{-5}$

# Background from $\mu^+ \rightarrow e^+e^+e^- \nu\nu$



R.M.Djilkibaev and  
R.V.Konoplich  
PRD79 (2009)

Good energy (momentum) resolution  $E_{\text{tot}} = \sum |E_i| \sim \sum |\mathbf{p}_i|$  essential !!!

# Comparison: $\mu$ -Decay Experiments

- Sindrum 1988:

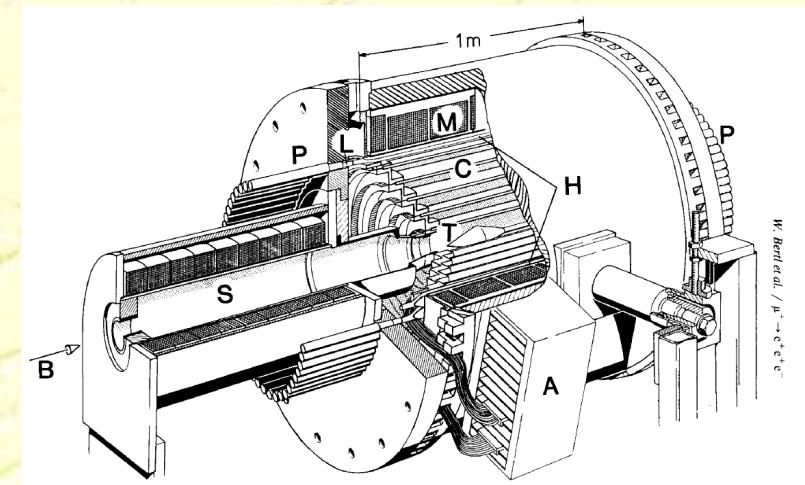
$$\sigma_p/p \text{ (50 MeV/c)} = 5.1\%$$

$$\sigma_p/p \text{ (20 MeV/c)} = 3.6\%$$

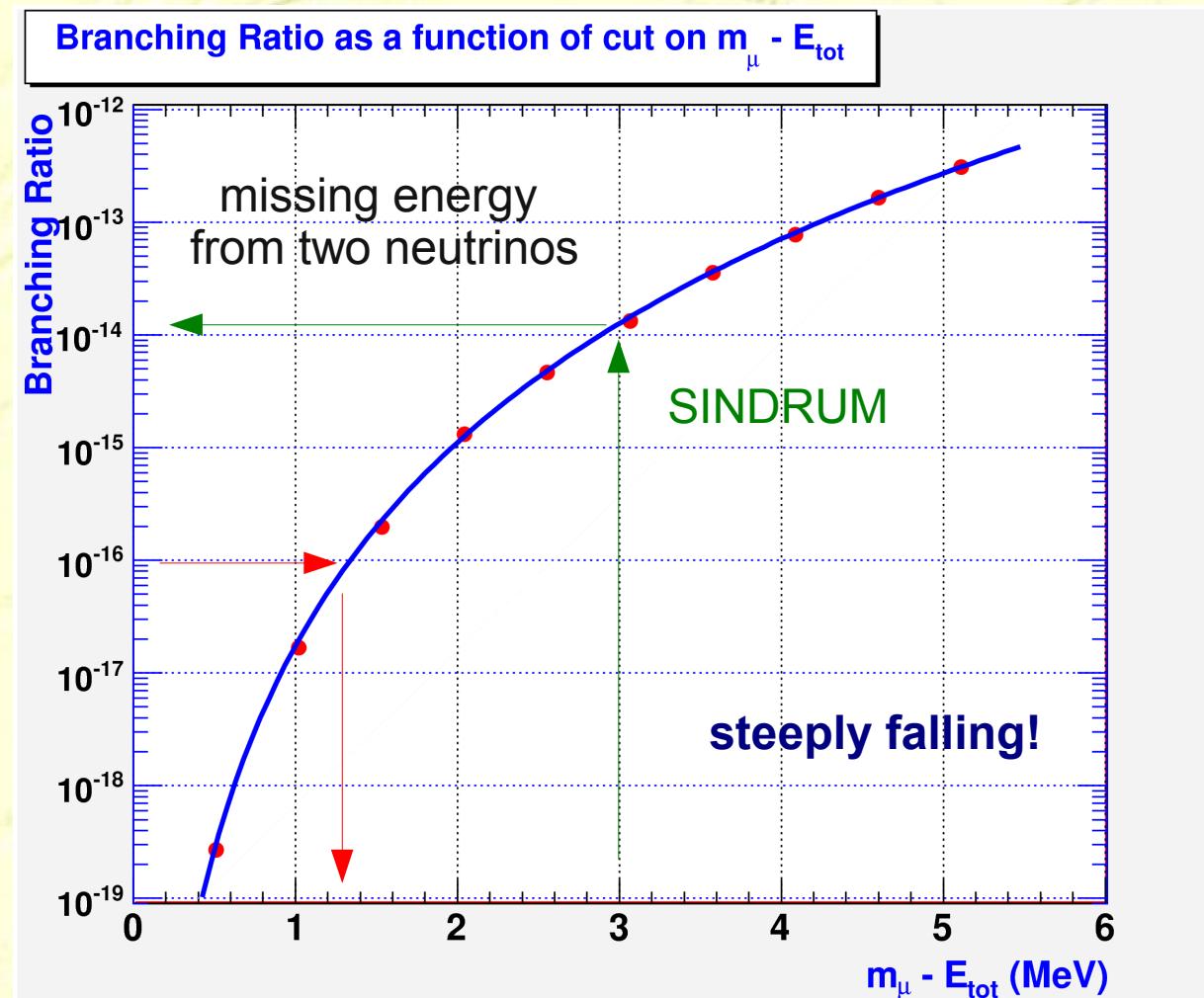
$$\sigma_\theta \text{ (20 MeV/c)} = 28 \text{ mrad}$$

$$\text{VTX: } \sigma_d = \sim 1 \text{ mm}$$

$$X_0(\text{MWPC}) = 0.08\% - 0.17\% \text{ per layer}$$



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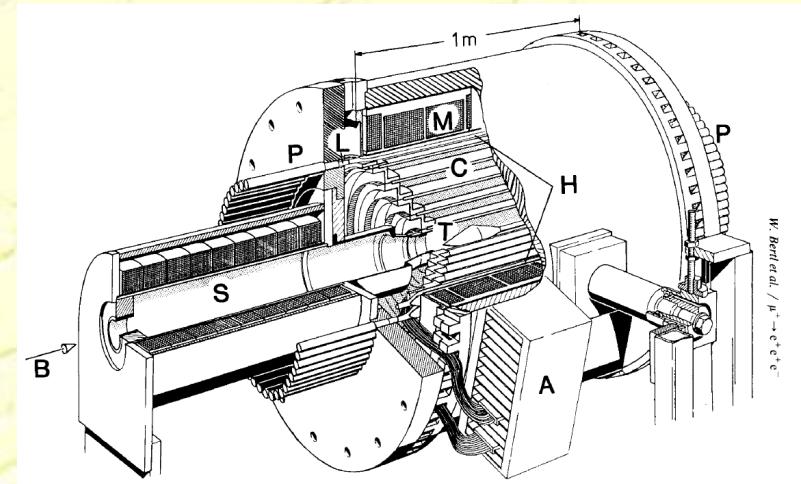
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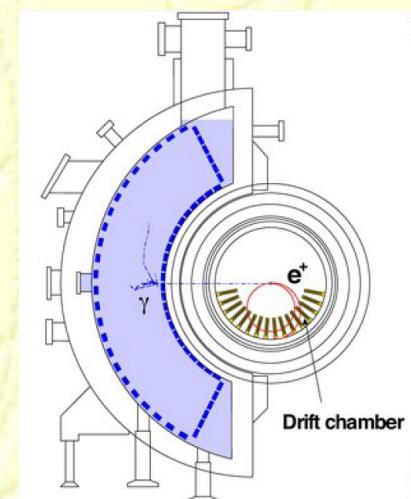
- MEG 2010 (preliminary):

$$\sigma_p/p \text{ (53 MeV/c)} = 0.7 \%$$

$$\sigma_\theta \text{ (53 MeV/c)} = 8 \text{ mrad}$$

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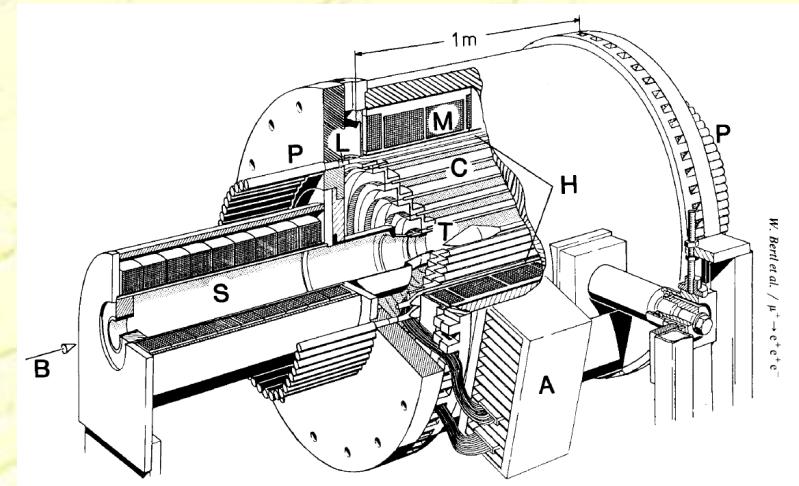
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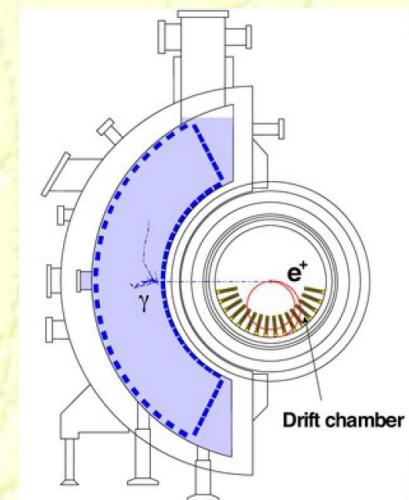
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$$\text{VTX: } \sigma_R = 1.4 \text{ mm}, \sigma_z = 2.5 \text{ mm}$$



• Aim for similar or better angular and momentum resolutions,  
high rates and better vertex resolution  $\sim 150 \mu\text{m}$  (combinatorial BG)

# **Detector Concept and Design**

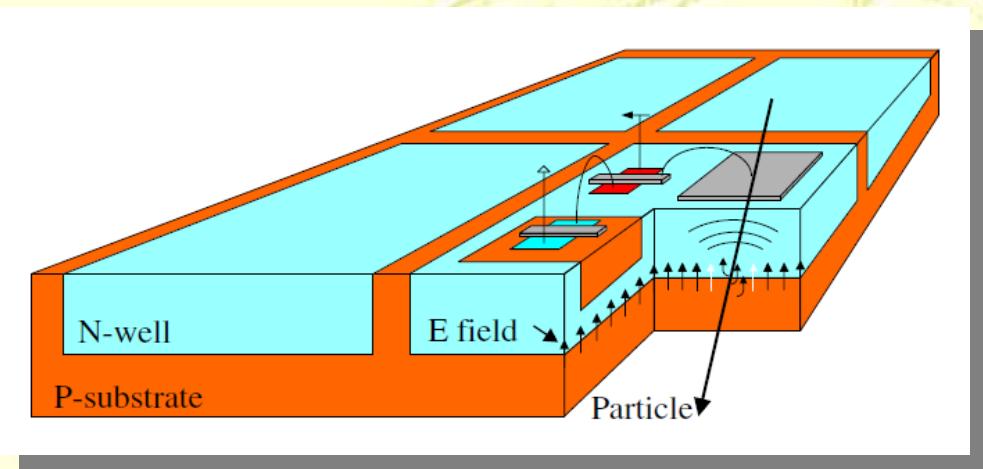
# Requirements for $\mu^+ \rightarrow e^+e^+e^-$

- Aim for  $B(\mu^+ \rightarrow e^+e^+e^-) = 10^{-16}$ 
  - need  $10^9$  stopped muons per second
  - high rate of electrons in detector!
- Tracking
  - gas detector disfavored → silicon detector
  - fast readout
- Momentum resolution
  - high precision detector → pixel sensor
  - low multiple scattering → thin sensors

# Silicon Detectors Technologies

Technologies	Thickness	Speed	Readout
ATLAS pixel	260 $\mu\text{m}$	25 ns	extra RO chip
DEPFET	50 $\mu\text{m}$	slow (frames)	extra RO chip
MAPS	50 $\mu\text{m}$	slow (diffusion)	fully integrated
HV-MAPS	>30 $\mu\text{m}$	O(100ns)	fully integrated

# High Voltage Monolithic CMOS Pixel



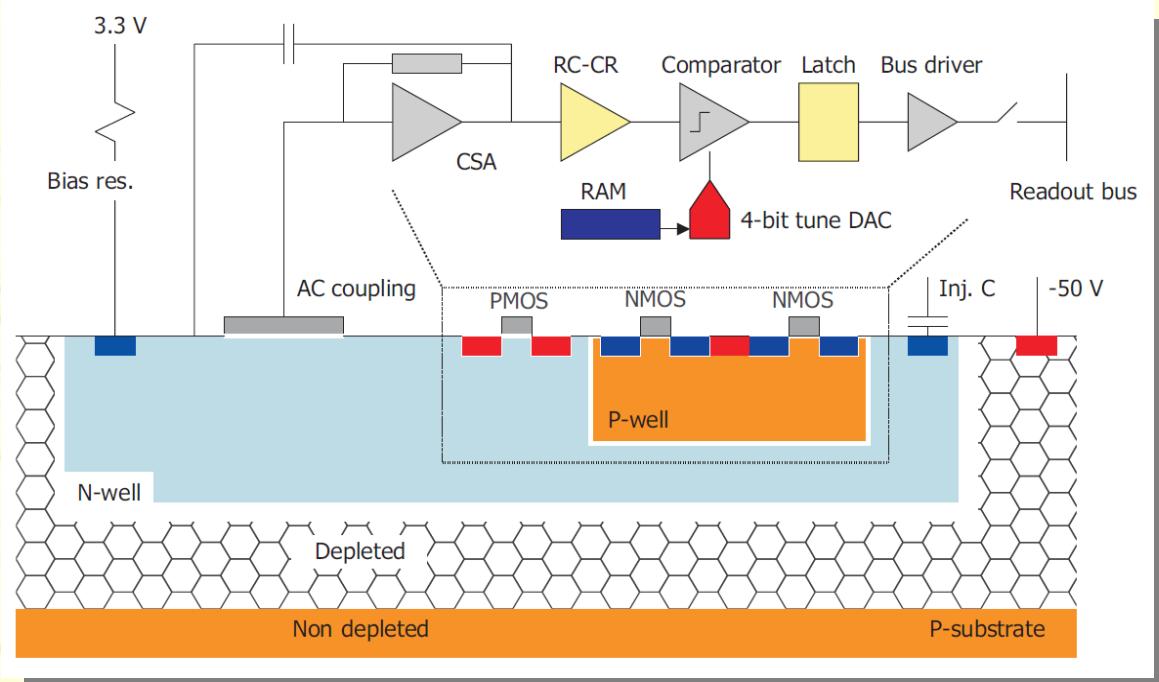
transistor logic embedded in N-well  
("smart diode array")

**New Technology!**

I.Peric, P. Fischer et al., NIM A 582 (2007) 876 (ZITI Mannheim, Uni Heidelberg)

Sensors tested successfully :

- radiation tolerant
- low noise:  $S/N > 40$
- tune DAC and zero suppression

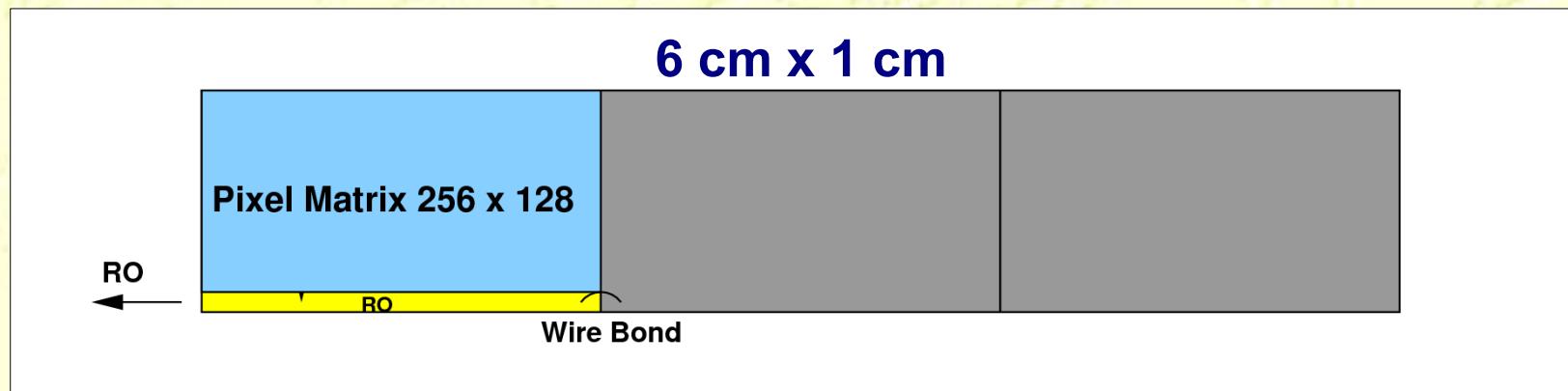


# HV MAPS Sensor

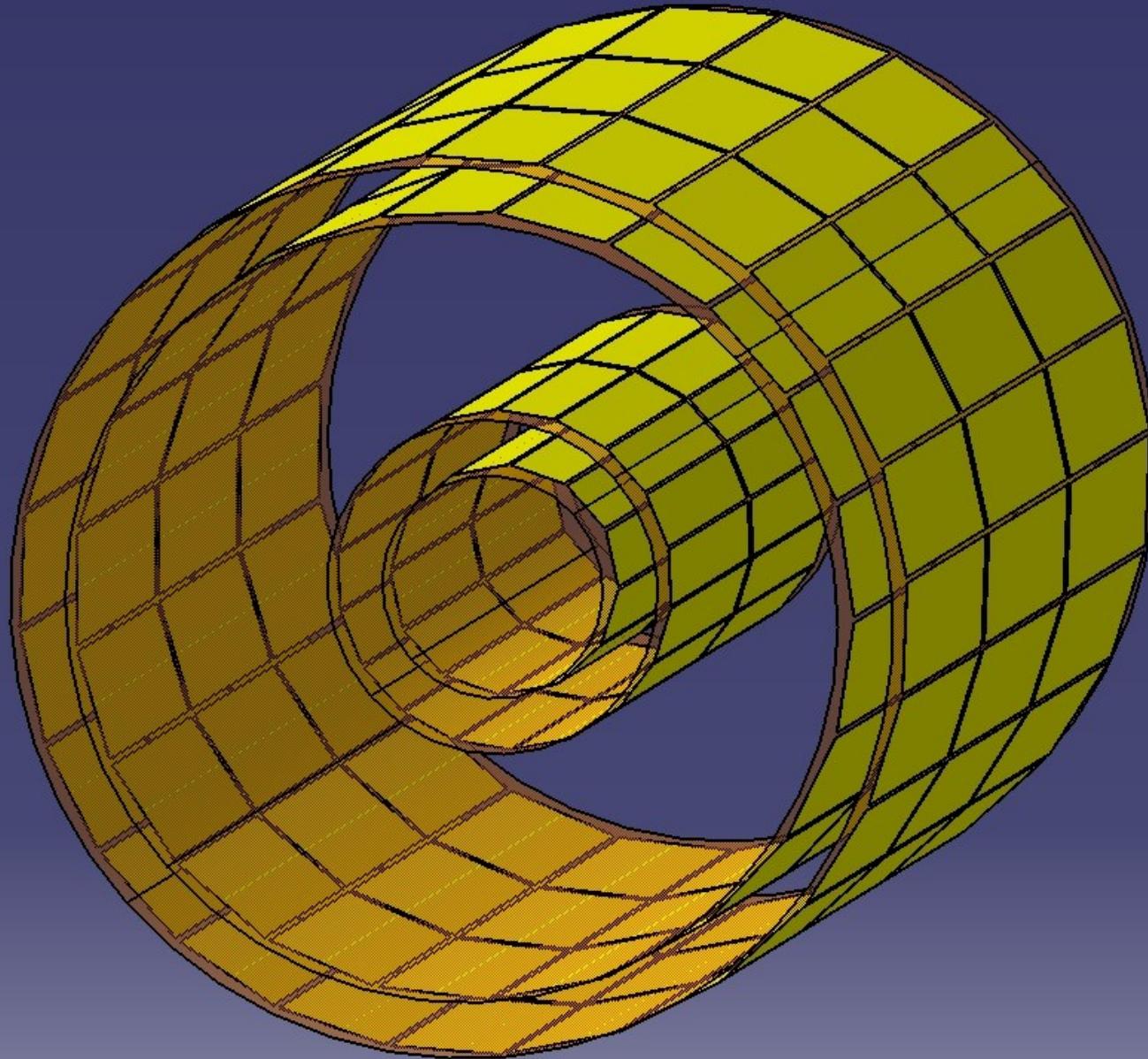
- Preliminary Sensor Specifications

- Module Size **1 cm x 6 cm** inner and **2 cm x 6 cm** outer layer
- Pixel Size **80 µm x 80 µm**
- **98k (196k) pixels 128 (256) x 768**
- resolution 1 bit per pixel
- power **150 mW/cm<sup>2</sup>**
- zero suppression
- data output **800 Mbit/s**
- time stamps every **100ns (10 MHz clock → power)**

first submission of test structures Feb. 2011  
(AMS HV 0.18 micron)



# Possible Tracker Layout



30-50  $\mu\text{m}$  Silicon  
on  
25  $\mu\text{m}$  Kapton

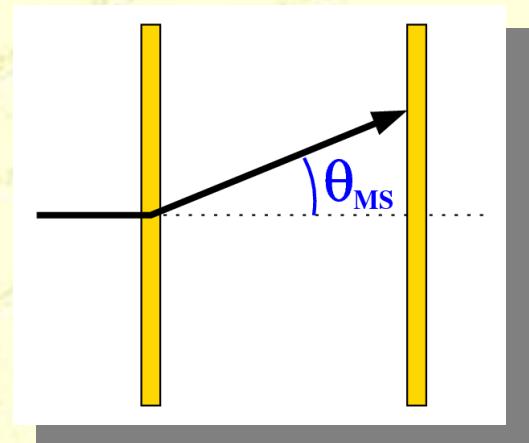
# Multiple Scattering in Silicon

Momentum range  $p = 15\text{-}53 \text{ MeV}$

→ multiple scattering!

Example:  $p = 53 \text{ MeV}/c$

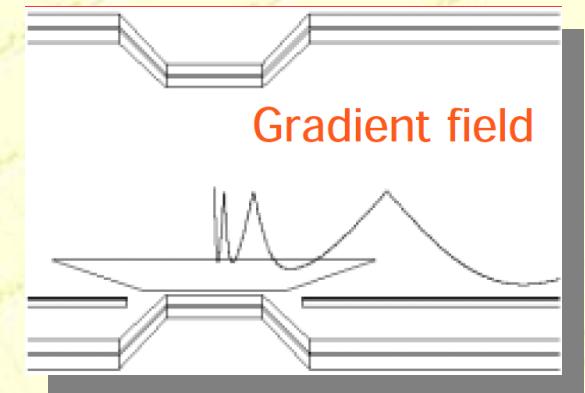
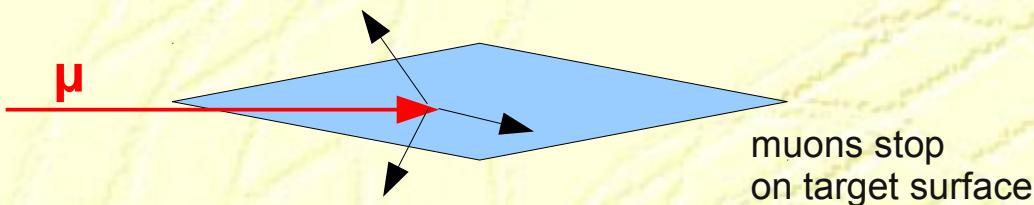
- MEG:  $\sigma_{\theta}^{\text{MS}} = 8 \text{ mrad}$ 
  - multiple scatt. per layer  $X/X_0 = 0.1\%$  → corresponds to **90 μm Silicon**
- $\mu \rightarrow eee$ :  $\sigma_{\theta}^{\text{MS}} = 5 \text{ mrad}$ 
  - multiple scatt. per layer  $X/X_0 = 0.044\%$  → corresponds to **40 μm Silicon**



Pixel sensors can be thinned down to **30-50 μm**  
(examples CMOS MAPS, DEPFET 50 μm)

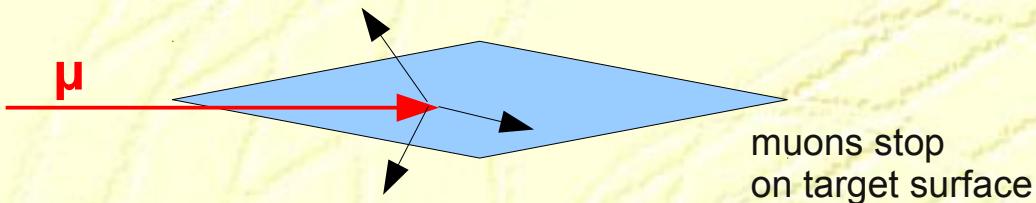
# “Novel” Experimental Concept

- Strong Magnet (e.g. Cobra from MEG)
- Hollow Double Cone Target (Sindrum)



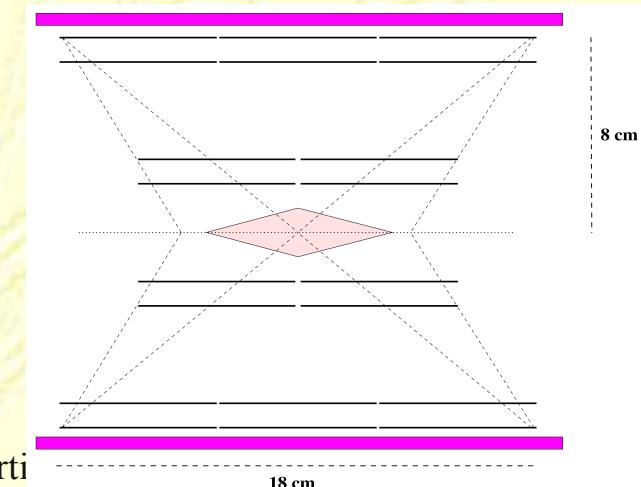
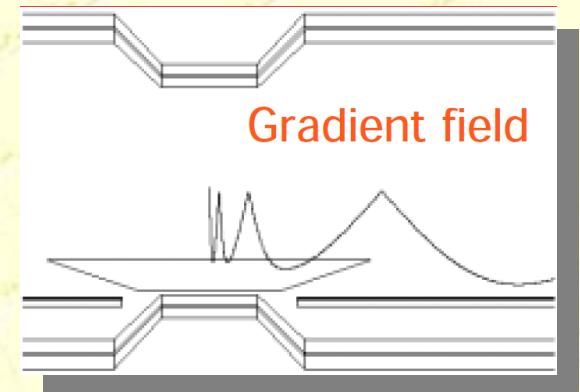
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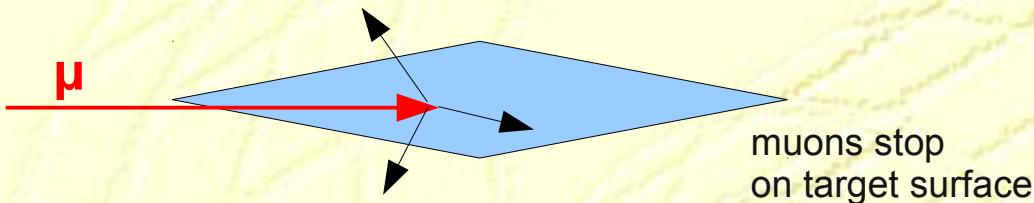
- Silicon pixel detector for tracking

- high resolution
- precise hit position  $80 \mu\text{m} \times 80 \mu\text{m}$  (c.t. multiple scattering  $\sigma_{\text{MS}} \sim 150 \mu\text{m}$ )



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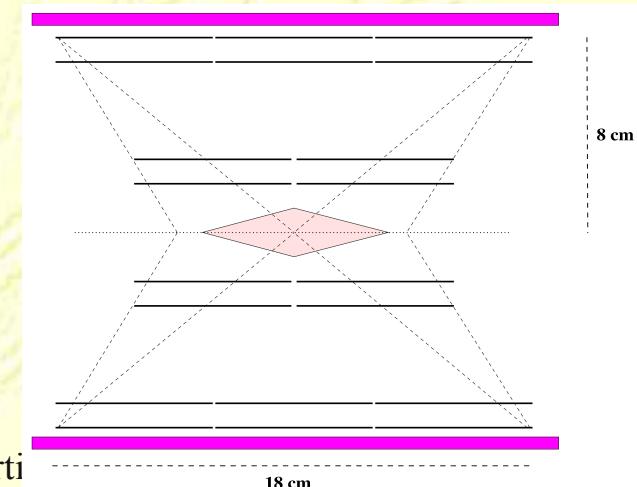
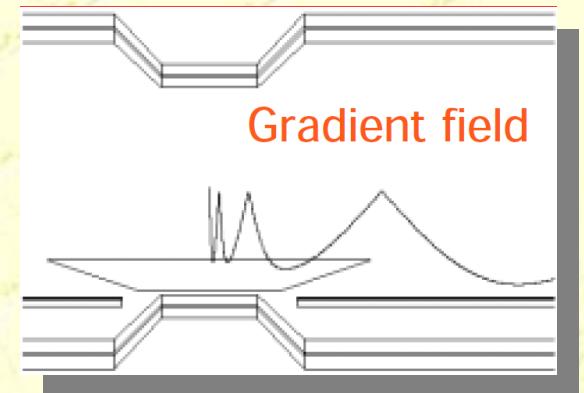


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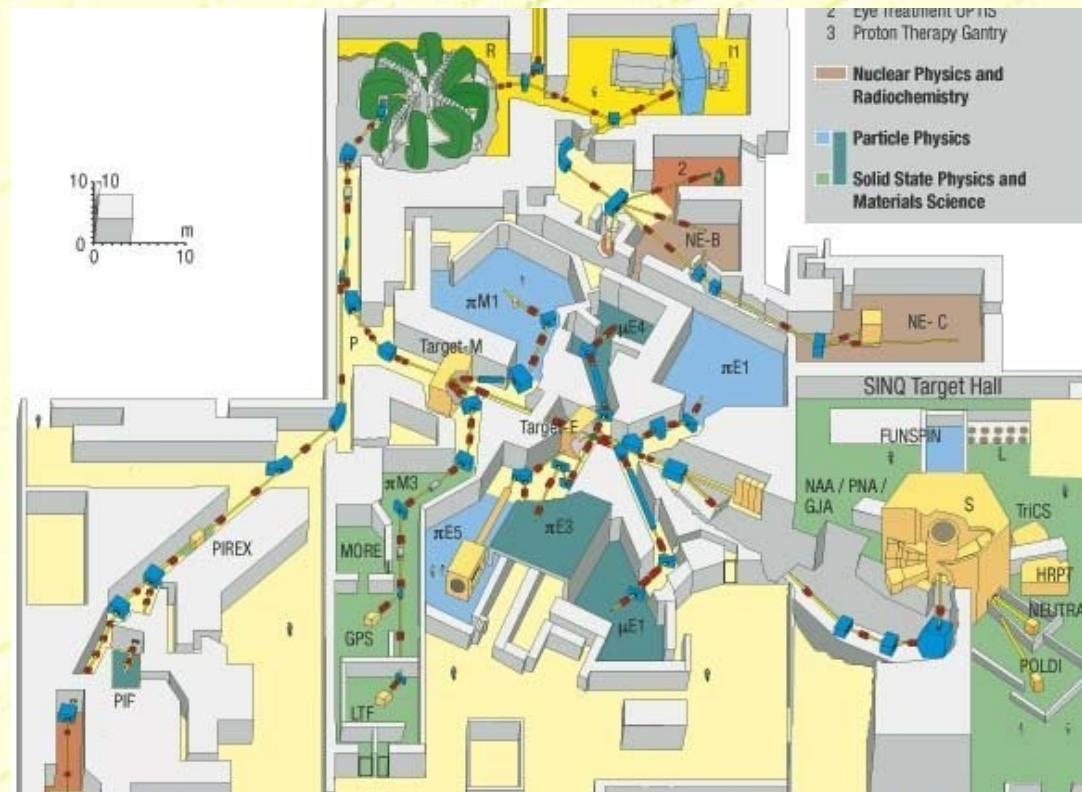
- Scintillating fiber tracker for timing

- excellent timing  **$\Delta T = 100 \text{ ps}$**
- good spatial resolution
- vector tracking (particle direction)



# DC Muon Beams at PSI

- $\mu E1$  beamline with rates up to  $\sim 5 \cdot 10^8$  muons/s
- $\pi E5$  beamline (MEG experiment)  $\sim 10^8$  muons/s
- $\mu E4$  beamline  $\sim 10^9$  muons/s
- SINQ target could even provide  $\sim 10^{10}$  muons/s
- New experiment (final stage) requires **muon rates  $\geq 1e9/s$**  focussed and collimated on a spot with about  $d=2$  cm diameter



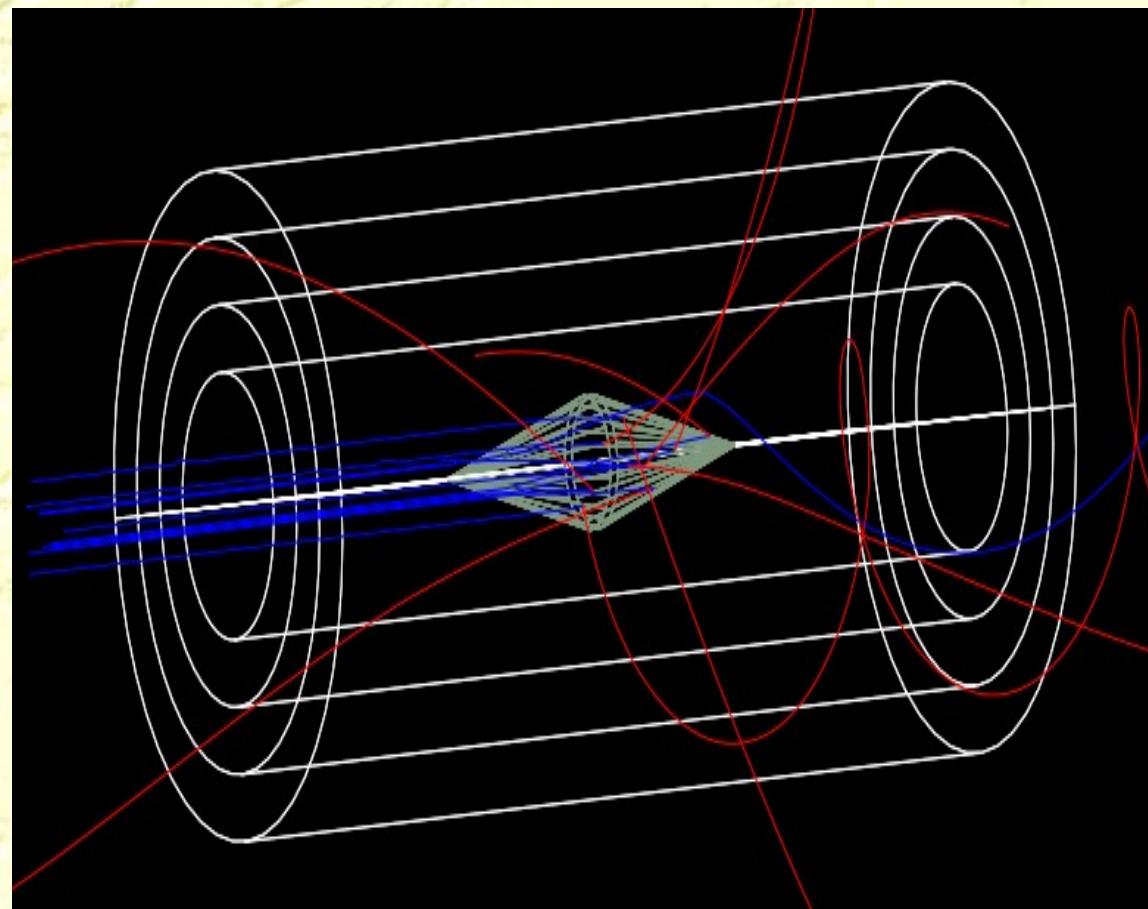
# Target and Vertex Resolution

## Sindrum-like Hollow Double Cone Target:

- total length of target:  $\sim 7$  cm
- diameter: 2 cm
- thickness of hollow cone  $\sim 60$   $\mu\text{m}$  (Al)
- **vertex resolution:  $\sim 150$   $\mu\text{m}$**

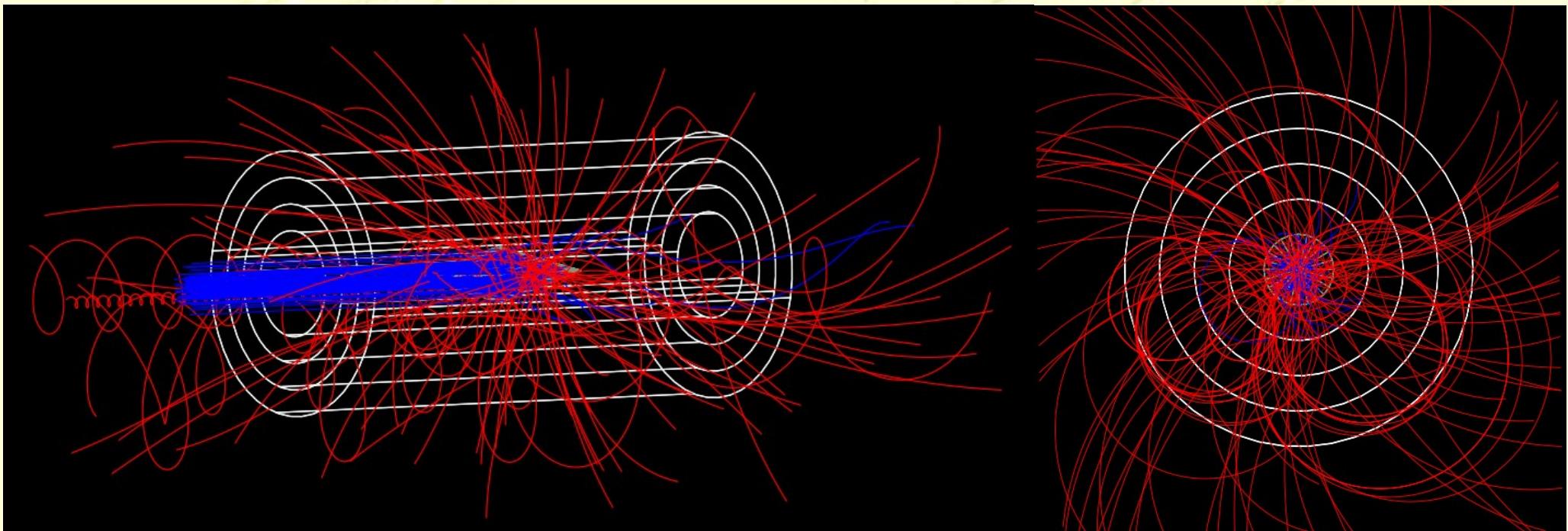
allows to suppress combinatorial BG  
by factor  $5 \cdot 10^{-5}$

Simulation Model



# Timing Resolution

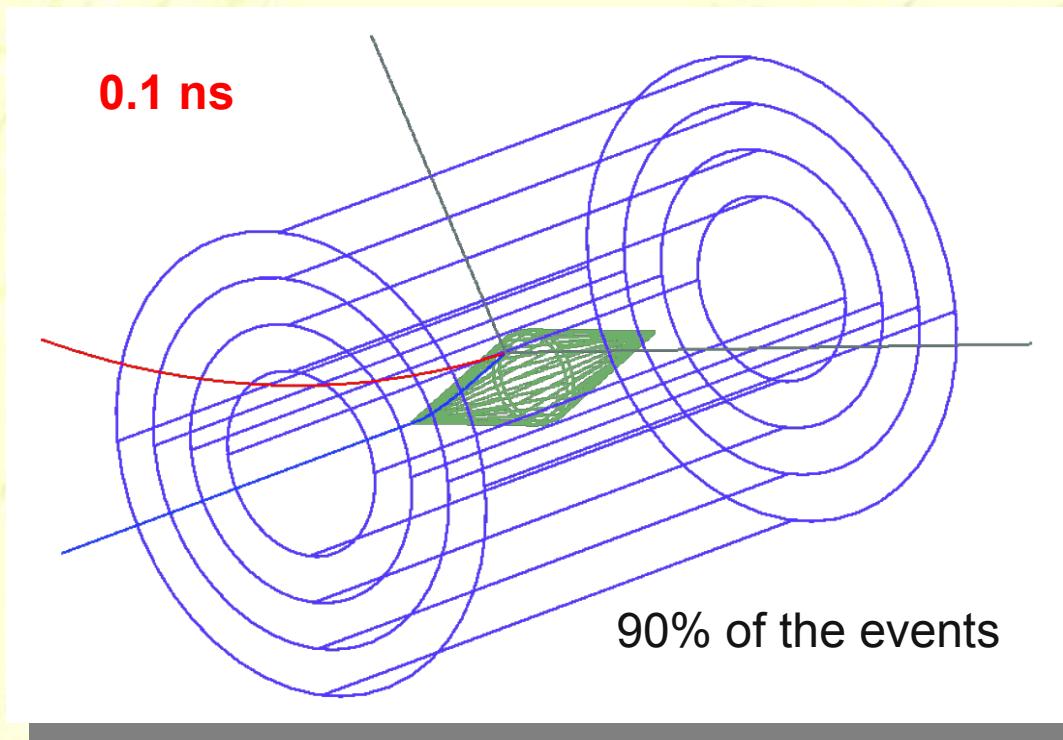
$\int dt = 100 \text{ ns: } 100 \text{ decays @ } 10^9 \text{ muon stops/s}$



timing resolution silicon: 100 ns

# Timing Resolution

$\Delta t = 0.1 \text{ ns}$ : <1 decay @  $10^9$  muon stops/s



timing resolution silicon: 100 ns

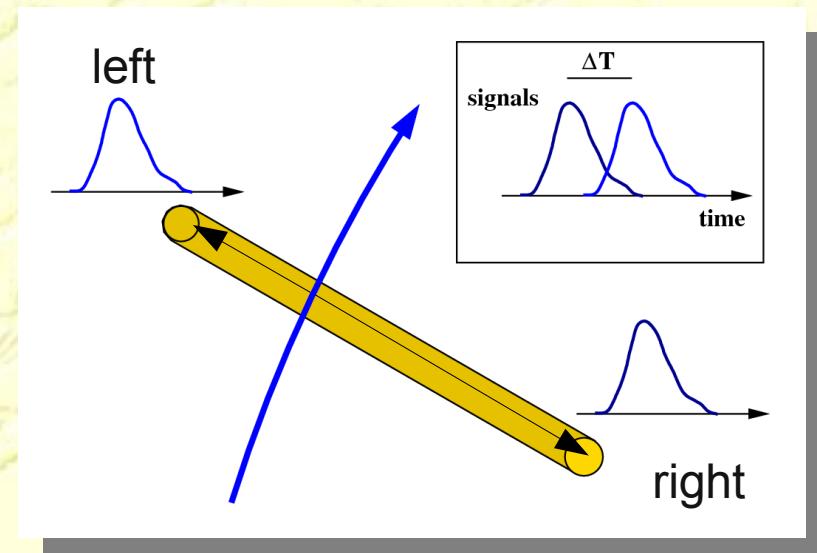
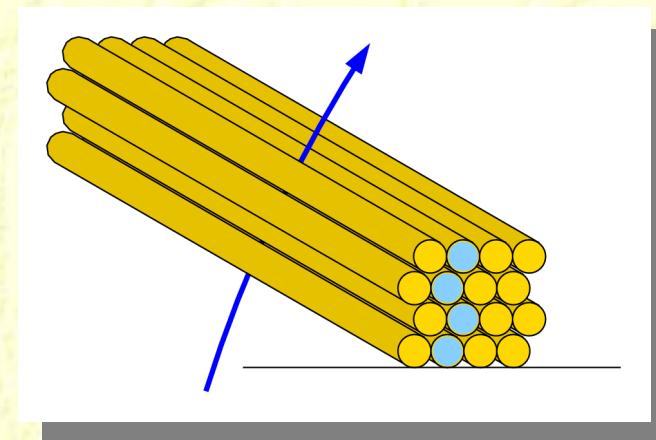
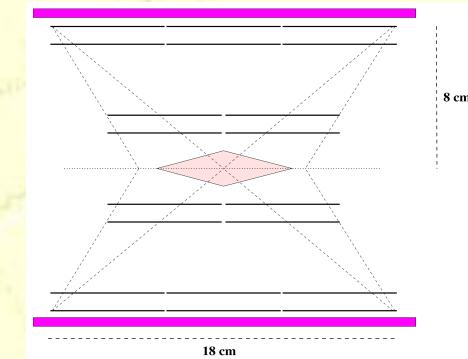
timing resolution fiber tracker: ~0.1ns

- allows to suppress combinatorial BG by factor 1000

# Scintillating Fiber Tracker

## Purpose:

- Measure timing of tracks precisely:  $\sigma_t = 50-100 \text{ ps}$
- Allows for unambiguous silicon hit assignment
- x-y plane:  $\varnothing = 0.25-1.0 \text{ mm}$  fibers
- z-position: relative time difference both ends (precision 1-2 cm)



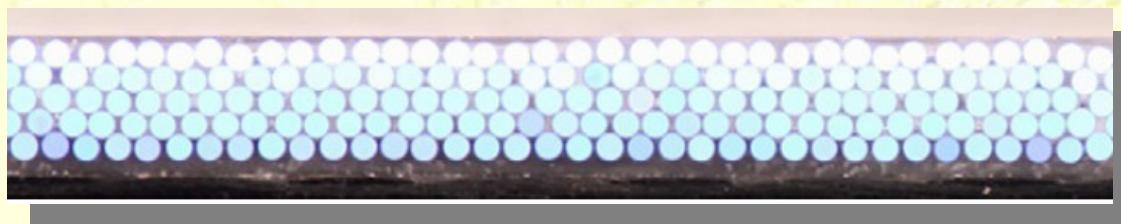
- Photodetector: SiPM

# Silicon Photomultipliers

- compact
- fast  $\Delta t < 100\text{ps}$ ,  $f_{\max} = 1\text{-}10 \text{ MHz}$
- high gain  $1\text{e}5\text{-}1\text{e}6$
- high efficiency
- radiation hard
- insensitive to magnetic fields

used in various experiments:

- KEK T2K INGRID (photon detection)
- PEPS balloon-borne detector (scintillating fiber tracker)

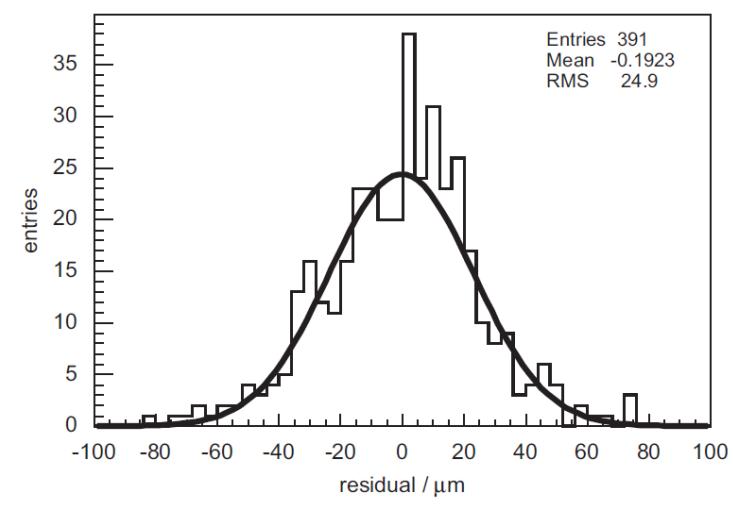


5 layers of scintillating fibers  $250\mu\text{m}$  diameter



pixel array of avalanche photo diodes

Beischer et al., NIM A622(2010)542



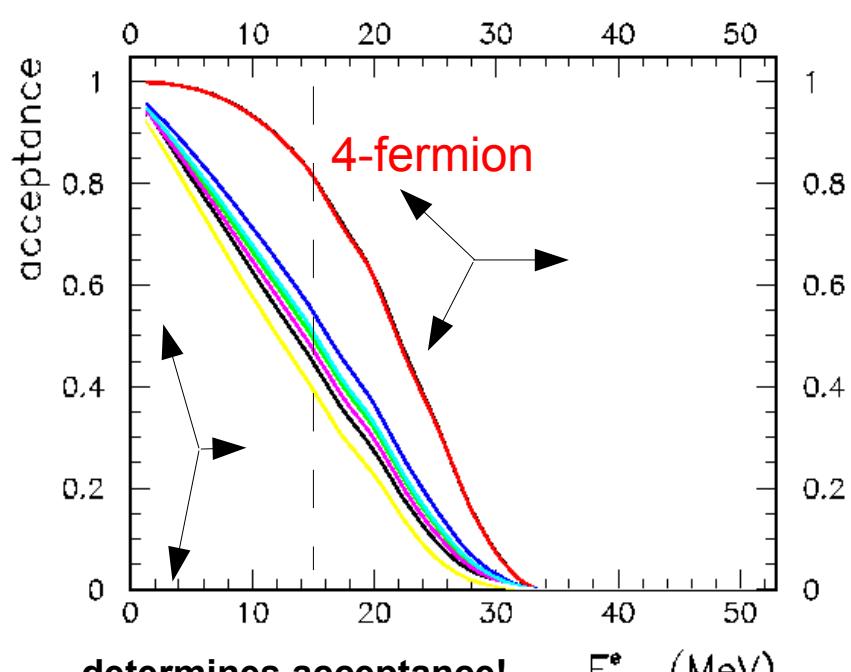
spatial resolution  $25 \mu\text{m}$

# Detector Acceptance $\mu^+ \rightarrow e^+e^+e^-$

## Model Dependence:

$$\frac{dB(\mu \rightarrow eee)}{dx_1 dx_2 d\cos\theta d\phi} = \sum_{k=1}^5 c_k \alpha_k(x_1, x_2)$$

## Minimum electron energy:



four fermion  photon penguin	$c_1 = \frac{g_1^2 + g_2^2}{16} + g_{34}^2$ $c_2 = g_{56}^2$ $c_3 = e A^2$ $c_4 = e A g_{34} \eta$ $c_5 = e A g_{56} \eta'$	acc ~ 80% acc ~ 40%
--	---	------------------------

T-odd

measure momenta  
in range:  $p=15-53 \text{ MeV}/c$

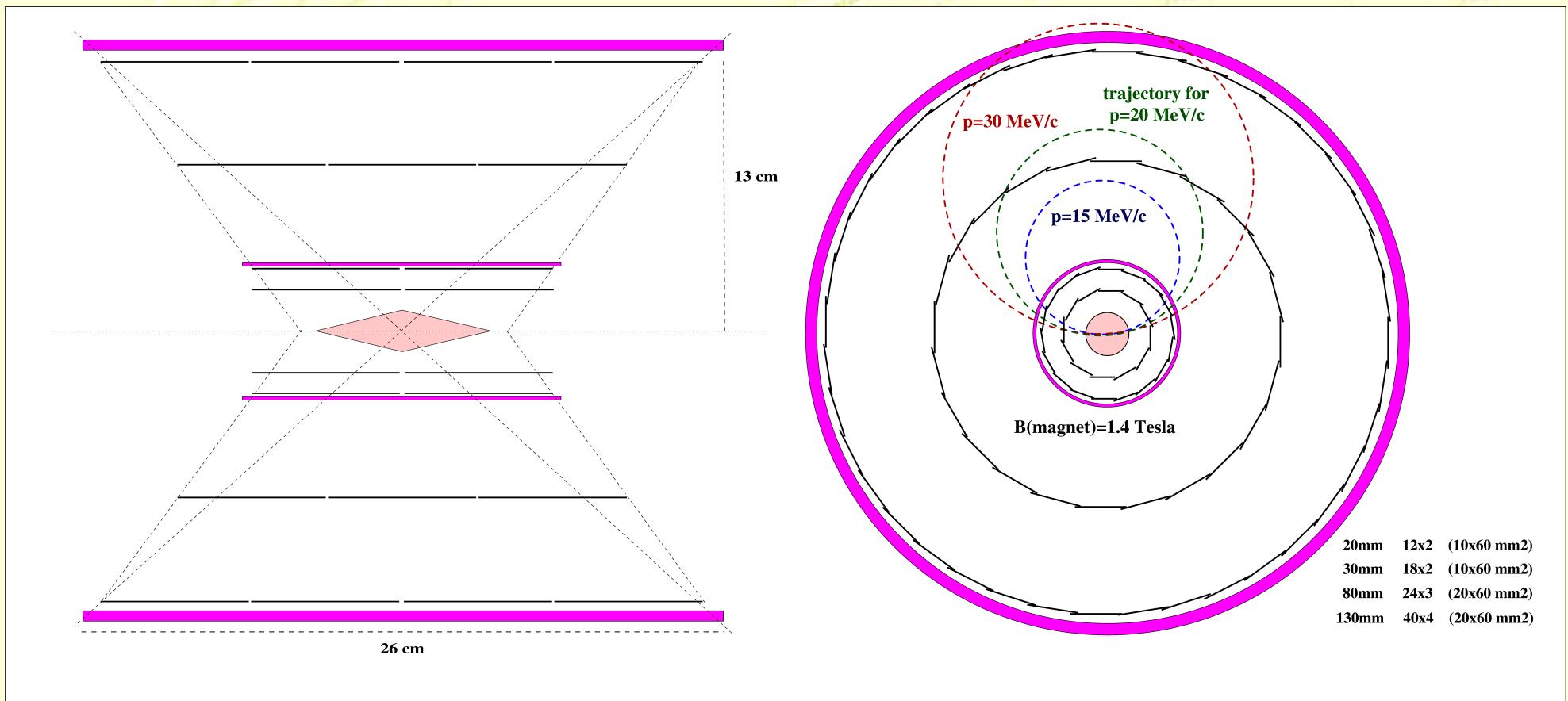
# “Big Barrel” Design

**momentum resolution:**  
**(half-circle fit)**

$$20 \text{ MeV/c: } \sigma_p/p = 2.3\% \rightarrow \sigma_p = 0.46 \text{ MeV/c}$$

$$35 \text{ MeV/c: } \sigma_p/p = 1.3\% \rightarrow \sigma_p = 0.45 \text{ MeV/c}$$

$$50 \text{ MeV/c: } \sigma_p/p = 1.3\% \rightarrow \sigma_p = 0.65 \text{ MeV/c}$$



**precise timing information for all tracks by second fiber tracker**

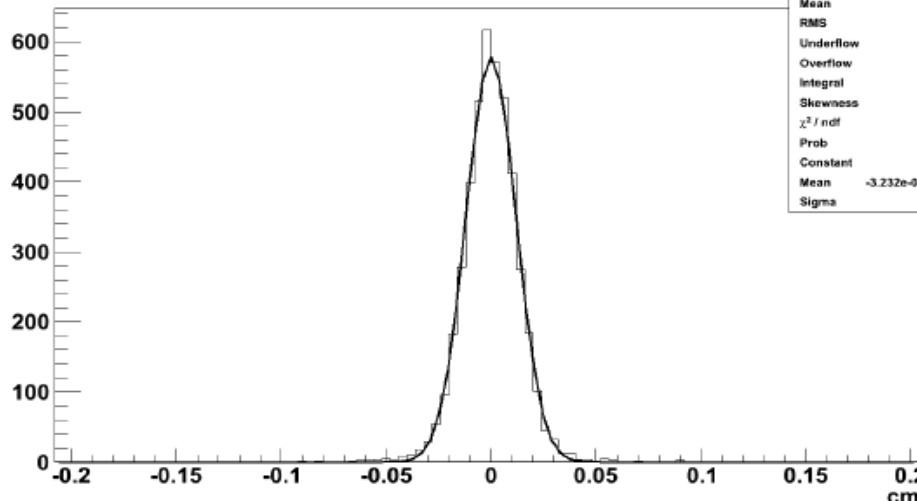
# Simulation Studies

# Tracking Resolutions Studies

- Preliminary results obtained using Geant4 by simulating a small scale detector (radial layers at 2, 3, 4, 5 cm)

(R.Narayan)

Z0 Resolution: pt cut 50 MeV

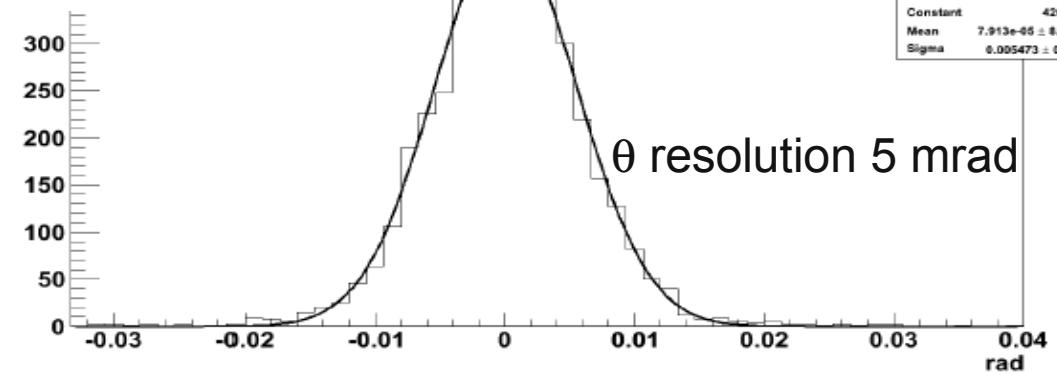


$Z_0$  (vertex) resolution 120  $\mu\text{m}$



results are from preliminary studies.  
work in progress!

Resolution: (pt = 50 MeV)



$\theta$  resolution 5 mrad

# Possible Improvements

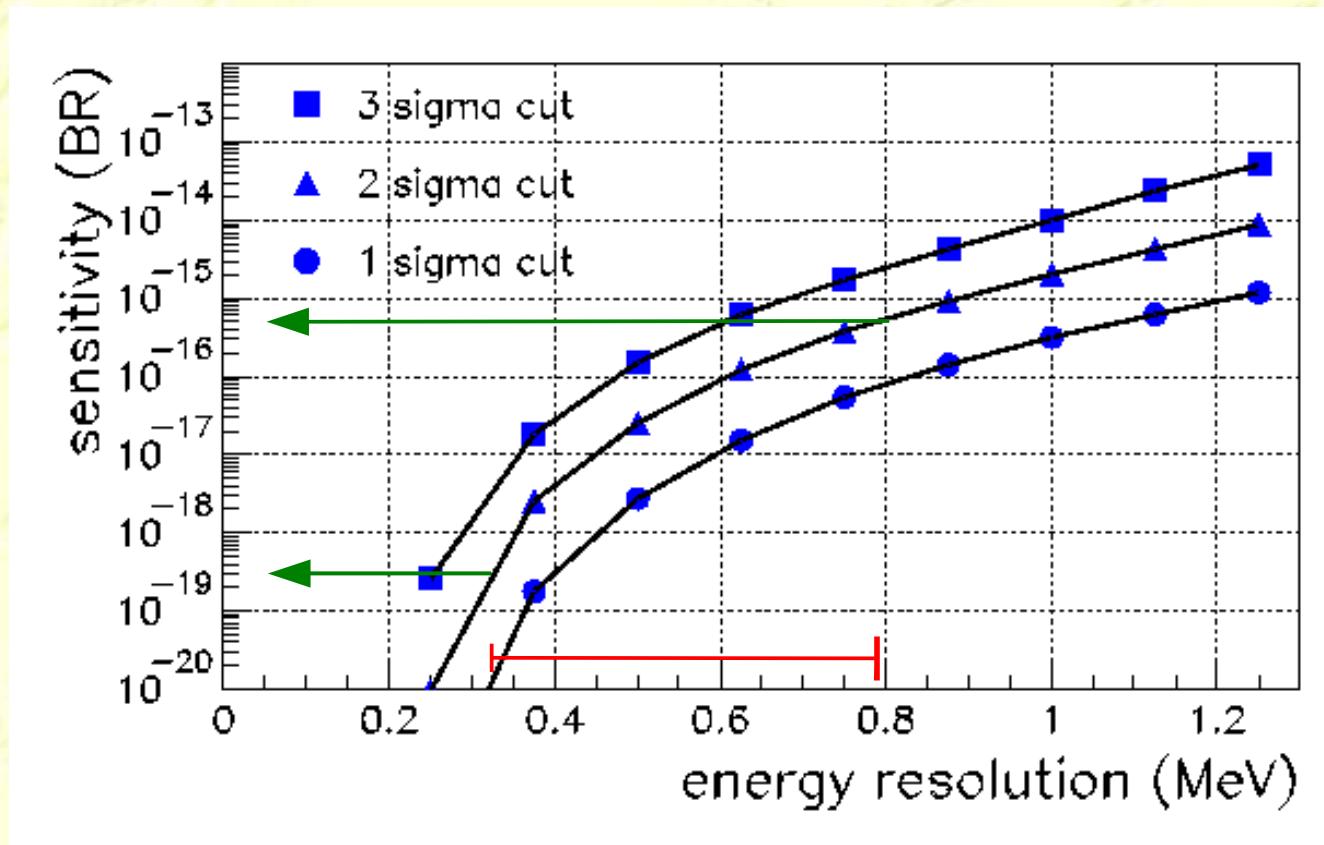
## Momentum resolution

- factor ~0.7 fitting second track half
  - factor ~0.8 primary vertex fit (3 tracks)
  - factor ~0.8 from improved fitting (broken line fit)?
  - factor ~0.9 no inner scintillating fiber tracker
- $\sigma_E = 0.78\text{-}0.91 \text{ MeV} \rightarrow \sigma_E = 0.32\text{-}0.36 \text{ MeV}$

# Simulated Sensitivity

Rate of  $\mu \rightarrow \text{eeeevv}$  as function of the energy resolution:

sensitivity ≡  
background

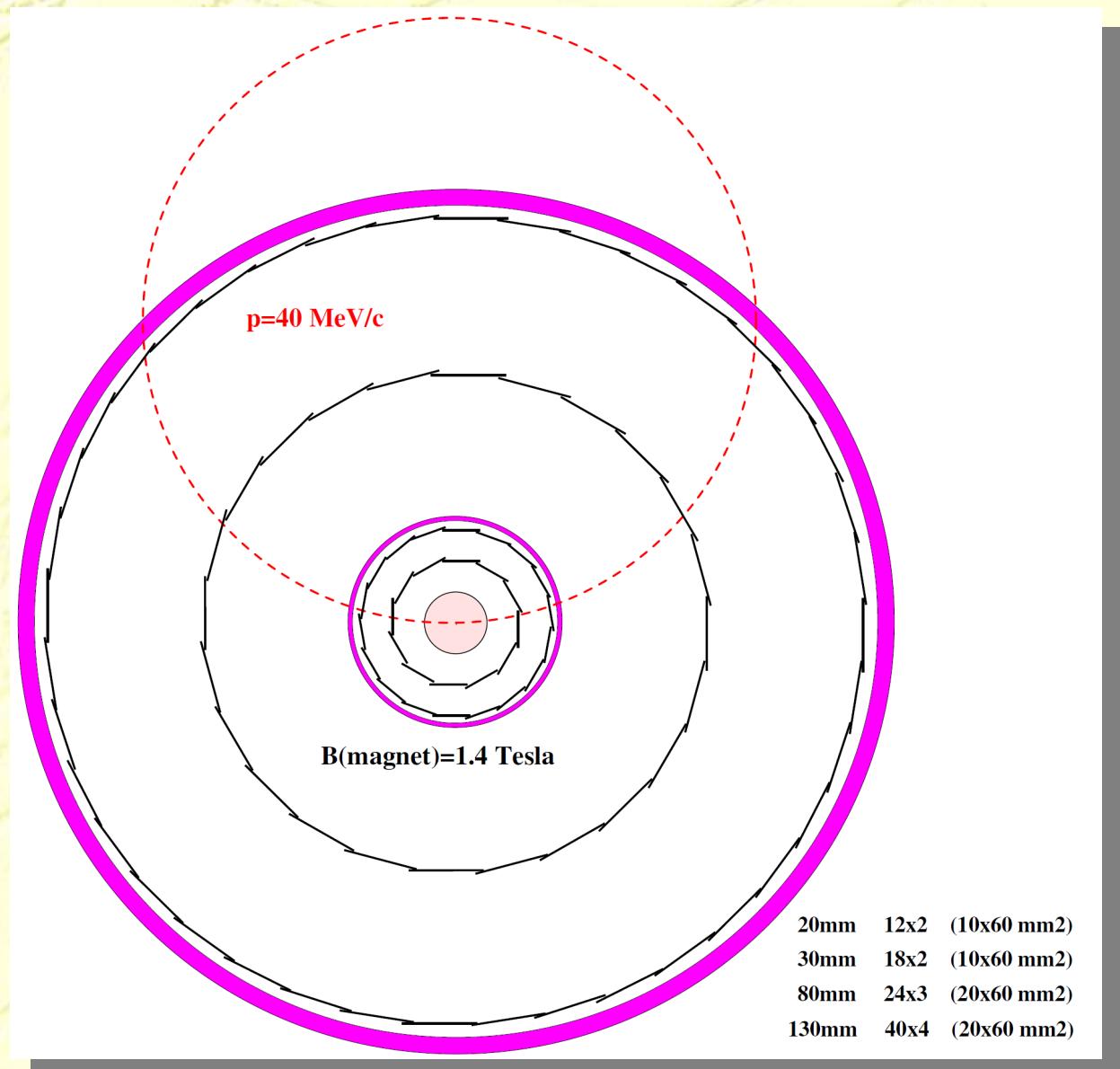


- good energy resolution suppresses  $\mu \rightarrow \text{eeeevv}$  BG effectively
- for  $\sigma_E = 0.3\text{-}0.6 \text{ MeV}$  sensitivity even below  $10^{-16}$

# Further Improvements?

Fit Recurling Track:

$\sigma_E \leq 0.1$  MeV ?



# Mu3e Project

## Status of Project

- **interesting new ideas**
- no name, looking for collaborators

## Interested groups:

- Uni Zürich, ETH Zürich?
- Rome “La Sapienza”
- Paul Scherrer Institute
- Geneva
- Heidelberg/Mannheim

## Status of Activities (Heidelberg / Mannheim)

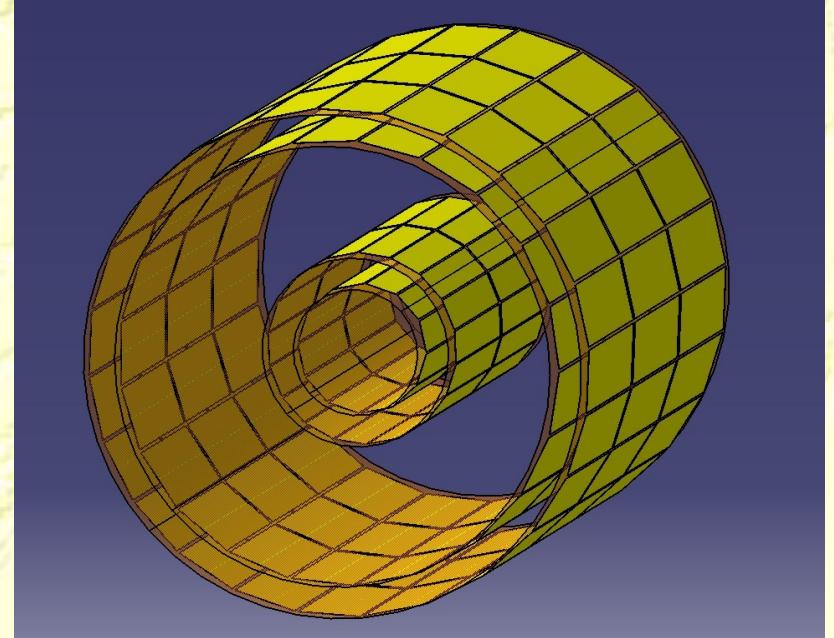
- **Tracker: Mechanical Stability / Construction studies**
- **Cooling studies**
- **MAPS HV CMOS design**  
first funding (50k€) for sensor prototype submission
- **Broken Line Fits and Fast Online Track Reconstruction**

# Summary

- Novel detector concept for  $\mu \rightarrow \text{eee}$  experiment
- Technologies: **Silicon Pixel** and **Scintillating Fibers Trackers**
- sensitivity  $\text{BR}(\mu \rightarrow \text{eee}) < 10^{-16}$  seems feasible  
but more detailed simulations are required
- first pixel tracker prototype for 2012?
- could replace completed MEG experiment (in 2-3 years)
- later go to an upgraded high intensity beamline

# Conclusion

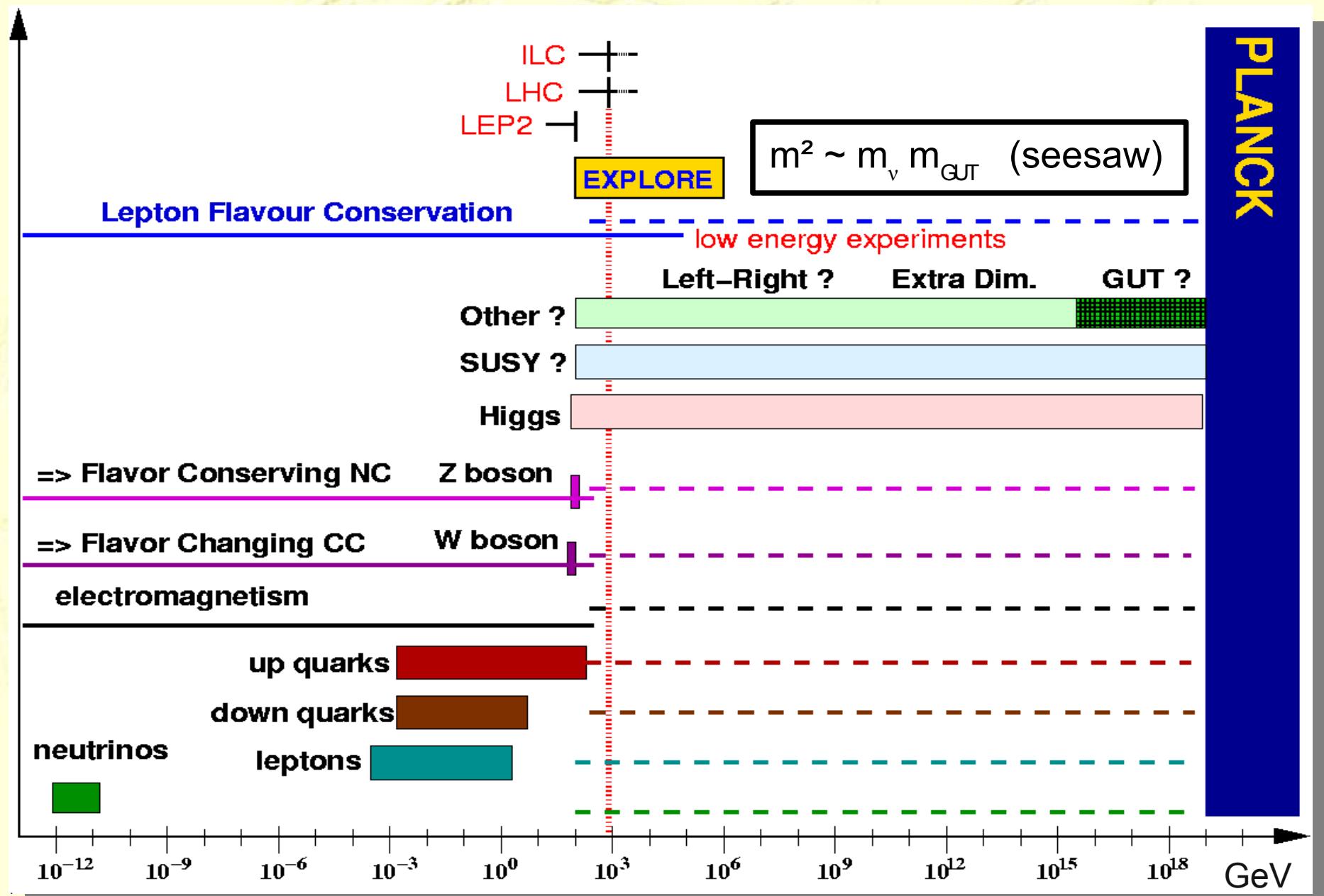
**After more than 20 years time has come to repeat a search for  $\mu \rightarrow eee$  and to repeat very a successful experiment (Sindrum)**



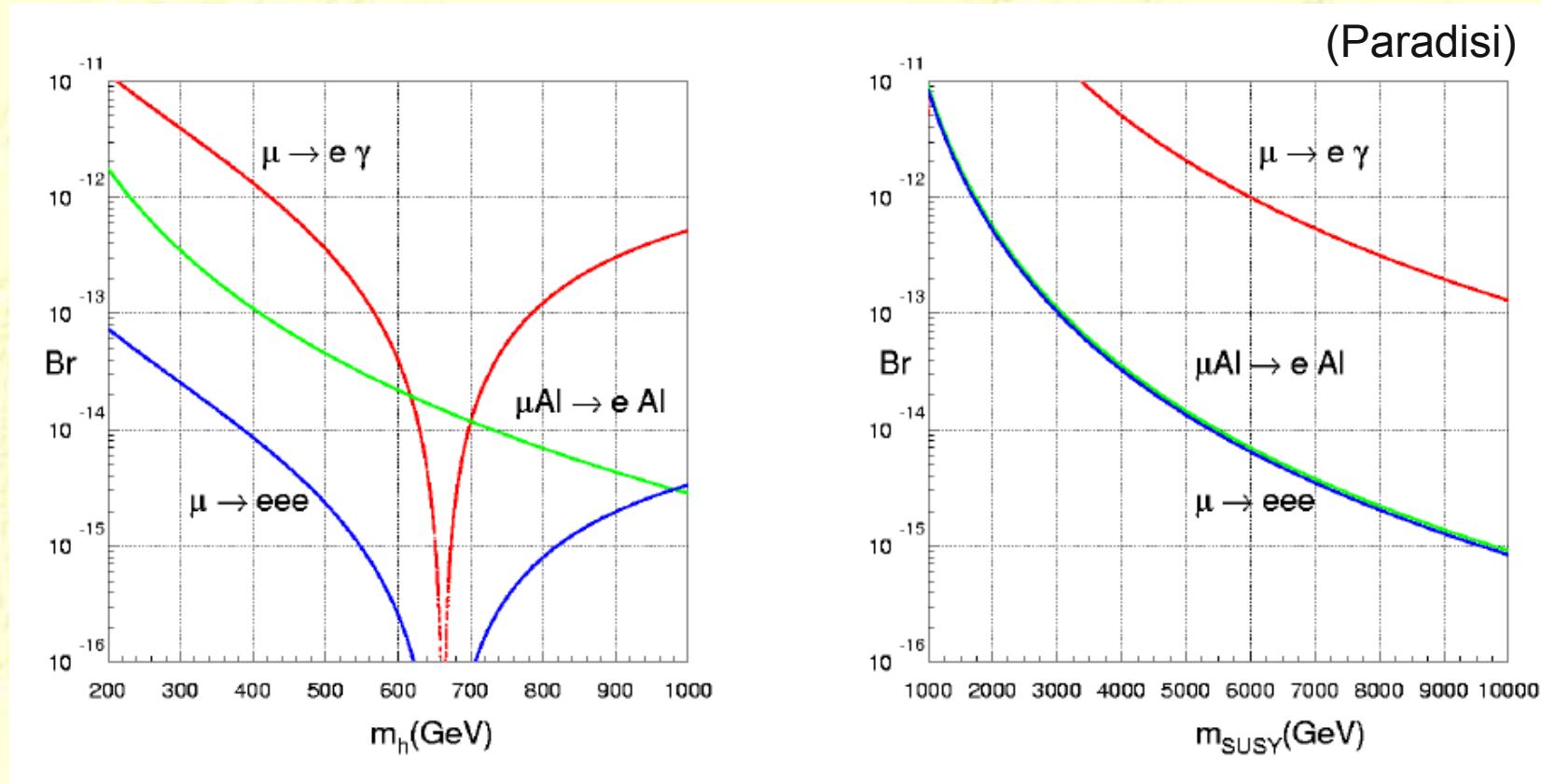
**A good detector is needed to resolve mysteries!**

# Backup

# Landscape of Mass Scales



# SUSY Higgs mediated LFV



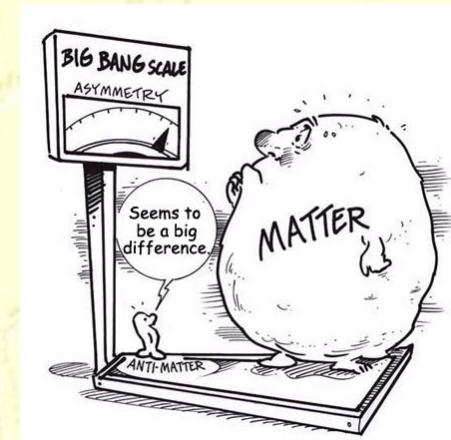
# Leptogenesis

Matter–anti matter asymmetry in the universe requires:

- Baryogenesis (Sacharov)
  - baryon number violation
  - CP (T) violation
  - non equilibrium process
- Leptogenesis (alternative)
  - lepton number violation
  - CP phase in lepton matrix
  - non equilibrium process

→ baryogenesis (sphaleron process)

(measured but small)



(not observed)

(might be measured by  $\nu$  oscillation)

➤ lepton flavor violation is a consequence of lepton number violation and CP phases

# Optimum Momentum Resolution

- minimum three layers → six coordinates
- momentum resolution multiple scattering dominated:

3 layers equidistant:

$$\frac{\sigma_p}{p} = 2 \frac{b}{BL}$$

4 layers equidistant:

$$\frac{\sigma_p}{p} = \frac{3}{\sqrt{2}} \frac{b}{BL} \approx 2.12 \frac{b}{BL}$$

$b \sim 0.001 \text{ Tm}$   
(for 40 $\mu\text{m}$  Silicon)

>4 equidistant layers:

$$\frac{\sigma_p}{p} = \frac{N-3}{\sqrt{N-2}} \frac{b}{BL} \approx \sqrt{N} \frac{b}{BL}$$

- resolution is given by  $1/BL$ 
  - but minimum momentum given by  $p_{\min} \sim BL$

# DAQ

- Number of (zero suppressed) channels in Silicon ~10-20 million
- Number of channels in Fiber Tracker 5-10k
- What matters is the events rate of  $\sim 10^9$ 
  - + data rate ~ 16 Gbyte/s
  - + triggerless readout (software filter only)

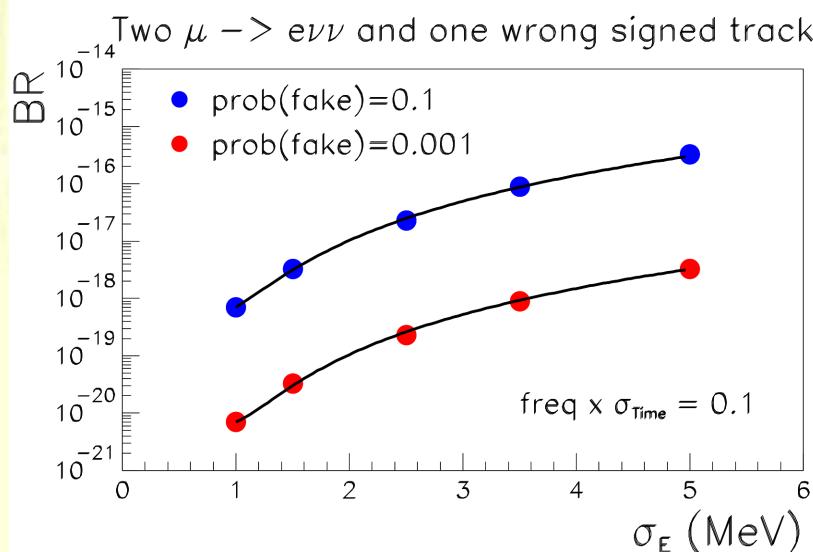
# Combinatorial Background

## Design Parameters:

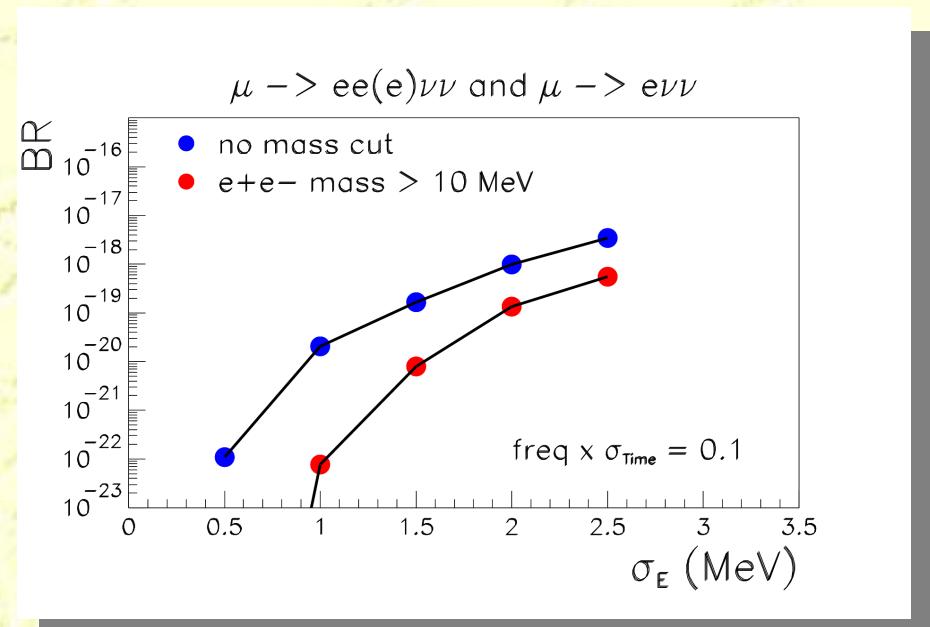
- prob (coincidence vertex) =  $5 \cdot 10^{-5}$
- prob (coincidence time) = 0.1

## BG as function of $E_{\text{tot}}$

fake track and two muon decays



internal conversion and muon decay

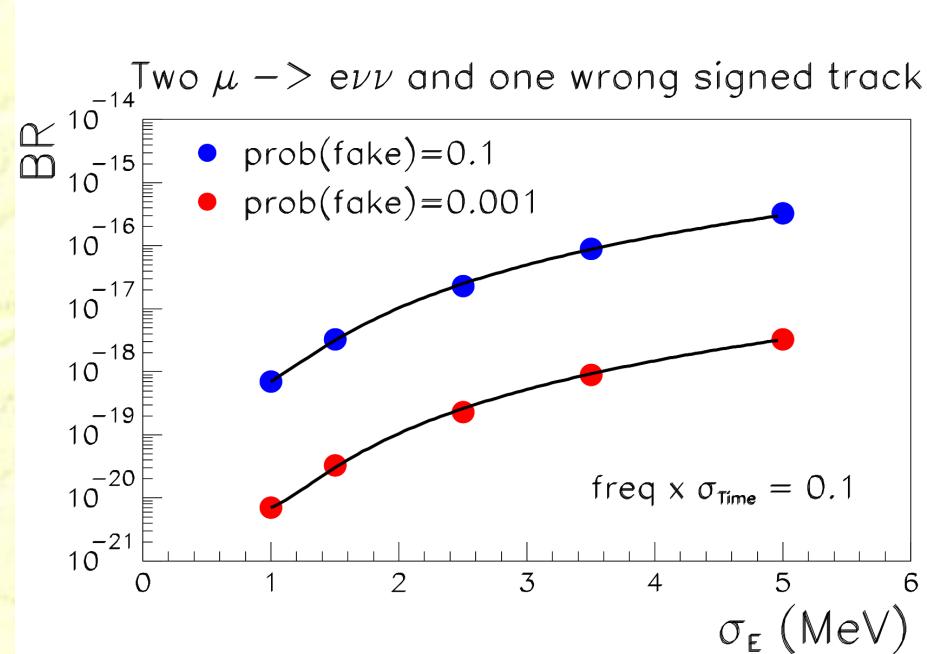


combinatorial BG can be ignored already for moderate energy resolution  $\sigma_E < 3$  MeV

# Maximum Muon Beam Intensity?

- Combinatorial Background increases!
- The maximum tolerable muon intensity depends mainly on vertex, timing, and tracking resolution (also fake rate).
- assuming that the fake track reconstruction rate is small (0.001) a sensitivity of  $10^{-17}$  could be achieved with beam intensities of  $3 \cdot 10^{10}$  muon stops/s

BG  $\sim$  rate<sup>2</sup>



# A new Silicon Detector for MEG?

Expected performance for electron  $p=53$  MeV/c:

$\sigma_p = 0.3\text{-}0.6$  MeV/c      (MEG 0.7 MeV/c)

$\sigma_\theta \sim 5$  mrad      (MEG 8 mrad)

$\sigma_{vtx} \sim 0.15$  mm      (MEG 1.4-2.5 mm)

momentum resolution could be further improved by increasing the lever arm:  
e.g. 13 cm → 20 - 25cm