

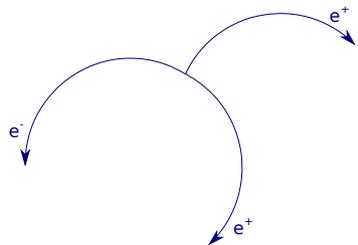
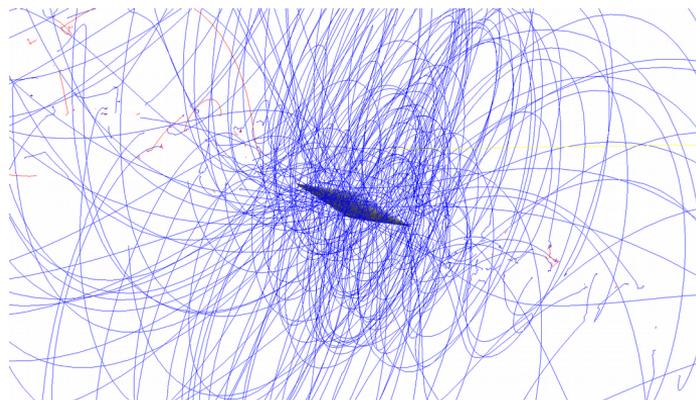
Online Track Reconstruction on GPUs for the Mu3e and LHCb experiments

IEEE Real Time 2018, Williamsburg, VA
Dorothea vom Bruch
For the Mu3e and LHCb Collaborations
June 11th, 2018



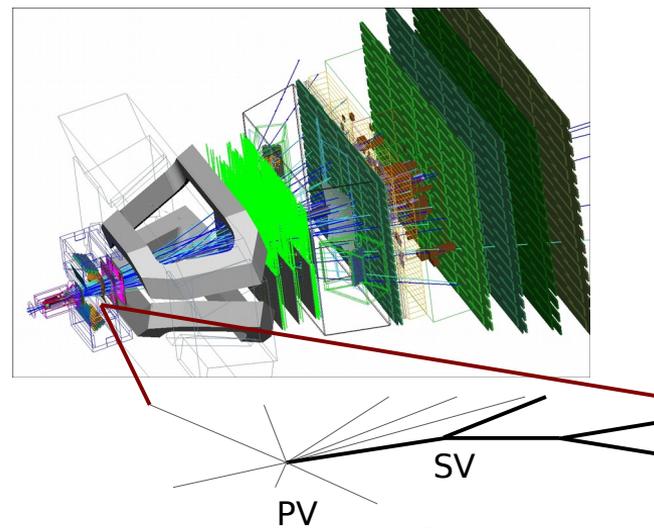
Why Reconstruct Tracks Online?

Mu3e: $\mu^+ \rightarrow e^+e^-e^+$



Continuous muon beam

LHCb: Specific decays



Study b- and c-hadrons

LHC bunch crossing at 40 MHz

Find specific track patterns

Challenges

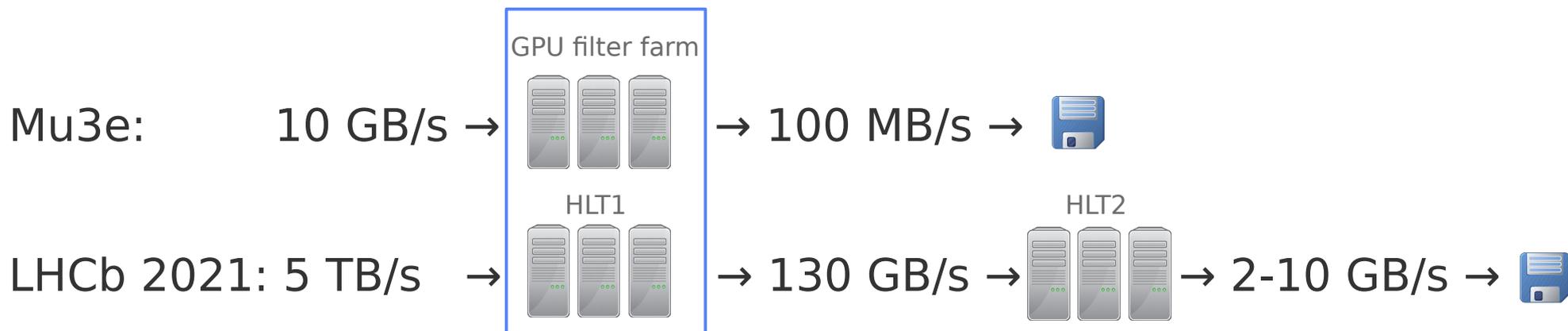
- No “easy” pattern to be used by hardware triggers
- Reconstruct all tracks at MHz rates
- Reduce data stream:

Mu3e: 10 GB/s →  → 100 MB/s → 

LHCb 2021: 5 TB/s →  → 130 GB/s →  → 2-10 GB/s → 

Challenges

- No “easy” pattern to be used by hardware triggers
- Reconstruct all tracks at MHz rates
- Reduce data stream:



Track reconstruction

Why Consider GPUs?

- Need many FPs/s at low cost
 - Care about high throughput
 - Market changing rapidly → be flexible with design choice
- Go massively parallel on GPUs

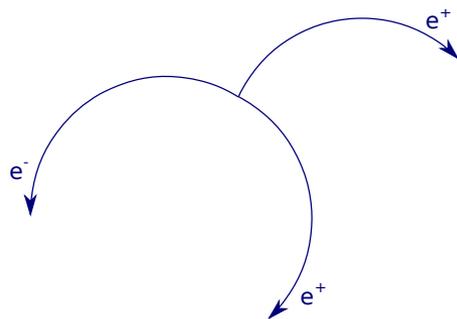


Image sources: <http://images.anandtech.com>,
<http://images.nvidia.com/pascal>

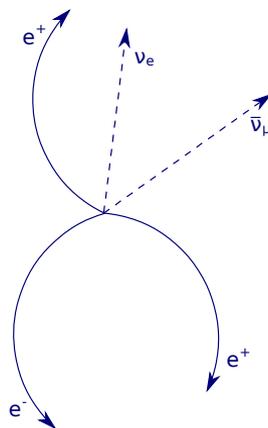
Mu3e

Mu3e Phase I

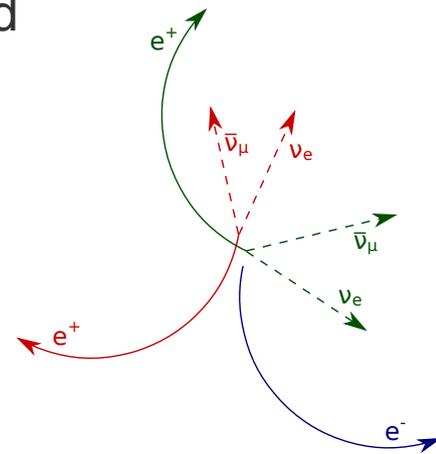
- Search for charged lepton flavour-violating decay $\mu^+ \rightarrow e^+e^-e^+$ with a sensitivity in branching ratio better than $2 \cdot 10^{-15}$
- In Standard Model: suppressed to $BR < 10^{-54}$
- Any hint of signal \rightarrow new physics
- Located at Paul-Scherrer Institute (PSI), Switzerland



Signal

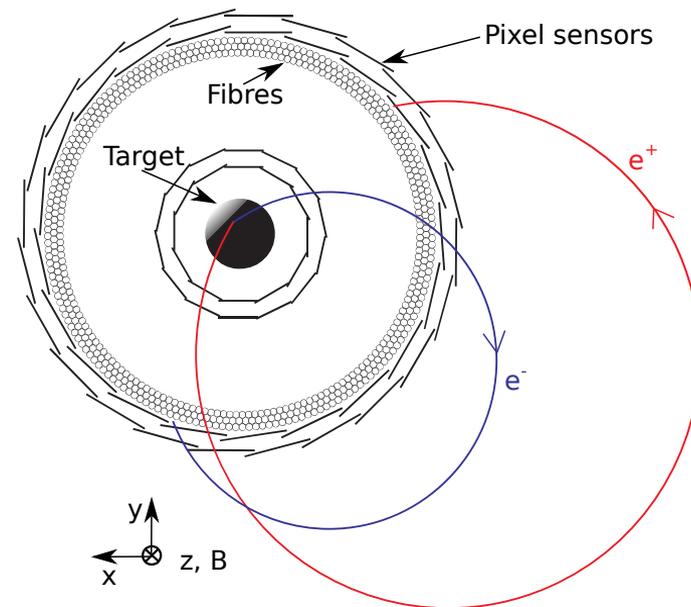
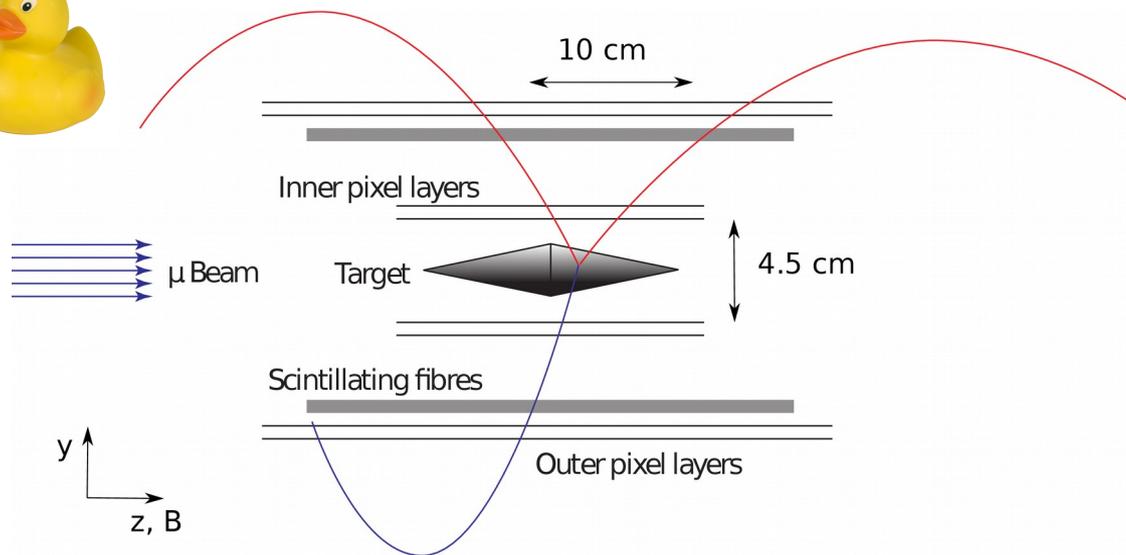


Internal conversion



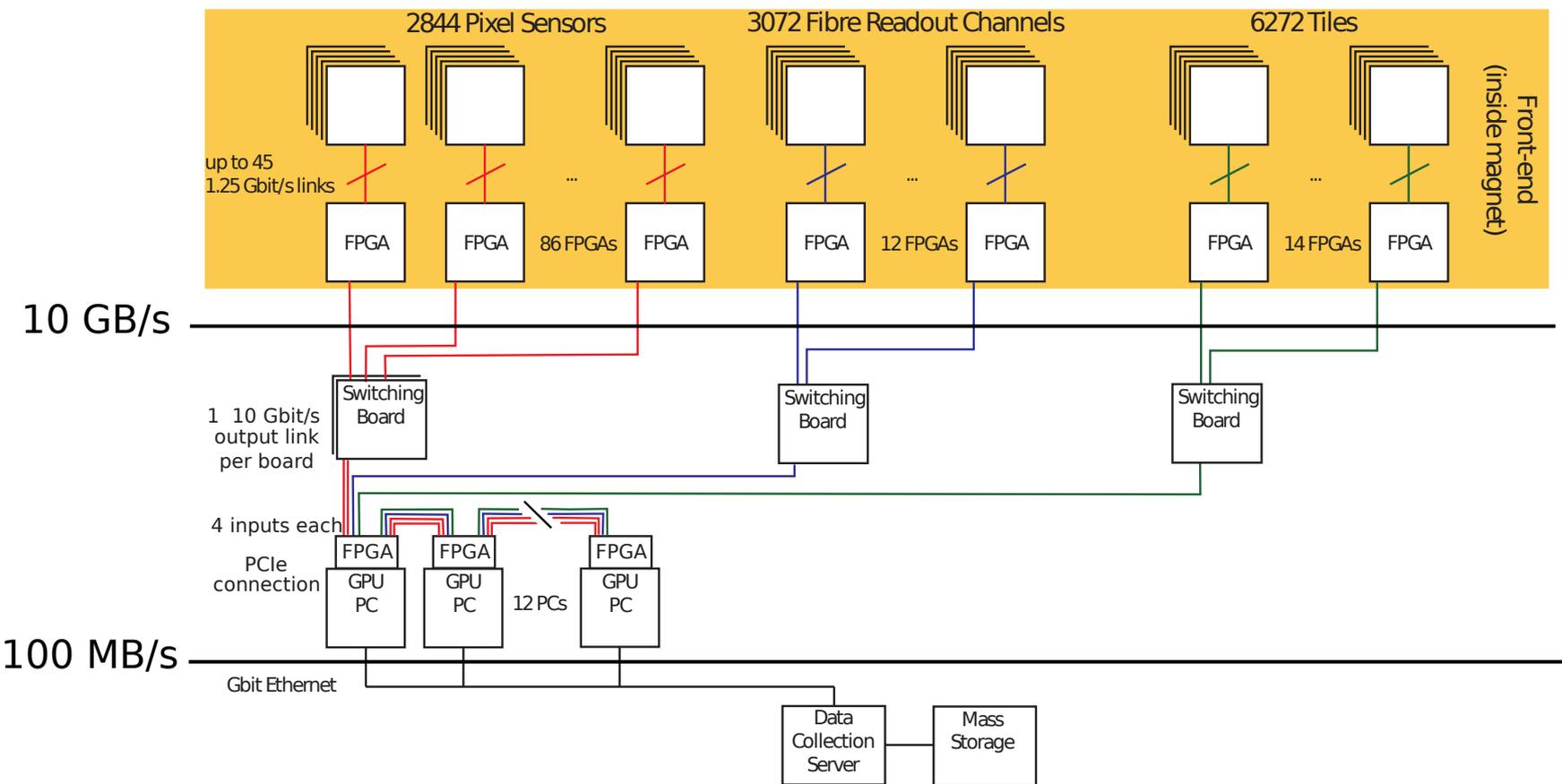
Combinatorics

Mu3e Detector, Central Region

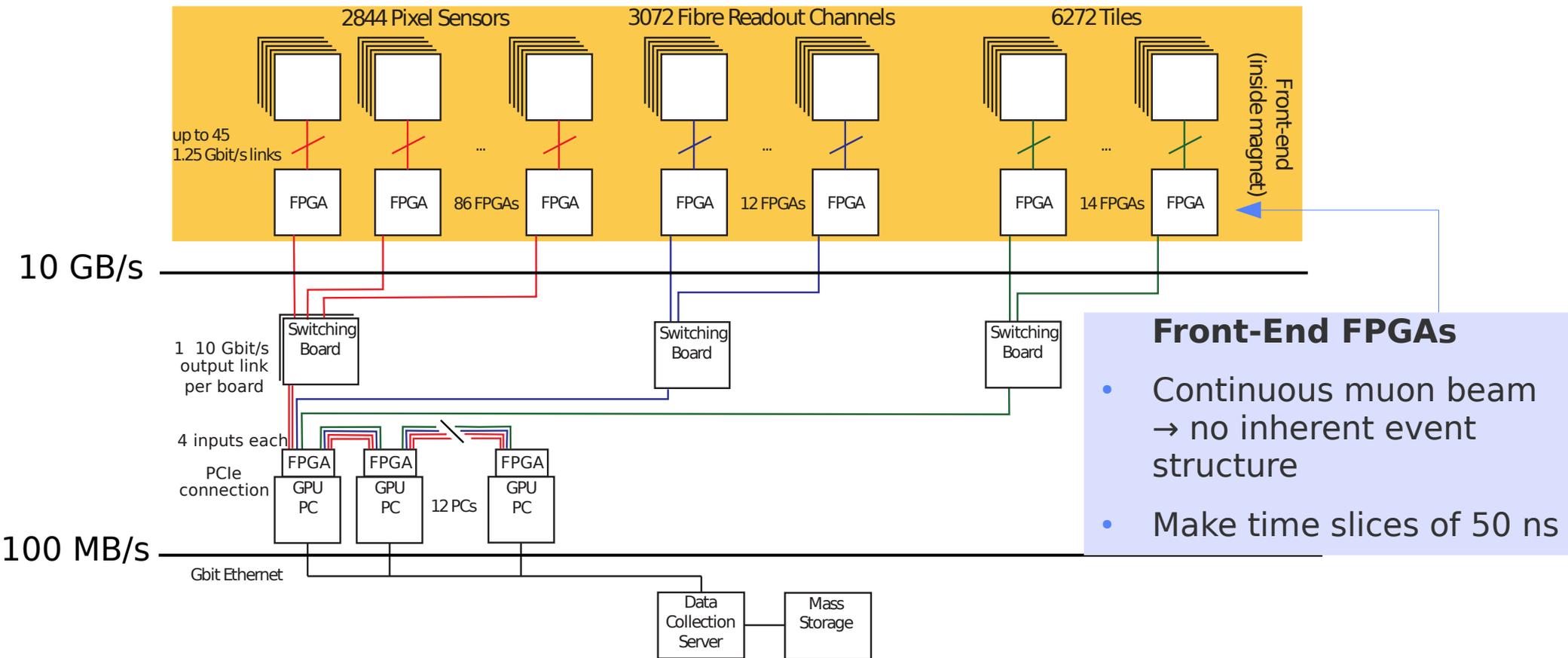


$10^8 \mu/s$ stopped on target, in solenoidal magnetic field

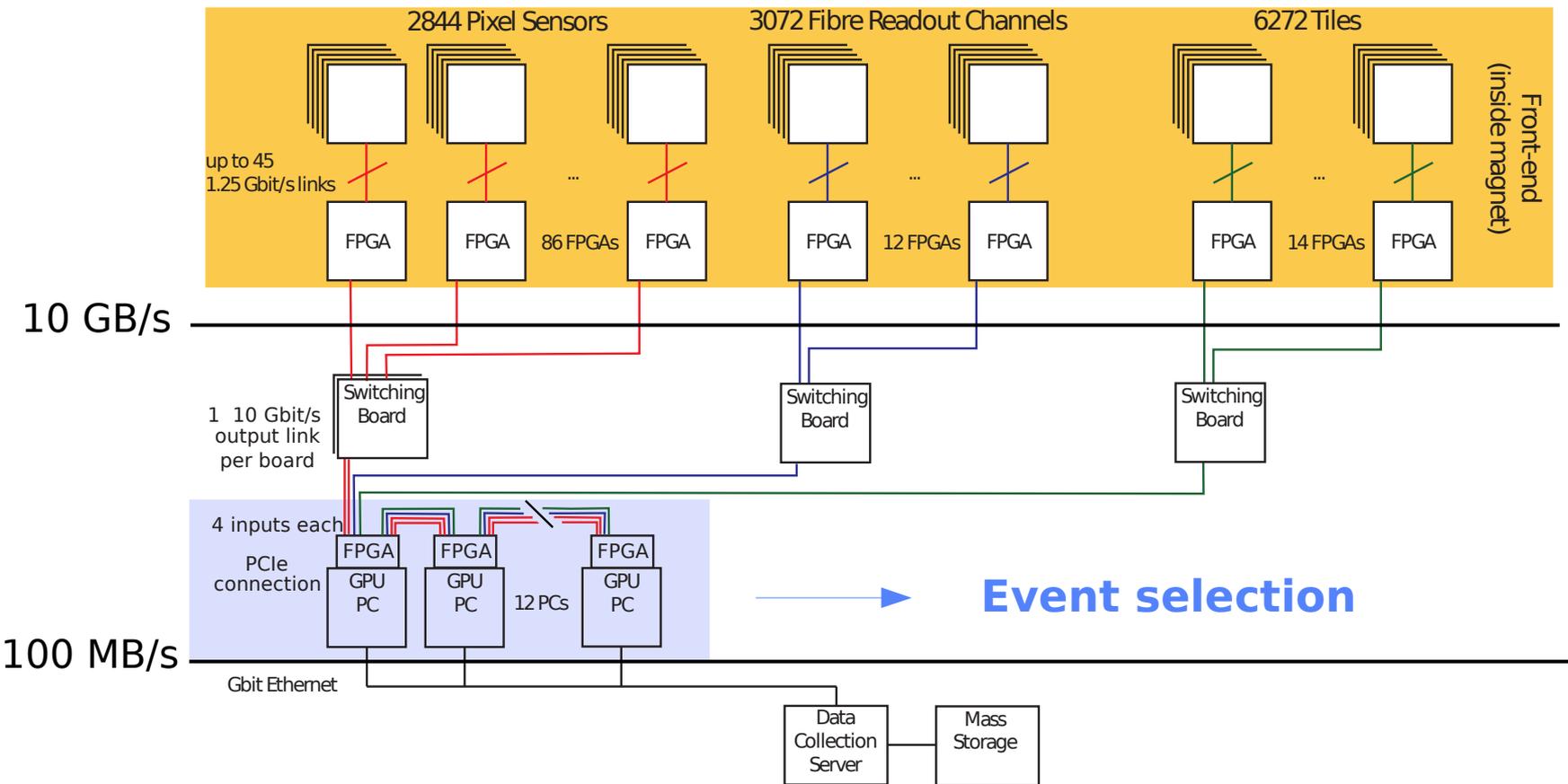
Mu3e Readout Scheme



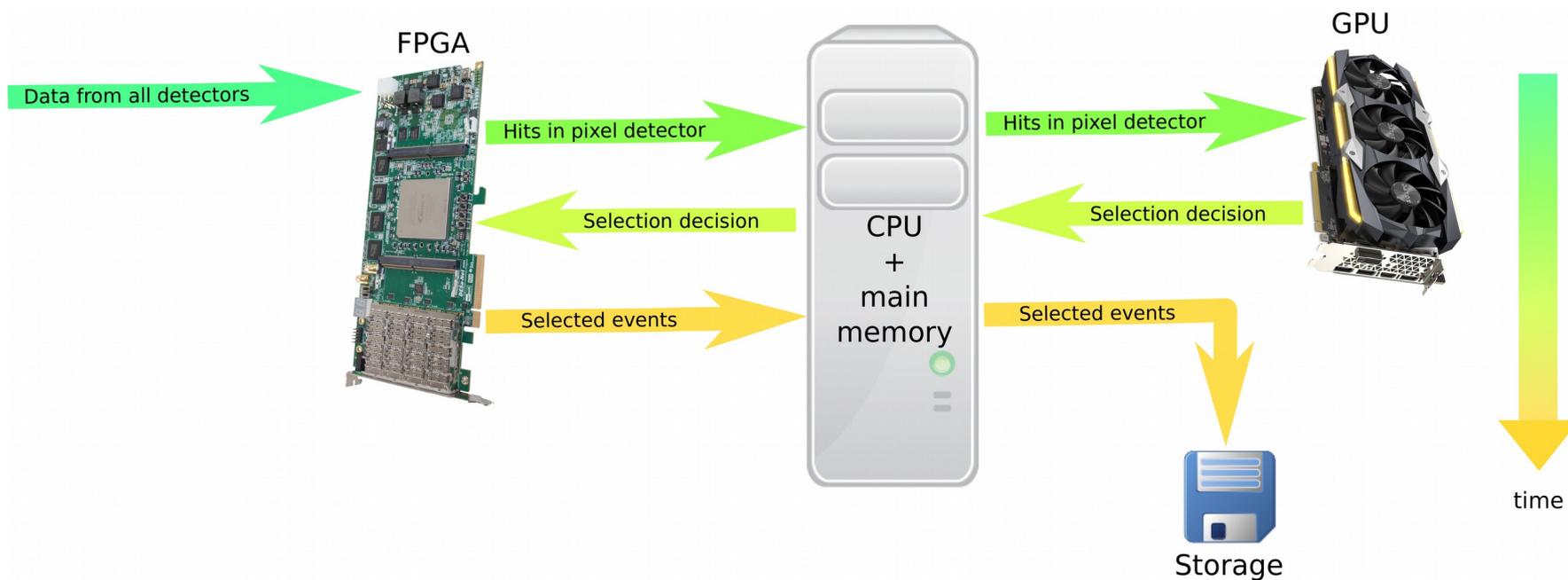
Mu3e Readout Scheme



Mu3e Readout Scheme

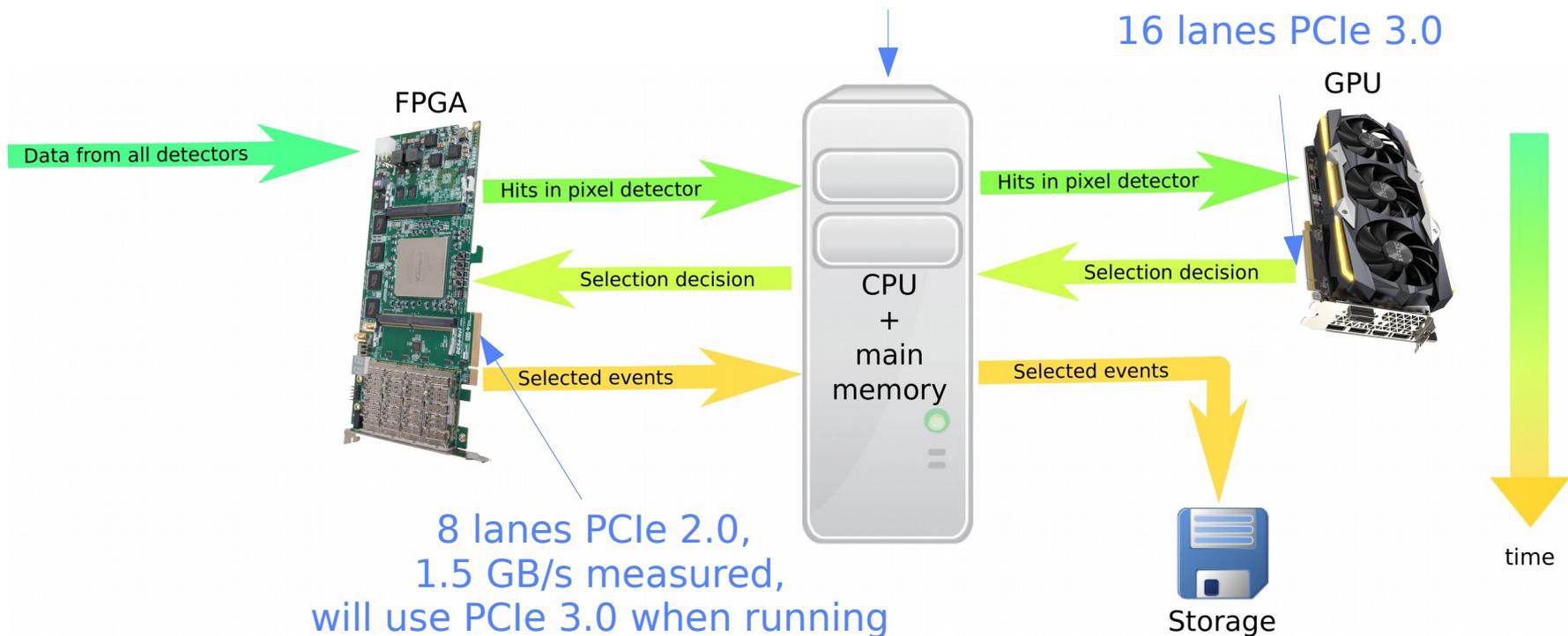


Data Flow



Data Flow

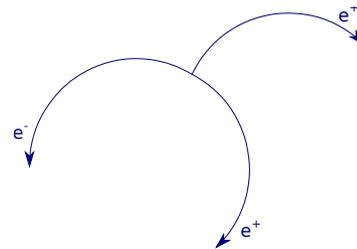
Direct Memory Access (DMA) to and from one memory buffer in main memory
→ No extra copy



Mu3e: Find 3 Signal Tracks



FPGA



GPU



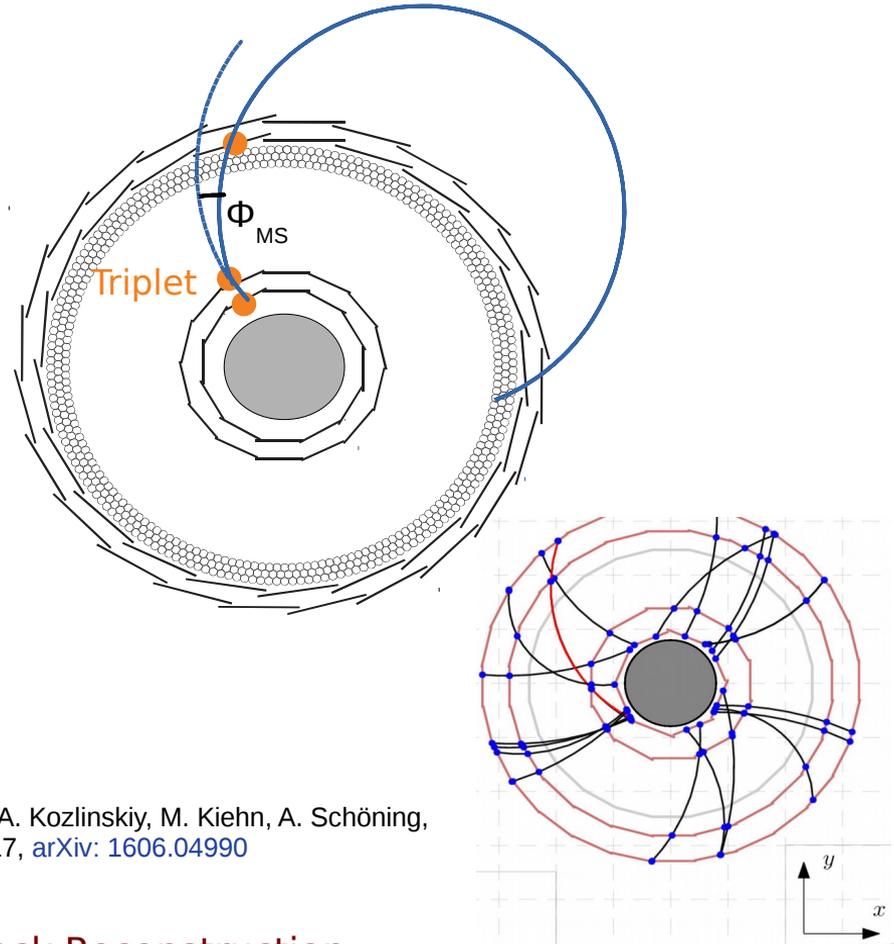
Find combinations of hits in first 3 layers	Fit tracks with fit developed for multiple scattering dominated resolution
Transfer these + hits in 4 th layer to GPU	
Reduce 3-hit combinations by factor 70	

Currently emulated on GPU

Mu3e: Multiple Scattering Fit

- Electrons: 12 - 53 MeV/c
- Resolution dominated by multiple Coulomb scattering
- Ignore hit uncertainty
- Three consecutive hits: “triplet”
- Assume multiple scattering at middle hit, minimize χ^2

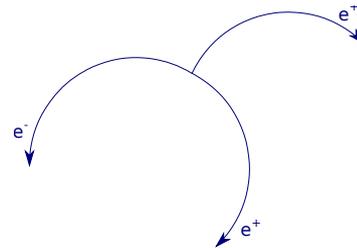
$$\chi^2 = \frac{\Phi_{MS}^2}{\sigma_{MS, \Phi}^2} + \frac{\theta_{MS}^2}{\sigma_{MS, \theta}^2}$$



Mu3e: Find 3 Signal Tracks



FPGA



GPU

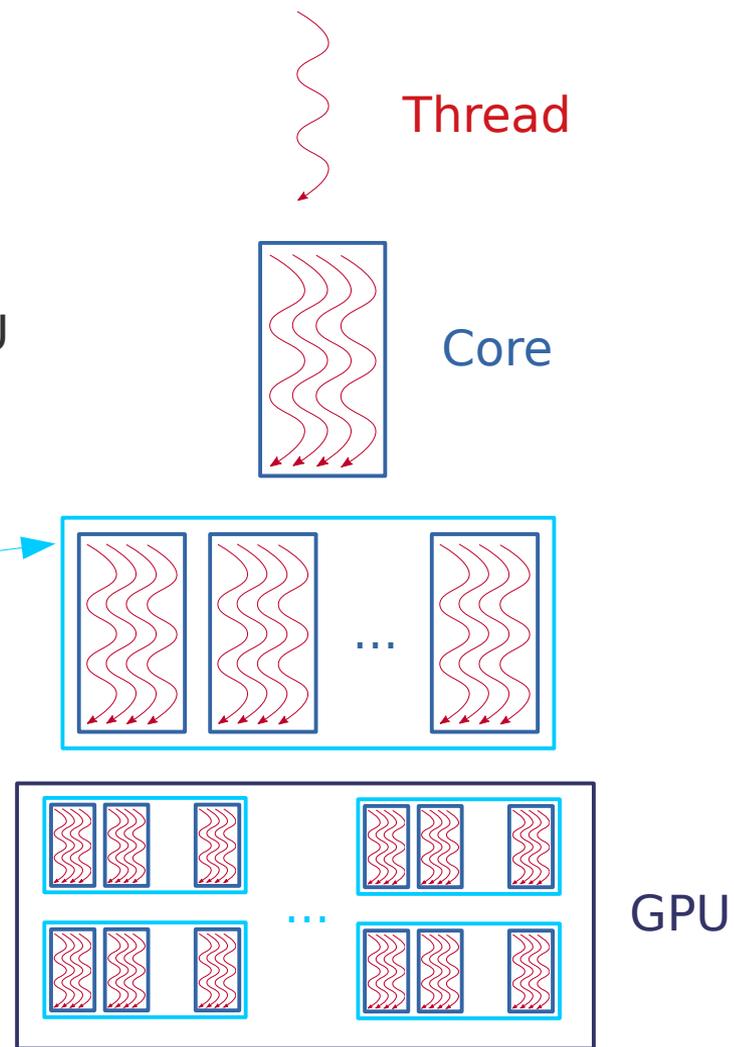
Find combinations of hits in first 3 layers	Fit tracks with fit developed for multiple scattering dominated resolution
Transfer these + hits in 4 th layer to GPU	Positive tracks Negative tracks Select combinations of 2 positive, 1 negative track from one vertex, based on circle intersections
Reduce 3-hit combinations by factor 70	Reduce # of time slices by factor 140

Signal selection efficiency: 98%

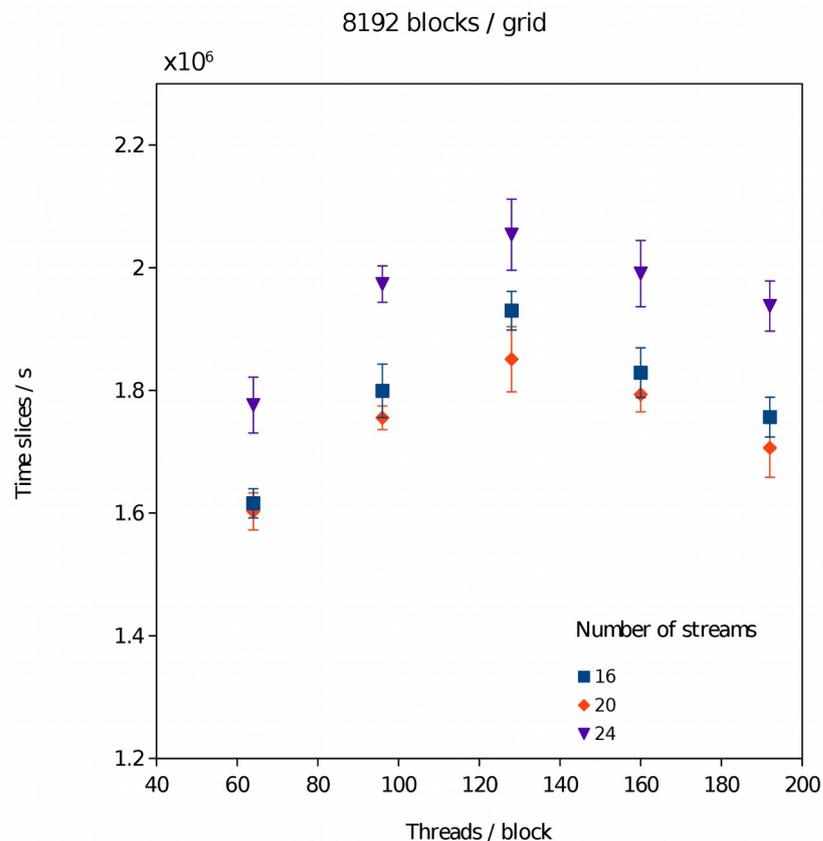
Currently emulated on GPU

GPU Architecture

- Lower frequency, higher cache latency than CPU
- Thousands of threads → hide latency
- SIMD: Single Instruction Multiple Data
- Threads in lockstep: Run on one **multiprocessor** unit in parallel, execute the same instruction
- Thread count per multiprocessor typically multiple of ALU count
- Threads on different cores / multiprocessors: completely independent of each other

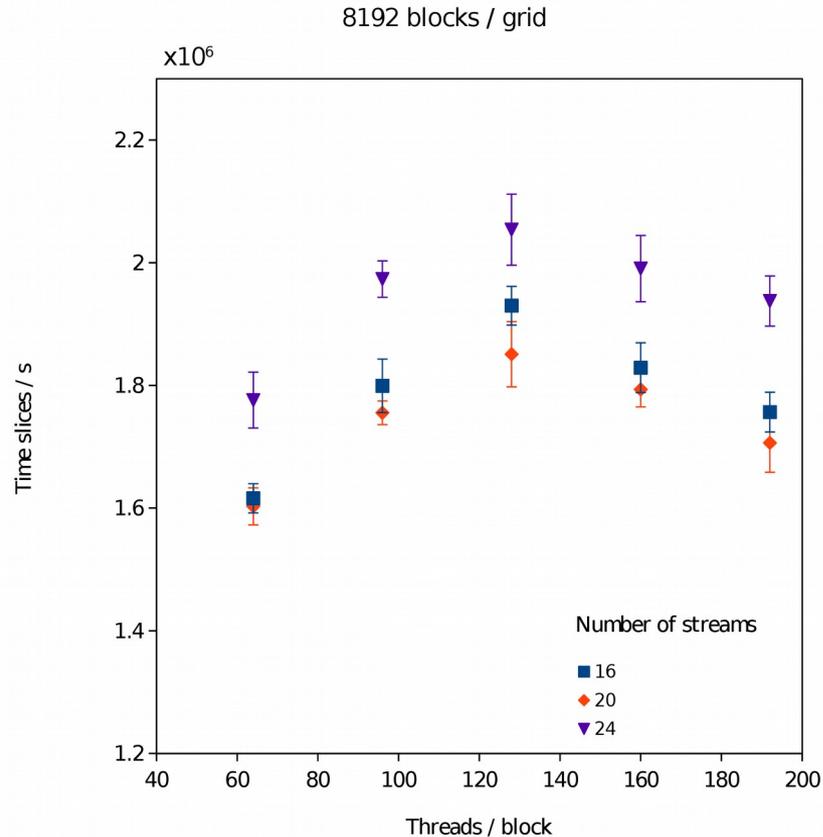


Mu3e Online Selection on GPUs



- Use 24 streams \rightarrow memory copy & computations concurrently
- Optimize grid: launch 8192 time slices in one grid, with 128 threads / block
- Optimized memory layout, prepare it on FPGA (3-hit pre-selection)
- Use single precision

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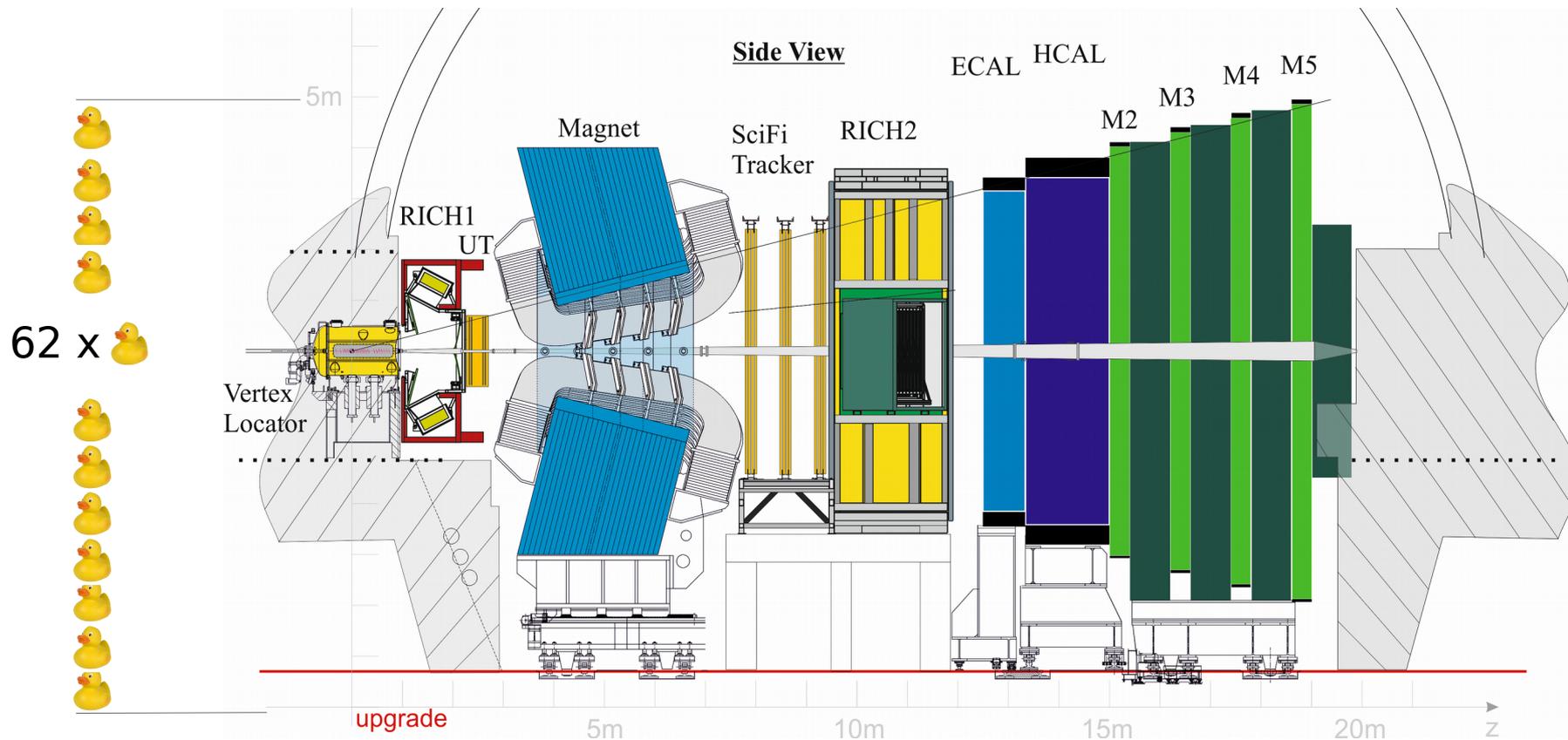
Process $2 \cdot 10^6$ time slices / s on one GTX1080Ti
 \rightarrow 12 PCs enough, meet requirements :-)

D. vom Bruch, [PhD thesis](#), 2017, Heidelberg University

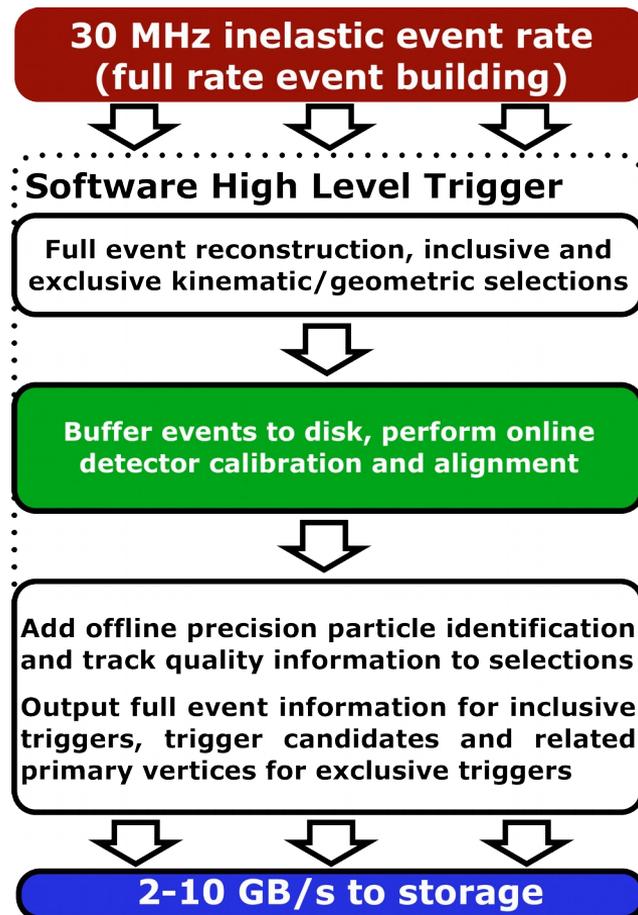
LHCb

LHCb Detector (2021+)

@ LHC, CERN, Switzerland



LHCb Software Trigger



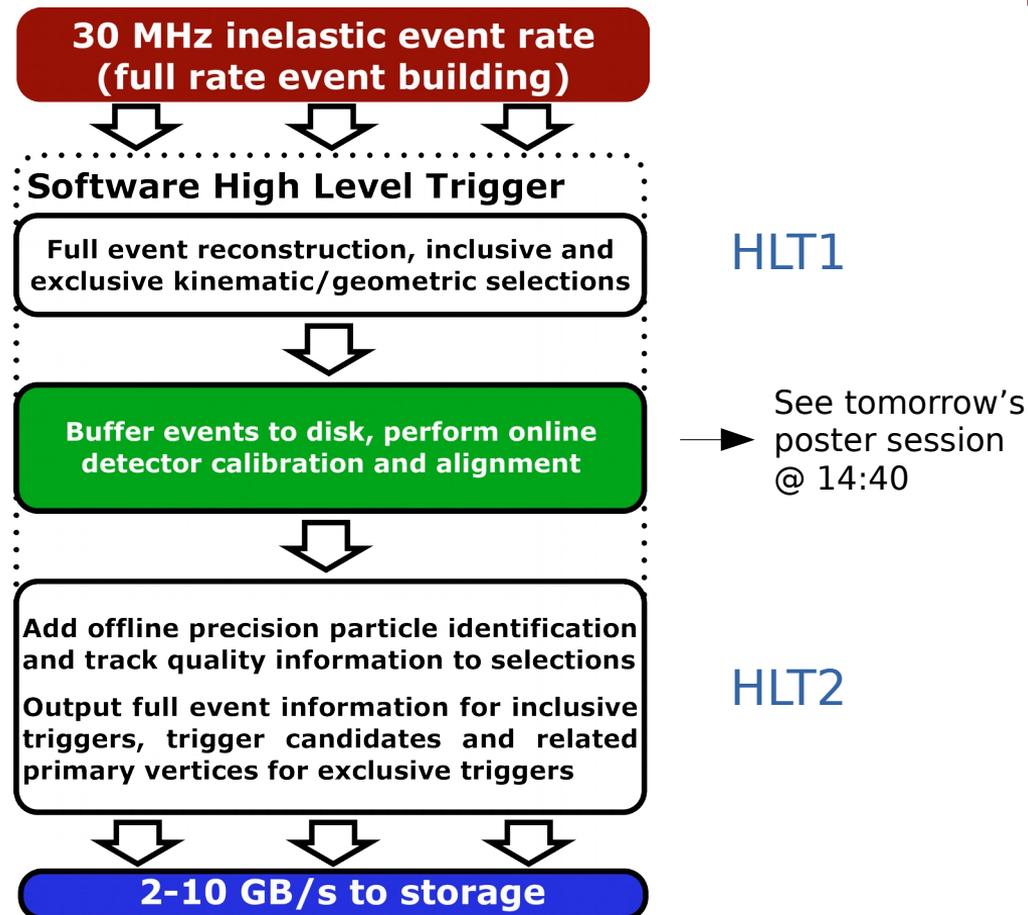
HLT1

→ See tomorrow's
poster session
@ 14:40

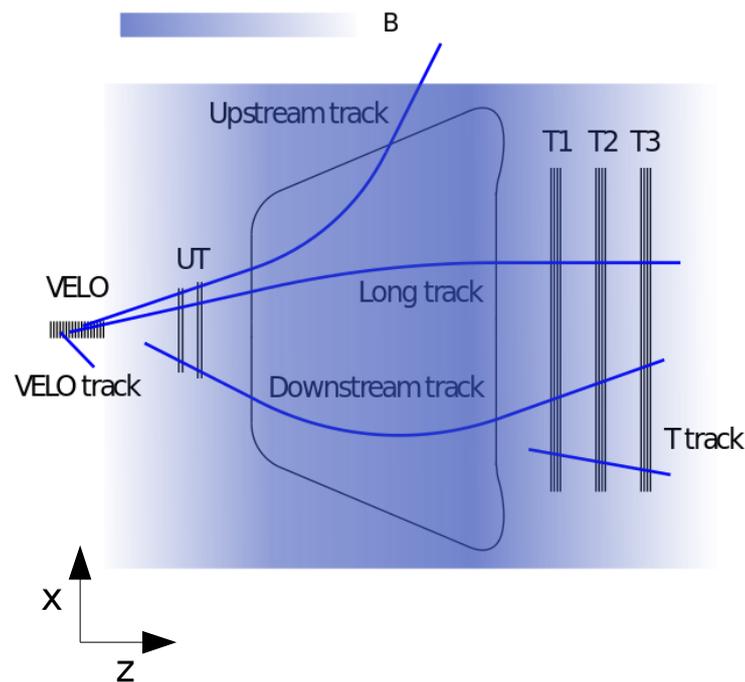
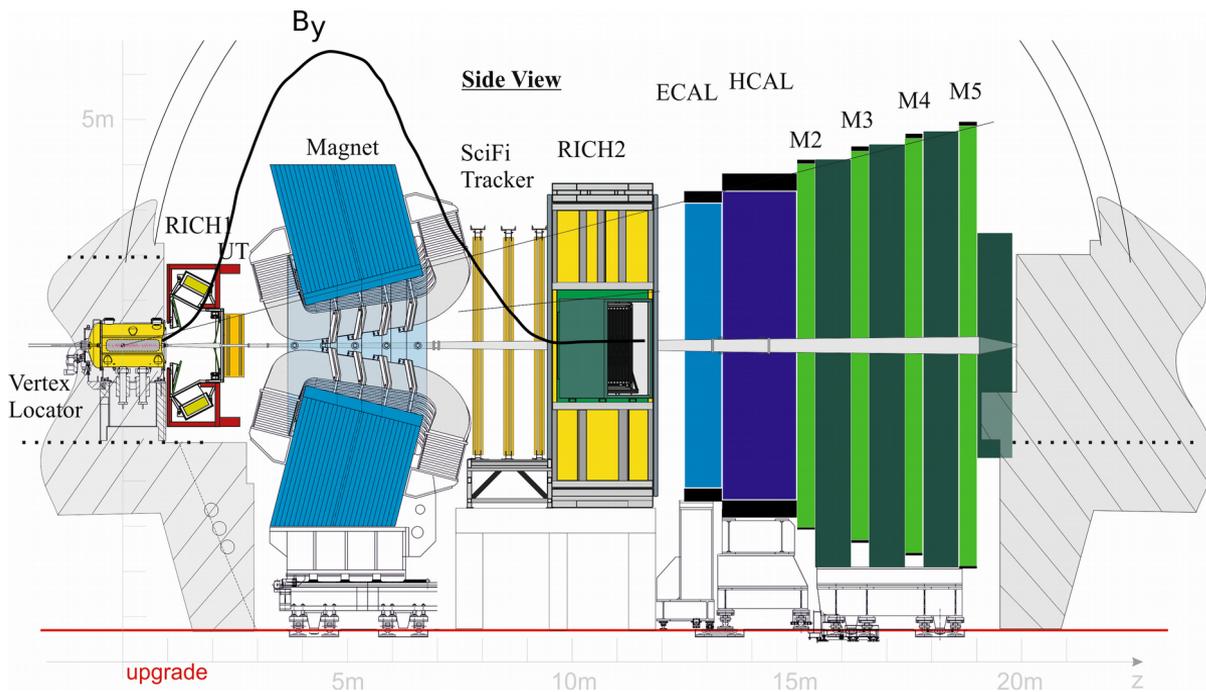
HLT2

LHCb Software Trigger

- 27 GB/s beauty hadrons available → secondary vertices alone do not suffice → need further selection
- Computing challenge
- Study different architectures → choose the one with best physics performance / \$
- One option: run **HLT1** (or parts of it) on GPUs

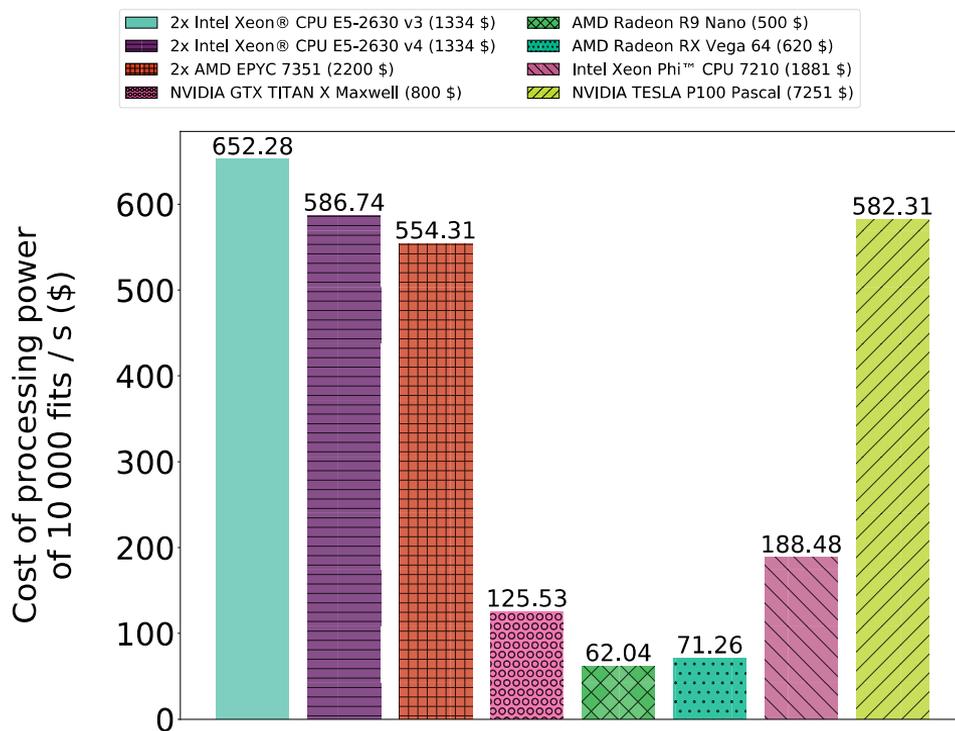


LHCb Track Reconstruction



LHCb Track Reconstruction on GPUs

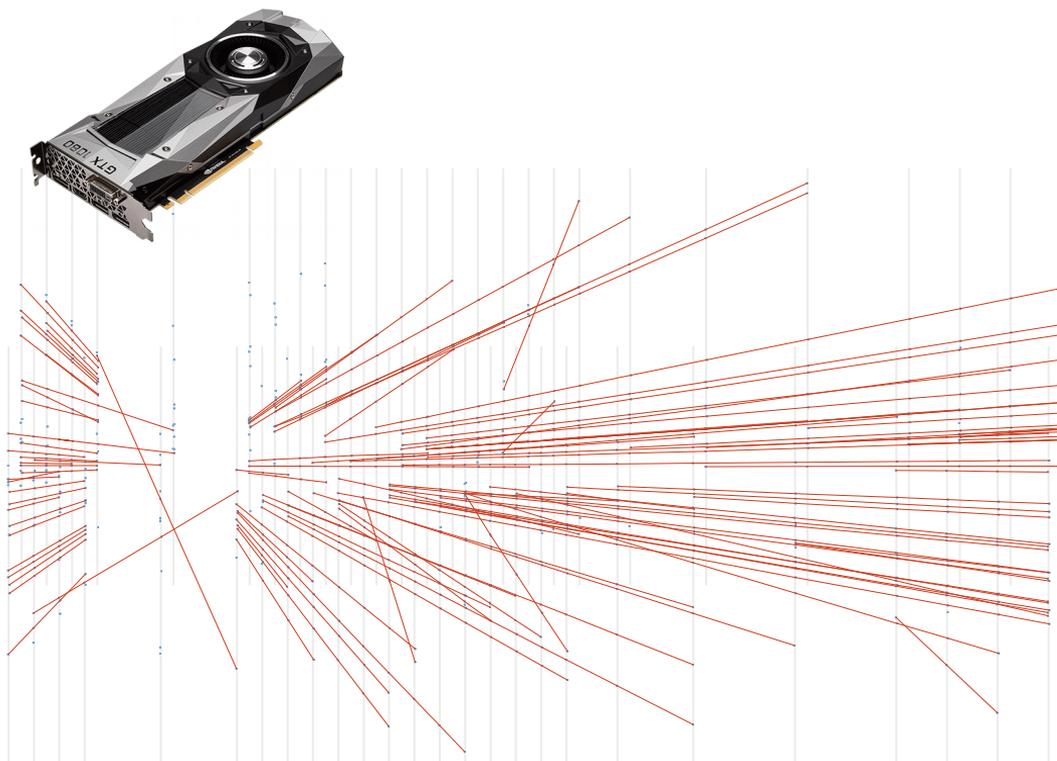
Kalman fit on various architectures



GPUs have shown to be price-performant for track fitting in LHCb

→ motivates us to study the performance of the whole sequence on GPUs

LHCb Velo Tracks on GPUs



- Tracks in VELO: straight lines
- Implemented on GPU
- Use as input for Velo → UT tracking

- Aim for similar setup as in Mu3e farm: place GPU in filter farm PC, transfer data via CPU
- GPU work: preparation for event building

A. Badalov, D. Cámpora, N. Neufeld, X. Vilasís-Cardona,
JINST, 2016, [10.1088/1748-0221/11/01/P01001](https://doi.org/10.1088/1748-0221/11/01/P01001)

LHCb: GPU Outlook

- Work in progress: VELO → UT tracking → first momentum estimate
- Later this year: add SciFi tracking and muon stations
→ full track reconstruction
- At the end of the year: Is the GPU solution realistic?



Conclusions



Mu3e

- Can reduce data rate by factor 140
- Keep 98 % of signal decays
- Process $2 \cdot 10^6$ time slices / s on one GTX1080Ti
- → Can run on the planned 12 DAQ PCs



LHCb

- Promising first results
- Velo tracking implemented on GPU
- Velo → UT tracking work in progress
- Plan: Implement full reconstruction chain

Backup

LHCb: Per Event Yields

For generator-level Monte-Carlo

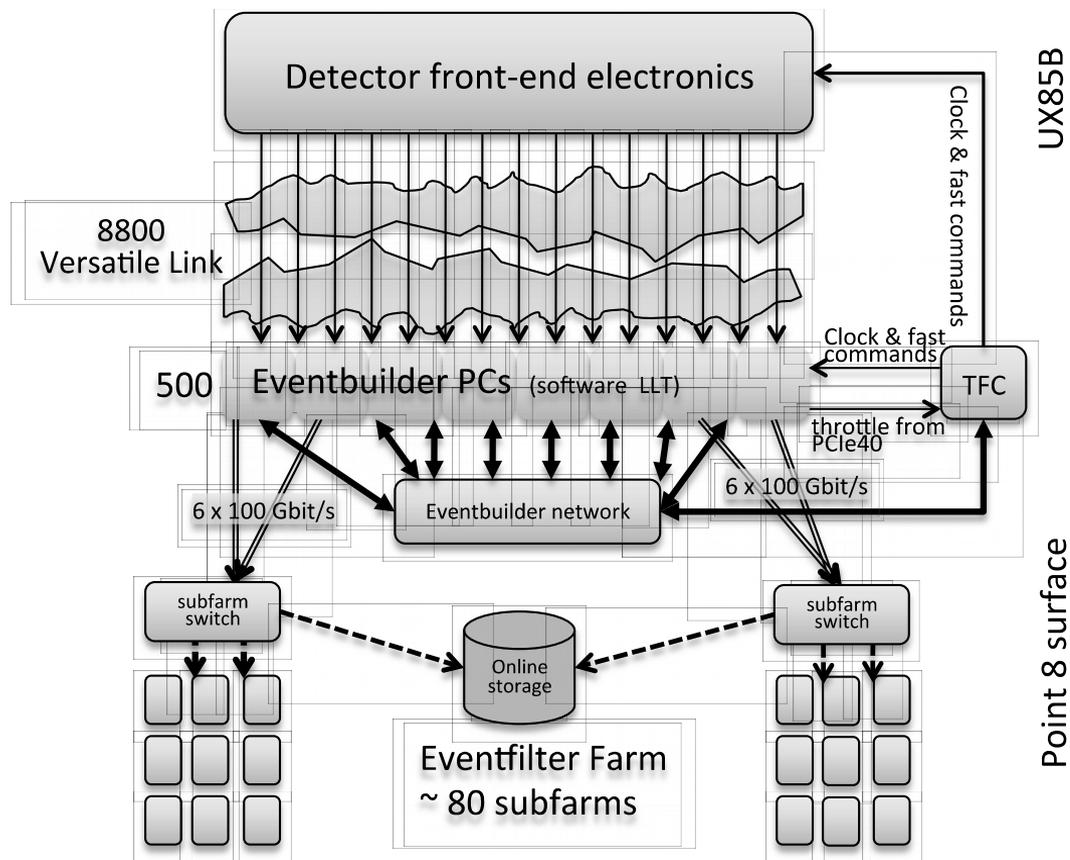
$\epsilon(\text{VELO})$: efficiency for candidates having at least two tracks traversing at least three modules in the VELO

$\epsilon(\text{LHCb})$: efficiency for candidates having all child tracks contained in the LHCb acceptance

Category	Run 1, Original VELO geometry		
	Yield in 4π	$\epsilon(\text{VELO})$	$\epsilon(\text{VELO}) \times \epsilon(\text{LHCb})$
<i>b</i> -hadrons	0.0258 ± 0.0004	$30.5 \pm 0.6\%$	$11.1 \pm 0.4\%$
<i>c</i> -hadrons	0.297 ± 0.001	$21.9 \pm 0.2\%$	$14.2 \pm 0.1\%$
light, long-lived hadrons	8.04 ± 0.01	$6.67 \pm 0.02\%$	$6.35 \pm 0.02\%$
Category	Upgrade, nominal luminosity, VELO pixel geometry		
	Yield in 4π	$\epsilon(\text{VELO})$	$\epsilon(\text{VELO}) \times \epsilon(\text{LHCb})$
<i>b</i> -hadrons	0.1572 ± 0.0004	$34.9 \pm 0.1\%$	$11.9 \pm 0.1\%$
<i>c</i> -hadrons	1.422 ± 0.001	$24.73 \pm 0.04\%$	$15.12 \pm 0.03\%$
light, long-lived hadrons	33.291 ± 0.006	$7.022 \pm 0.004\%$	$6.257 \pm 0.004\%$

Source: [LHCb Upgrade TDR, Trigger and Online](#), CERN/LHCC 2014-016

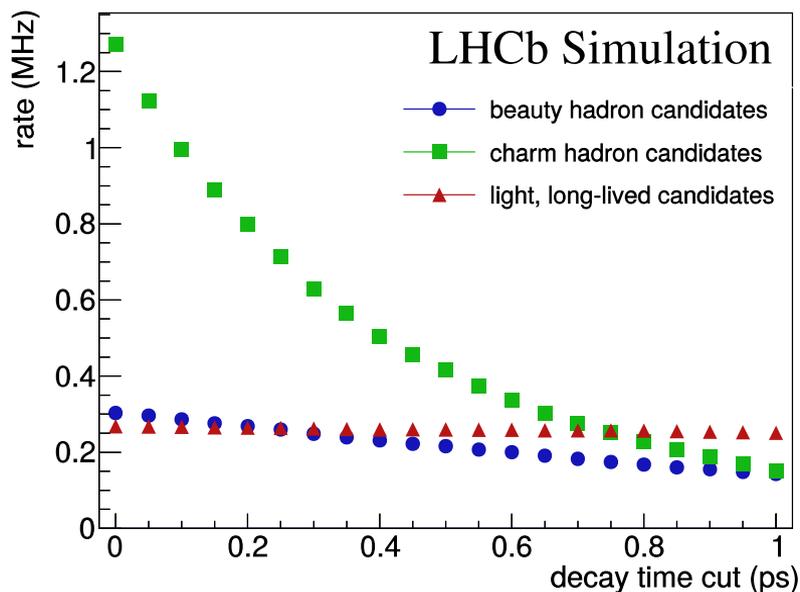
LHCb Upgrade Readout Scheme



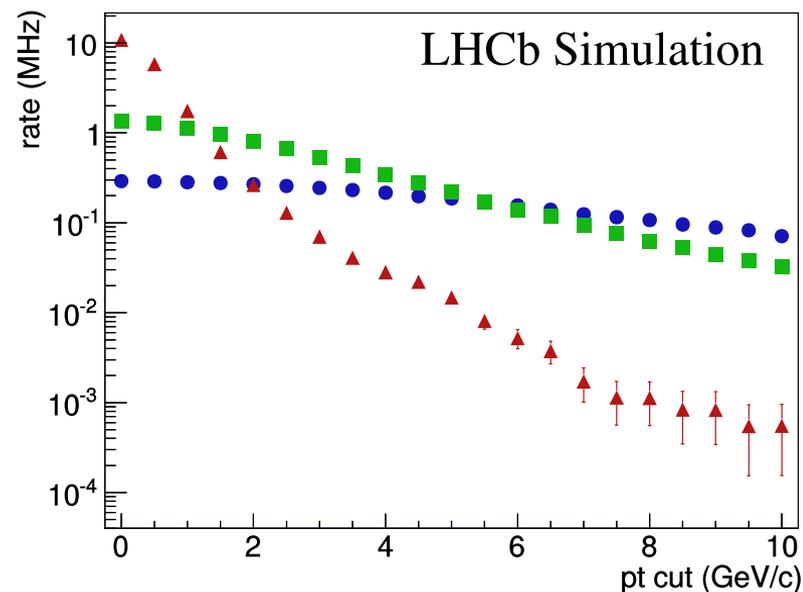
LHCb Upgrade TDR, Trigger and Online, CERN/LHCC 2014-016

LHCb: Secondary Vertices

Rates as a function of decay time cut for part. reco. candidates



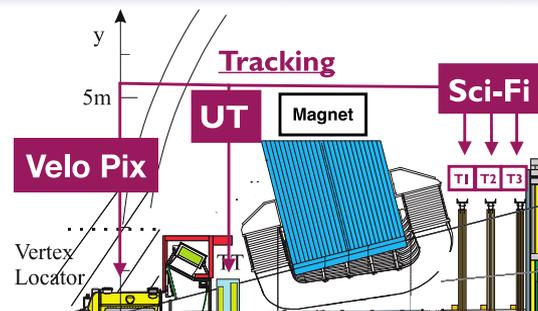
Rates as a function of pT cut for part. reco. candidates



Partial reconstruction sequence : Velo tracking and PV finding

Velo Pix

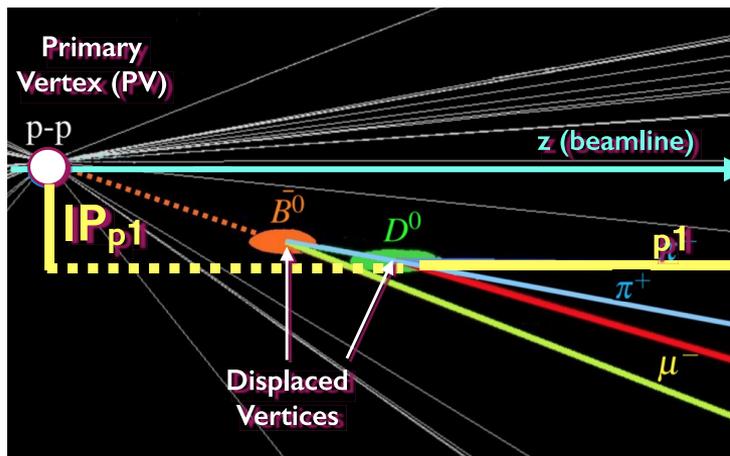
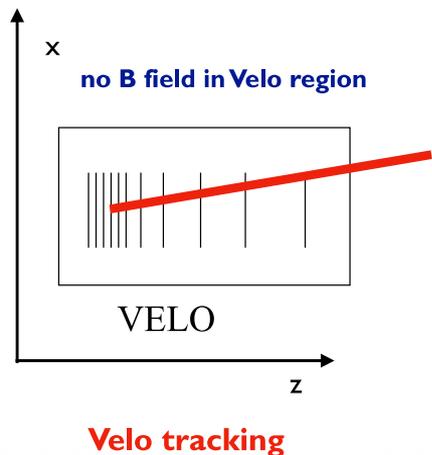
- 👉 2-D pixel sensor @-20°C: direct x-y-z measurement.
- 👉 Tracking on raw data.
- 👉 5.1 mm distance from interaction point (8.2 mm current VELO)



Velo tracking and PV reconstruction

Velo tracks used to find the PVs.

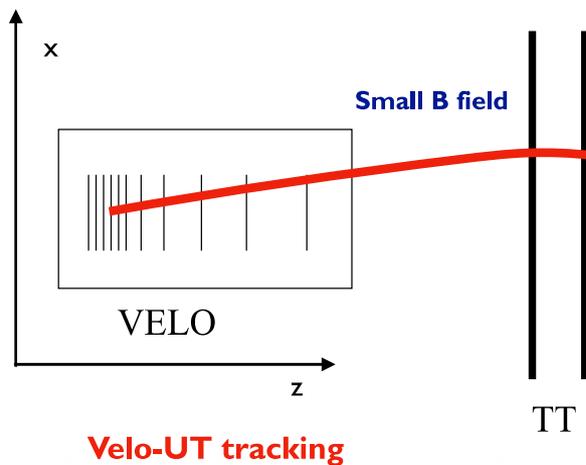
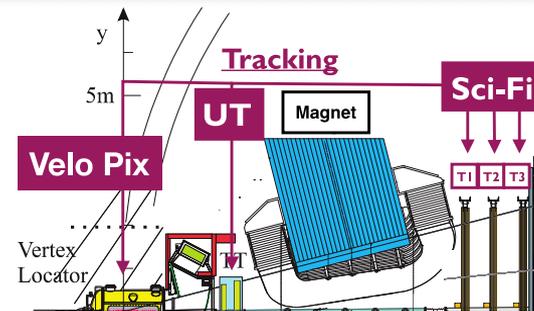
PV position used to identify displaced tracks in the event.



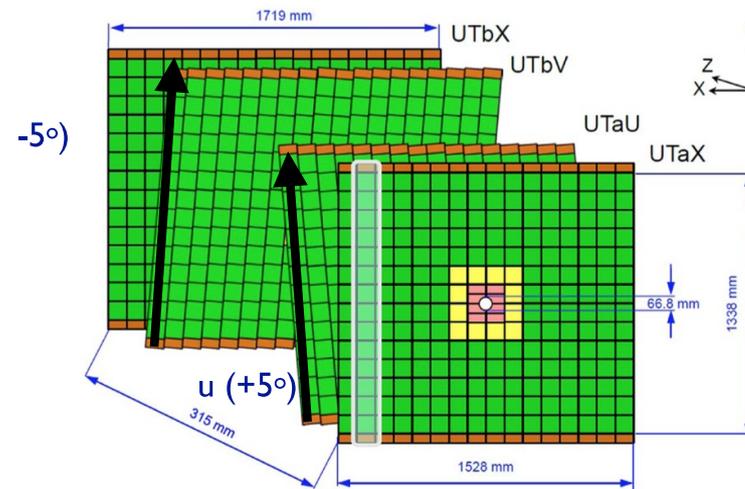
Partial reconstruction sequence : Velo-UT tracking

Upstream tracker (UT)

- 👉 Larger acceptance in central region
- 👉 Reduced thickness
- 👉 Improved $\sigma_{x-z} \sim 50 \mu\text{m}$
- 👉 Achievable $\Delta p/p \sim 15\text{-}30\%$



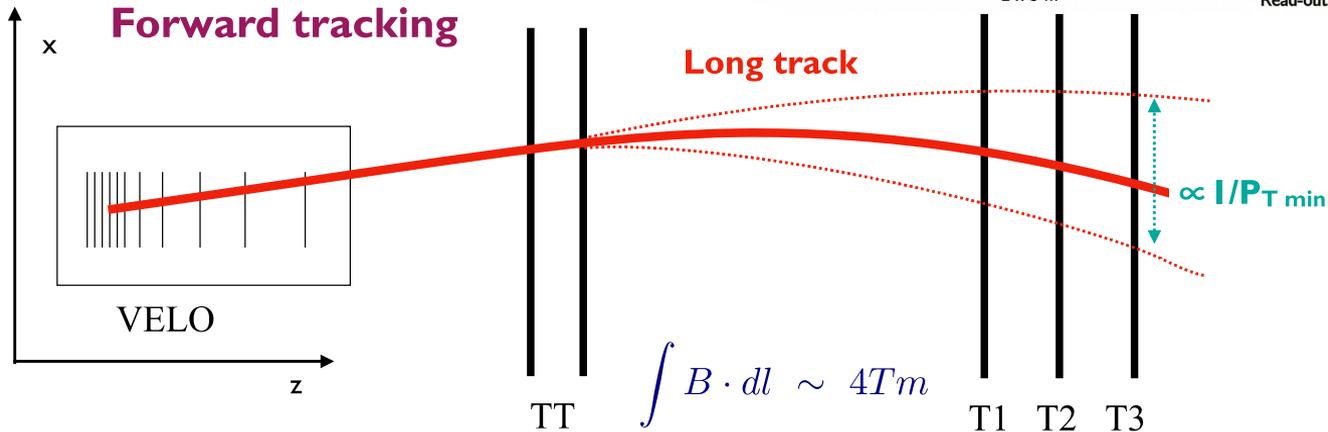
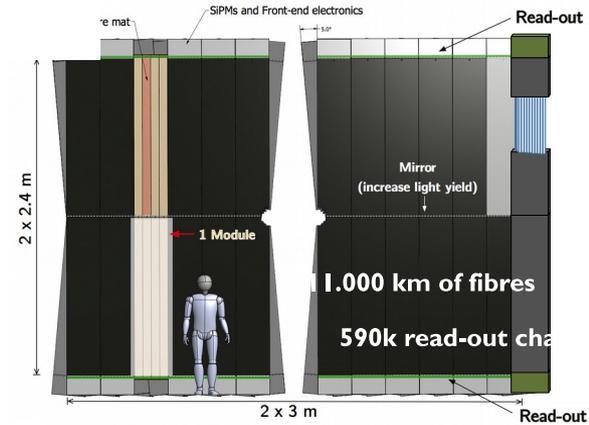
CERN-LHCC-2013-021



Partial reconstruction sequence : Forward tracking

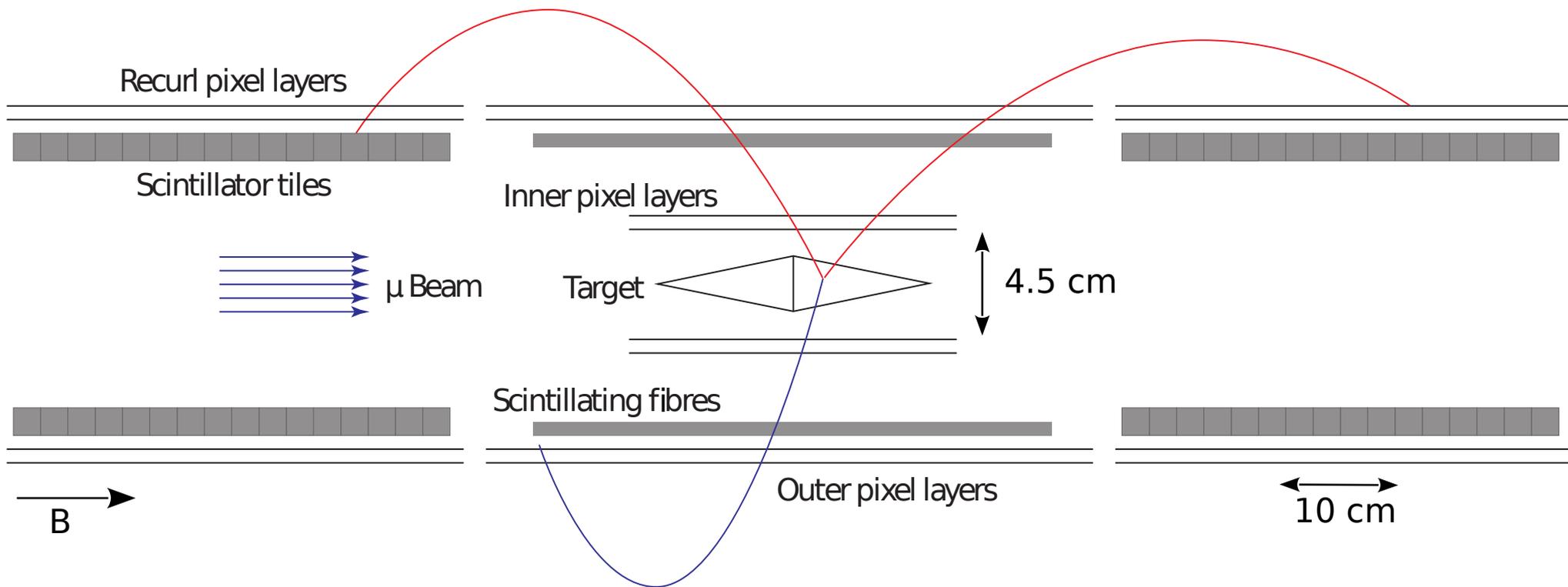
Scintillating Fibre Tracker (Sci-Fi)

- 3 stations x 4 planes (x/u/v/x) of 6 stacked 2.4 m long scintillating fibres ($\phi=250 \mu\text{m}$)
- Read-out by Silicon-Photon multipliers (250 μm channel pitch)

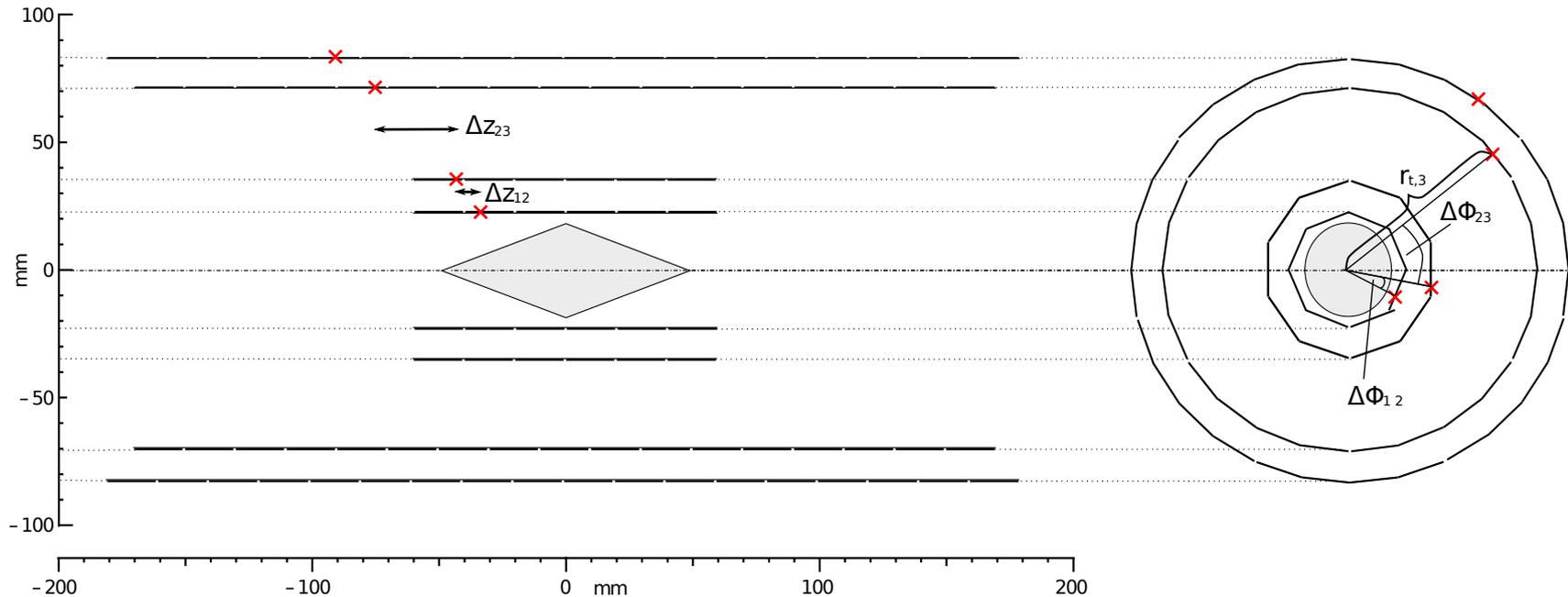


Find matching segments in SciFi according to transverse momentum tolerances

Mu3e: Full Detector

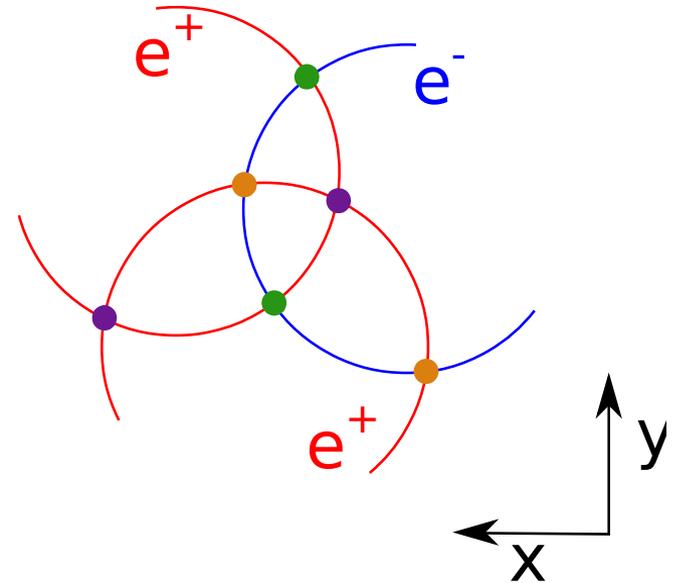


Mu3e: Geometrical selection cuts



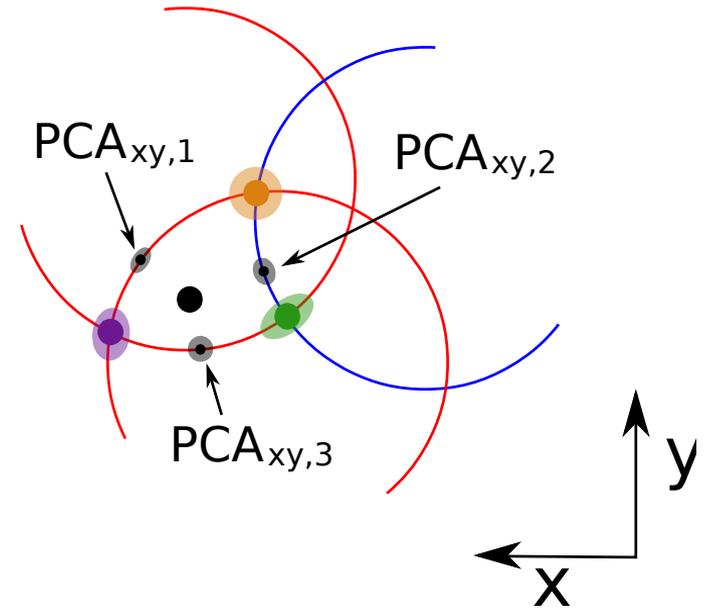
Mu3e: Vertex Estimate

- Study each combination of two e^+ , one e^-
- In xy -plane: find intersections of track circles
- Calculate weights of intersections based on uncertainties due to
 - multiple scattering
 - pixel size

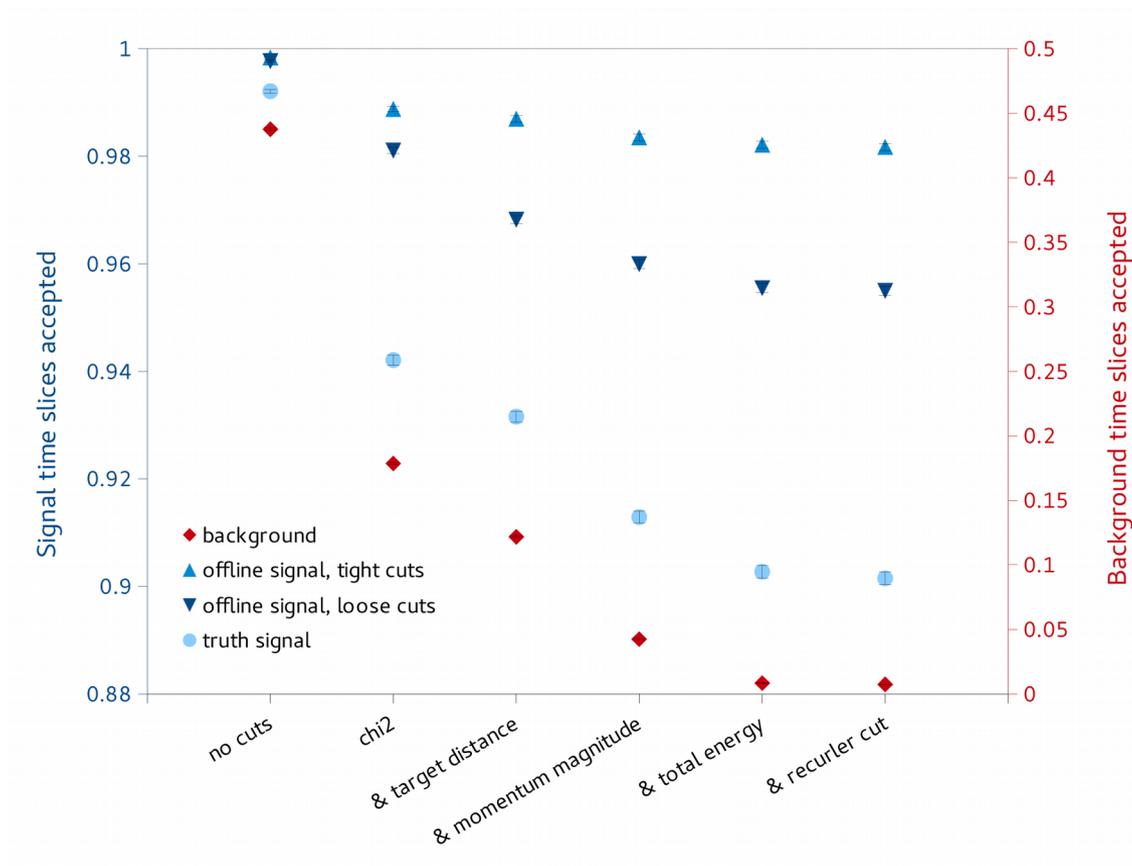


Mu3e: Vertex Estimate

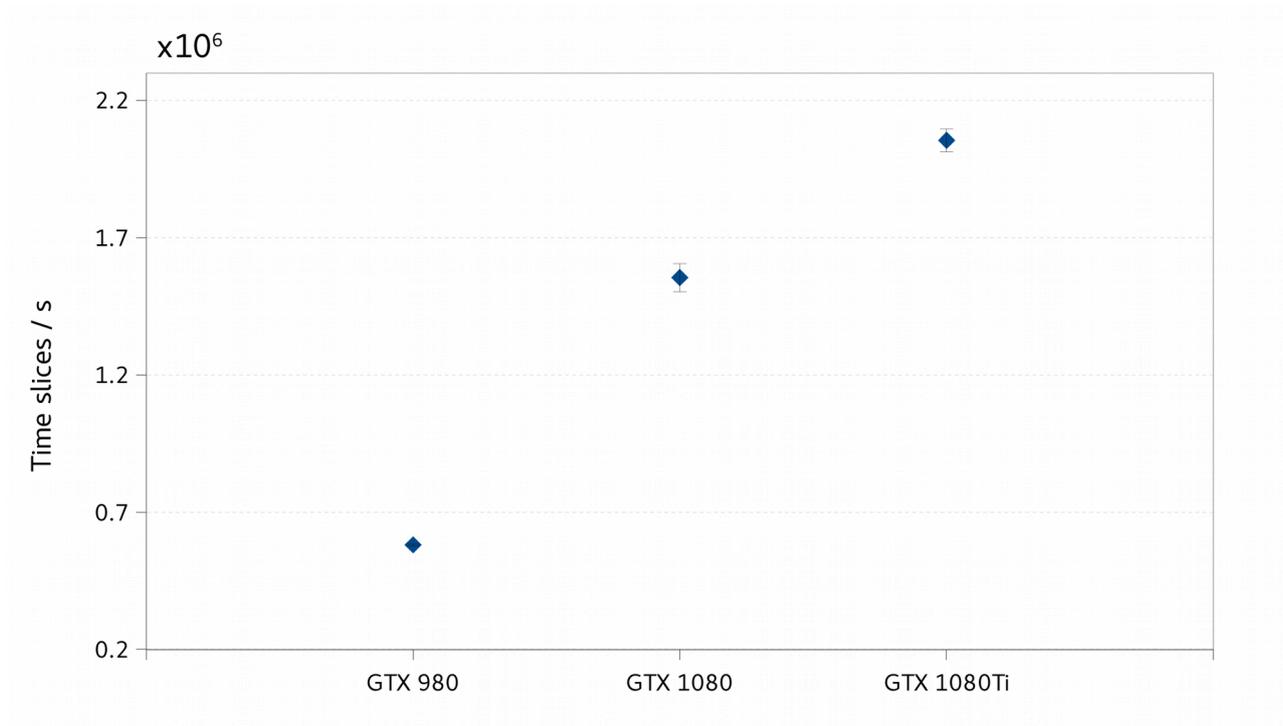
- Calculate weighted mean of intersections from three different tracks
- Find point of closest approach (PCA_{xy}) to weighted mean in xy-plane on each track
- Calculate z-position PCA_z and weight at PCA_{xy}
- Find weighted mean in z-coordinate
- Achieve vertex resolution of $\sim 400 \mu\text{m}$ sigma



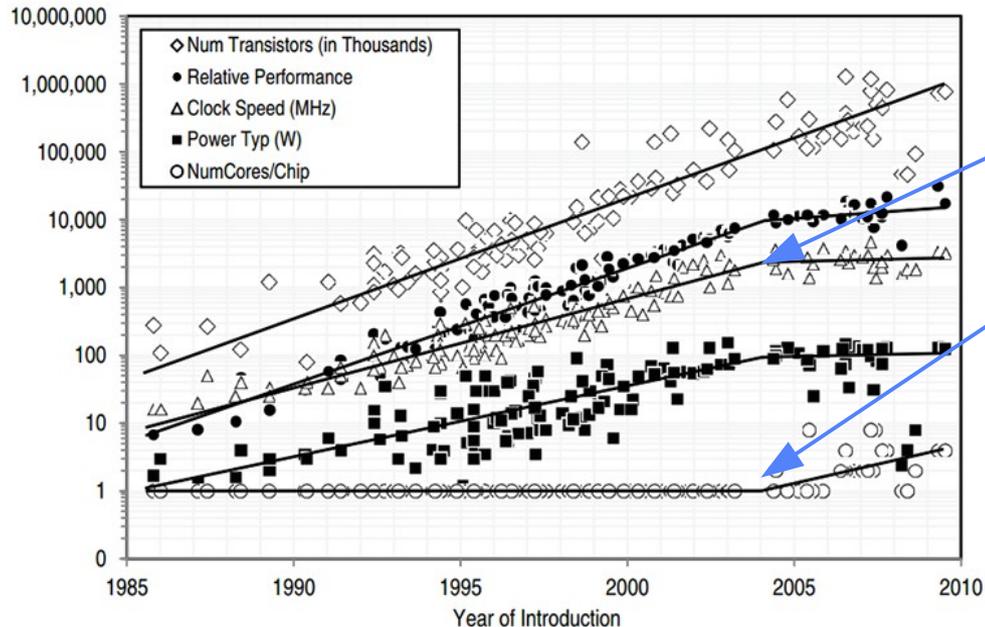
Mu3e: Signal Selection



Mu3e: GPU Generations



Clock speed no longer increasing



- 2004: clock speed stopped increasing due to heat limit
- → Multiple core processors
 - (Intel i7: 4 cores)
- Next: quantum mechanics limit: O(10 nm)

<https://hackadaycom.files.wordpress.com/2015/09/numtransistors.png>