New Perspectives on Lepton Flavor Violation

Julian Heeck

Paul Scherrer Institute

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The Standard Model



Symmetries of the Standard Model

• Rephasing lepton and quark fields:

 $\mathsf{U}(1)_\mathsf{B} \times \mathsf{U}(1)_{\mathsf{L}_\mathsf{e}} \times \mathsf{U}(1)_{\mathsf{L}_\mu} \times \mathsf{U}(1)_{\mathsf{L}_\tau} \,.$

• B+L broken non-perturbatively,

$$\Delta B = 3 \quad \wedge \quad \Delta L_e = \Delta L_\mu = \Delta L_ au = 1 \,,$$

but unobservably suppressed at low temperatures. ['t Hooft '76]

• Real global symmetry of SM:

$$\mathsf{U}(1)_{\mathsf{B}-\mathsf{L}} \times \mathsf{U}(1)_{\mathsf{L}_{\mu}-\mathsf{L}_{\tau}} \times \mathsf{U}(1)_{\mathsf{L}_{\mu}+\mathsf{L}_{\tau}-2\mathsf{L}_{\mathsf{e}}}.$$

- Can even promote to gauge symmetry by adding 3 N_R . [Araki, Heeck, Kubo, 1203.4951]

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Neutrino oscillations

- Observations of $v_{\alpha} \rightarrow v_{\beta}$ prove that $M_{\nu} \neq 0$ and $U(1)_{L_{\mu}-L_{\tau}} \times U(1)_{L_{\mu}+L_{\tau}-2L_{e}}$ is broken!
- B L could still be conserved if neutrinos are Dirac.

[Heeck, 1408.6845]



Neutrino oscillation between three generations

Lepton flavor definitely violated, so where is it?

Neutrino mass \Rightarrow charged LFV?

• SM + Dirac neutrinos: *all* LFV is GIM suppressed:

$$\frac{\Gamma(\ell_{\alpha} \to \ell_{\beta} \gamma)}{\Gamma(\ell_{\alpha} \to \ell_{\beta} \nu_{\alpha} \overline{\nu}_{\beta})} \simeq \frac{3\alpha_{\rm EM}}{32\pi} \left| \sum_{j=2,3} U_{\alpha j} \frac{\Delta m_{j1}^2}{M_W^2} U_{j\beta}^{\dagger} \right|^2 < 5 \times 10^{-53} \,.$$

[Petcov '77; Cheng & Li '77]

• SM + heavy seesaw neutrinos:



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Neutrino mass \Rightarrow charged LFV!

• Neutrino-mass induced charged LFV is unobservable.

Observation of CLFV \rightarrow beyond SM and beyond M¹

- (Only exception: $0\nu\beta\beta$ can probe LFV ($\Delta L_e = 2$) via M_{ν} .)
- arXiv: many ν-mass models *can* actually give large LFV:
 - Low-scale/inverse/linear seesaw;
 - SUSY seesaw;
 - Radiative seesaw (Zee-Babu, Ma,...);
- $M_{v} \Leftrightarrow LFV$ connection possible but not necessary.

Approximate symmetries

- Flavor still *approximate* symmetry in *charged* lepton sector.
- Unavoidably broken by M_v, but this is unobservable.

Search for CLFV to learn more about flavor!

• Assuming *heavy new physics*, the best channels are

 $\ell \to \ell' \gamma, \ \ell \to \ell' \ell'' \ell''', \ \mu \to e \text{ conv.}, \ h \to \ell \ell', \ had \to \ell \ell', \ \dots$

• Organize operators/processes by quantum numbers under

$$\mathsf{U}(1)_{\mathsf{L}_{\mu}-\mathsf{L}_{\tau}}\times\mathsf{U}(1)_{\mathsf{L}_{\mu}+\mathsf{L}_{\tau}-2\mathsf{L}_{\mathsf{e}}}\,.$$

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[Heeck, 1610.07623]



[Heeck, 1610.07623]









Interpretation of LFV

Observation of charged lepton flavor violation \Rightarrow	≽	Remaining symmetry
$\Delta(L_{\alpha} - L_{\beta}) = 2$		$U(1)_{L_{lpha}+L_{eta}-2L_{\gamma}}$
$\Delta(L_{\alpha} + L_{\beta} - 2L_{\gamma}) = 6$		$U(1)_{L_{lpha}-L_{eta}}$
$\Delta(L_{\alpha} + L_{\beta} - 2L_{\gamma}) = 6 \text{ and } \Delta(L_{\alpha} - L_{\beta}) = 2$		$\mathbb{Z}_2: \ \ell_\gamma o - \ell_\gamma$
$\Delta(L_{\alpha} + L_{\beta} - 2L_{\gamma}) = 6 \text{ and } \Delta(L_{\alpha} + L_{\gamma} - 2L_{\beta}) = 6$		\mathbb{Z}_3 : $(\ell_{\alpha}, \ell_{\beta}, \ell_{\gamma}) \sim (0, 1, 2)$
$\Delta(L_{\alpha} - L_{\beta}) = 2$ and $\Delta(L_{\alpha} - L_{\gamma}) = 2$		_
$\Delta(L_{\alpha} - L_{\beta}) = 2$ and $\Delta(L_{\alpha} + L_{\gamma} - 2L_{\beta}) = 6$		_

- At least two orthogonal channels required for full LFV.
- Flavor violation by higher units more challenging.
- Easy to build models that single out certain channels, e.g. $\tau^- \rightarrow \mu^- \gamma$ or $\tau^- \rightarrow e^- e^- \mu^+$.

Example: $\tau^- \rightarrow e^-e^-\mu^+$

- Conserves $L_{\mu} L_{\tau}$, so impose this symmetry.
- Simplest UV model: add SU(2), singlet k⁺⁺:

 $\mathcal{L} \supset (g_{\mu\tau}\overline{\mu}_{R}^{c}\tau_{R} + g_{ee}\overline{e}_{R}^{c}e_{R}) k^{++} + h.c.$



- $\tau^- \rightarrow e^-e^-\mu^+$ allowed, everything else forbidden.
- Add N_R and singlet scalars to break $L_{\mu} L_{\tau}$ in M_R .
- Could even use symmetry for texture zeroes in M_y.

[Araki, Heeck, Kubo, 1203.4951]

v oscillations but approximate symmetry in ℓ^- sector.



$\tau^- \rightarrow \mu^- \mu^- \mu^- e^+ e^+?$

- Conserves L_{μ} +4 L_{e} -5 L_{τ} , impose to kill other modes.
- Not difficult to build, but rate is

$$\Gamma \propto \langle H
angle^2 rac{m_{ au}^{11}}{m_S^{12}}$$



- Secretly dimension 10 operator.
- Would need new particles at 10 GeV for observable rate! Only possible for neutral fields, otherwise $Z \rightarrow SS$.

Not pretty...

Baryon number violation

Baryon number violation

- So far assumed $\Delta B = 0$, but can also do LFV with $\Delta B \neq 0$.
- Example: proton decay ($\Delta B = 1$).
- Super-K limits on $p \rightarrow e^+\pi^0$, $\mu^+\pi^0$ are 10^{34} yrs!

Baryon number violation

- So far assumed $\Delta B = 0$, but can also do LFV with $\Delta B \neq 0$.
- Example: proton decay ($\Delta B = 1$).
- Super-K limits on $p \rightarrow e^+\pi^0$, $\mu^+\pi^0$ are 10^{34} yrs!
- More interesting for flavor: $p \rightarrow \overline{\ell \ell} \ell$:



[Weinberg, '79 & '80]

Different symmetry properties

• $\Delta B = 1$ proton decay operators:

[Weinberg, '79 & '80]

- $QQQL: \qquad d=6, \ \Delta L=1, \ e.g. \ p \rightarrow \ e^{\scriptscriptstyle +} \ \pi^{\scriptscriptstyle 0}.$
- QQLHd: d=7, ΔL = -1, e.g. p $\rightarrow e^{-}\pi^{+}K^{+}$.
- QQQLLH^ℓ: d=10, ΔL = 1, e.g. p → e⁺e⁻e⁺.
- dddLLLH: d=10, ΔL = -3, e.g. p → e⁻νν π⁺π⁺.
- QudLLLHH: $d=11, \Delta L = 3, e.g. p \rightarrow e^+ \overline{\nu \nu}.$

Different symmetry properties

Impose B+L

• $\Delta B = 1$ proton decay operators:



Impose B+L

Impose B+3L

• $\Delta B = 1$ proton decay operators:



Impose B+3L

Impose B-L

- $\Delta B = 1$ proton decay operators:

Impose B-L

Impose
$$L_e^+ 2L_\mu^- 3L_\tau$$

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• $\Delta B = 1$ proton decay operators:



Impose $L_e + 2L_\mu - 3L_\tau$

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Lepton-flavored proton decay

$$\Gamma\propto \langle H\rangle^2 \tfrac{m_p^{11}}{\Lambda^{12}}\sim (10^{33}\,{\rm yr})^{-1}(100\,{\rm TeV}/\Lambda)^{12}$$

[Hambye, Heeck, in progress]

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Lepton-flavored proton decay

- The decay $p \rightarrow e^+e^+\mu^-$ or $p \rightarrow \mu^+\mu^+e^-$ could be dominant!
- Conserves B-L, L_{τ} , and $L_{e}+2L_{\mu}-3L_{\tau}$ (or $L_{\mu}+2L_{e}-3L_{\tau}$).
- 35 d=10 operators of the form $QQQL\overline{L}H\ell$.
- Rate suppressed:

$$\Gamma \propto \langle H
angle^2 rac{m_p^{11}}{\Lambda^{12}} \sim (10^{33}\,{
m yr})^{-1} (100\,{
m TeV}/\Lambda)^{12}\,.$$

- Easy channels, Super-K can probe 10³⁴ yrs!
- UV completion @ 100 TeV could show up in flavor physics.
- Other channels, e.g. $p \rightarrow e^+ \pi^0$, suppressed by ν mass.

[Hambye, Heeck, in progress]

[Hambye, Heeck, in progress]

$p \rightarrow e^+e^+\mu^-$

- Conserves $L_e + 2L_u 3L_{\tau}$; Impose!
- Only d = 10 survives:

 $\frac{QQQL}{\Lambda^2} + \frac{QQQL\overline{LH}}{\Lambda^3} + \cdots + \frac{QQQL\overline{LHe}}{\Lambda^6}.$

- Rate very suppressed: $\Gamma \propto \langle \mathsf{H} \rangle^2 \frac{\mathsf{m}_p^{11}}{\Lambda^{12}} \sim (10^{33} \, \mathrm{yr})^{-1} (100 \, \mathrm{TeV}/\Lambda)^{12} \,.$
- UV complete with leptoquarks. Analogous for $p \rightarrow \mu^+\mu^+e^-$.
- More extreme: $p \rightarrow e^+e^+e^+\mu^-\mu^-$ etc., probes $\Lambda \sim \text{few TeV}!$

Low-hanging fruit for Super-K.

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[Hambye, Heeck, in progress]

$p \rightarrow \mu^+ \mu^+ e^-$

• Minimal leptoquark example:

 $\phi_1 \sim (\mathbf{3}, \mathbf{3}, -2/3), \, \phi_2 \sim (\mathbf{3}, \mathbf{2}, 7/3).$

- L_{μ} +2 L_{e} -3 L_{τ} ensures simple structure $y_{j}\overline{L}_{\mu}\phi_{1}Q_{j}^{c} + f_{j}\overline{u}_{j}\phi_{2}L_{e} + \lambda\phi_{1}^{2}\phi_{2}H$.
- Also conserves B-L and lepton flavor, but gives lepton non-universality.
- Triplet LQ perfect for $b \rightarrow s\mu\mu$ anomalies:

 $m_{\phi_1}\simeq 30\,{
m TeV}\sqrt{y_2y_3}\,.$



Interesting pheno from proton decay @ 100 TeV!

[Hambye, Heeck, in progress]

 $p \rightarrow e^+e^+\mu^-$

• R-parity violating MSSM:

$$\begin{split} \lambda_{ijk} \mathsf{L}_{i} \mathsf{L}_{j} \overline{\mathsf{I}_{k}} + \lambda_{ijk}^{\prime\prime} \overline{\mathsf{u}_{i}} \, \overline{\mathsf{d}_{j}} \, \overline{\mathsf{d}_{k}} \\ + \lambda_{ijk}^{\prime} \mathsf{L}_{i} \mathsf{Q}_{j} \overline{\mathsf{d}}_{k} + \mu_{i}^{\prime} \mathsf{L}_{i} \mathsf{H}_{u} \, . \end{split}$$

• Impose $L_{\mu}+2L_{e}+L_{\tau}$ for $\lambda' = 0 = \mu'$ and $\lambda = \lambda_{132}$.



- Add soft terms for sfermion mixing: $A_{d_{ij}}H_d \overline{d}_i \widetilde{Q}_j m_{ij}^2 \widetilde{L}_i \widetilde{L}_j$.
- $\tau^- \rightarrow e^-\gamma$ and $n-\overline{n}$ oscillations also allowed.
- Known for neutrino modes $p \rightarrow e^+\nu\nu$, $\mu^+\nu\nu$, $K^+\mu^+e^-\nu$... [Carlson, Roy, Sher, '95; Bhattacharyya, Pal, '99; Faroughy, Prabhu, Zheng, '15]
- Rich phenomenology.

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Summary so far

- SM symmetry: $G = U(1)_{B-L} \times U(1)_{L_{\mu}-L_{\tau}} \times U(1)_{L_{\mu}+L_{\tau}-2L_{e}}$.
- Effective field theory with Majorana v:



But what if new physics is light?

Simple example: majoron

• 3 singlets N_R + new scalar $\sigma = (f + \sigma^0 + iJ)/\sqrt{2}$. B - L breaking scale Heavy scalar (inflaton?) Goldstone boson: majoron

[Chikashige, Mohapatra, Peccei, '81; Schechter, Valle, '82]

- Break U(1)_{B-L} spontaneously: $\mathcal{L} = -\overline{L}yHN_R \frac{1}{2}\overline{N}_R^c\lambda\sigma N_R + h.c.$ $\sqrt{-1}$ $M_R = \frac{\lambda f}{\sqrt{2}}$
- For $M_R \gg m_D \colon M_\nu \simeq -m_D M_R^{-1} m_D^T$

$$\simeq 1 eV \left(\frac{m_D}{100 GeV}\right)^2 \left(\frac{10^{13} GeV}{M_R}\right)$$

Majoron couplings

• Tree level coupling only to neutrinos:



$$\frac{iJ}{2f}\overline{\nu}_{\alpha}^{c}\gamma_{5}(m_{D}^{*}M_{R}^{-1}m_{D}^{\dagger})_{\alpha\beta}\nu_{\beta} = -\frac{iJ}{2f}\sum_{k}\overline{\nu}_{k}\gamma_{5}m_{k}\nu_{k}$$

• One loop:

$$J = \frac{1}{m_{j}} \bigvee_{W} \overline{f} = \frac{iJ}{f} \overline{f} \gamma_{5} f \frac{m_{f} T_{3}^{f}}{8\pi^{2}v^{2}} tr \left(m_{D} m_{D}^{\dagger}\right) \qquad \text{Off-diagonal!}$$

$$J = \frac{n_{j}}{\sqrt{W}} \bigvee_{\ell} \frac{iJ}{f} \overline{\ell}_{\alpha} \left(\frac{m_{\beta}}{8\pi^{2}v^{2}} P_{R} - \frac{m_{\alpha}}{8\pi^{2}v^{2}} P_{L}\right) \ell_{\beta} \left(m_{D} m_{D}^{\dagger}\right)_{\alpha\beta} \bigvee_{\ell}$$

• Two loop: $\Gamma(J \to \gamma \gamma) \simeq \frac{\alpha^2 \operatorname{tr} \left(\operatorname{m_D} \operatorname{m_D}^\dagger \right)^2}{4096\pi^7} \frac{\operatorname{m_J}^3}{\operatorname{v}^4 \operatorname{f}^2} \left| \sum_f \operatorname{N_c}^f \operatorname{T_3}^f \operatorname{Q}_f^2 \operatorname{g} \left(\frac{\operatorname{m_J}^2}{4\operatorname{m_f}^2} \right) \right|^2$

[Heeck, Camilo Garcia-Cely, 1701.07209; see also Pilaftsis '94]

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Properties

• Crucial observation: the two matrices are independent!

$${\mathsf{m}}_{\mathsf{D}}, {\mathsf{M}}_{\mathsf{R}} \} \leftrightarrow {\mathsf{M}}_{\nu}, {\mathsf{m}}_{\mathsf{D}}{\mathsf{m}}_{\mathsf{D}}^{\dagger} \}.$$

[Davidson, Ibarra, hep-ph/0104076]

- $J\bar{\ell}\ell$ coupling can be *large* and of arbitrary structure.
- Similar couplings arise for familons or flavor Z'. [Wilczek, '82; Reiss, '82; Grinstein, Preskill, Wise, 85; ...]
- Boson not necessarily massless, e.g. pseudo-Goldstone.
- Experimental signature depends on decay channel:

 $\ell \to \ell' \mathsf{J}, \ \mathsf{J} \to \operatorname{inv}, \ell'' \ell''', \gamma \gamma.$

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$\ell \rightarrow \ell' J$ with $J \rightarrow invisible$

• Standard LFV in seesaw:

$$\frac{\Gamma(\ell \to \ell' \gamma)}{\Gamma(\ell \to \ell' \nu_{\ell} \overline{\nu}_{\ell'})} \simeq \frac{3\alpha}{8\pi} |(\mathbf{m}_{\mathsf{D}} \mathsf{M}_{\mathsf{R}}^{-2} \mathsf{m}_{\mathsf{D}}^{\dagger})_{\ell \ell'}|^{2}.$$

- Great signature, but requires light N_{R.}
- With majoron: look for mono-energetic lepton: [Pilaftsis, '94; Feng, Moroi, Murayama, Schnapka, '98; Hirsch, Vicente, Meyer, Porod, '09]

anolo, 04, reng, morol, marayama, comapha, 00, rinoon, vicence, meyer, roroa, oc

$$\frac{\Gamma(\ell \to \ell' J)}{\Gamma(\ell \to \ell' \nu_{\ell} \overline{\nu}_{\ell'})} \simeq \frac{3}{16\pi^2} \frac{1}{m_{\ell}^2 f^2} |(m_D m_D^{\dagger})_{\ell \ell'}|^2.$$

• If
$$M_R = \text{diag}(M)$$
: $\frac{\Gamma(\ell \to \ell' \gamma)}{\Gamma(\ell \to \ell' J)} \simeq 2\pi \alpha \frac{m_\ell^2}{M^2} \frac{f^2}{M^2} \begin{cases} \gg 1 \text{ for } M \ll f , \\ \ll 1 \text{ for } , M \sim f \gg m_\ell . \end{cases}$

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$\mu \rightarrow e \; J \; with \; J \rightarrow \; invisible$

- TWIST, '15: limits on different anisotropies.
- Chiral coupling µP_LeJ suppresses sensitivity!

[Heeck, Garcia-Cely, 1701.07209]

- Bremsstrahlung is competitive: $\mu \rightarrow e J \gamma$. [Goldman et al, '87]
- Approximate limit

$$rac{|(\mathsf{m}_{\mathrm{D}}\mathsf{m}_{\mathrm{D}}^{\dagger})_{\mu\mathsf{e}}|}{\mathsf{vf}} \lesssim 10^{-5}.$$



Julian Heeck (ULB) - LFV

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Searches for $\mu \rightarrow e X$ with Mu3e Full reconstruction of all Michel decays is a big challenged for data acquisition B(µ → e X) ~ 10⁻⁸ at 90 % CL Branching Fraction 90% CL -4-hit -6-&8-hit recurling track in Mu3e TWIST 10⁻⁶ 10^{-7} Mu3e simulation required full reconstruction 10⁻⁸ of "recurlers" 10⁻⁹

30

50

40

60

70

90

Familon Mass [MeV]

80

$\mu \rightarrow e X$ with $X \rightarrow$ visible

- Take $Xey_5e m_e/\Lambda_{ee}$.
- Decay length determines signature.
- Displaced vertex gives new observable. [Heeck, Rodejohann, 1710.02062]
- Muon at rest:

$$\gamma c au \simeq rac{\pi m_{\mu} \Lambda_{ee}^2}{m_e^2 m_X^2} \simeq 2.5 \, \mathrm{cm} \left(rac{\Lambda_{ee}}{100 \, \mathrm{GeV}}
ight)^2 \left(rac{10 \, \mathrm{MeV}}{m_X}
ight)^2.$$

Sub-GeV X with ee coupling allowed?

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$\mu \rightarrow e X$ with $X \rightarrow e e$



 $\text{Log}_{10}(m_X/\text{GeV})$

$$\begin{split} \mathrm{BR}(\mu \to \mathsf{eX}) \mathrm{BR}(\mathsf{X} \to \mathsf{ee}) (1 - \mathsf{P}(\mathsf{I}_{\mathrm{dec}})) \\ \simeq \mathrm{BR}(\mu \to \mathsf{eX}) \frac{\mathsf{I}_{\mathrm{dec}}}{\gamma \mathsf{c} \tau} \,. \end{split}$$

$\mu \rightarrow e \ X \ with \ X \rightarrow \ \gamma \gamma$



MEG(II) or Mu3e extension?

[Recent limits: Dolan et al, 1709.00009]

Muons difficult, taus easier.

$\tau \rightarrow \ell J$ with $J \rightarrow$ invisible



Improvement with Belle-II.

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[Heeck, 1602.03810; Altmannshofer et al, 1607.06832]

Improvement with Belle-II.

 $egin{aligned} & rac{|(\mathsf{m}_{\mathsf{D}}\mathsf{m}_{\mathsf{D}}^{\dagger})_{ au\mathsf{e}}|}{\mathsf{v}\mathsf{f}} \lesssim 6 imes10^{-3}, \ & rac{|(\mathsf{m}_{\mathsf{D}}\mathsf{m}_{\mathsf{D}}^{\dagger})_{ au\mu}|}{\mathsf{c}} \lesssim 10^{-3}. \end{aligned}$

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$\tau \rightarrow e X$ with $X \rightarrow visible$

- Tau at rest, higher X boost.
- Arbitrary decay lengths possible.
- Similar for X → ee, µµ, µe.
- Worthwhile in LHCb and Belle (II).



[Recent limits: Dolan et al, 1709.00009]

Muons difficult, taus easier...

Summary

- Charged LFV gives info *complementary* to ν oscillations.
- Not simple yes/no question, need to find out if/how

$$\mathsf{U}(1)_{\mathsf{B}-\mathsf{L}} imes \mathsf{U}(1)_{\mathsf{L}_{\mu}-\mathsf{L}_{ au}} imes \mathsf{U}(1)_{\mathsf{L}_{\mu}+\mathsf{L}_{ au}-2\mathsf{L}_{\mathsf{e}}}$$

is broken in ℓ⁻ sector.

 \Rightarrow Need to search all possible channels!

- Non-trivial breaking: $\tau \rightarrow ee\mu$, $\tau \rightarrow \mu\mu e$, $p \rightarrow e\mu\mu$, $p \rightarrow \mu ee$,...
- Keep light new physics in mind: $\ell \rightarrow \ell' X, X \rightarrow inv, \ell\ell, \gamma\gamma$.
- Hope for sign in Mu3e, MEG-II, Belle-II, Mu2e, LHC,...

Still some streetlights to search under!