

Rare B decays & new physics

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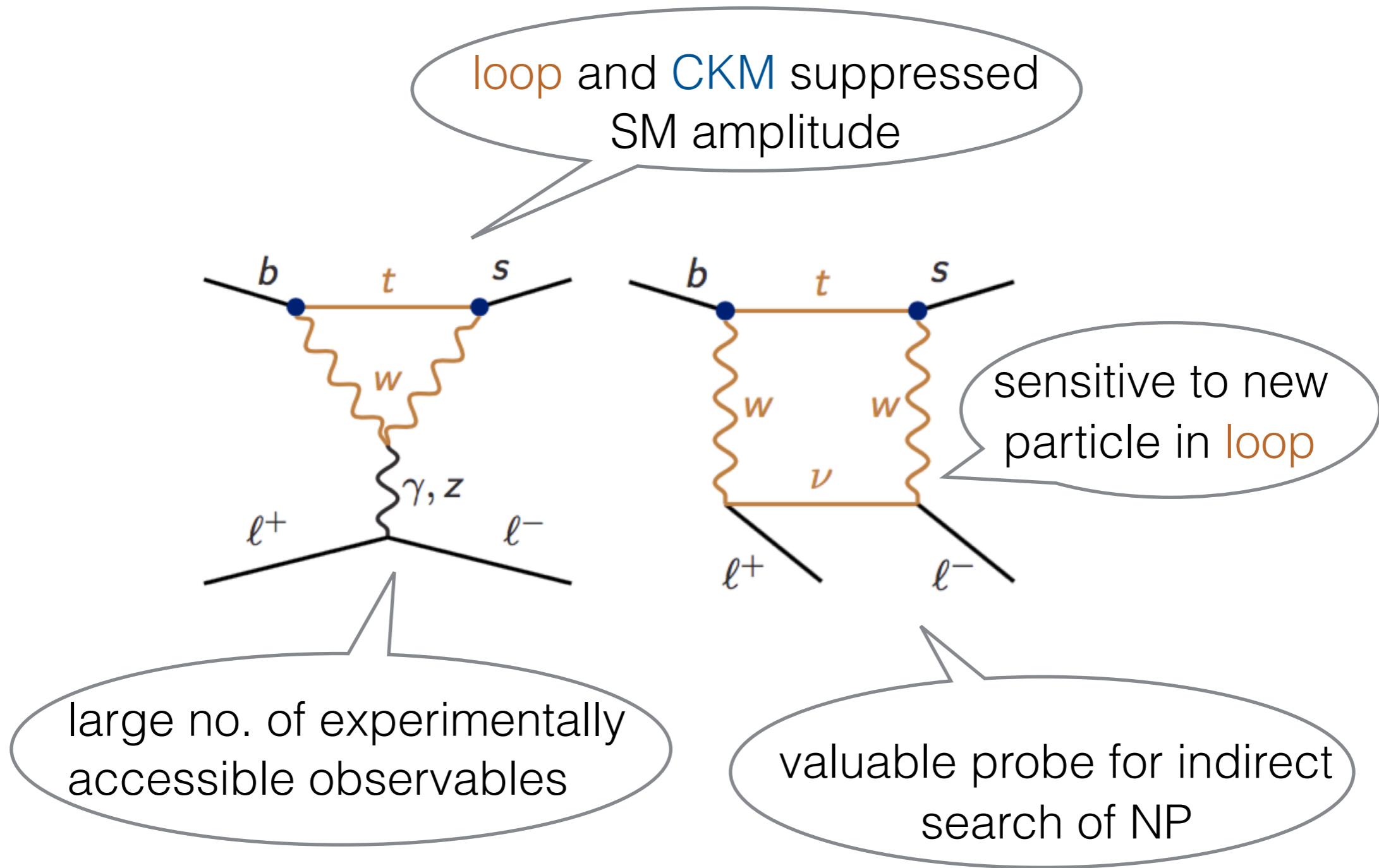
on arXiv: 1603.04355, 1706.08437



Outline

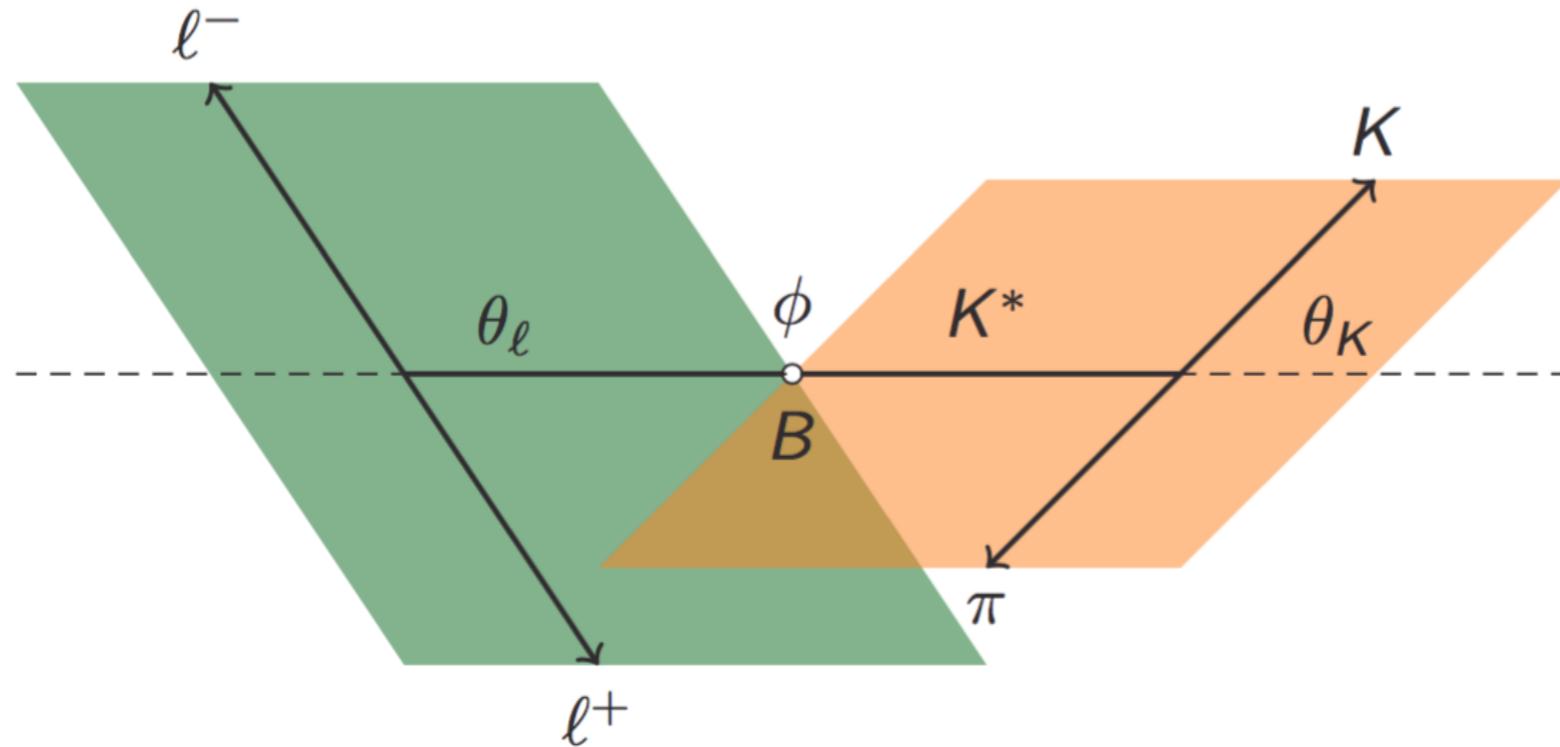
- Introduction
- Rare semileptonic mode $B \rightarrow K^* \ell^+ \ell^-$
 - ▶ Model independent framework
 - ▶ Evidence of new physics
- Lepton flavor non-universality
- Summary

Introduction



Introduction

Angular analysis in well known helicity frame [Kruger, Sehgal, Sinha, Sinha '99]



The differential distribution

$$\frac{d^4\Gamma(B \rightarrow K^* \ell^+ \ell^-)}{dq^2 d\cos\theta_l d\cos\theta_k d\phi}$$

$$\begin{aligned} &= \frac{9}{32\pi} \left[I_1^s \sin^2 \theta_K + I_1^c \cos^2 \theta_K + (I_2^s \sin^2 \theta_K + I_2^c \cos^2 \theta_K) \cos 2\theta_l + I_3 \sin^2 \theta_K \sin^2 \theta_l \cos 2\phi \right. \\ &\quad + I_4 \sin 2\theta_K \sin 2\theta_l \cos \phi + I_5 \sin 2\theta_K \sin \theta_l \cos \phi + I_6^s \sin^2 \theta_K \cos \theta_l \\ &\quad \left. + I_7 \sin 2\theta_K \sin \theta_l \sin \phi + I_8 \sin 2\theta_K \sin 2\theta_l \sin \phi + I_9 \sin^2 \theta_K \sin^2 \theta_l \sin 2\phi \right] \end{aligned}$$

Motivation

- ▶ $I_i = \text{short distance} + \text{long distance}$

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Wilson coefficients:
perturbatively calculable

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Form-factors:
non-perturbative estimates
from LCSR, HQET, Lattice ...
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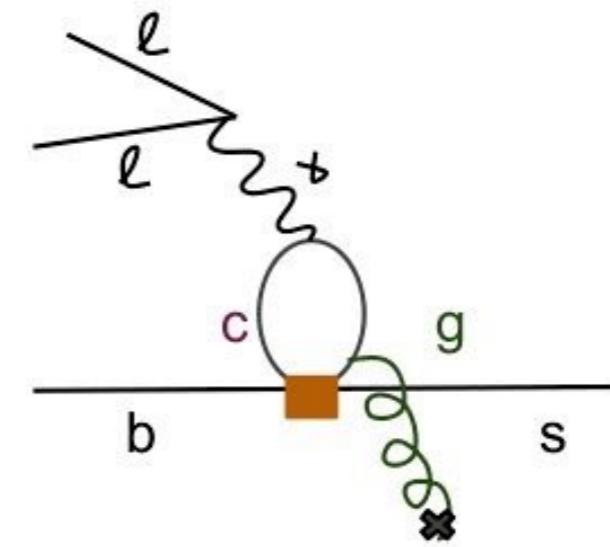
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Non-factorizable
contributions:



no quantitative computation

► Challenge: either estimate accurately or eliminate

Model Independent Framework

- The amplitude $\mathcal{A}(B(p) \rightarrow K^*(k)\ell^+\ell^-)$ [RM, Sinha, Das '14]

$$= \frac{G_F \alpha}{\sqrt{2}\pi} V_{tb} V_{ts}^* \left[\left\{ C_9 \langle K^* | \bar{s} \gamma^\mu P_L b | \bar{B} \rangle - \frac{2C_7}{q^2} \langle K^* | \bar{s} i \sigma^{\mu\nu} q_\nu (m_b P_R + m_s P_L) b | \bar{B} \rangle \right. \right.$$
$$\left. \left. - \frac{16\pi^2}{q^2} \sum_{i=\{1-6,8\}} C_i \mathcal{H}_i^\mu \right\} \bar{\ell} \gamma_\mu \ell + C_{10} \langle K^* | \bar{s} \gamma^\mu P_L b | \bar{B} \rangle \bar{\ell} \gamma_\mu \gamma_5 \ell \right]$$

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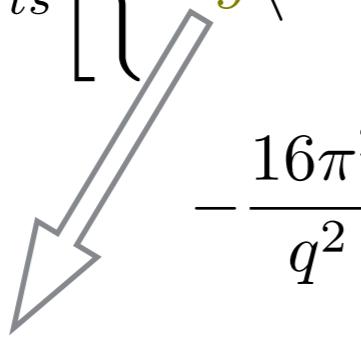
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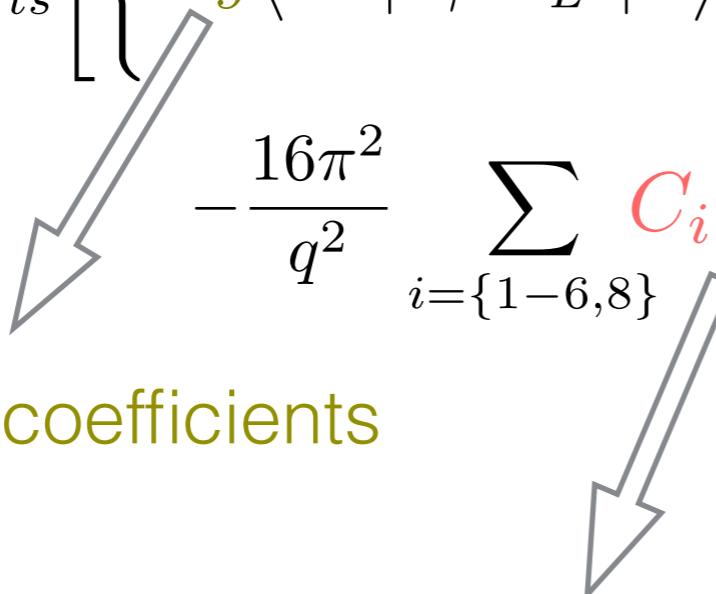


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allow general parametrization
with form-factors $\mathcal{X}_j, \mathcal{Y}_j$

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Wilson coefficients

non-local operator
for non factorization contributions

lorentz & gauge invariance
allow general parametrization
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$$\mathcal{H}_i^\mu \sim \left\langle K^* | i \int d^4x e^{iq \cdot x} T\{ j_{em}^\mu(x), \mathcal{O}_i(0) \} | \bar{B} \right\rangle \Rightarrow \text{parametrize with 'new' form-factors } \mathcal{Z}_j^i$$

[Khodjamirian et. al '10]

Model Independent Framework

- ▶ Absorbing factorizable & non-factorizable contributions into

$$C_9 \rightarrow \tilde{C}_9^{(j)} = C_9 + \Delta C_9^{(\text{fac})}(q^2) + \Delta C_9^{(j),(\text{non-fac})}(q^2)$$

$$\underbrace{}_{\sim \sum_i C_i z_j^i / \chi_j}$$

$$\frac{2(m_b+m_s)}{q^2} C_7 \mathcal{Y}_j \rightarrow \tilde{\mathcal{Y}}_j = \frac{2(m_b+m_s)}{q^2} C_7 \mathcal{Y}_j + \dots$$

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$$\underbrace{\Delta C_9^{(\text{fac})}(q^2) + \Delta C_9^{(j),(\text{non-fac})}(q^2)}_{\sim \sum_i \mathcal{C}_i \mathcal{Z}_j^i / \mathcal{X}_j}$$

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- ▶ Most general parametric form of amplitude in SM

$$\mathcal{A}_\lambda^{L,R} = (\tilde{C}_9^\lambda \mp C_{10}) \mathcal{F}_\lambda - \tilde{\mathcal{G}}_\lambda \quad \quad \mathcal{A}_t|_{m_\ell=0} = 0$$

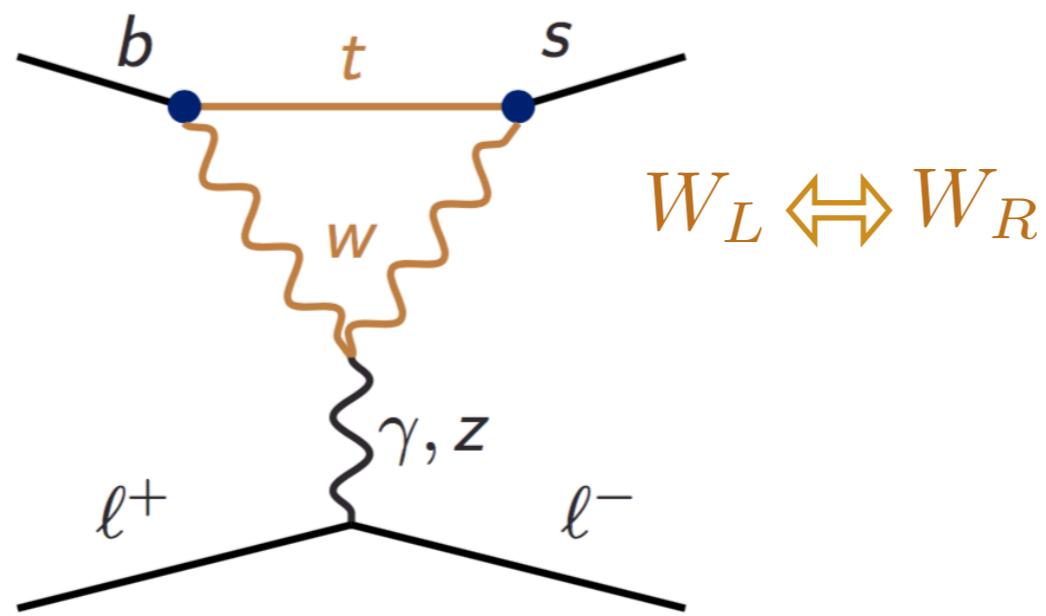
Form-factors: $\mathcal{F}_\lambda \equiv \mathcal{F}_\lambda(\mathcal{X}_j)$ and $\tilde{\mathcal{G}}_\lambda \equiv \tilde{\mathcal{G}}_\lambda(\tilde{\mathcal{Y}}_j)$

Right-Handed Current

- ▶ Chirality flipped operators $\mathcal{O} \leftrightarrow \mathcal{O}'$

$$\bar{s}\gamma_\mu P_L b \quad \longleftrightarrow \quad \bar{s}\gamma_\mu P_R b$$

$$\bar{s}i\sigma_{\mu\nu} P_R b \quad \longleftrightarrow \quad \bar{s}i\sigma_{\mu\nu} P_L b$$



- ▶ In presence of right-handed gauge boson or other kind of new particles like leptoquarks etc..

RH Current

► Amplitudes $\mathcal{A}_\perp^{L,R} = ((\tilde{C}_9^\perp + C'_9) \mp (C_{10} + C'_{10})) \mathcal{F}_\perp - \tilde{\mathcal{G}}_\perp$

$\mathcal{A}_{\parallel,0}^{L,R} = ((\tilde{C}_9^{\parallel,0} - C'_9) \mp (C_{10} - C'_{10})) \mathcal{F}_{\parallel,0} - \tilde{\mathcal{G}}_{\parallel,0}$

► Notation $r_\lambda = \frac{\text{Re}(\tilde{\mathcal{G}}_\lambda)}{\mathcal{F}_\lambda} - \text{Re}(\tilde{C}_9^\lambda)$ $\xi = \frac{C'_{10}}{C_{10}}$ $\xi' = \frac{C'_9}{C_{10}}$

► Variables $R_\perp = \frac{\frac{r_\perp}{C_{10}} - \xi'}{1 + \xi}, R_\parallel = \frac{\frac{r_\parallel}{C_{10}} + \xi'}{1 - \xi}, R_0 = \frac{\frac{r_0}{C_{10}} + \xi'}{1 - \xi}.$

► HQET limit $\frac{\tilde{\mathcal{G}}_\parallel}{\mathcal{F}_\parallel} = \frac{\tilde{\mathcal{G}}_\perp}{\mathcal{F}_\perp} = \frac{\tilde{\mathcal{G}}_0}{\mathcal{F}_0} = -\kappa \frac{2m_b m_B C_7}{q^2},$ [Grinstein, Prijol '04]
[Bobeth *et. al* '10]



$r_0 = r_\parallel = r_\perp \equiv r$ ignoring non-factorisable corrections



$R_0 = R_\parallel \neq R_\perp$ *in presence of RH currents*

RH Current

At kinematic endpoint



- exact HQET limit
- polarization independent non-factorisable correction

► Observables $F_L(q_{\max}^2) = \frac{1}{3}$, $F_{\parallel}(q_{\max}^2) = \frac{2}{3}$, $A_4(q_{\max}^2) = \frac{2}{3\pi}$,
 $F_{\perp}(q_{\max}^2) = 0$, $A_{\text{FB}}(q_{\max}^2) = 0$, $A_{5,7,8,9}(q_{\max}^2) = 0$.

[Hiller, Zwicky '14]

► Taylor series expansion around $\delta \equiv q_{\max}^2 - q^2$

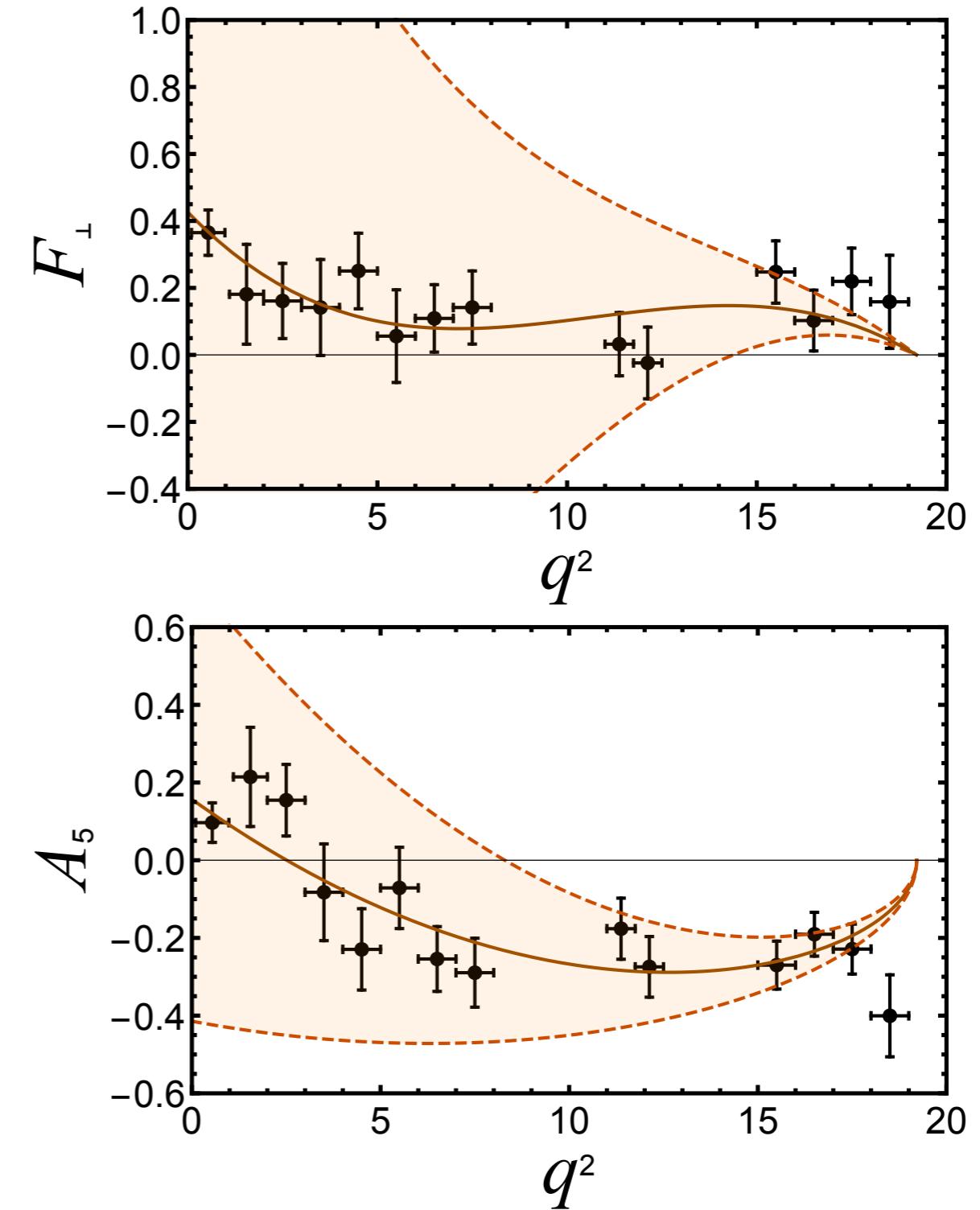
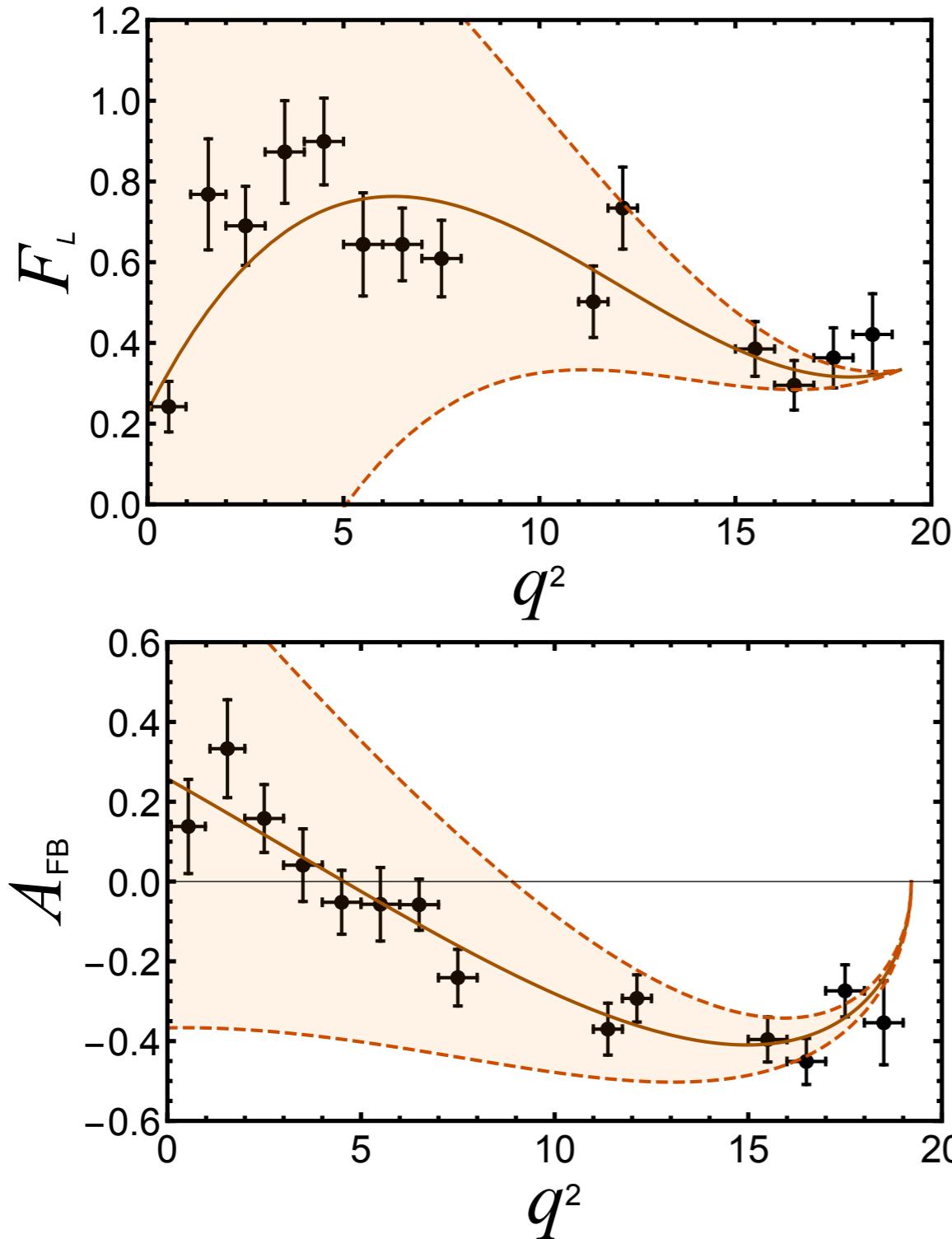
$$F_L = \frac{1}{3} + F_L^{(1)}\delta + F_L^{(2)}\delta^2 + F_L^{(3)}\delta^3$$

$$F_{\perp} = F_{\perp}^{(1)}\delta + F_{\perp}^{(2)}\delta^2 + F_{\perp}^{(3)}\delta^3$$

$$A_{\text{FB}} = A_{\text{FB}}^{(1)}\delta^{\frac{1}{2}} + A_{\text{FB}}^{(2)}\delta^{\frac{3}{2}} + A_{\text{FB}}^{(3)}\delta^{\frac{5}{2}}$$

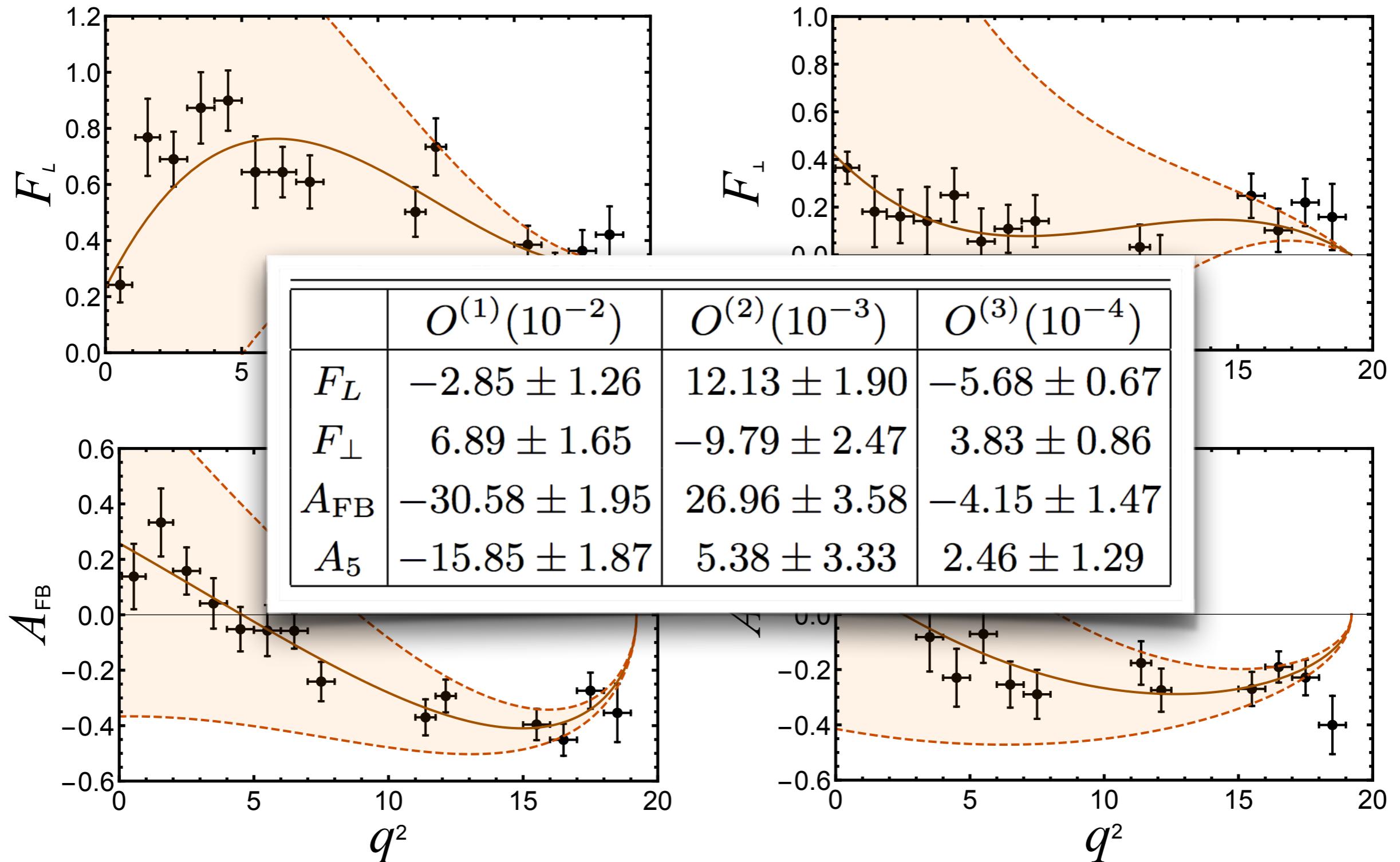
$$A_5 = A_5^{(1)}\delta^{\frac{1}{2}} + A_5^{(2)}\delta^{\frac{3}{2}} + A_5^{(3)}\delta^{\frac{5}{2}},$$

RH Current



Fit to 14 bin LHCb data including correlation among observables

RH Current



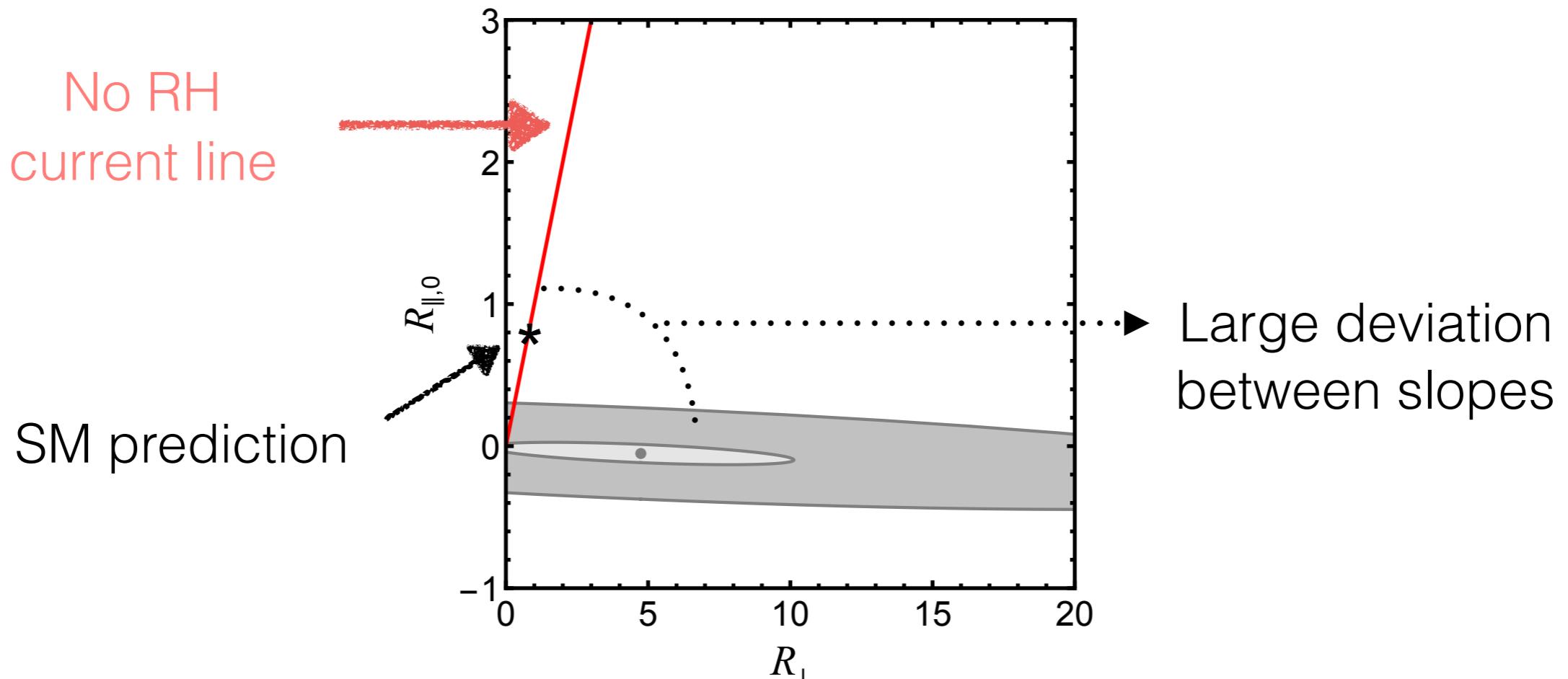
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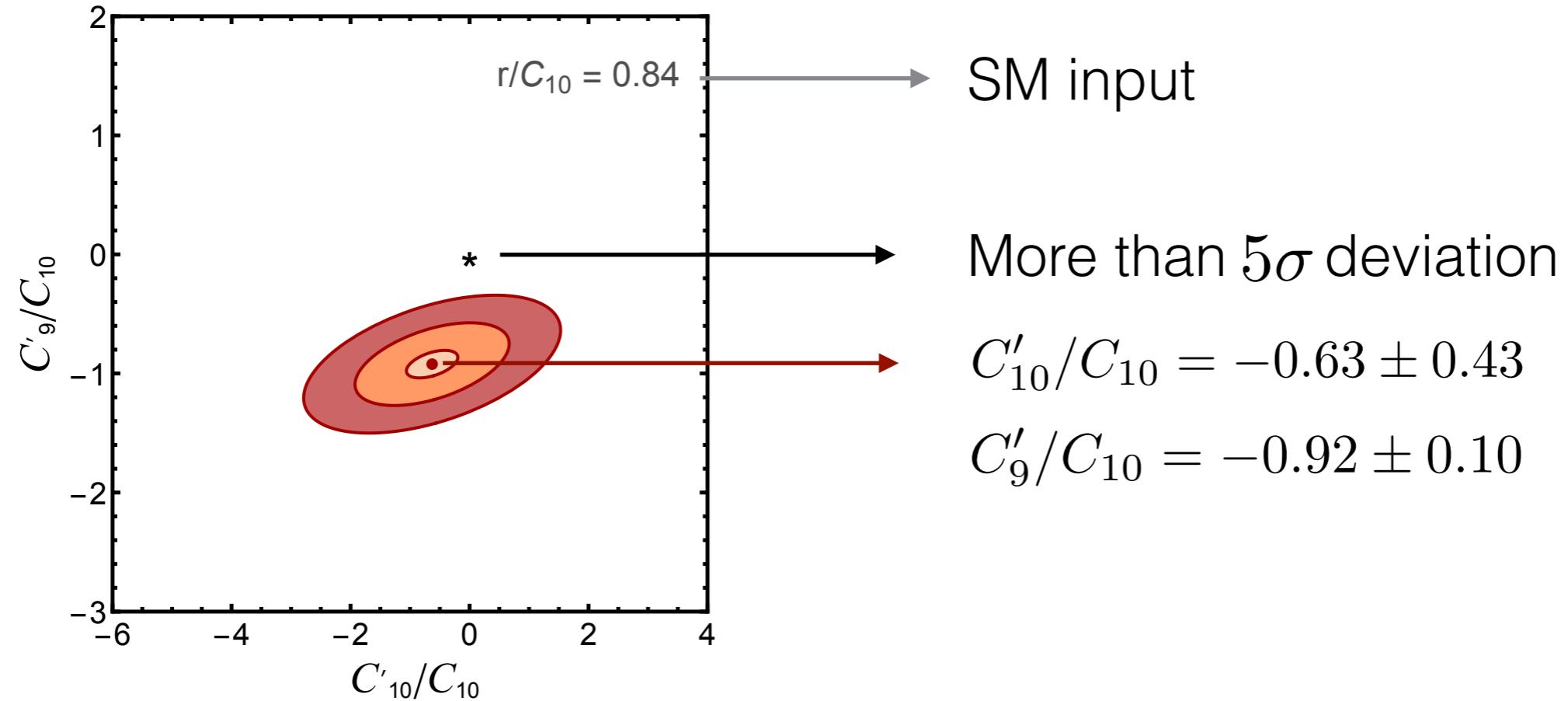
► Limiting analytic expressions

$$R_{\perp}(q_{\max}^2) = \frac{\omega_2 - \omega_1}{\omega_2 \sqrt{\omega_1 - 1}}, \quad R_{\parallel}(q_{\max}^2) = \frac{\sqrt{\omega_1 - 1}}{\omega_2 - 1} = R_0(q_{\max}^2)$$

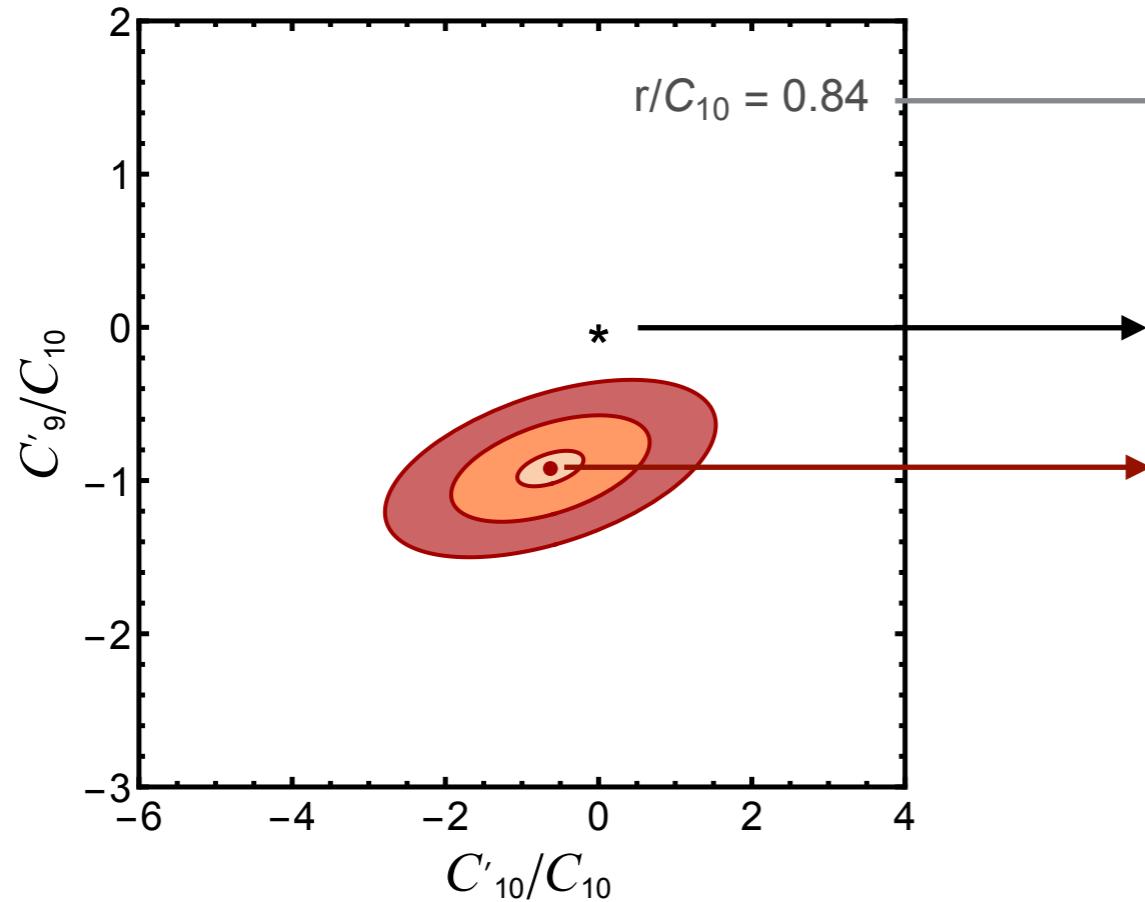
$$\omega_1 = \frac{3}{2} \frac{F_{\perp}^{(1)}}{A_{\text{FB}}^{(1)2}} \quad \text{or} \quad \frac{3}{8} \frac{F_{\perp}^{(1)}}{A_5^{(1)2}} \quad \text{and} \quad \omega_2 = \frac{4 \left(2A_5^{(2)} - A_{\text{FB}}^{(2)}\right)}{3 A_{\text{FB}}^{(1)} \left(3F_L^{(1)} + F_{\perp}^{(1)}\right)} \quad \text{or} \quad \frac{4 \left(2A_5^{(2)} - A_{\text{FB}}^{(2)}\right)}{6 A_5^{(1)} \left(3F_L^{(1)} + F_{\perp}^{(1)}\right)}$$



Results in $C'_{10}/C_{10} - C'_9/C_{10}$



Results in $C'_{10}/C_{10} - C'_9/C_{10}$



SM input

More than 5σ deviation

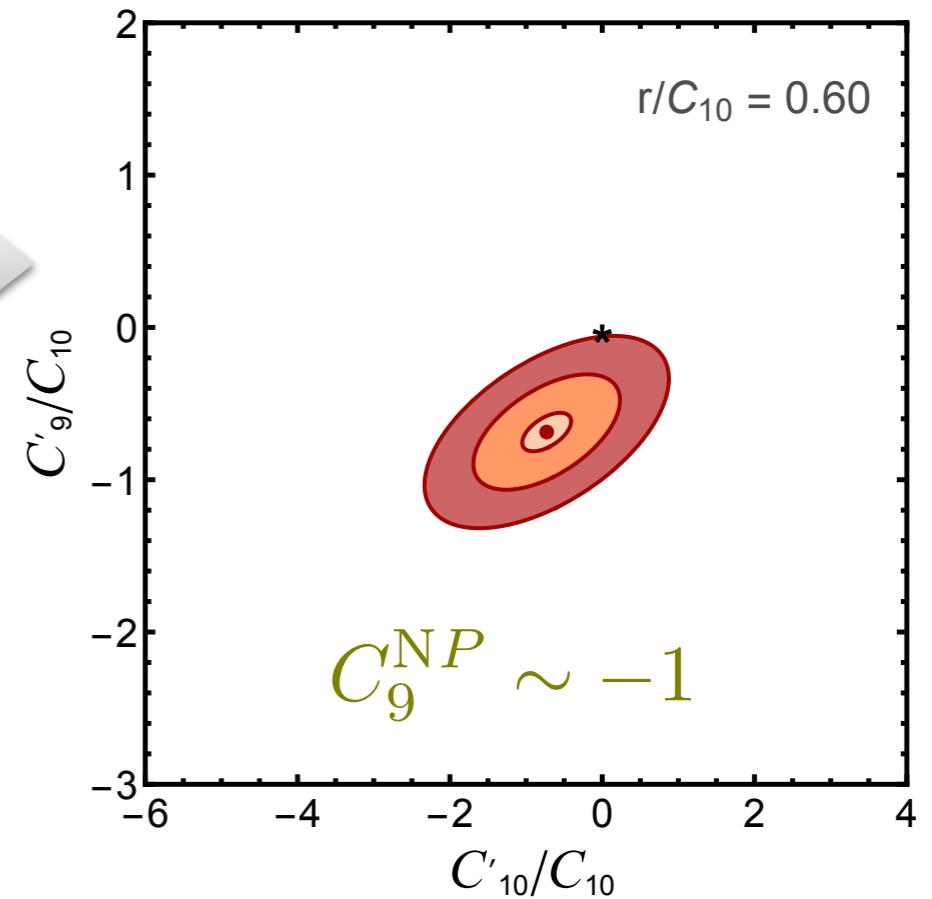
$$C'_{10}/C_{10} = -0.63 \pm 0.43$$

$$C'_9/C_{10} = -0.92 \pm 0.10$$

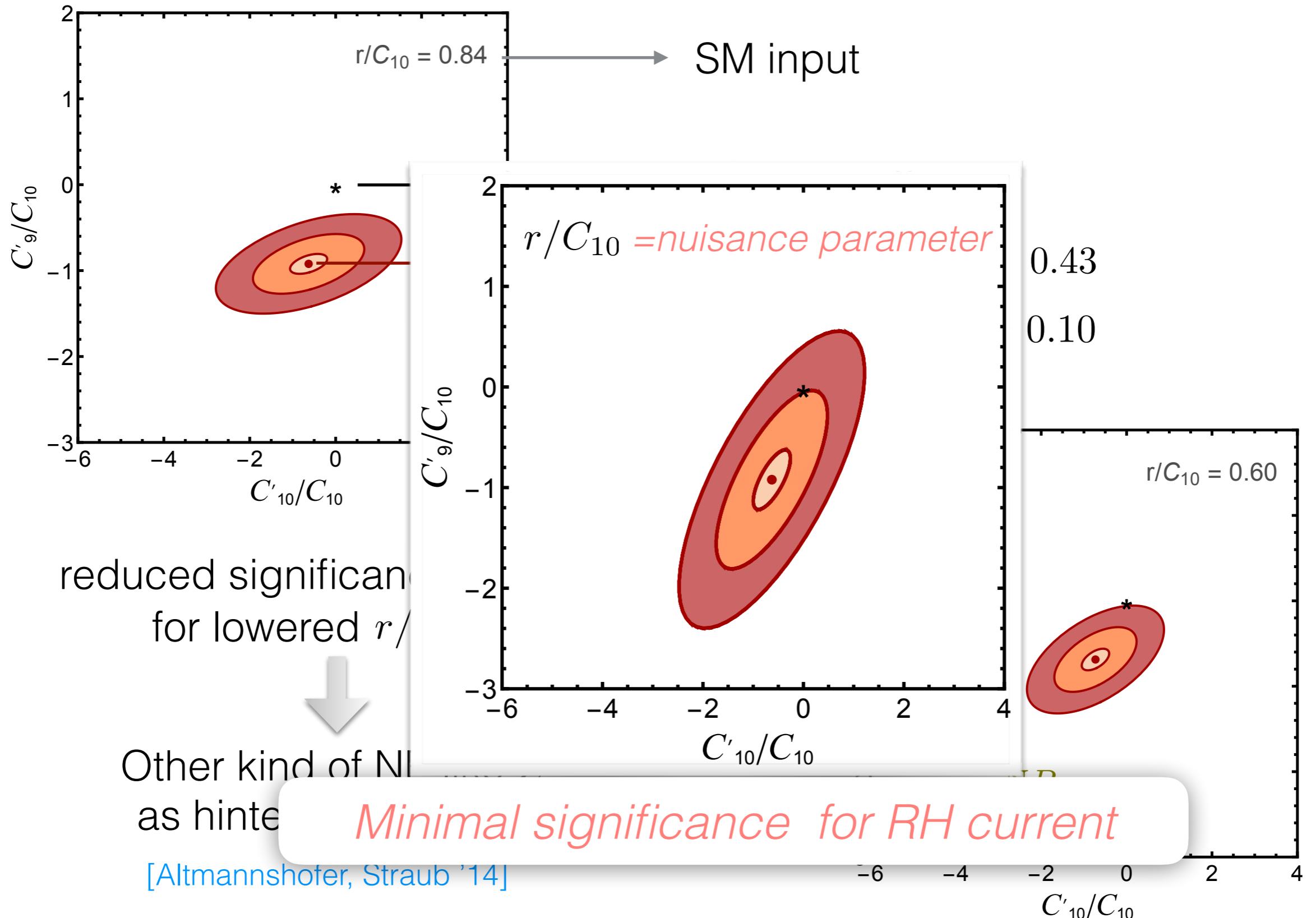
reduced significance of deviation
for lowered r/C_{10} value

Other kind of NP like Z'
as hinted in global fits

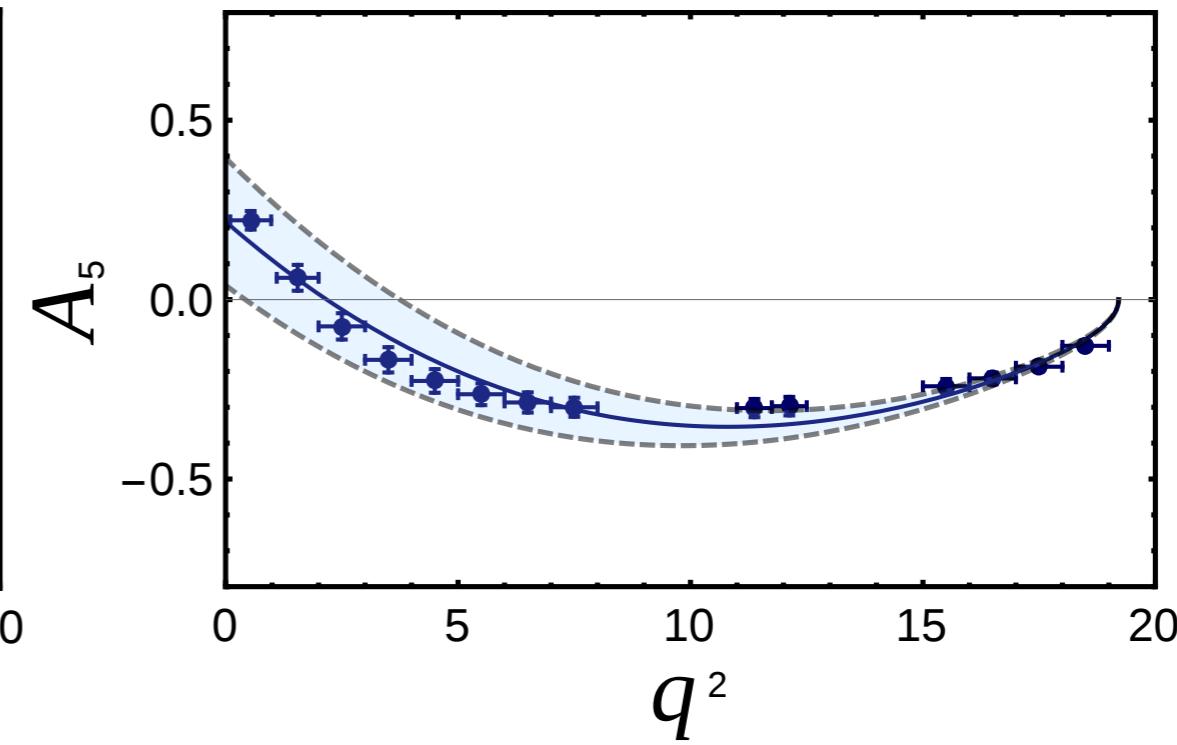
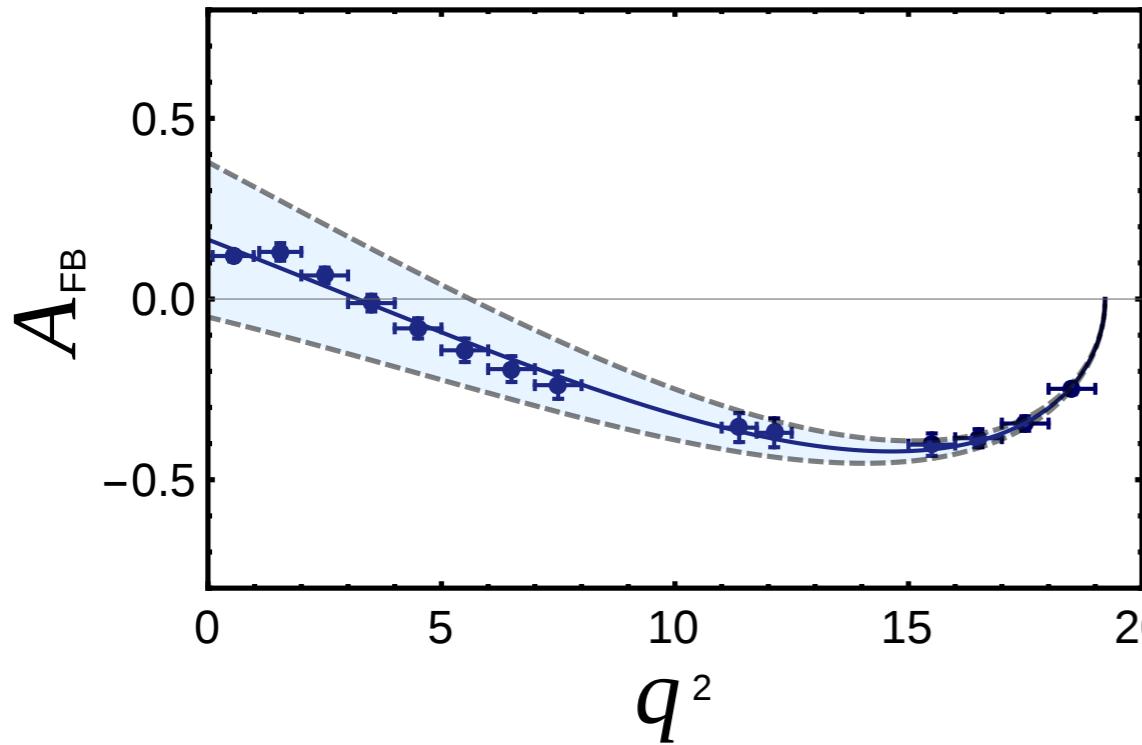
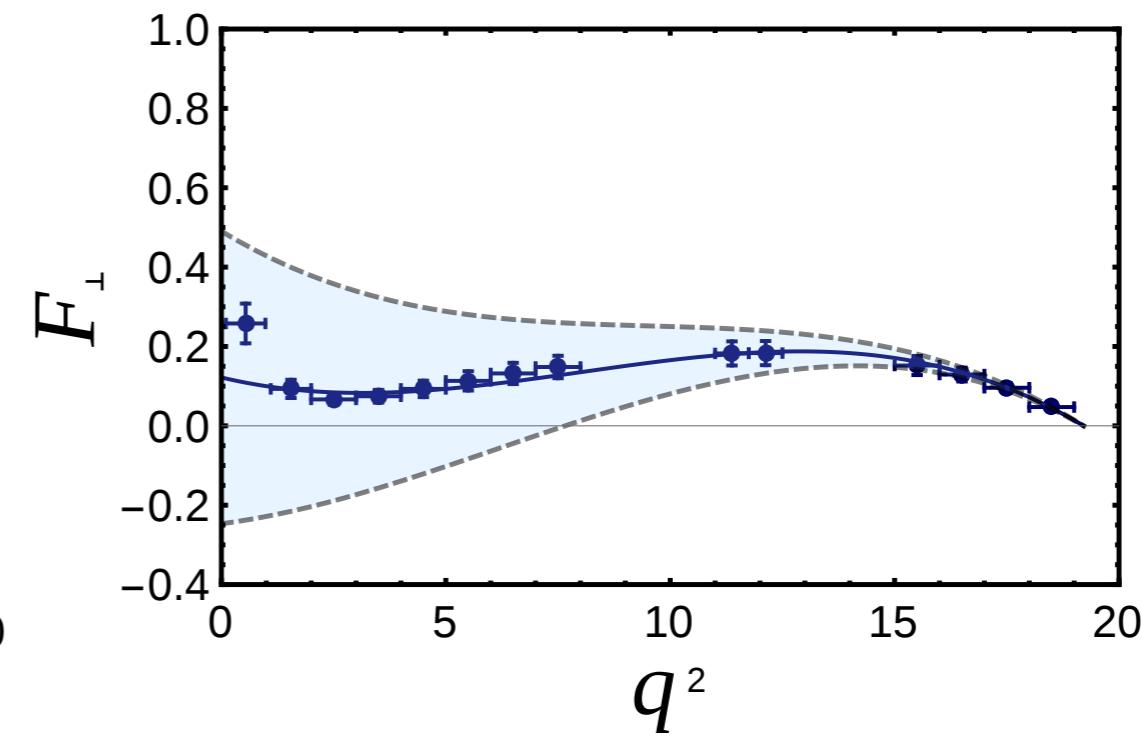
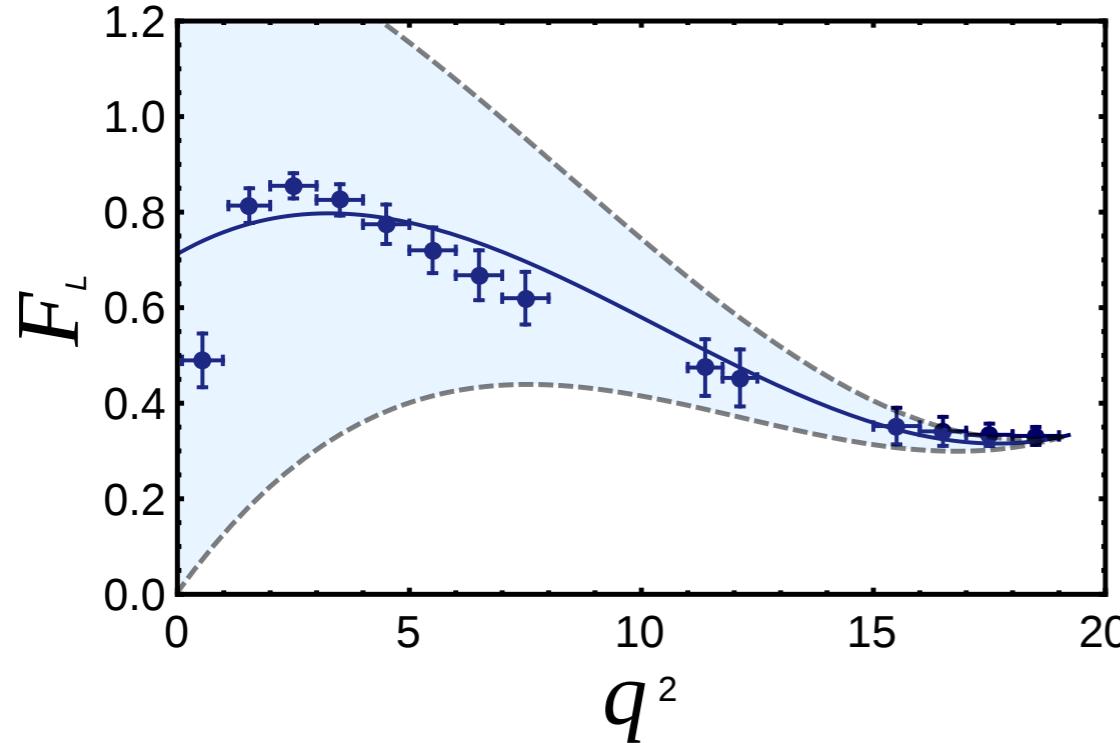
[Altmannshofer, Straub '14]



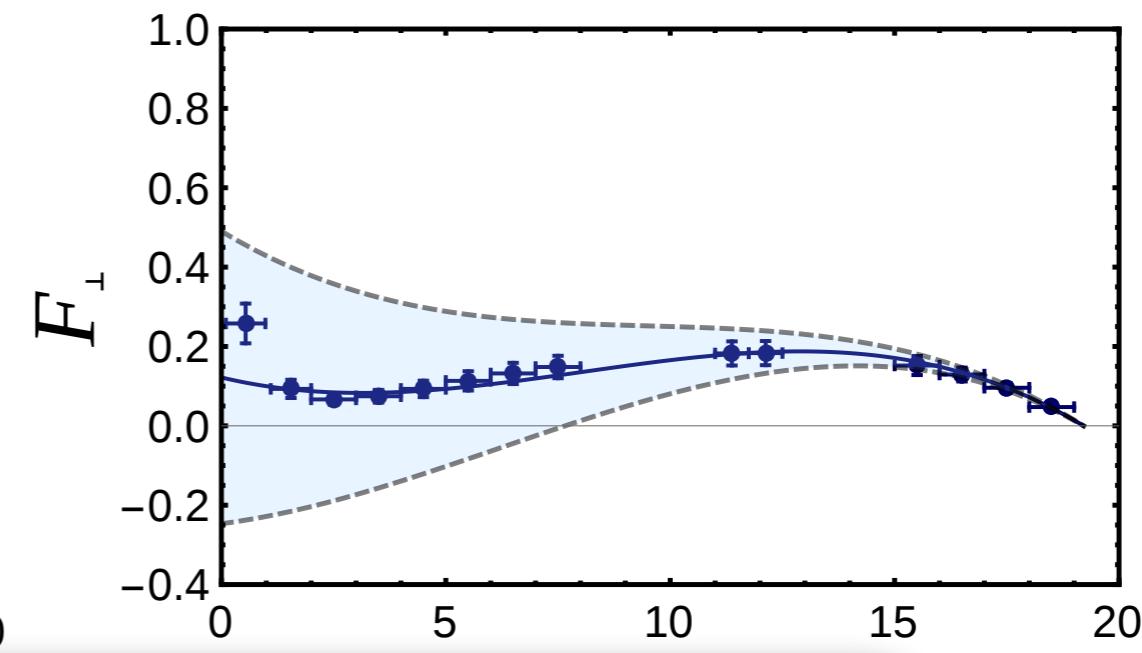
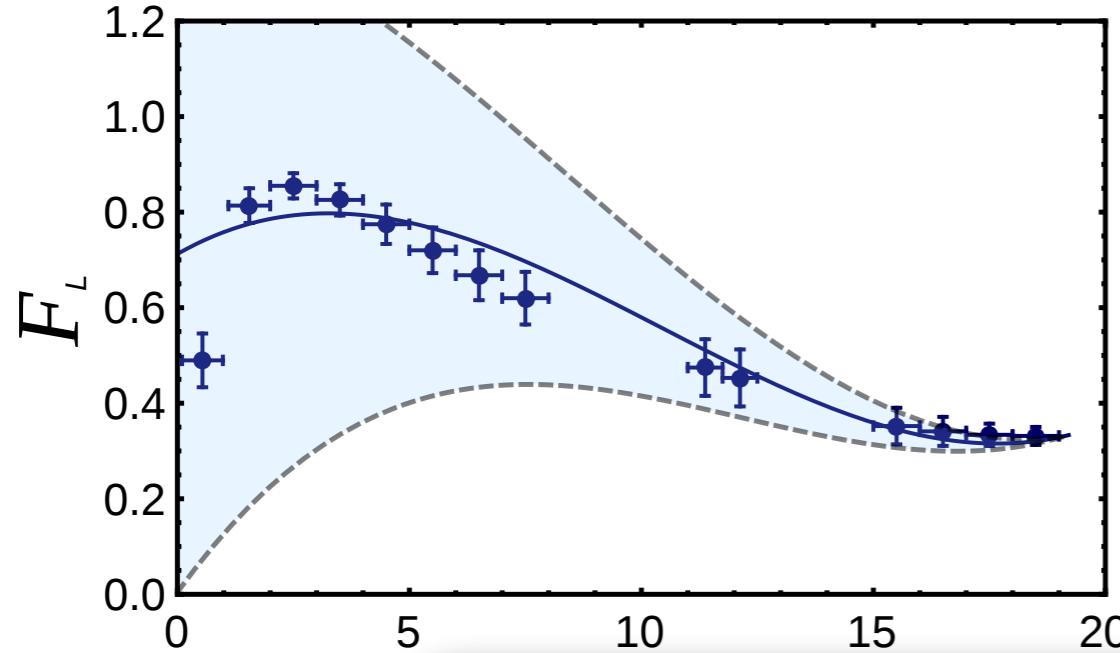
Results in $C'_{10}/C_{10} - C'_9/C_{10}$



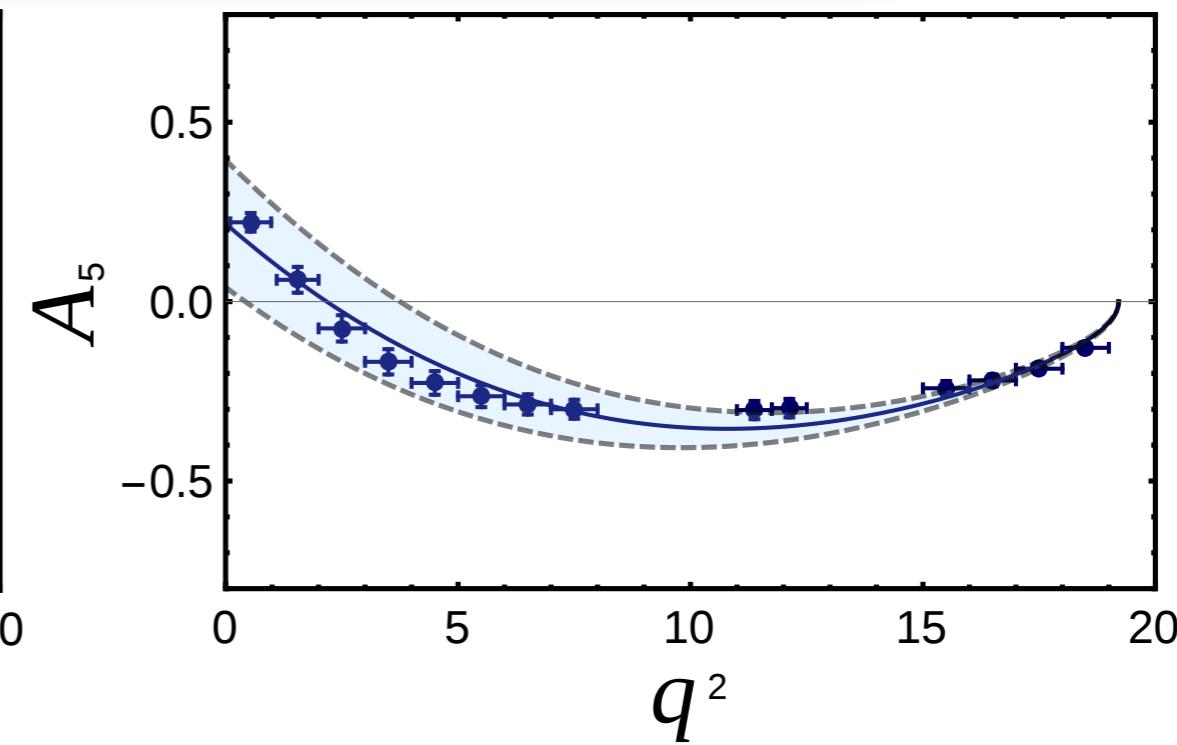
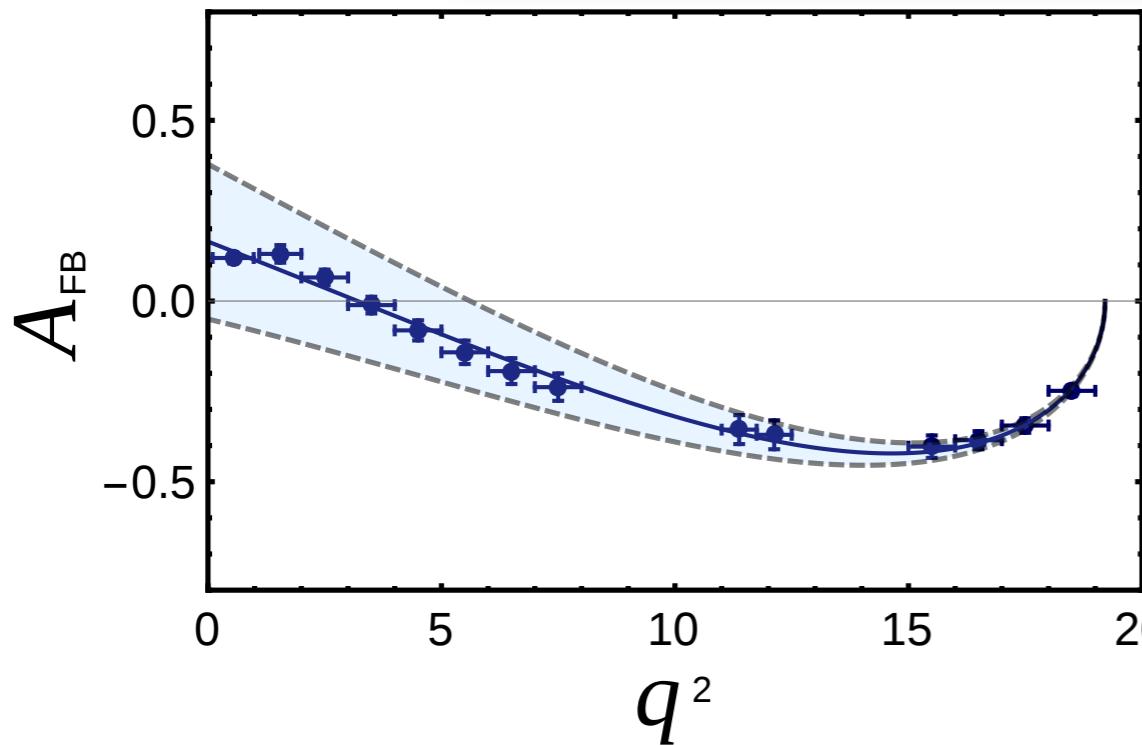
Fit to form factor observables



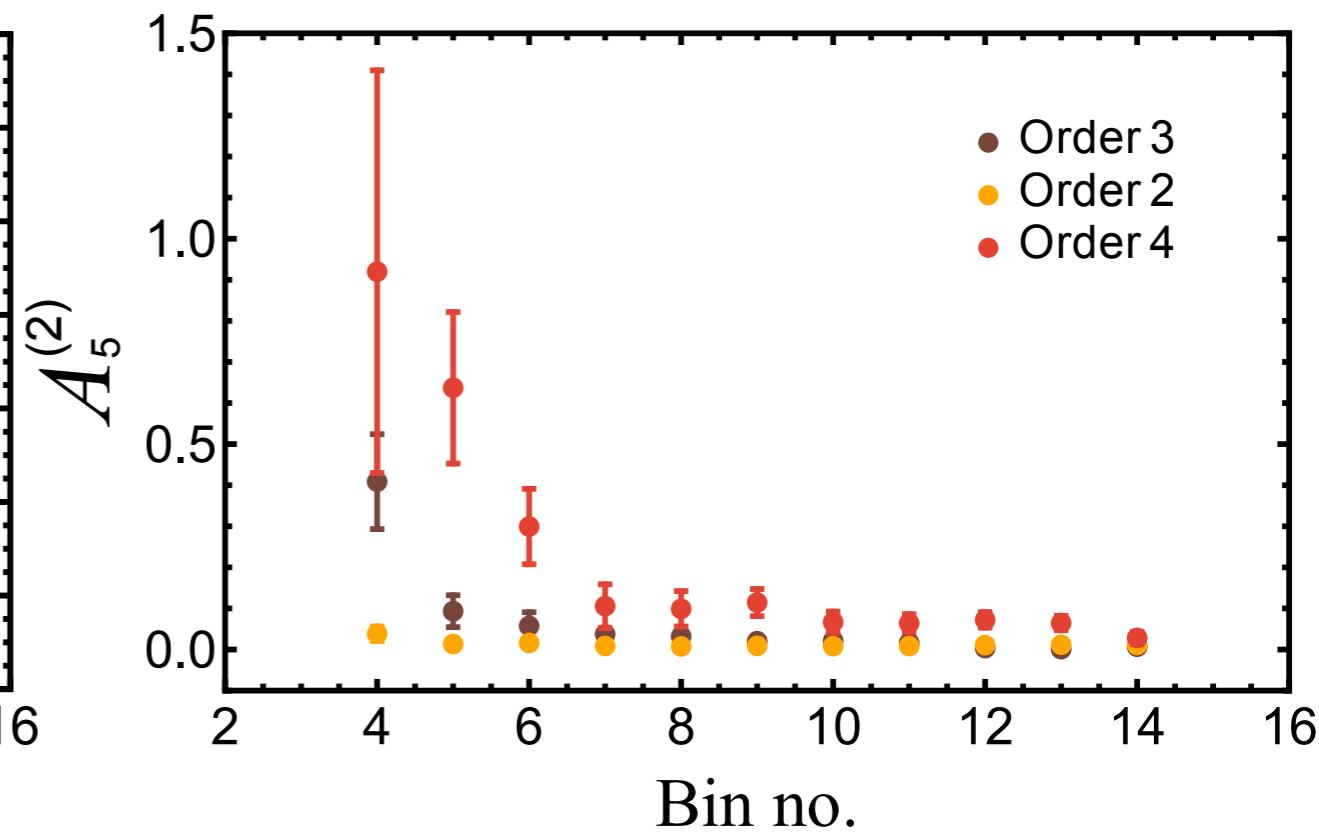
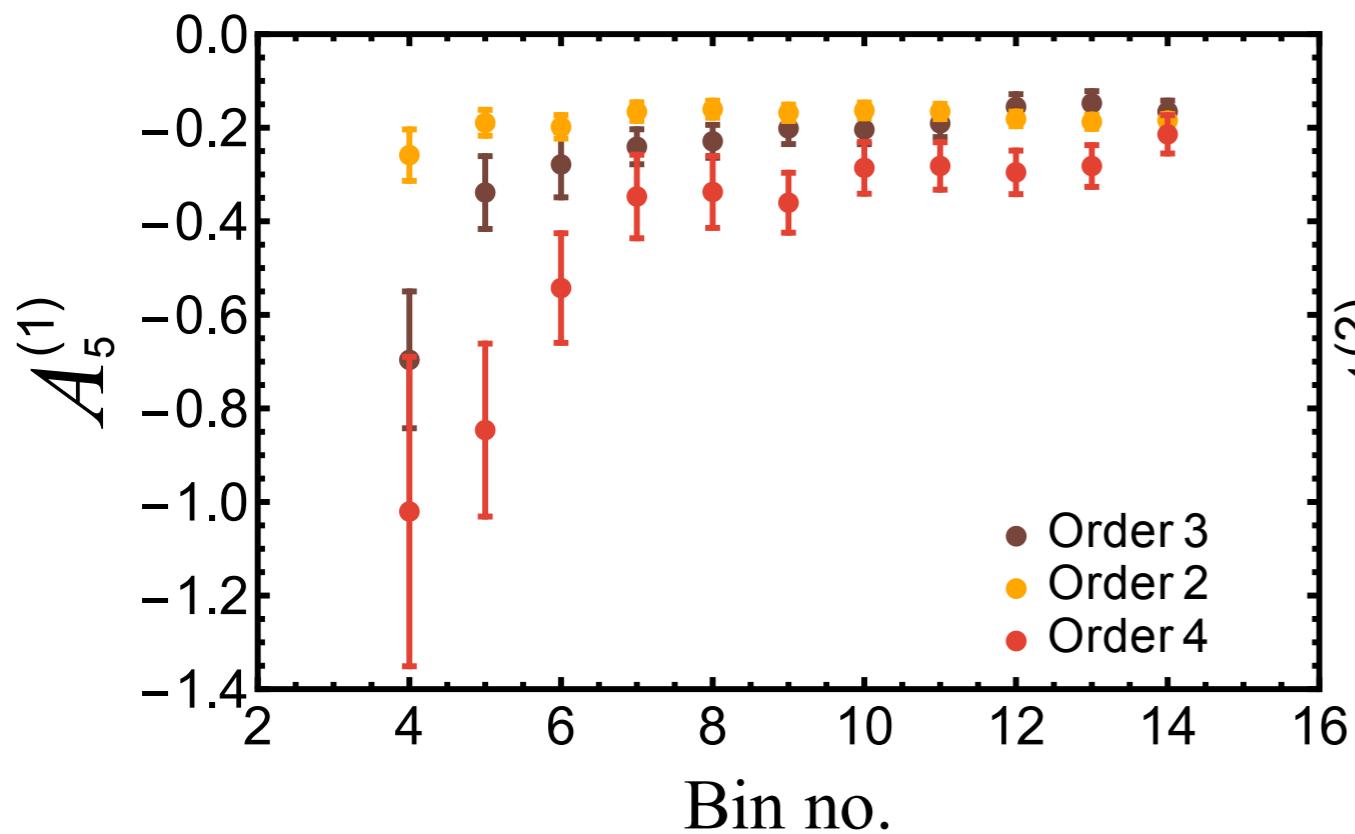
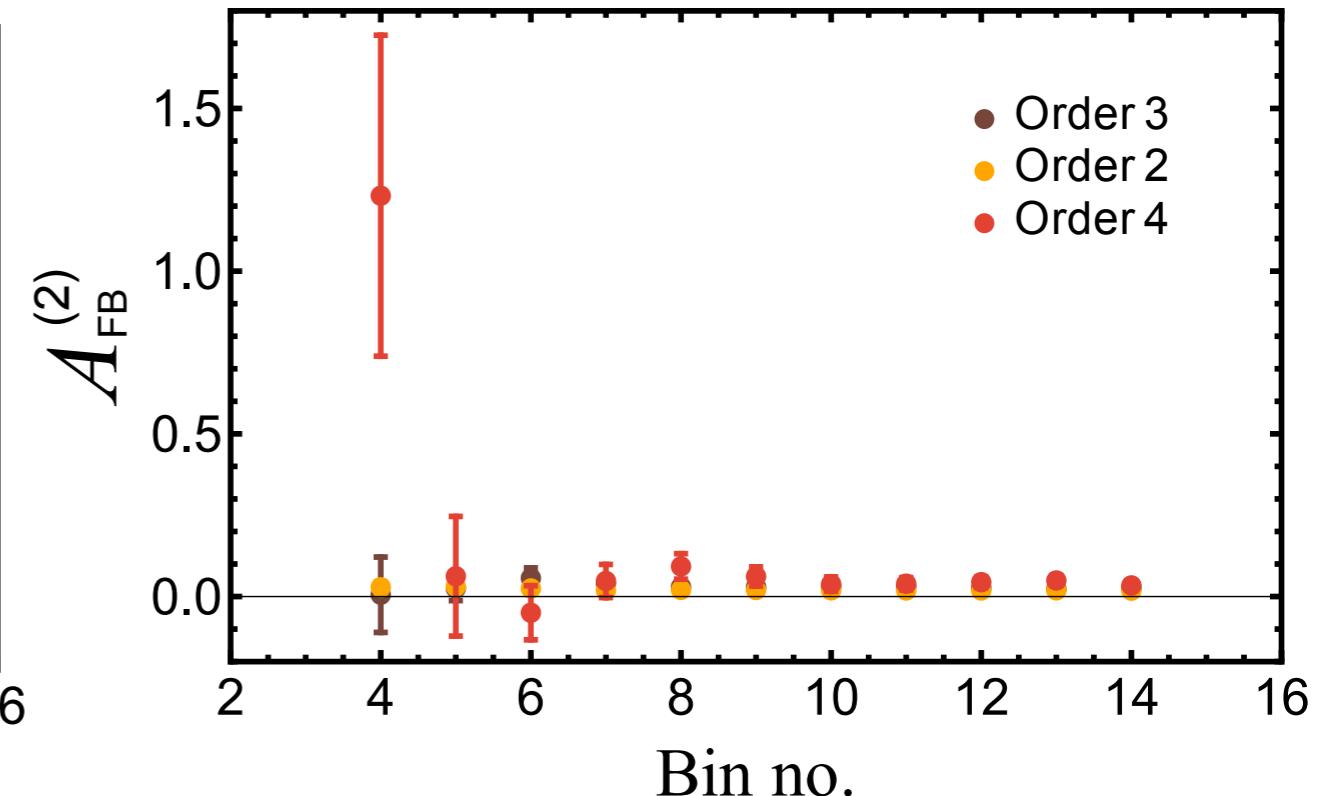
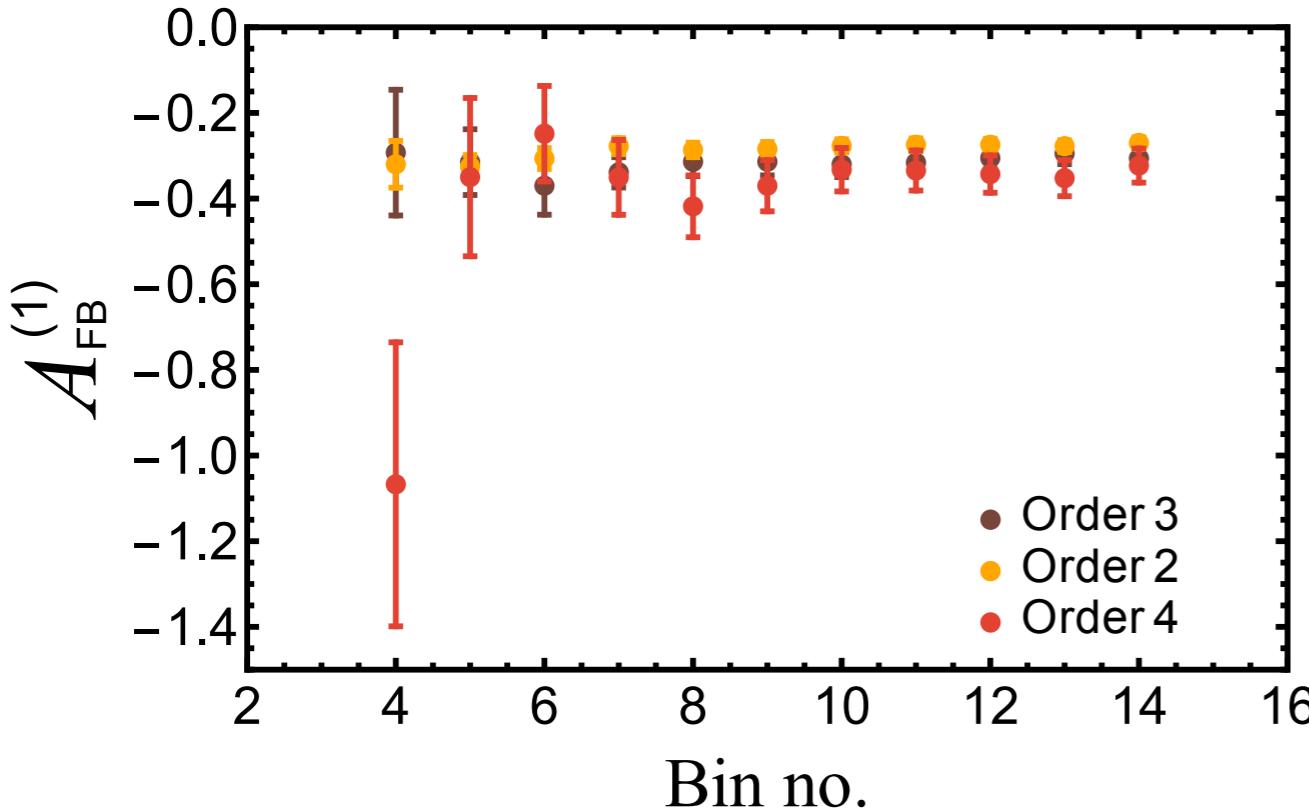
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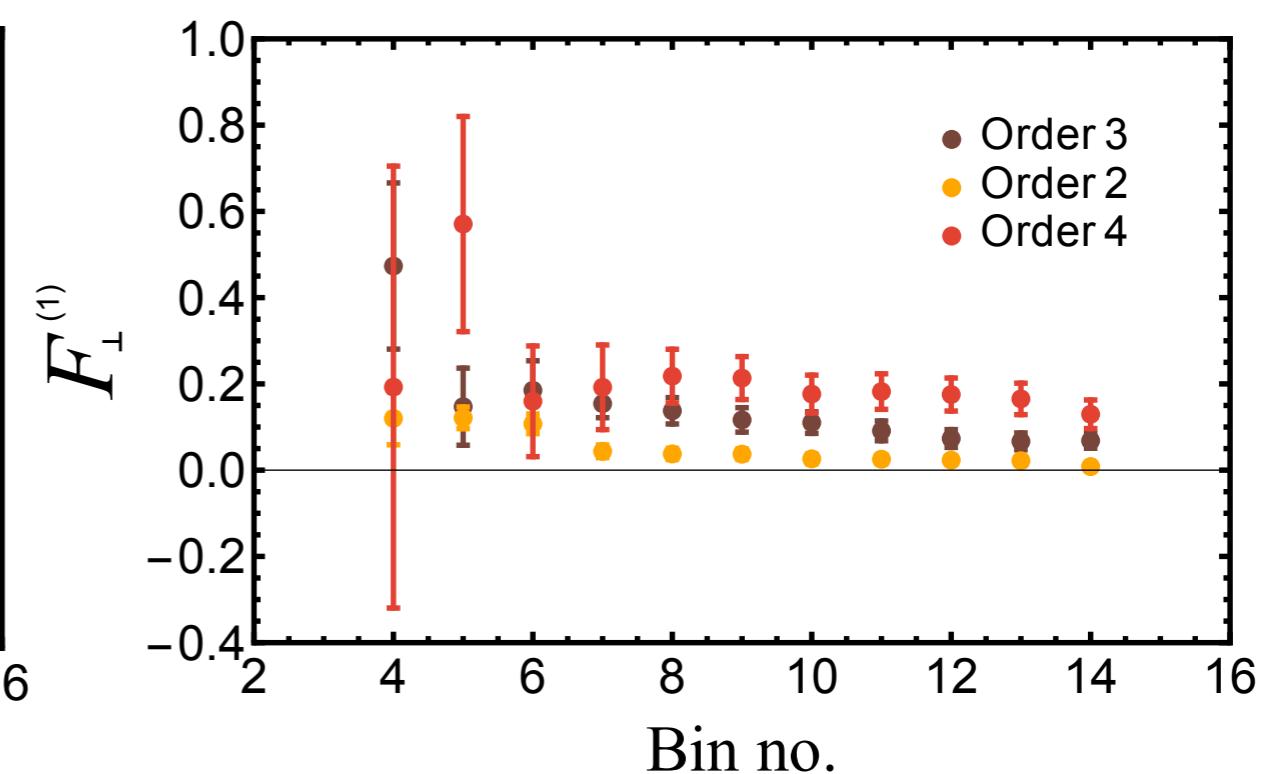
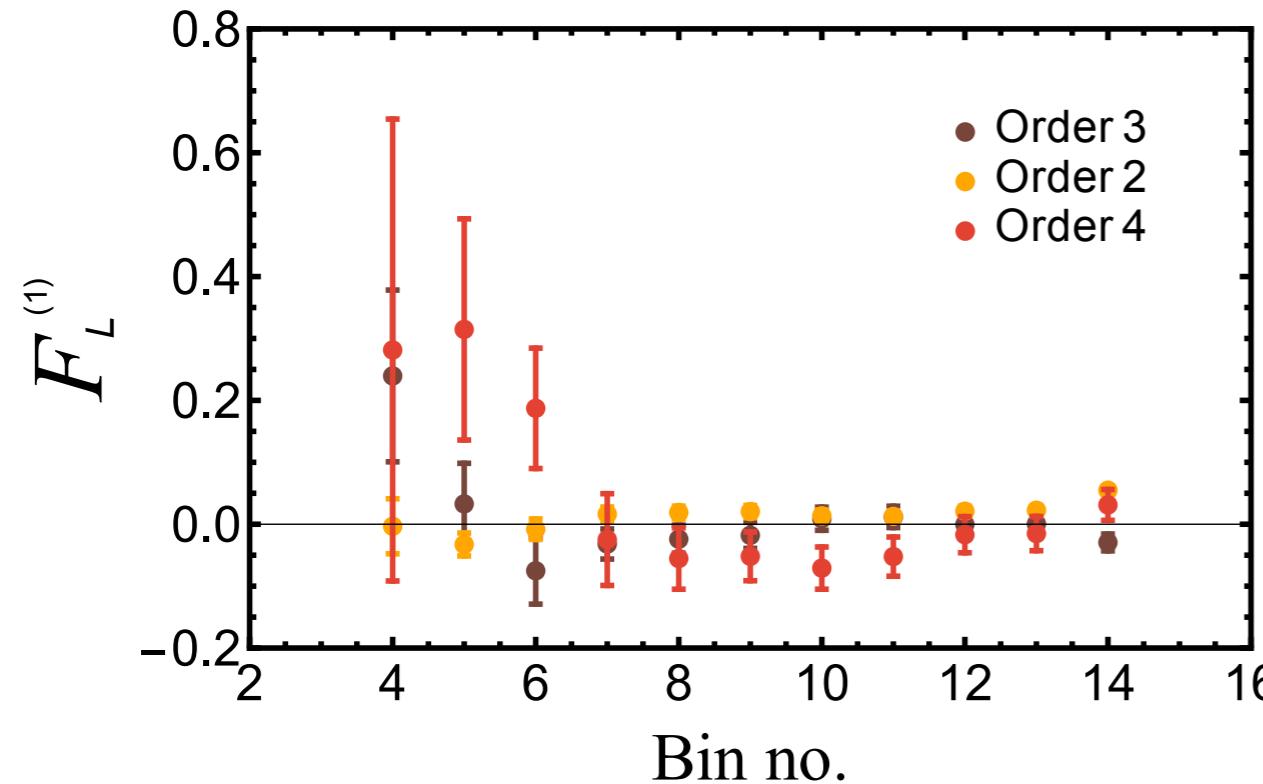
nicely explained by 3rd order polynomial



Convergence of coefficients



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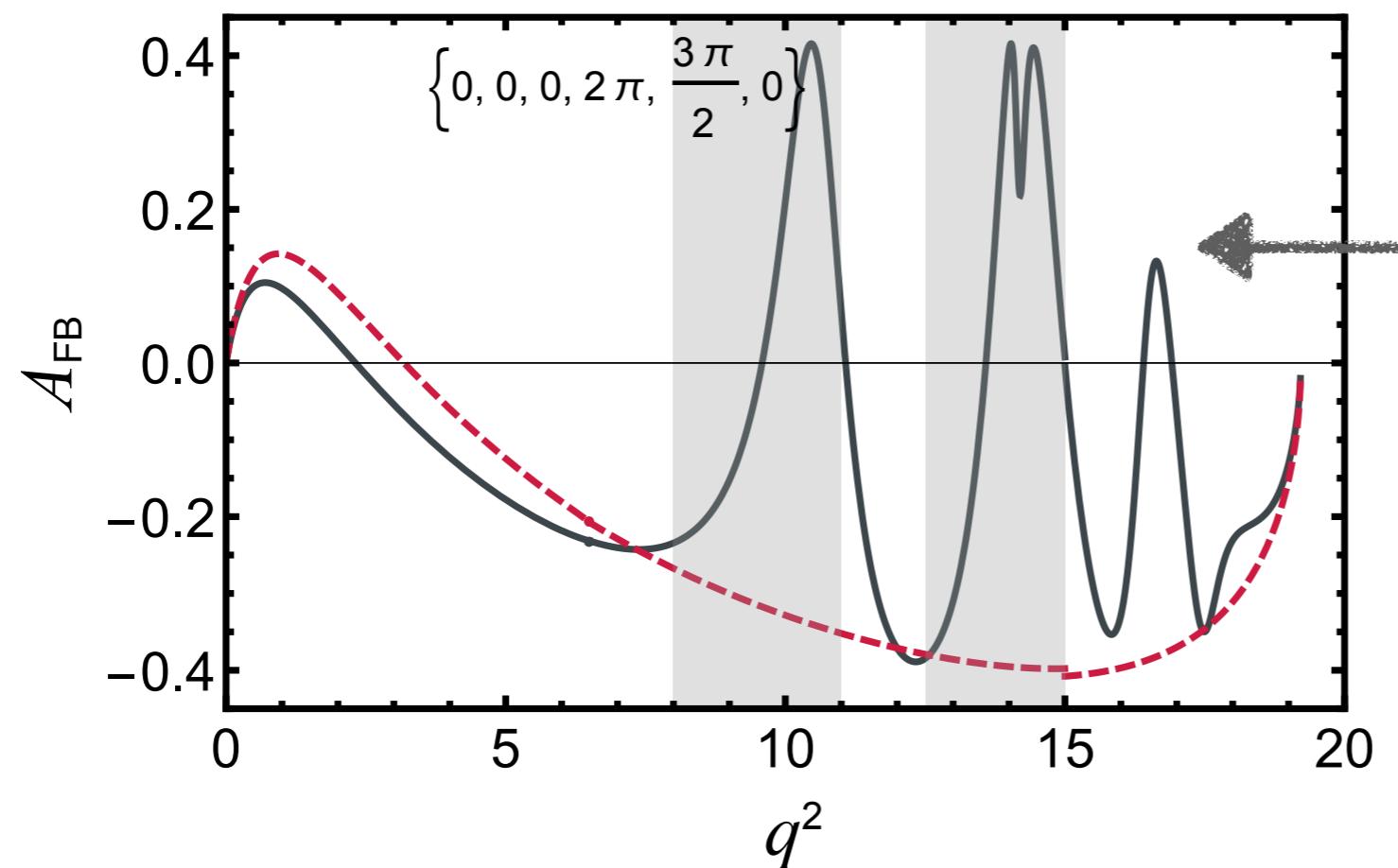


Shows a good convergence with variation in polynomial order & no. of bins used for the data fit

Resonances

$c\bar{c}$ bound states added: $J/\psi, \psi(2S), \psi(3770), \psi(4040), \psi(4160), \psi(4415)$.

Observable = Form-factors + Kruger & Sehgal parametrization



Asymmetries decrease
in high q^2 region

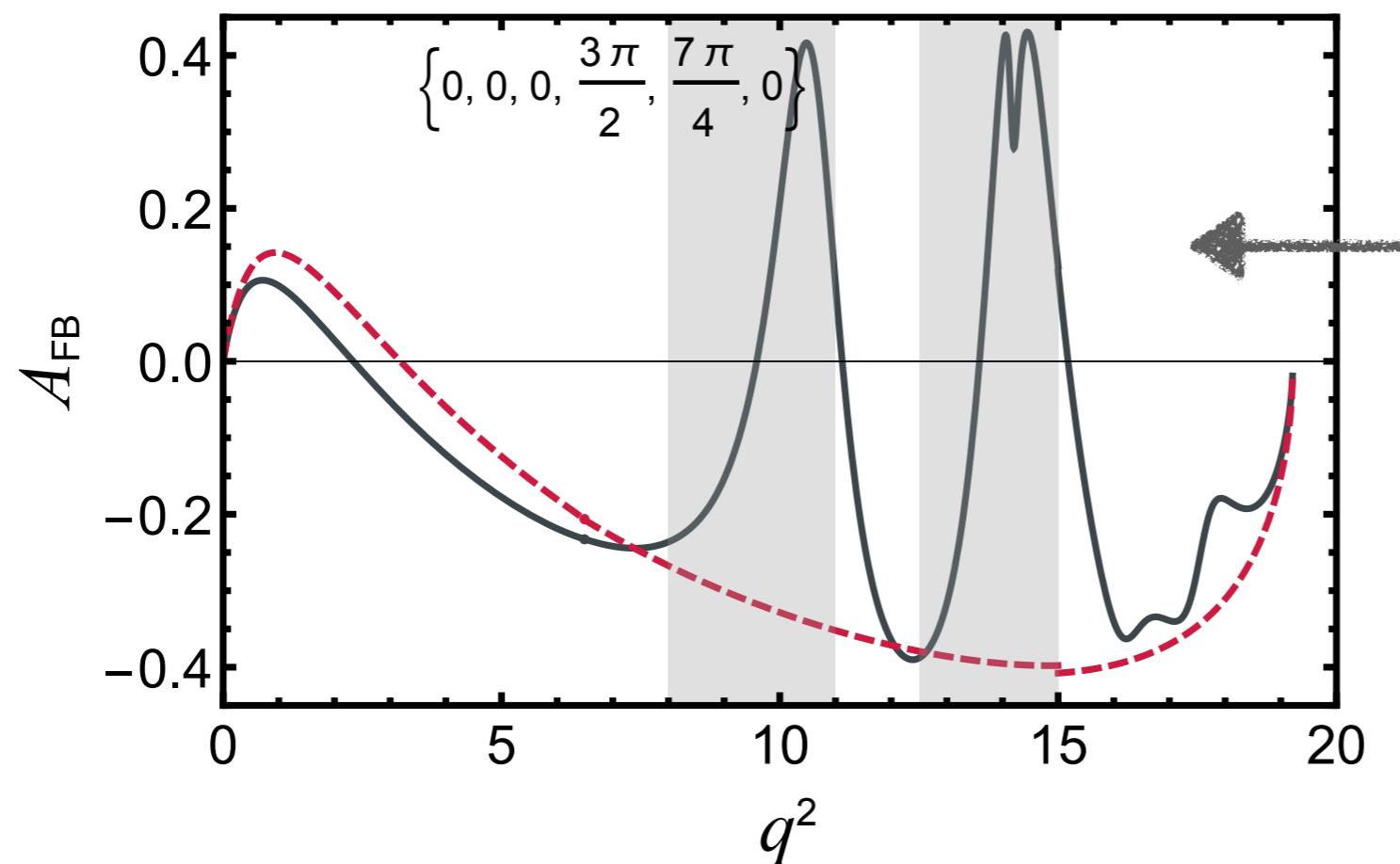
makes observable
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Random variation of each strong phases

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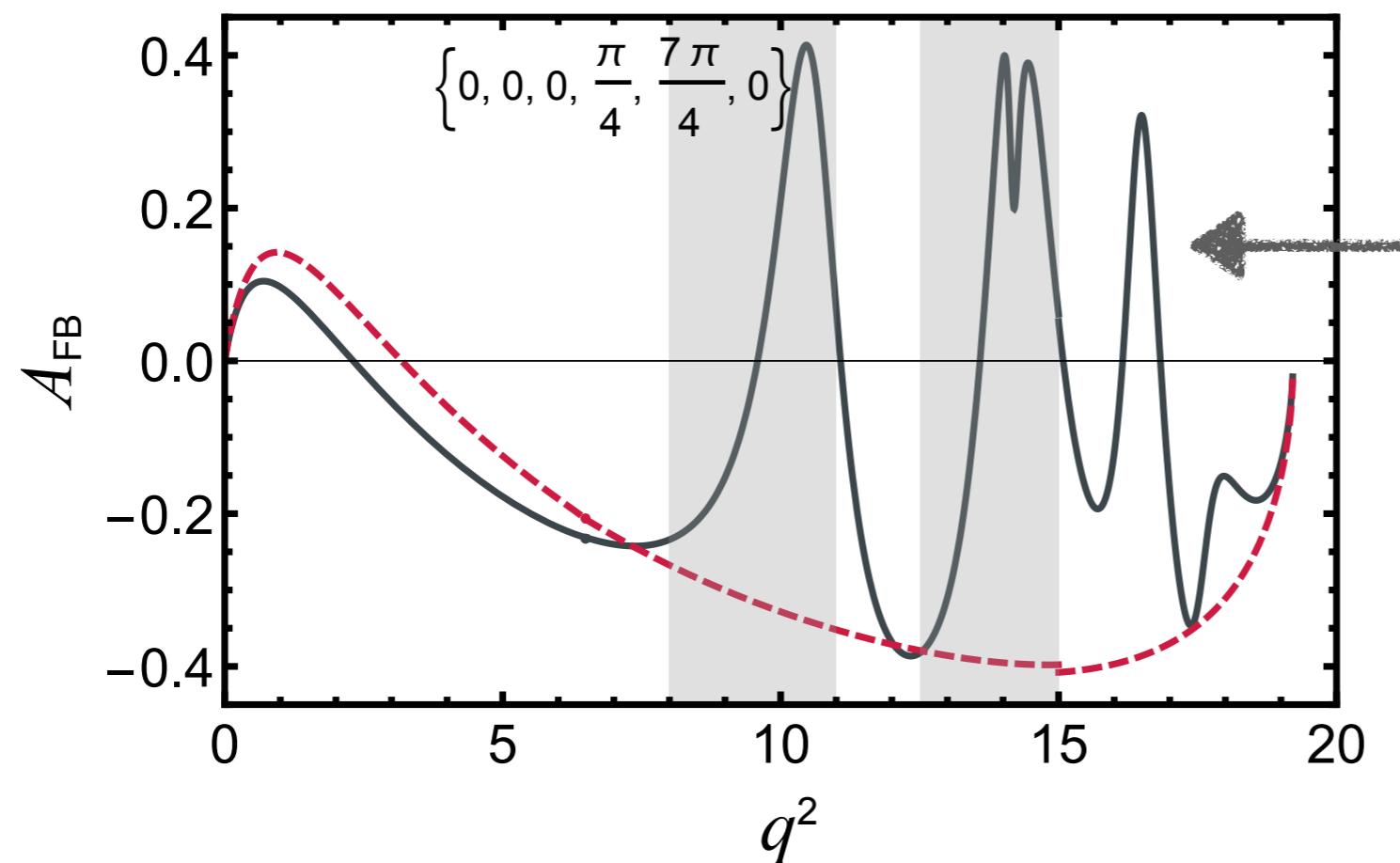
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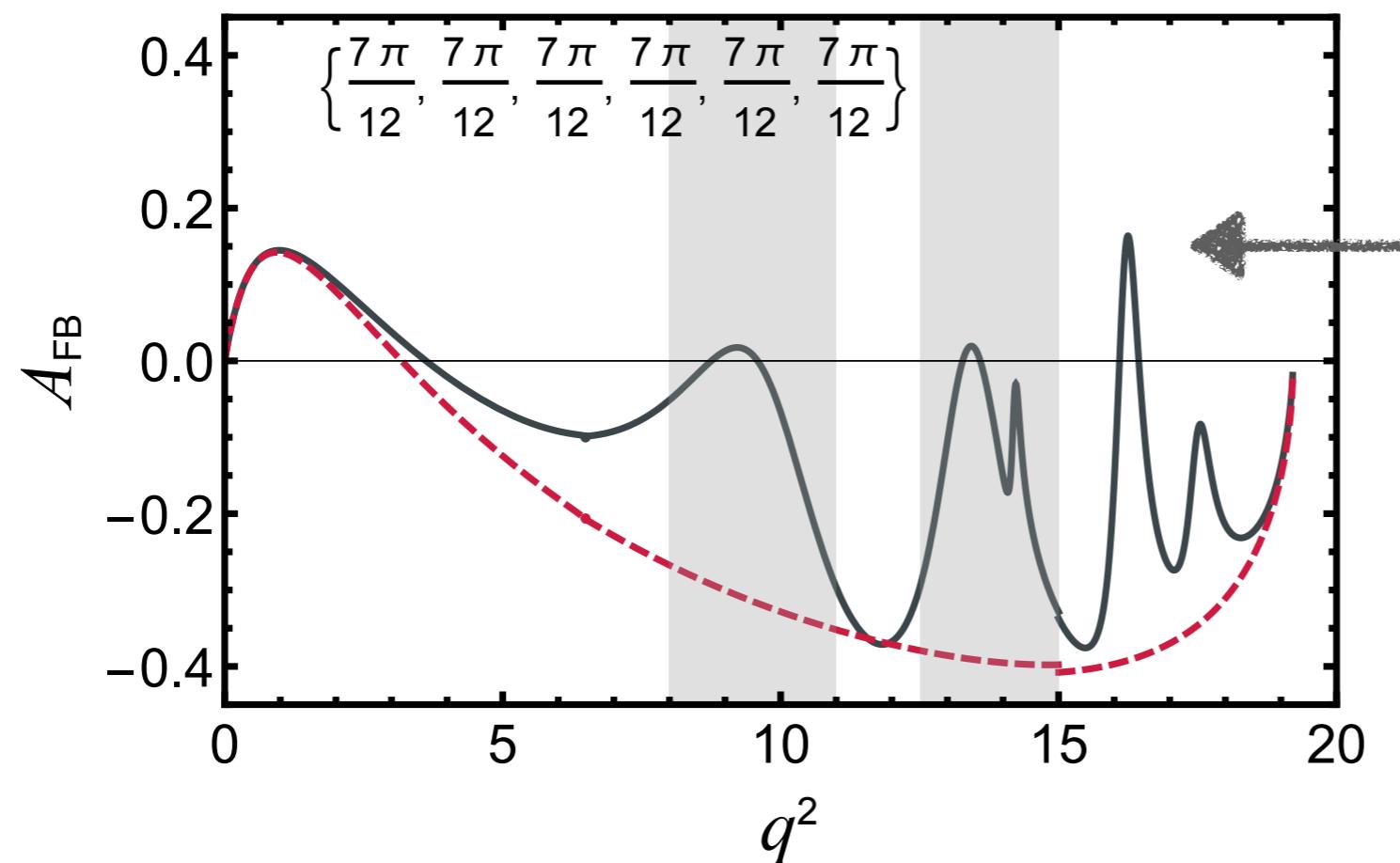
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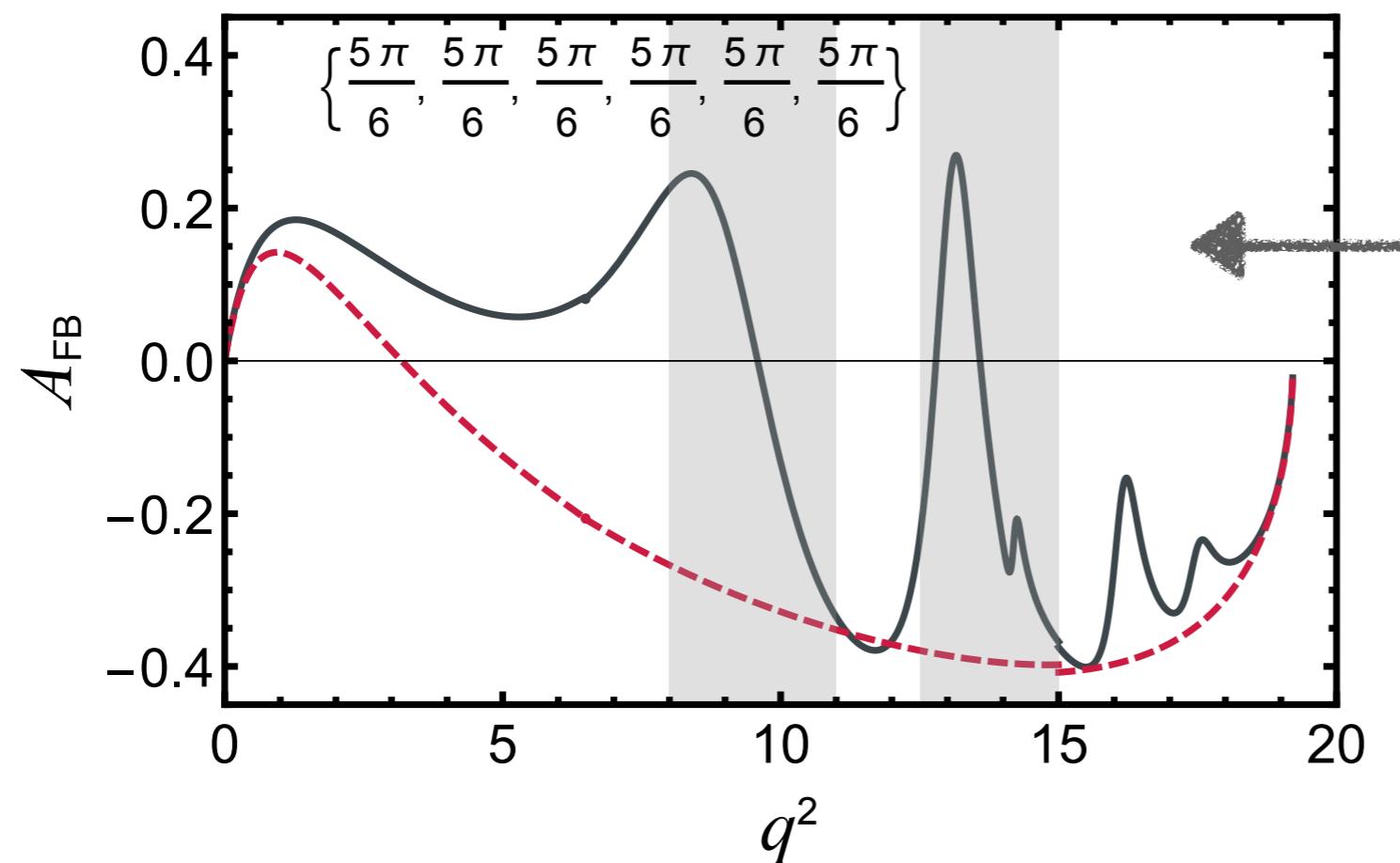
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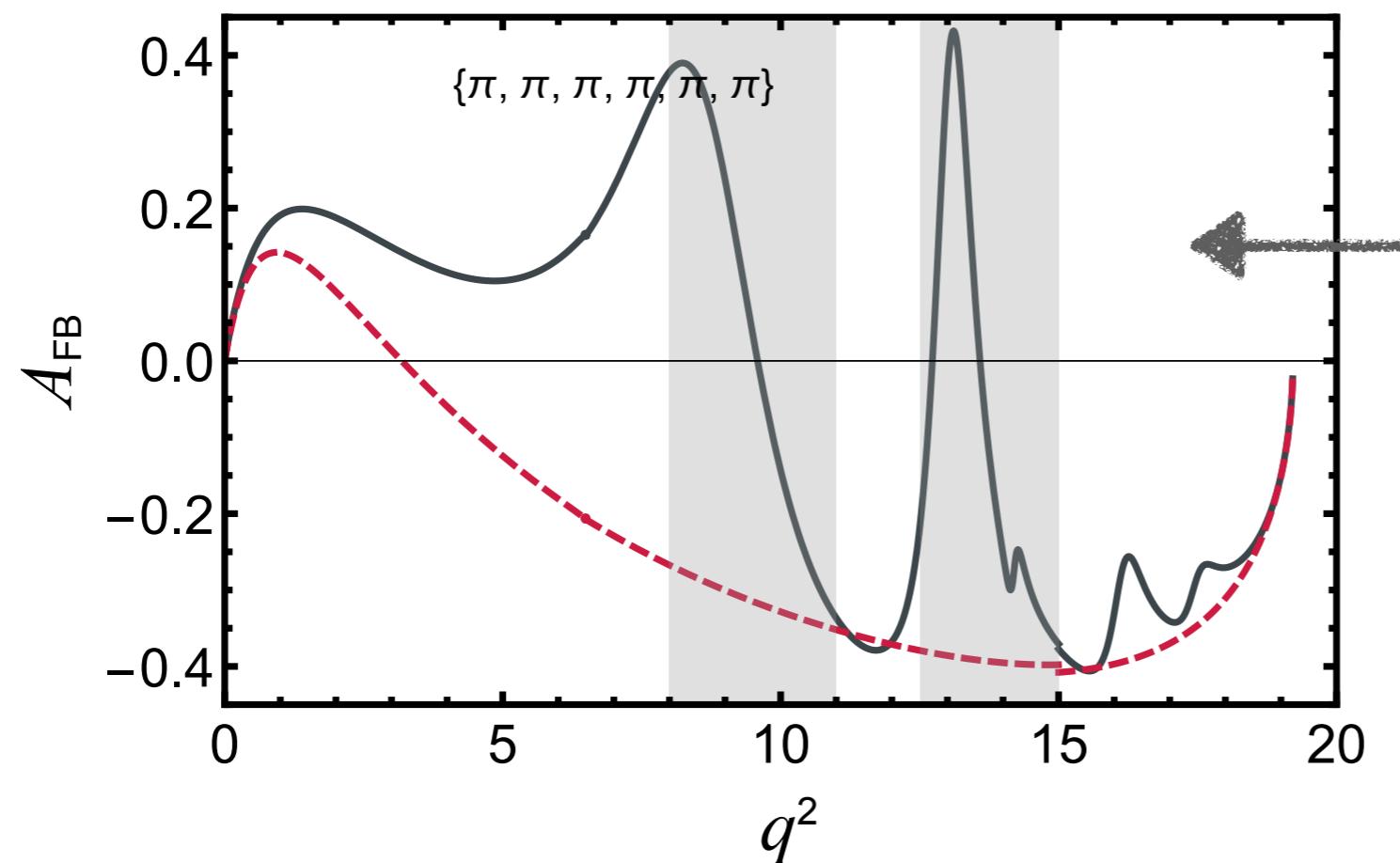
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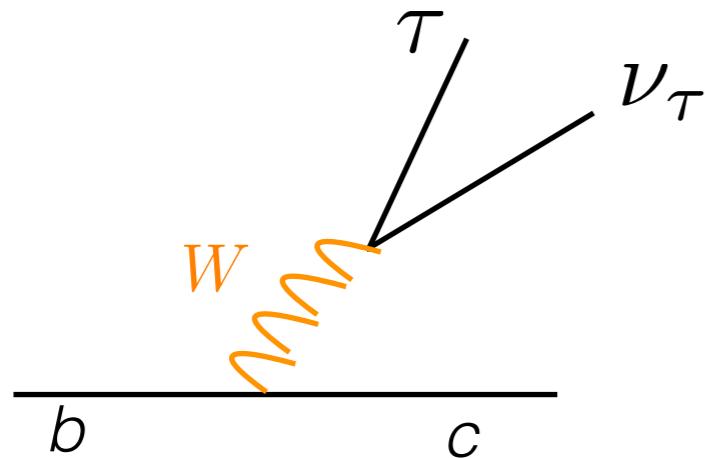
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Random variation of each strong phases

Lepton non-universality

- ▶ Exciting discrepancies observed in charged current B decays



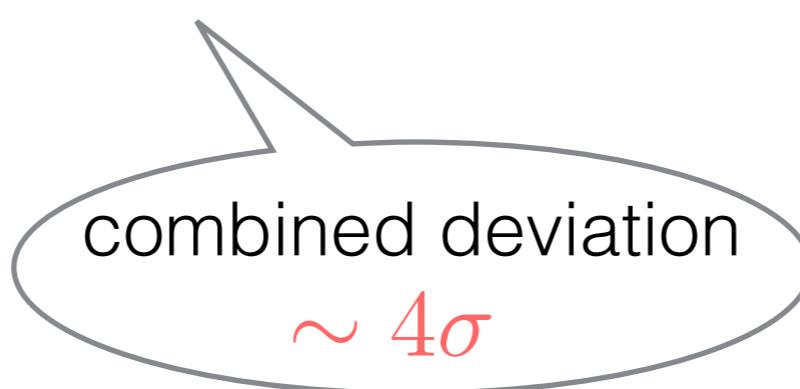
$$\mathcal{H}^{\text{eff}} = \frac{4G_F}{\sqrt{2}} V_{cb} (1 + C^{\text{NP}}) (\bar{c}_L \gamma_\mu b_L)(\bar{\tau}_L \gamma^\mu \nu_\tau)$$

$$R(D^{(*)}) \equiv \frac{\text{BR}(B \rightarrow D^{(*)}\tau\nu)}{\text{BR}(B \rightarrow D^{(*)}\ell\nu)}, \quad \ell \in \{e, \mu\}$$

$$R(D) = (1.34 \pm 0.17) \times R(D)_{\text{SM}}, \quad R(D^*) = (1.23 \pm 0.07) \times R(D^*)_{\text{SM}}$$

2.2σ

3.3σ



Lepton non-universality

- ▶ Discrepancies in neutral current B decays also

$$R_{K^{(*)}} \equiv \frac{\text{BR}(B \rightarrow K^{(*)}\mu\mu)}{\text{BR}(B \rightarrow K^{(*)}ee)}$$

$R_K = 0.745^{+0.090}_{-0.074} \pm 0.036$	$q^2 \in [1 : 6] \text{ GeV}^2$	$\xrightarrow{\text{red arrow}}$ 2.6σ
$R_{K^*}^{\text{low}} = 0.660^{+0.110}_{-0.070} \pm 0.024$	$q^2 \in [0.045 : 1.1] \text{ GeV}^2$	$\xrightarrow{\text{red arrow}}$ 2.1σ
$R_{K^*}^{\text{cntr}} = 0.685^{+0.113}_{-0.069} \pm 0.047$	$q^2 \in [1.1 : 6] \text{ GeV}^2$	$\xrightarrow{\text{red arrow}}$ 2.4σ

$$\begin{aligned}\Phi &\equiv d\text{BR}(B_s \rightarrow \phi\mu\mu)/dq^2 \Big|_{q^2 \in [1:6] \text{ GeV}^2} \\ &= (2.58^{+0.33}_{-0.31} \pm 0.08 \pm 0.19) \times 10^{-8} \text{ GeV}^{-2} \quad (\text{exp}) \\ &= (4.81 \pm 0.56) \times 10^{-8} \text{ GeV}^{-2} \quad (\text{SM})\end{aligned}$$

3 σ

Lepton non-universality

- ▶ Constraints from other modes

$$\text{BR}(B_s \rightarrow \mu\mu) = \frac{(3.0 \pm 0.6^{+0.3}_{-0.2}) \times 10^{-9} \text{ (exp.)}}{(3.65 \pm 0.23) \times 10^{-9} \text{ (SM)}}$$

well in agreement

$$\text{BR}(B \rightarrow K^{(*)}\nu\bar{\nu}) < 1.6 \text{ (2.7)} \times 10^{-5}$$

$$\text{BR}(B^+ \rightarrow K^+\mu^\pm\tau^\mp) < 4.5 \text{ (2.8)} \times 10^{-5}$$

$$\text{BR}(B_s \rightarrow \tau\tau) < 6.8 \times 10^{-3}$$

Quite challenging to explain all anomalies together by evading all the bounds.

Lepton non-universality

- ▶ NP operators with 2nd & 3rd generation fields

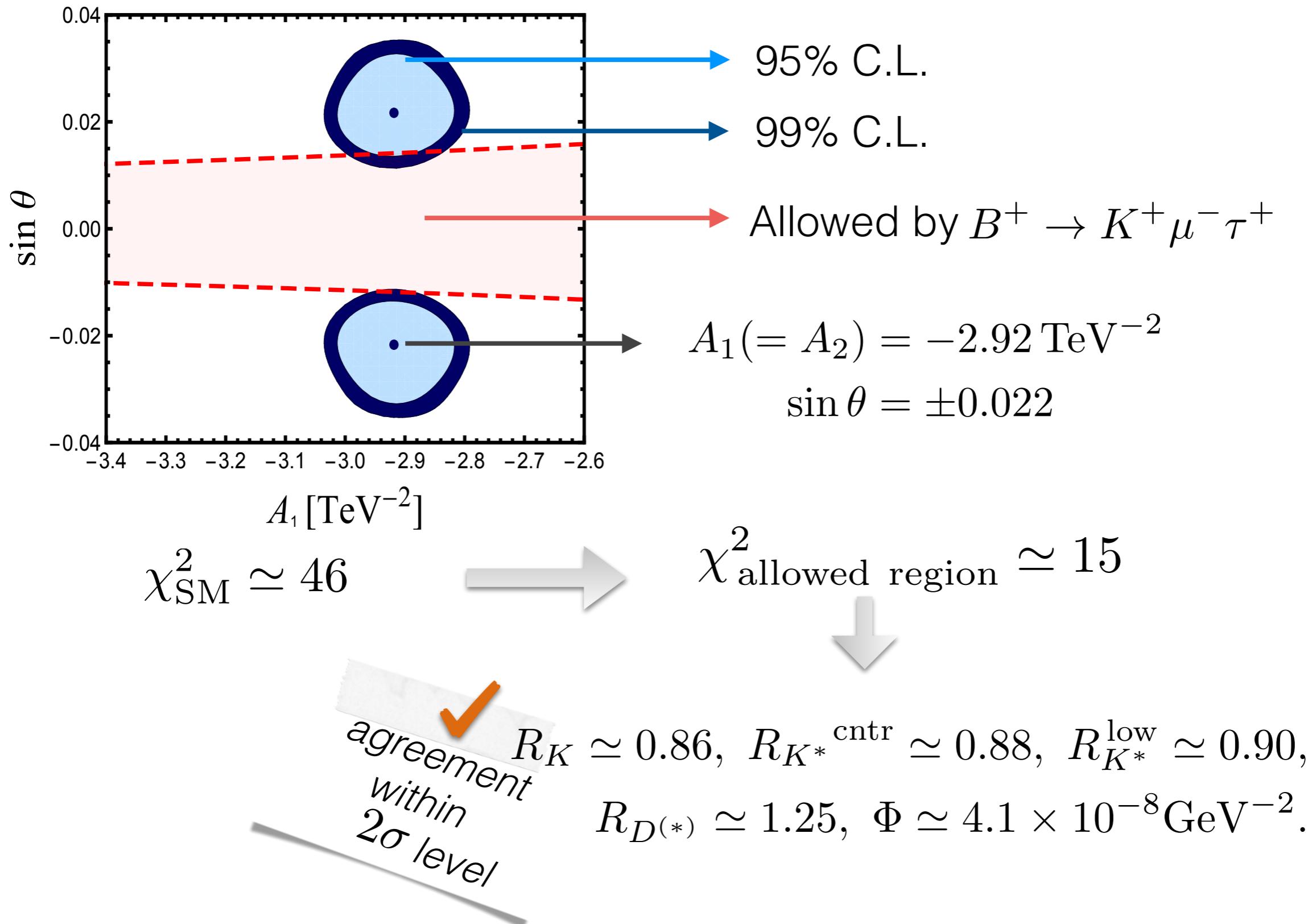
$$\mathcal{H}^{\text{NP}} = A_1 (\bar{Q}_{2L} \gamma_\mu L_{3L}) (\bar{L}_{3L} \gamma^\mu Q_{3L}) + A_2 (\bar{Q}_{2L} \gamma_\mu Q_{3L}) (\bar{\tau}_R \gamma^\mu \tau_R)$$

- ▶ Directly contributes to $R(D^{(*)})$
- ▶ Diagonalisation of Hamiltonian for lepton part through small mixing angle θ : interaction basis  mass basis

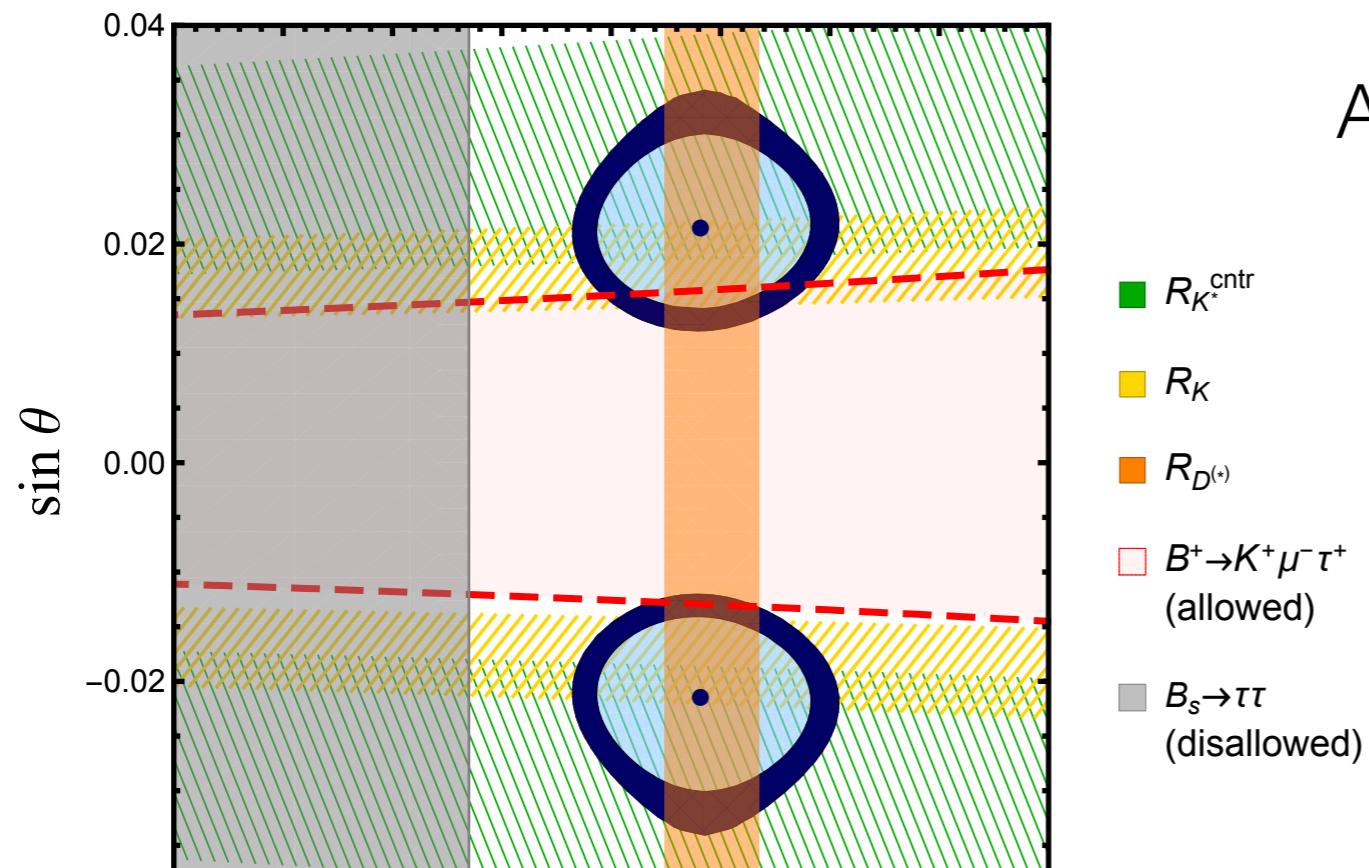
$$\tau = \cos \theta \tau' + \sin \theta \mu'$$

Contribution to $b \rightarrow s\mu\mu$ is generated

Lepton non-universality



Lepton non-universality



$$\chi^2_{\text{SM}} \simeq 46$$



Allowing 20% breaking

$$A_2 = 4A_1/5$$

from quantum corrections
or unknown dynamics of the
UV completion of the model

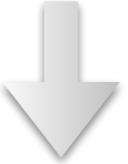
$$\chi^2_{\text{allowed region}} \simeq 10$$



*agreement
within
 1σ level*

$$R_K \simeq 0.80, R_{K^*}^{\text{cntr}} \simeq 0.83, R_{K^*}^{\text{low}} \simeq 0.88, \\ R_{D^{(*)}} \simeq 1.24, \Phi \simeq 3.8 \times 10^{-8} \text{GeV}^{-2}.$$

Summary

Popular approaches	Our approach
<input checked="" type="checkbox"/> Combine all $b \rightarrow s$ transitions	<input checked="" type="checkbox"/> Most general parametric form of SM amplitude
	+
many decay modes i.e observables	$B \rightarrow K^* \ell^+ \ell^-$ observables
+	+
more hadronic uncertainties	eliminate hadronic uncertainties
+	
conservative assumption of non-factorisable contributions	no/minimal dependency on form-factors & independent of non-factorisable contributions
<input checked="" type="checkbox"/> Focusing on low q^2 region	<input checked="" type="checkbox"/> Conclusion derived at endpoint

Summary

- ☒ Formalism developed to include all possible effects within SM
- ☒ Strong evidence of RH currents derived at endpoint limit —
 - ▶ systematics studied by varying polynomial order & bin no.
 - ▶ finite K^* width effect is considered
 - ▶ resonance effects increase the deviation

Summary

- ☒ Several hints of lepton non universality are observed by various experimental groups
- ☒ In terms of effective operators we show a possible explanation to all the anomalies together
 - ▶ The model has only two new parameters
 - ▶ It predicts some interesting signatures both in the context of B decays as well as high-energy collisions
- ☒ Opens up way to construct UV complete theory
- ☒ Fluctuation? Wait for more data to be accumulated!

Summary

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Thank you!