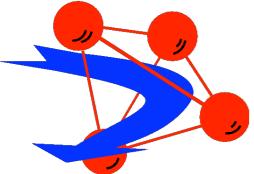


Diffraction at swiss spallation neutron source SINQ: applications to magnetic structure solutions

Vladimir Pomjakushin

Laboratory for Neutron Scattering and Imaging, LNS, Paul Scherrer Institute



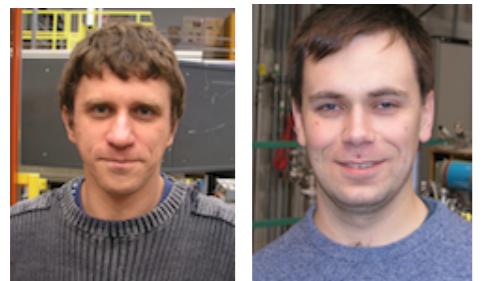
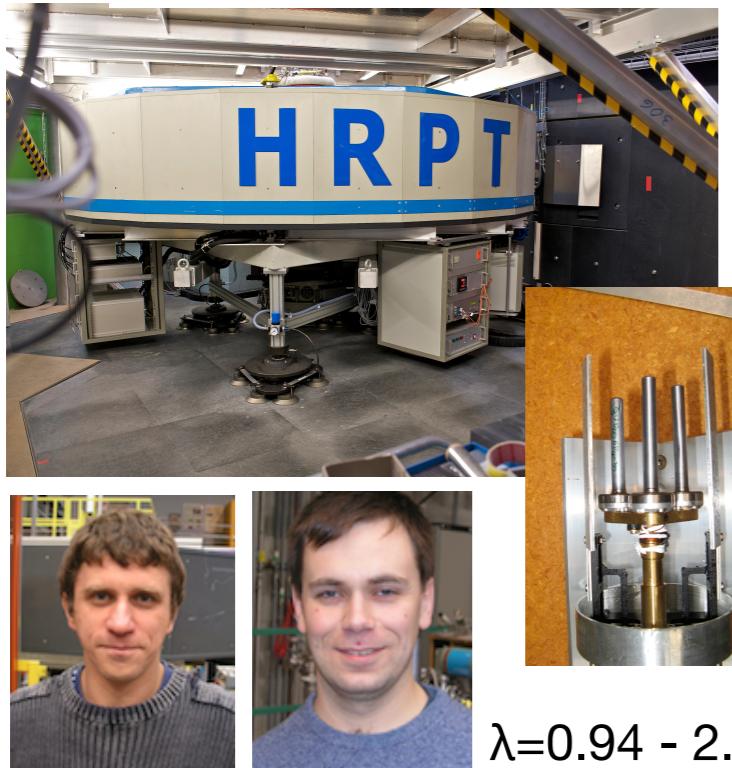
SINQ diffraction instruments overview

PAUL SCHERRER INSTITUT



Instruments HRPT&DMC (Powder), TriCS (Single crystal), POLDI (strain) and TASP/MuPAD (polarised, 3D spherical neutron polarimetry)

New materials in condensed matter physics, chemistry and materials science with a focus on magnetism
Examples are: energy research, frustrated systems, crystallography, ferroelectrics



$\lambda=0.94 - 2.96 \text{ \AA}$

HRPT: V. Pomjakushin, D. Sheptyakov



$\lambda=2.35-5.4 \text{ \AA}$

DMC: L. Keller, M. Frontzek

Laboratory for Neutron Scattering and Imaging, Paul Scherrer Institute, Villigen, Switzerland

SINQ diffraction instruments overview

PAUL SCHERRER INSTITUT



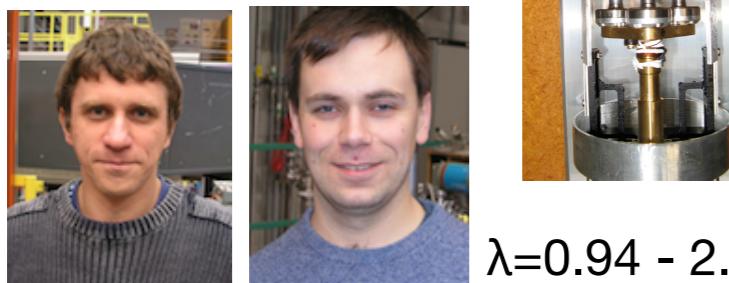
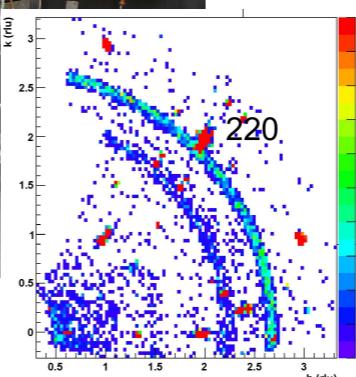
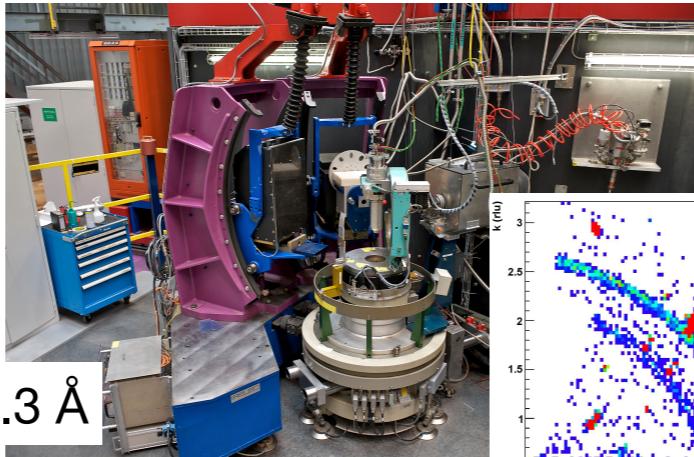
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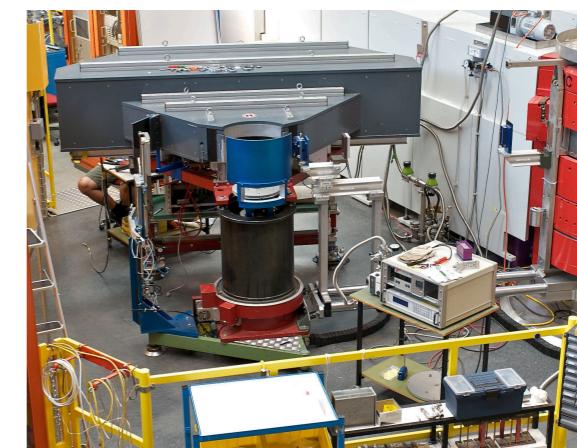
TriCS: O. Zaharko, J. Schefer

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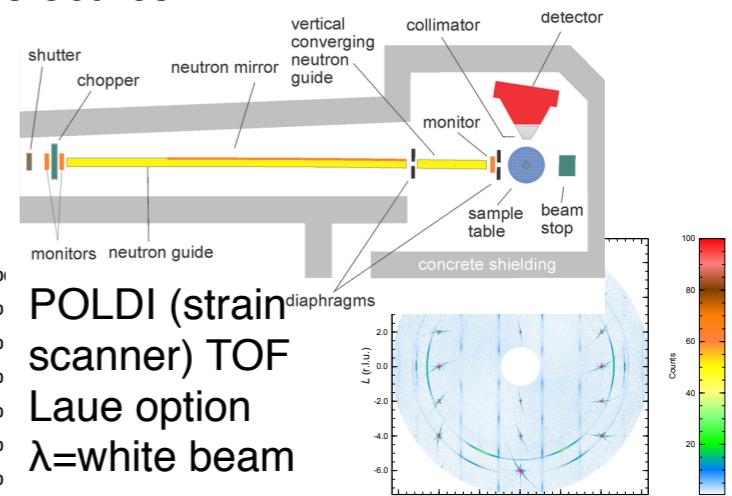
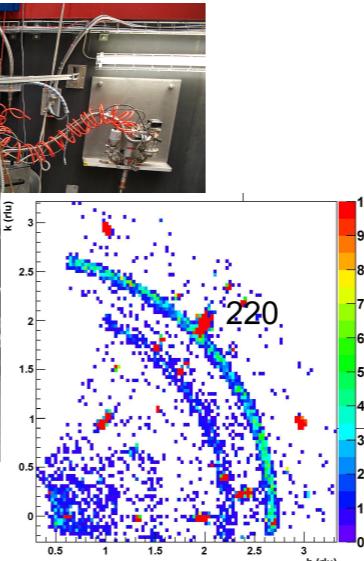
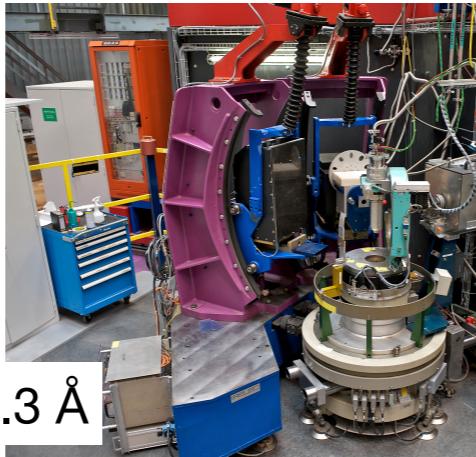
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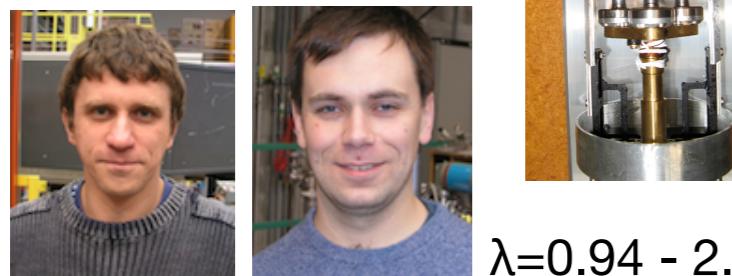


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$\lambda=1.18, 2.3 \text{ \AA}$



POLDI (strain scanner) TOF
Laue option
 $\lambda=\text{white beam}$



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$\lambda=2.35-5.4 \text{ \AA}$



DMC: L. Keller, M. Frontzak

Laboratory for Neutron Scattering and Imaging, Paul Scherrer Institute, Villigen, Switzerland

SINQ diffraction instruments overview

PAUL SCHERRER INSTITUT

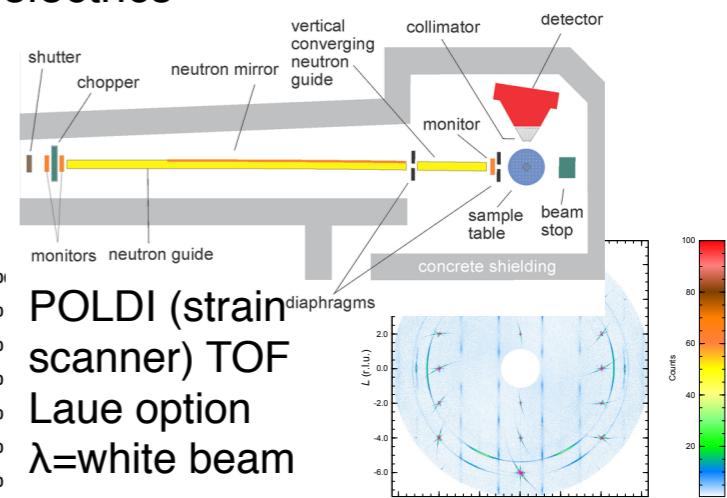
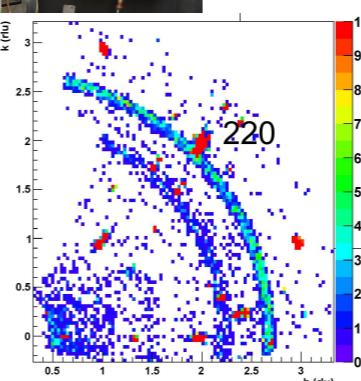
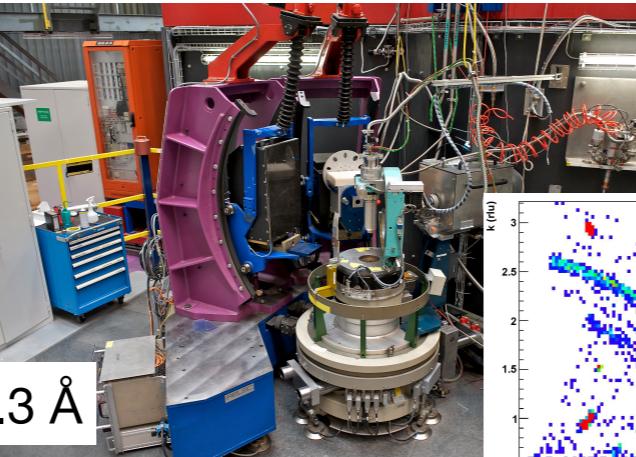


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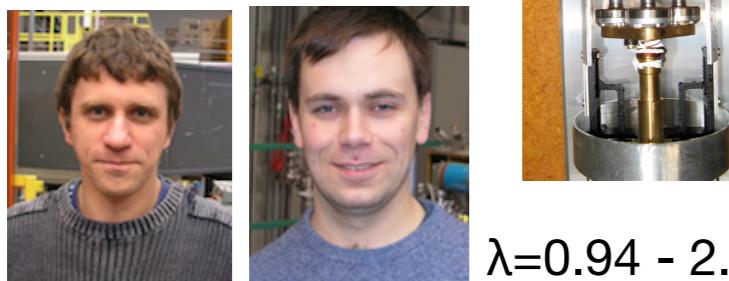
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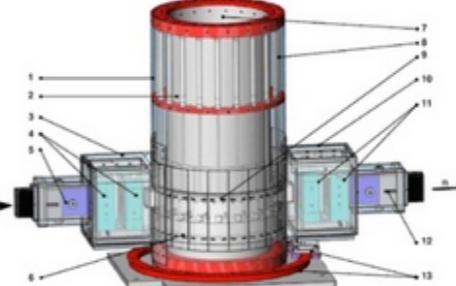


POLDI (strain
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TASP/
MuPAD:
B. Roessli



$\lambda=2.35-5.4 \text{ \AA}$



DMC: L. Keller, M. Frontzak

Laboratory for Neutron Scattering and Imaging, Paul Scherrer Institute, Villigen, Switzerland

Scientific case of neutron diffraction (ND) experiments at SINQ

“hard matter” topics:

Atom and spin ordering. Indirectly charge and orbital ordering.

Finding crystal and magnetic symmetry adapted structures in “any” material...

1. Strongly correlated electrons

(quantum/low D, frustrated) magnetism, superconductivity (SC), multiferroics...

SANS: very long period mag. str., like skyrmions or flux lattice in SC

2. Materials science: *def.== “Discovery and design of new materials.”; a relaxed def.== “Study of any materials interesting to you if your project got funding”*

Materials:

mainly inorganic: oxides, pnictides, selenides, intermetallic, etc...

organic ones or liquids are less common

neutron diffraction experiment ($\lambda=\text{const}$)

Nuclear structure factor

$$F(\mathbf{q}) = \sum_j b(\mathbf{r}_j) \exp(i\mathbf{q}\mathbf{r}_j)$$

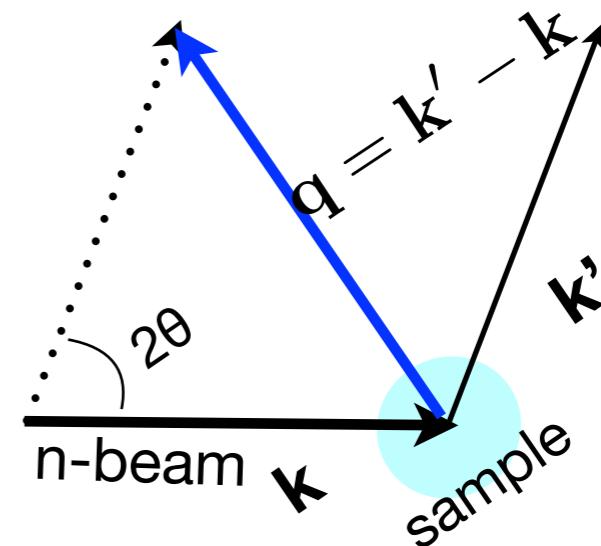
Magnetic structure factor

$$\mathbf{F}(\mathbf{q}) \propto \sum_j \mathbf{S}_{0\perp j} \cdot \exp(i\mathbf{q}\mathbf{r}_j)$$

Intensity in the detector

$$\frac{d\sigma}{d\Omega} \propto F(\mathbf{q})F^*(\mathbf{q}) \cdot \delta(H - \mathbf{q})$$

momentum transfer or
scattering vector $\mathbf{q} = \mathbf{k}' - \mathbf{k}$



$$|\mathbf{k}| = |\mathbf{k}'| = \frac{2\pi}{\lambda}$$

neutron diffraction experiment ($\lambda=\text{const}$)

Nuclear structure factor

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atom position and spin

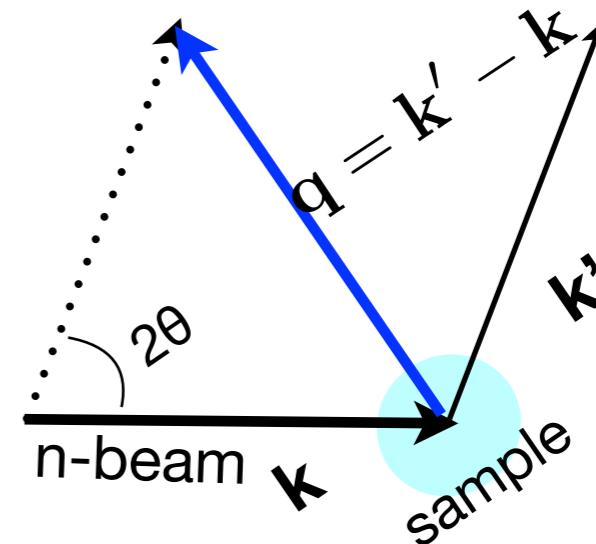
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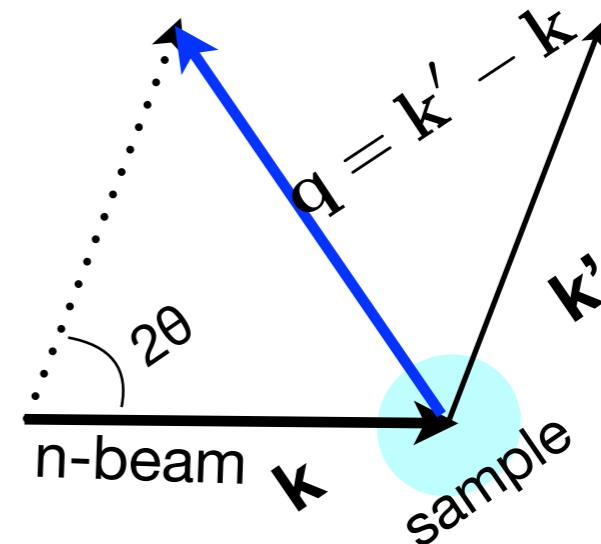
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$$q = \frac{4\pi \sin(\theta)}{\lambda}, \theta = 0.. \leq 90\text{deg.}$$

$$q_{max} = \frac{4\pi}{\lambda} \quad \text{small wavelength is a must to have large } q_{max} \rightarrow \text{good spatial resolution}$$

$(d_{min} = \frac{\lambda}{2})$

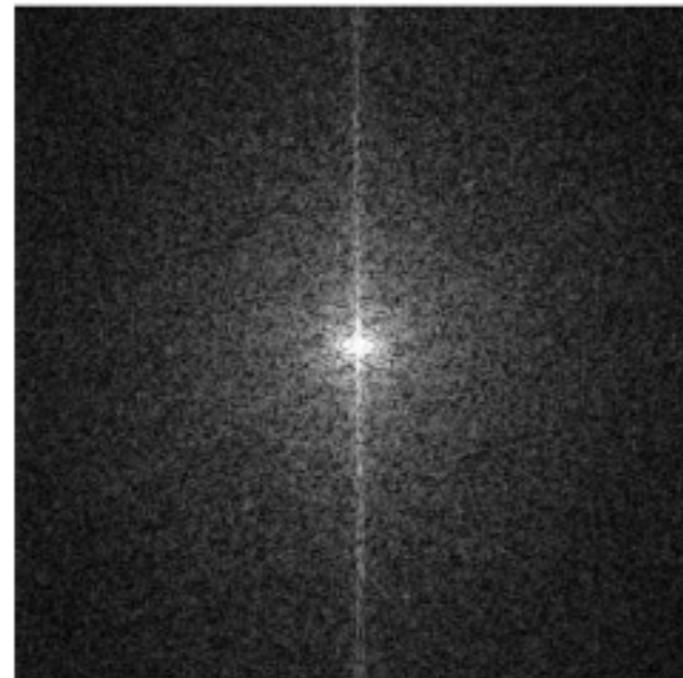


$$|k| = |k'| = \frac{2\pi}{\lambda}$$

Q-range limitation – image quality (min δr)

Object

$$b(r) \sim \int_0^{\infty} e^{-iqr} f(q) dq$$



Fourier image

$$f(q) \sim \int e^{iqr} b(r) dr$$

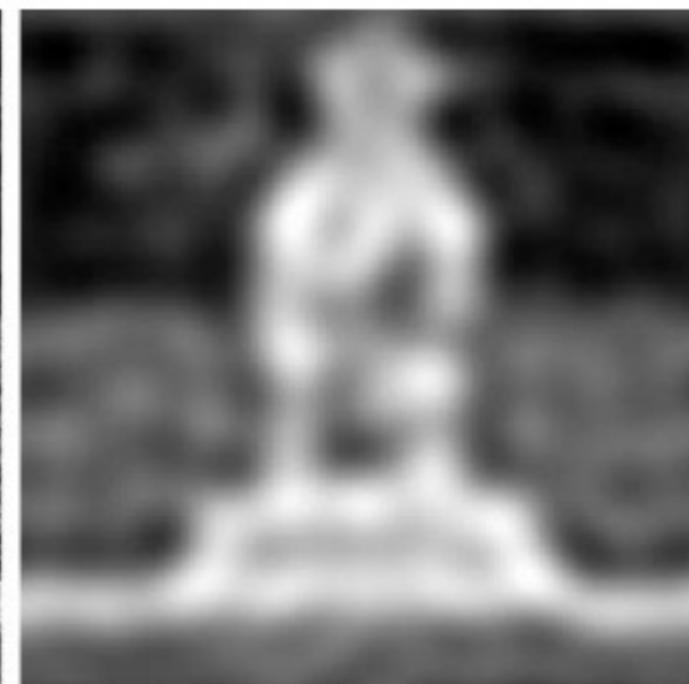
Structure factor

$$F(\mathbf{q}) = \sum_j b(\mathbf{r}_j) \exp(i\mathbf{qr}_j)$$

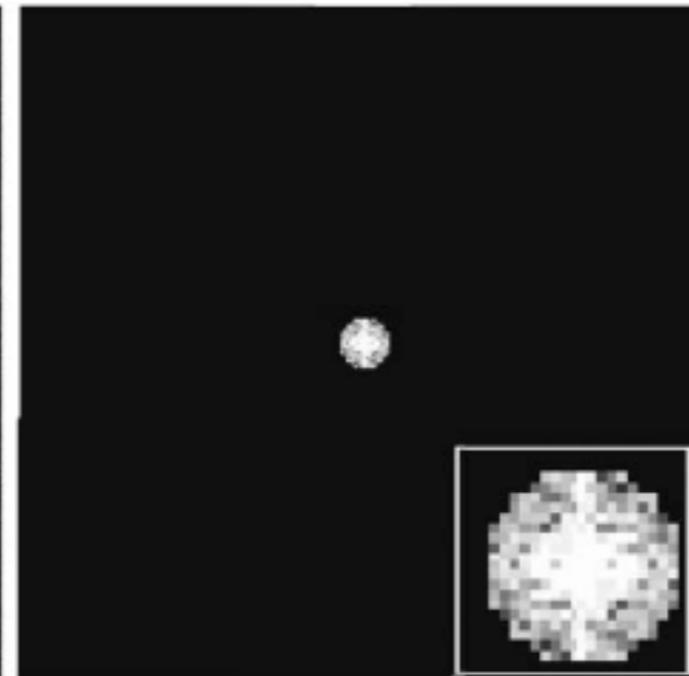
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$$b(r) \sim \int_0^{q_{\max}} e^{-iqr} f(q) dq$$



Fourier image

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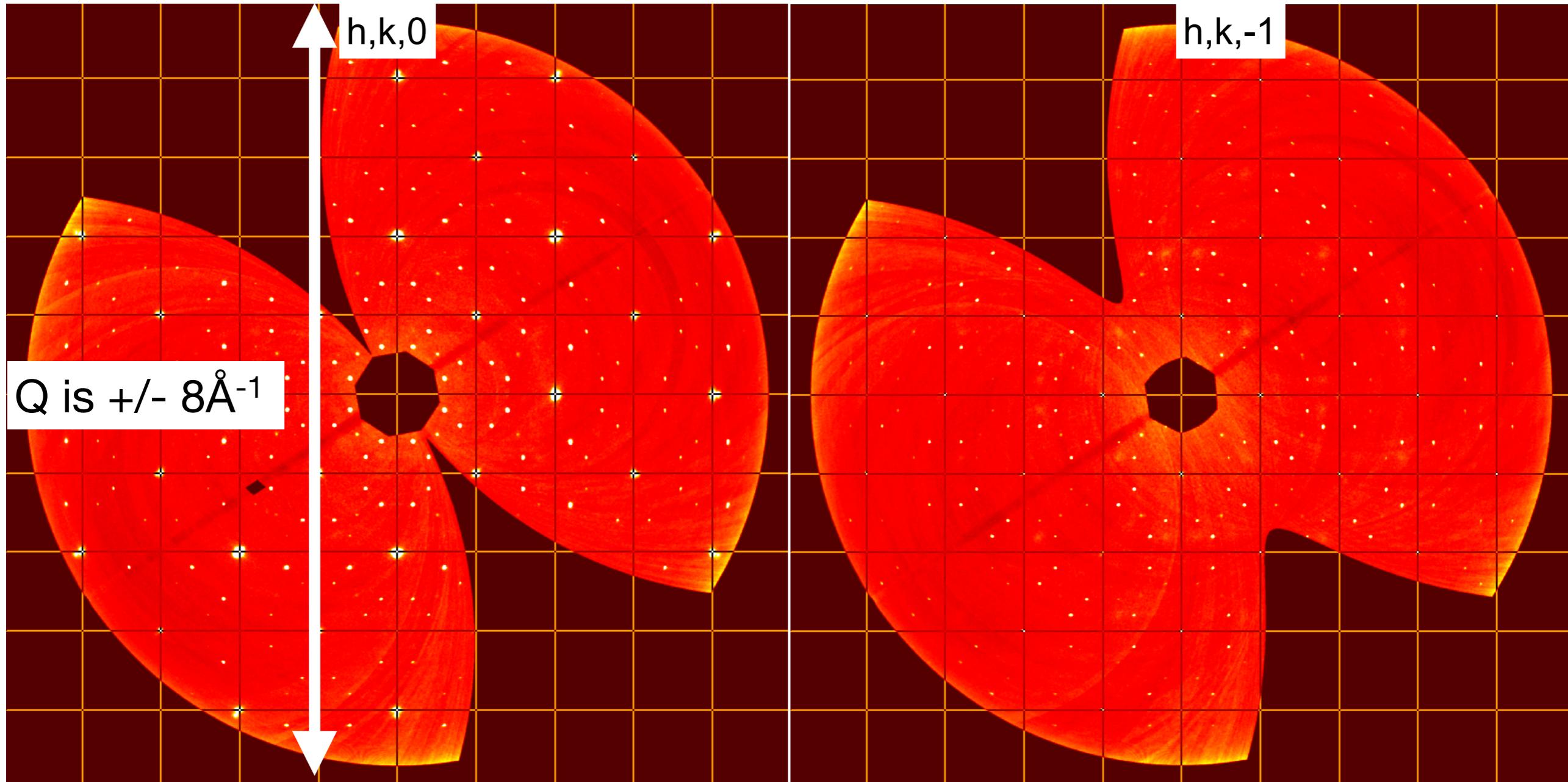
Structure factor

$$F(\mathbf{q}) = \sum_j b(\mathbf{r}_j) \exp(i\mathbf{qr}_j)$$

Fourier image
without high q

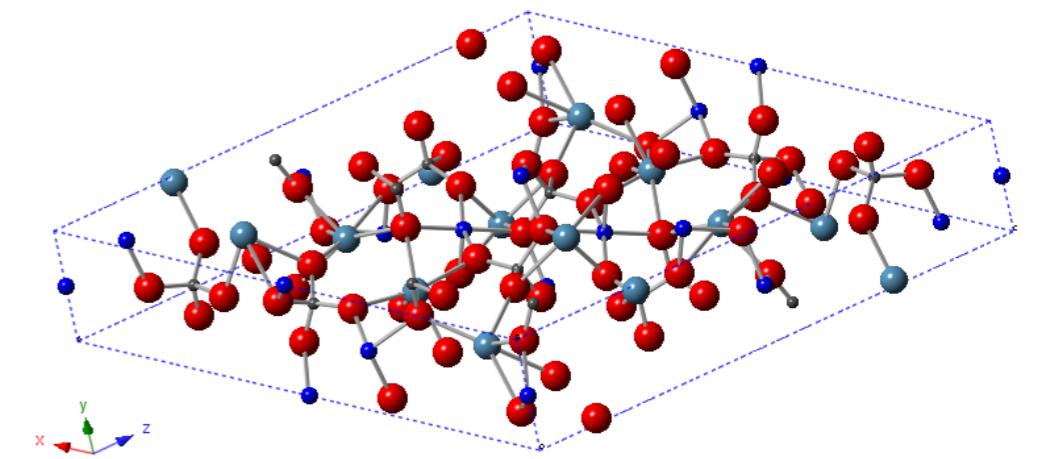
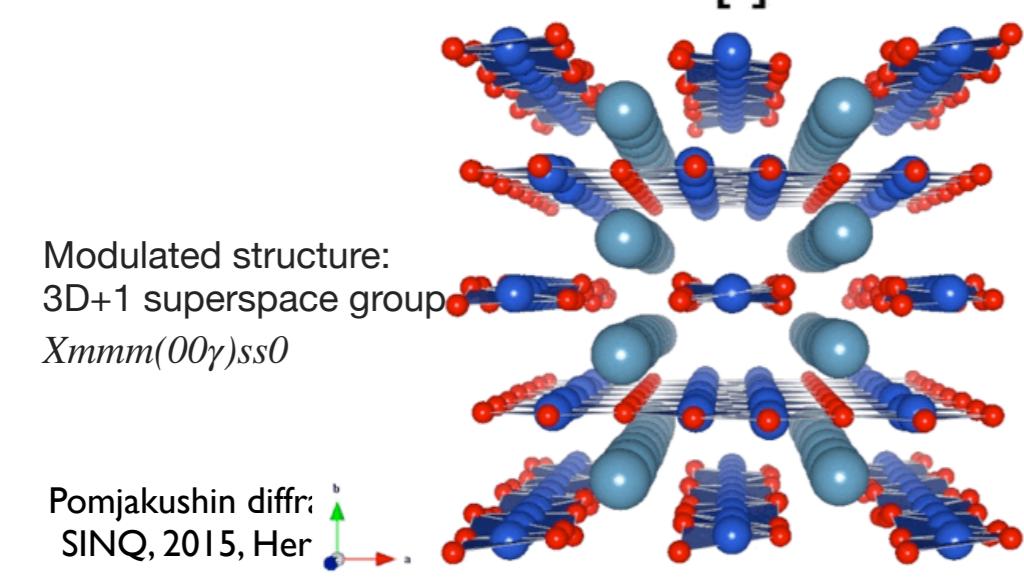
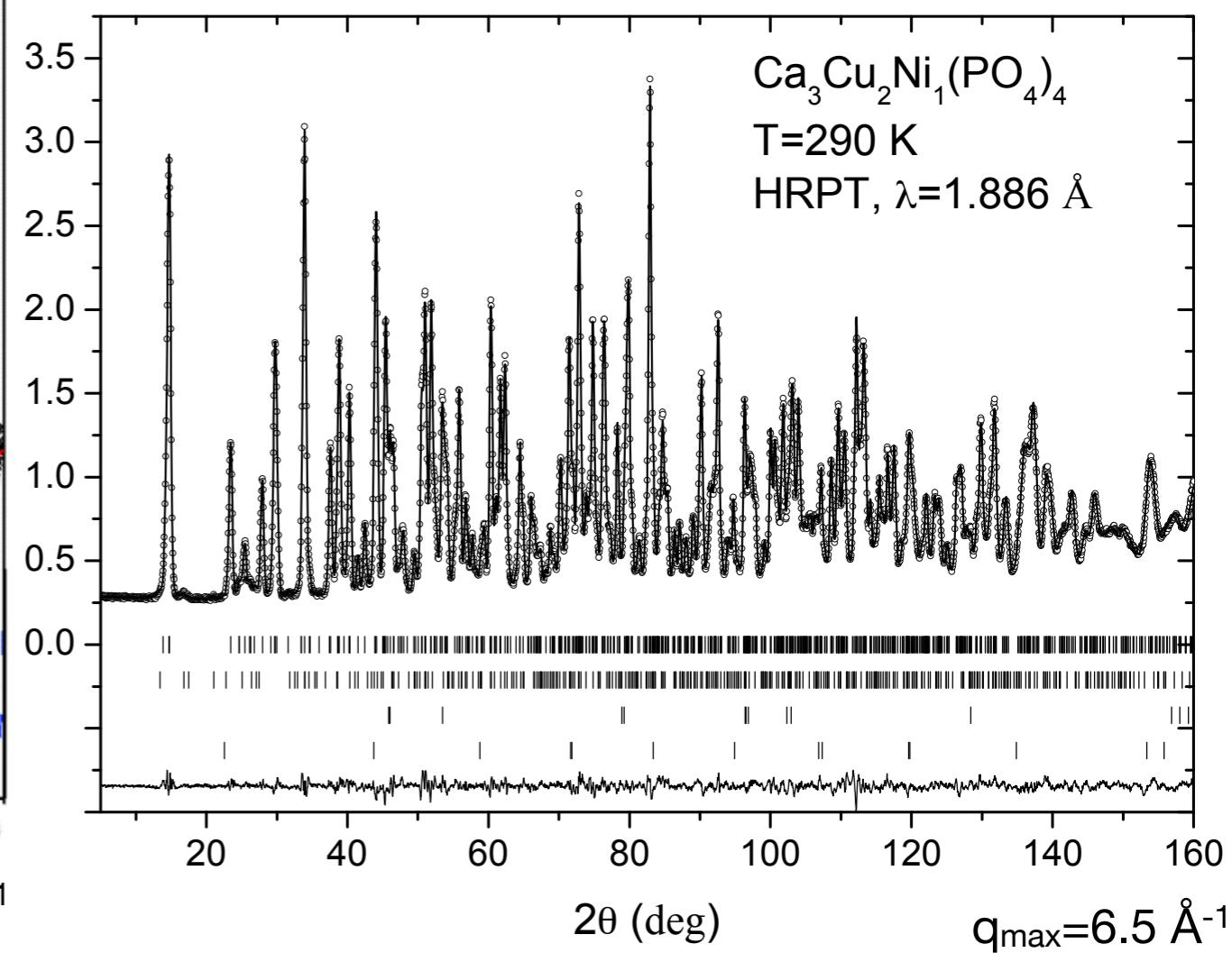
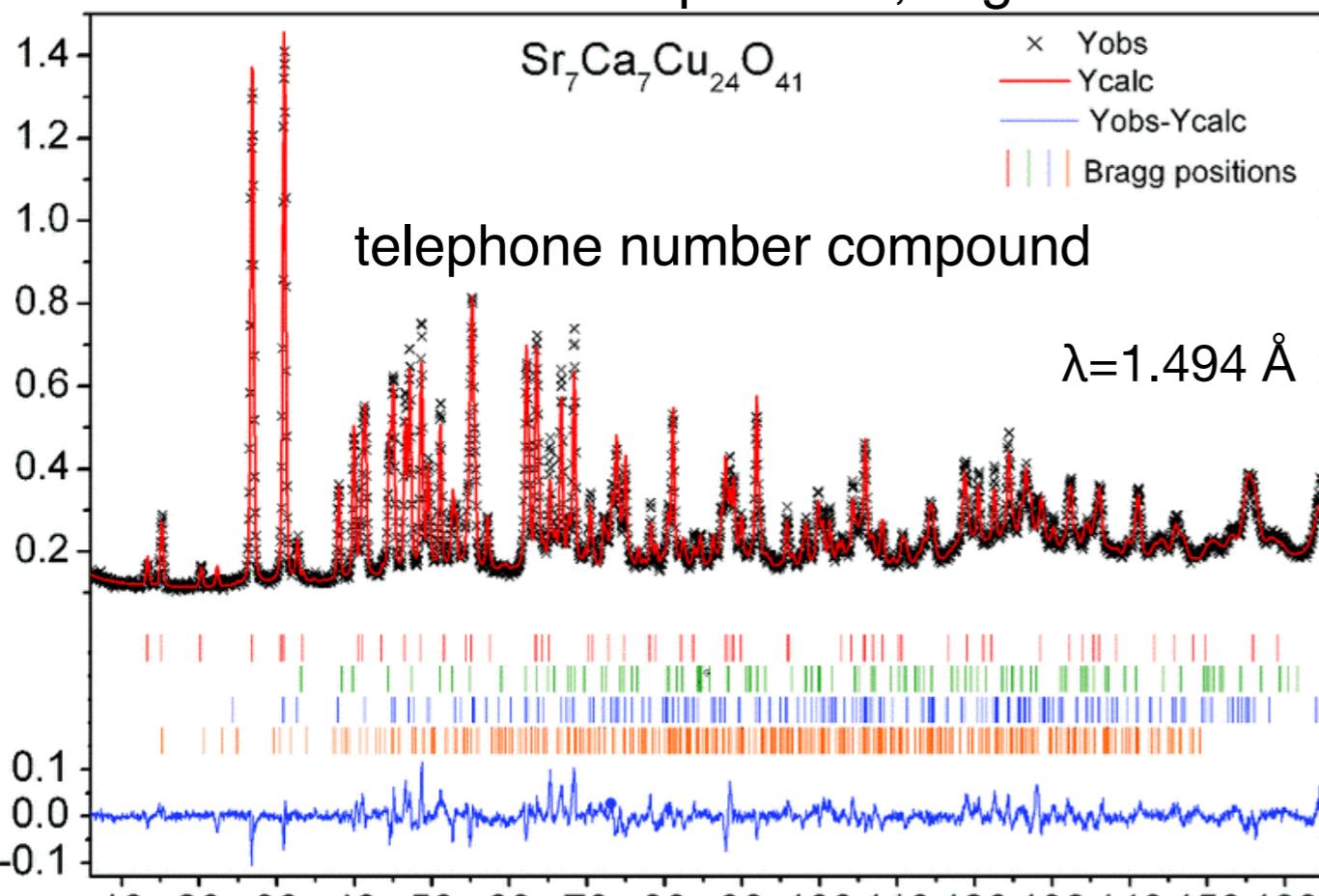
$\delta q/q$ resolution limitations

the mesh is for the parent I4/mmm cell $a=4\text{\AA}$
 $T=300\text{K}$, $(hk0)$ plane of $\text{Cs}_y\text{Fe}_{2-x}\text{Se}_2$



Q-range/resolution in powder diffraction. Peak overlap.

Diffraction patterns, High resolution powder diffractometer **HRPT** @ SINQ



Limitations on maximal unit cell volume (number of atoms) in powder neutron diffraction

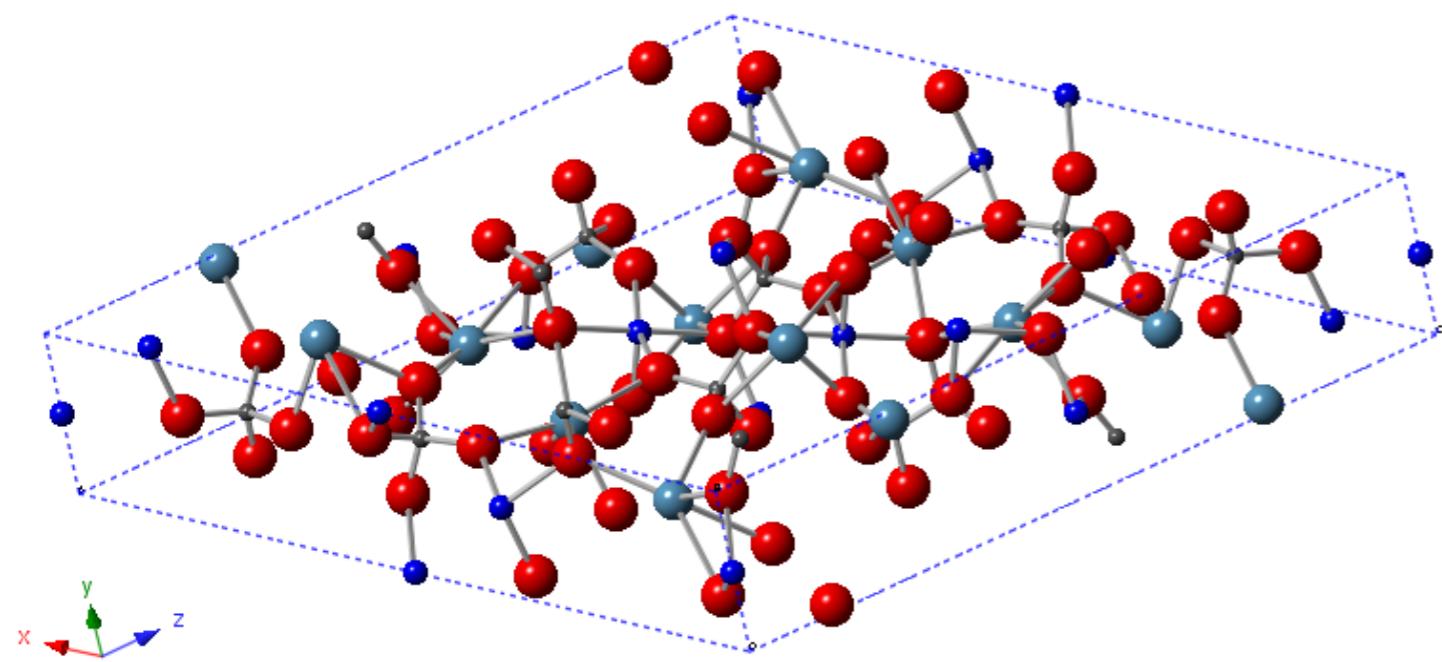
Volumes up to 1000-2000 Å, about 100-200 atoms, concentration 0.08-0.1 at/Å³

bond lengths accuracy ~0.001 Å



18x5x18 Å, V=1300 Å³

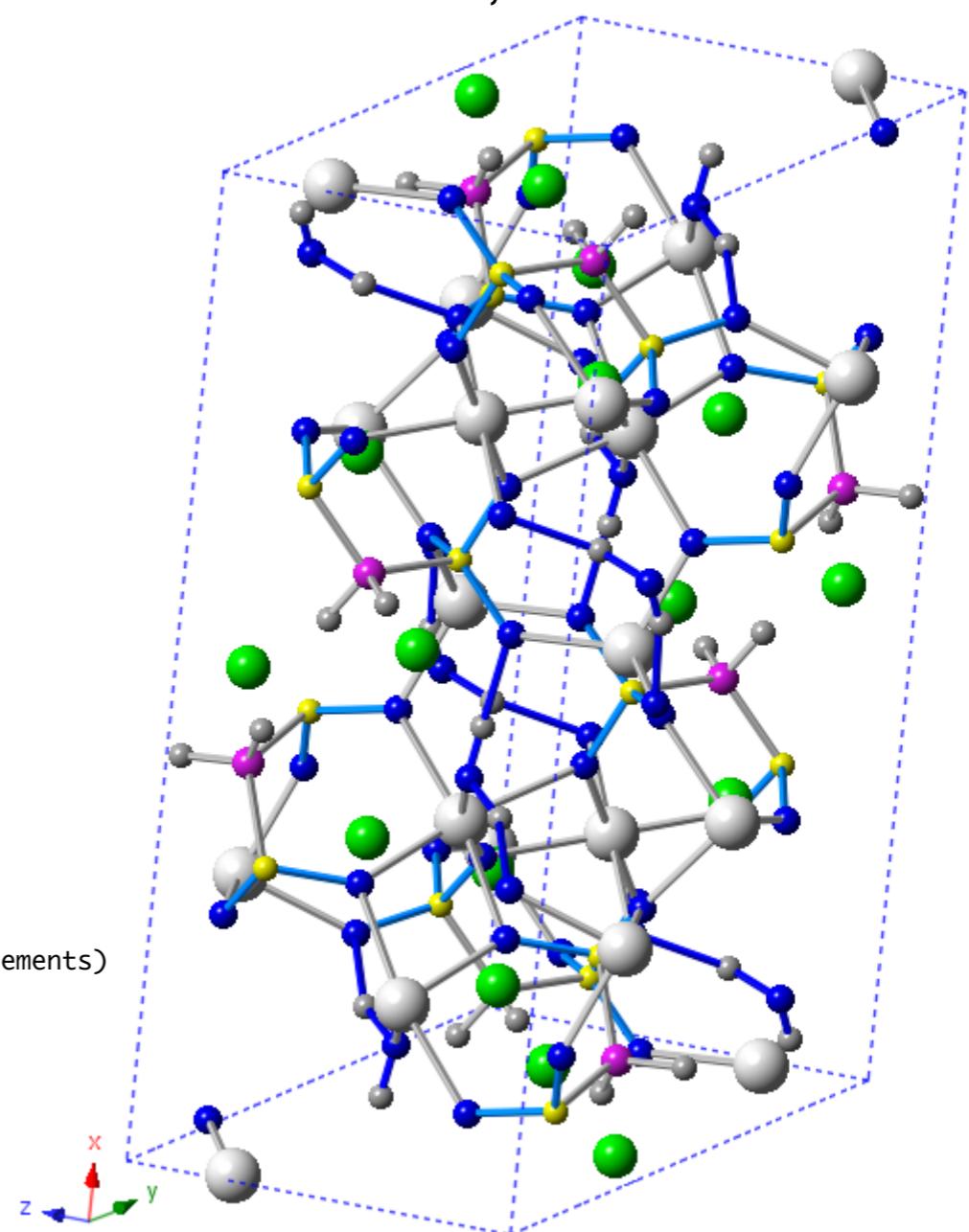
C2/c sp.gr.



(114 atoms, 14 sites, 4 elements)



18x8x9 Å, V=1300 Å³ 144 atoms



(148 atoms, 19 sites, 6 elements)

Structures: solved/refined from HRPT NPD data

Magnetic structure - limitations

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1. High q-range is not needed (usually)
 - Atomic positions are known
 - Magnetic form-factor $f(q) \sim \exp(-q^2)$

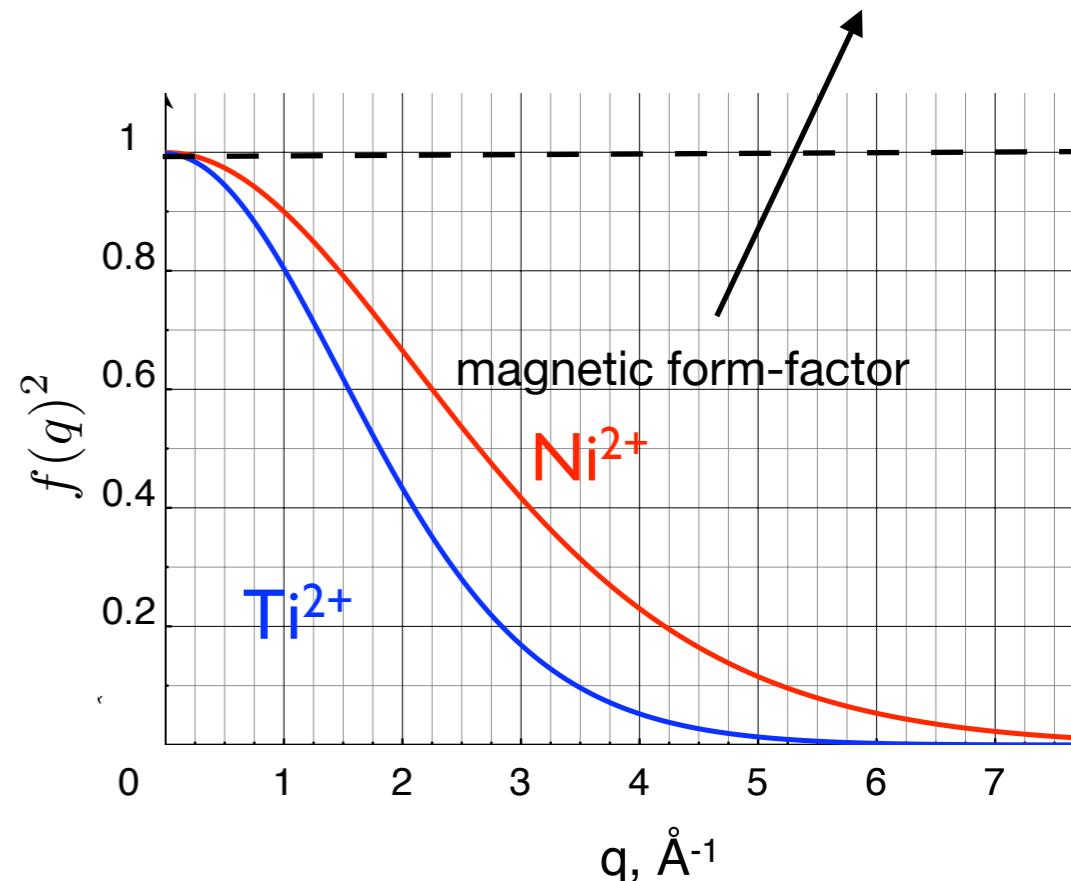
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$$I \sim |F(q)|^2 f^2(q) \sim S^2 f^2(q)$$

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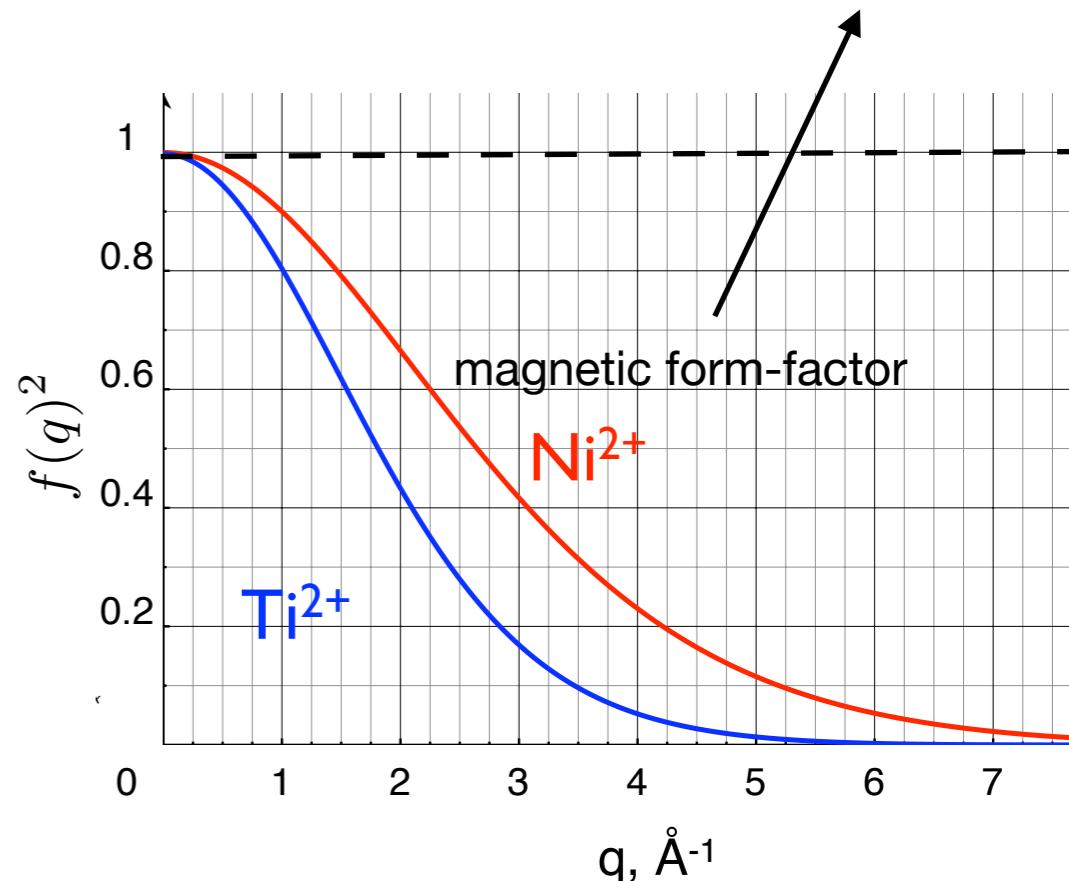


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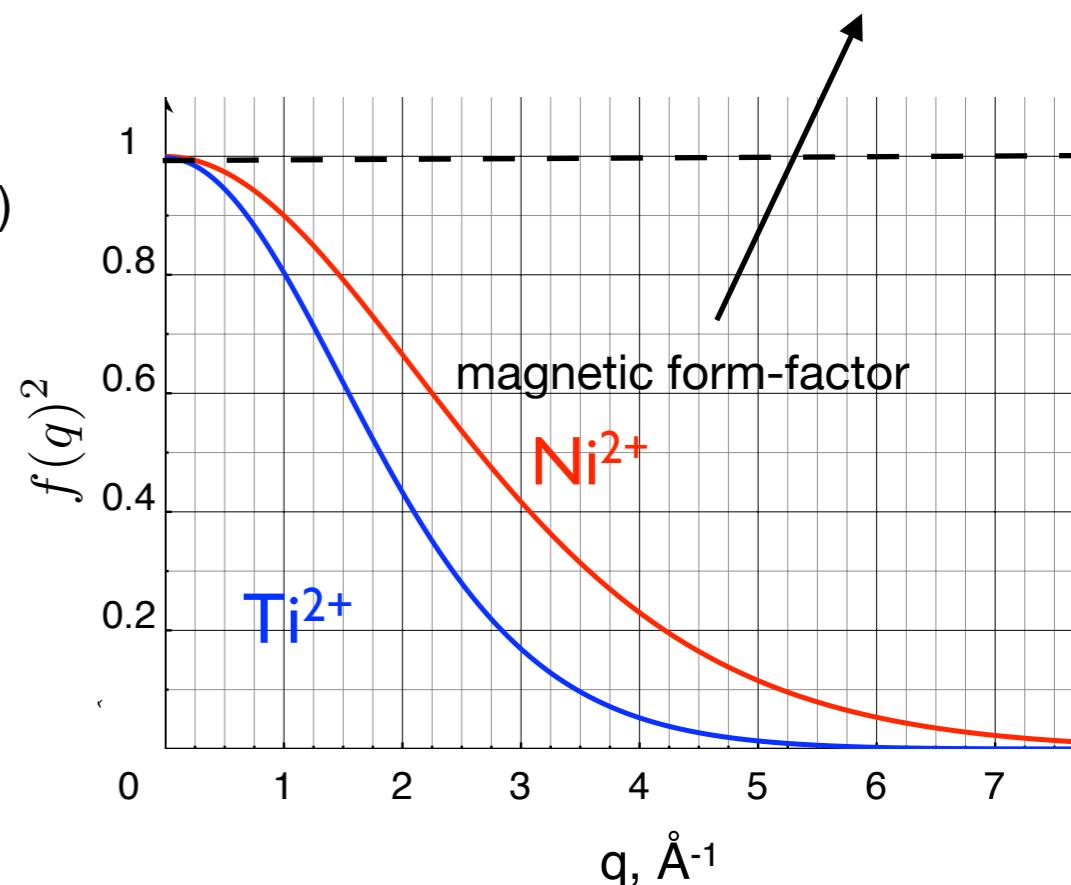


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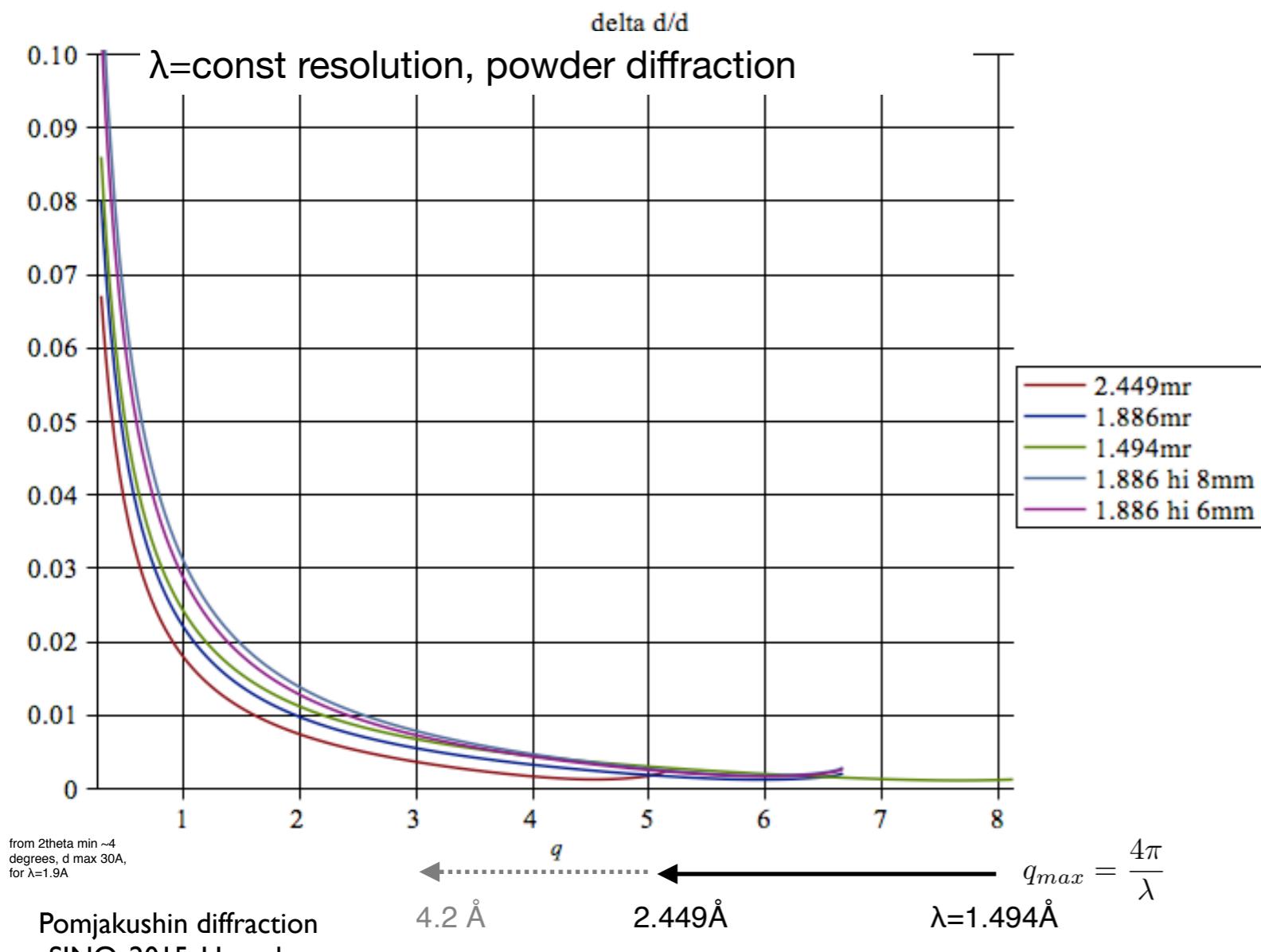
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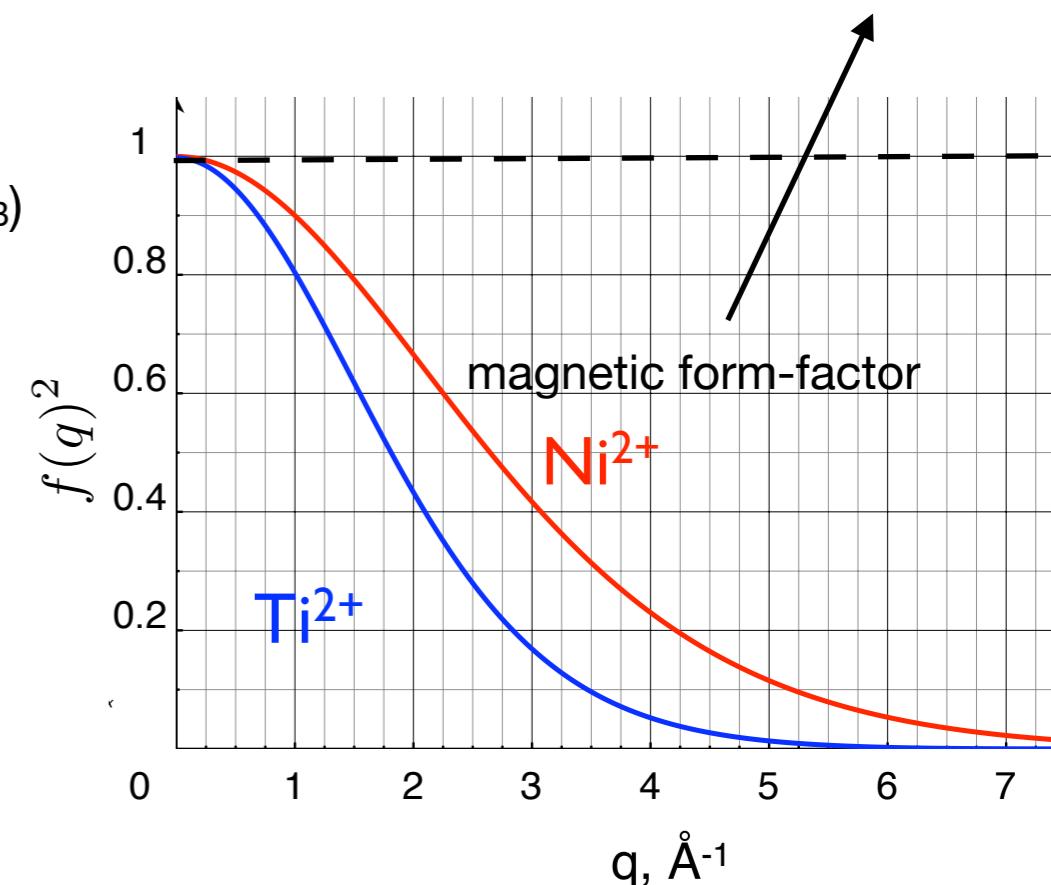
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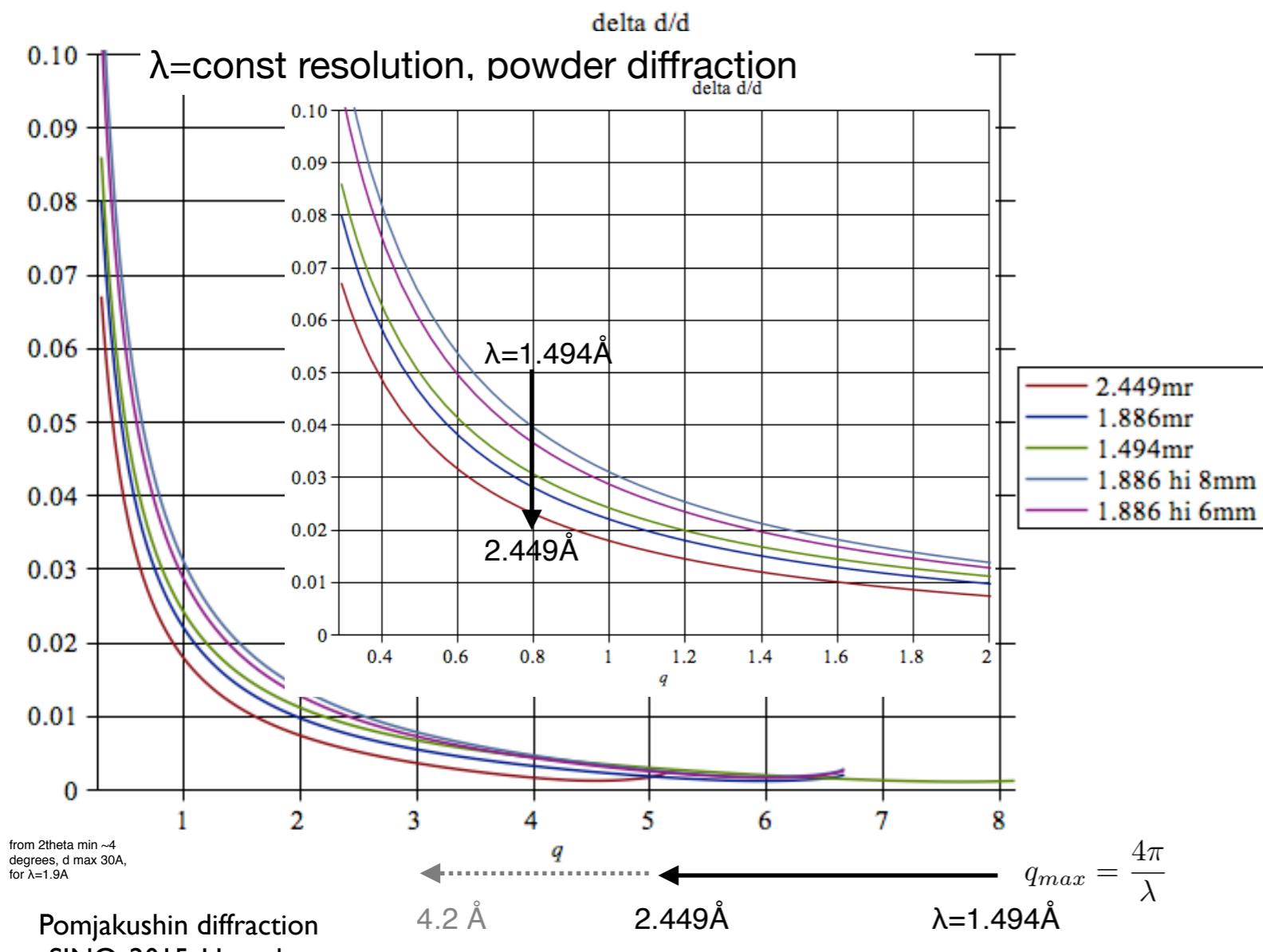
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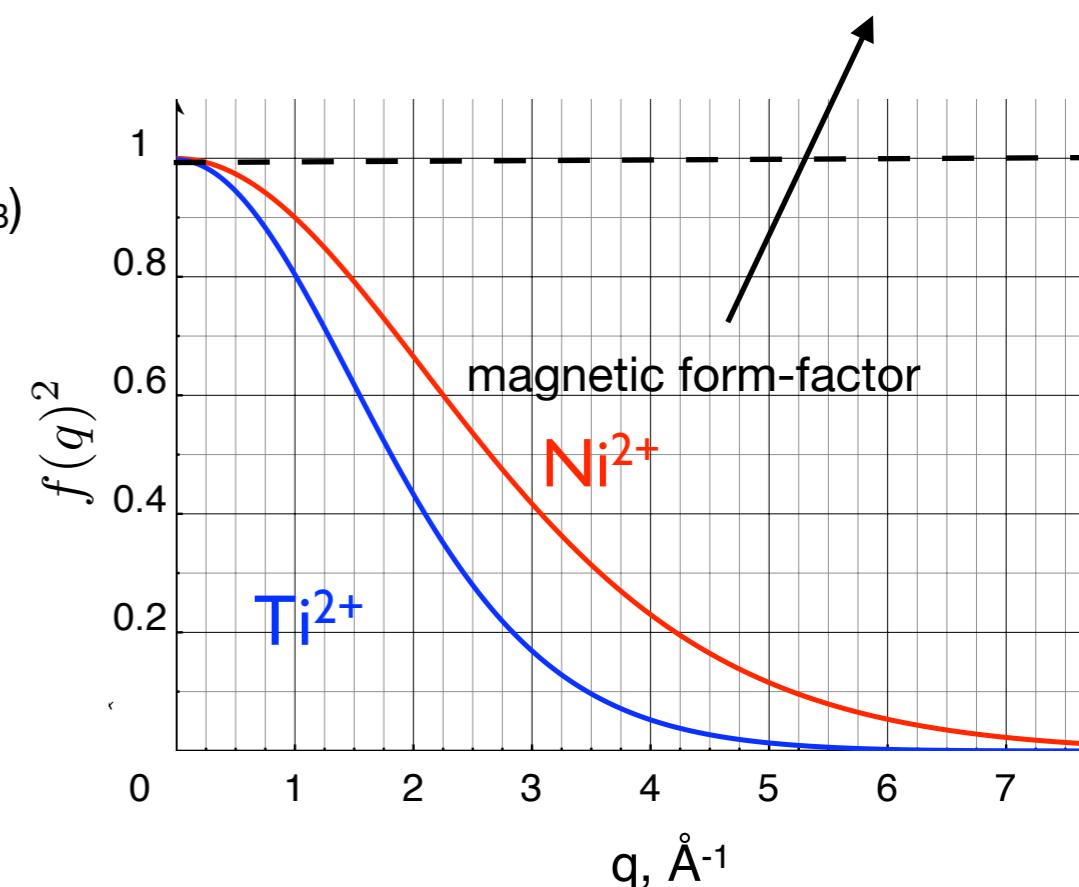
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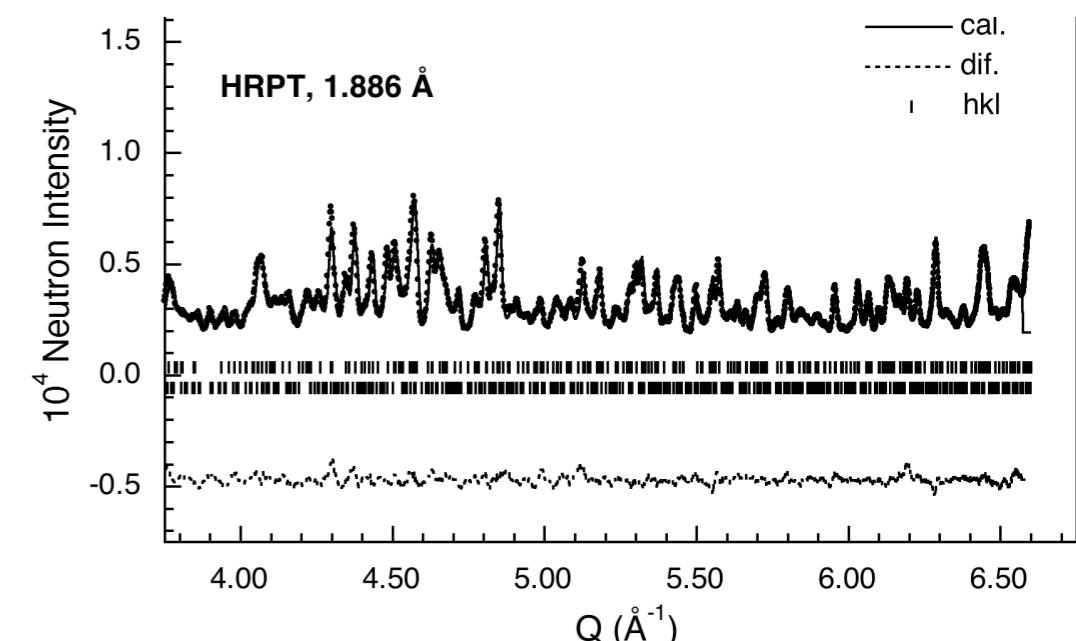
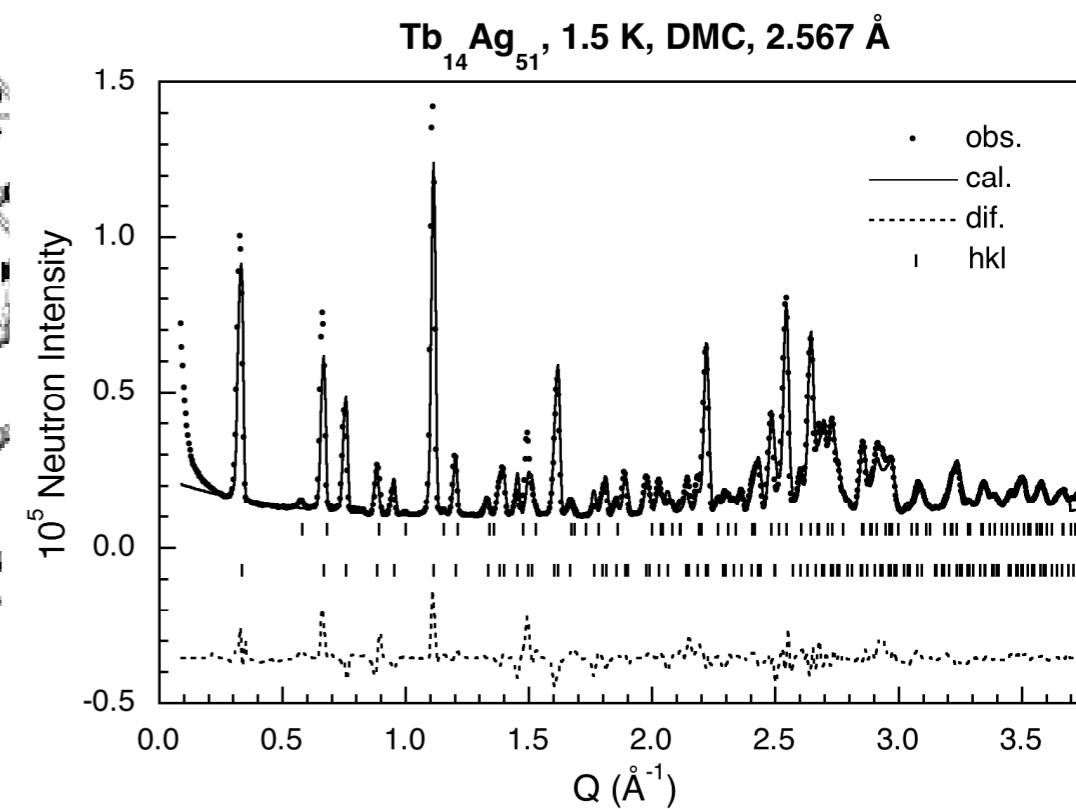
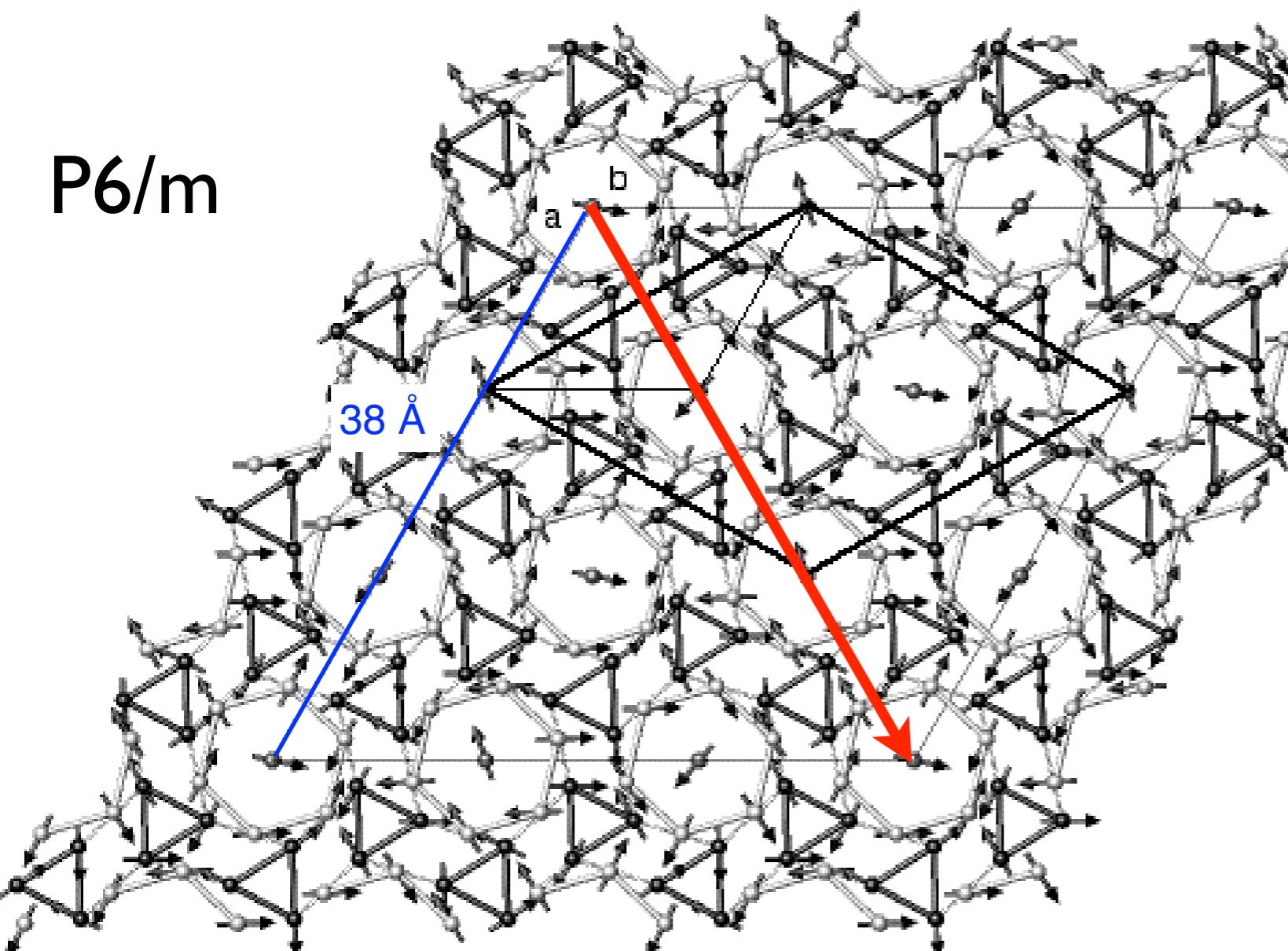


Example: Magnetic structure solved from DMC & HRPT NPD data

Antiferromagnetic three sub-lattice ordering in $Tb_{14}Au_{51}$

Conventional magnetic unit cell $a=38 \text{ \AA}$, $c=9 \text{ \AA}$
(Volume = $11'137 \text{ \AA}^3$!!) contains 126 spins of Tb^{3+} .

P6/m



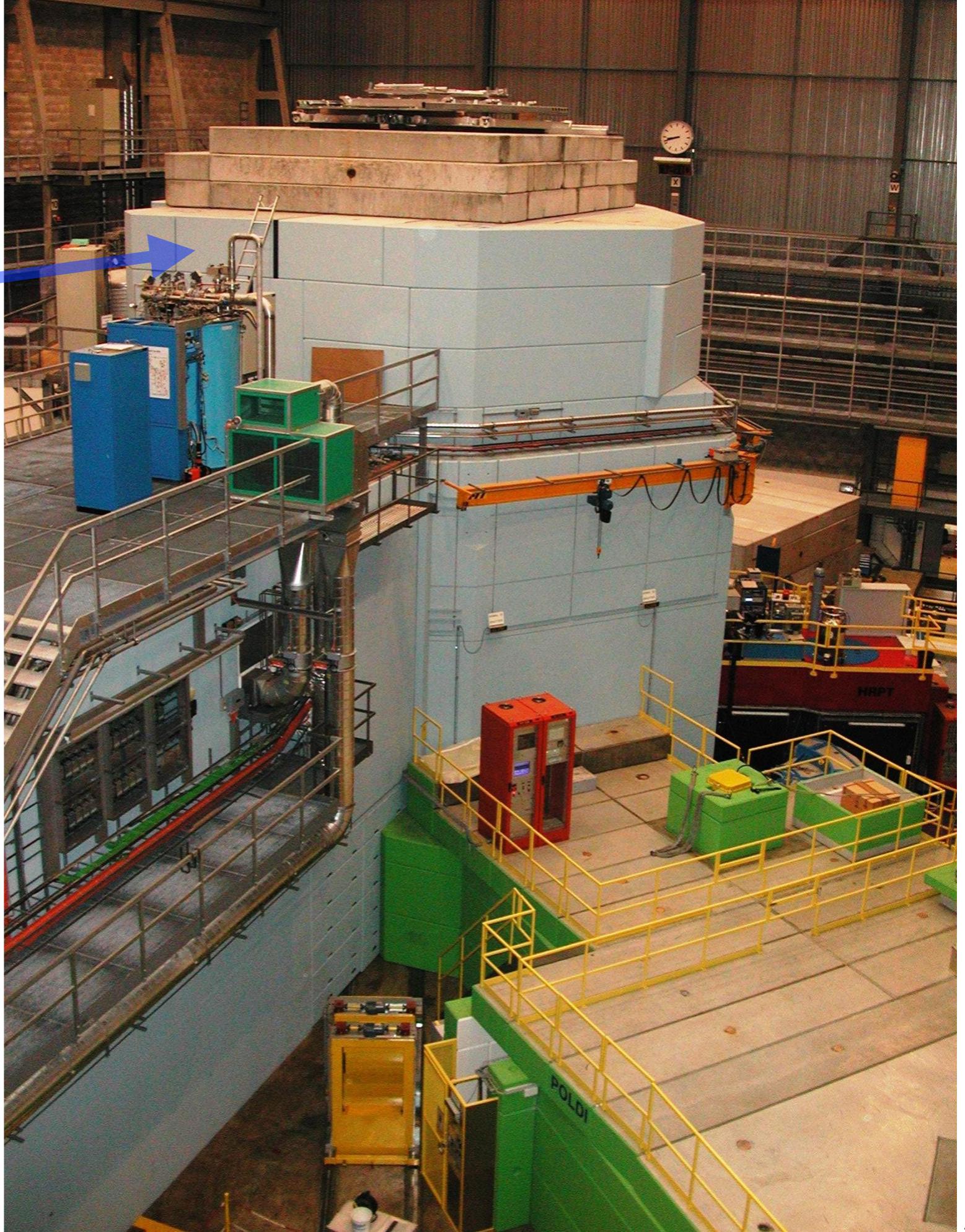
Diffraction instruments at swiss spallation source SINQ

- HRPT - High Resolution Powder Diffractometer for Thermal Neutrons,
 $\lambda=0.94 - 2.96 \text{ \AA}$, High Q-range $\leq 11\text{\AA}^{-1}$
- DMC – High Intensity Powder Diffractometer for Cold Neutrons,
 $\lambda=2.35 - 5.4 \text{ \AA}$, High flux and good resolution at low and moderate Q $\leq 4\text{\AA}^{-1}$
- TriCS - Single crystal diffractometer,
 $\lambda=1.18, 2.3 \text{ \AA}$, Thermal Neutrons
- TASP (triple axes) with MuPAD for polarised ND, Cold Neutrons

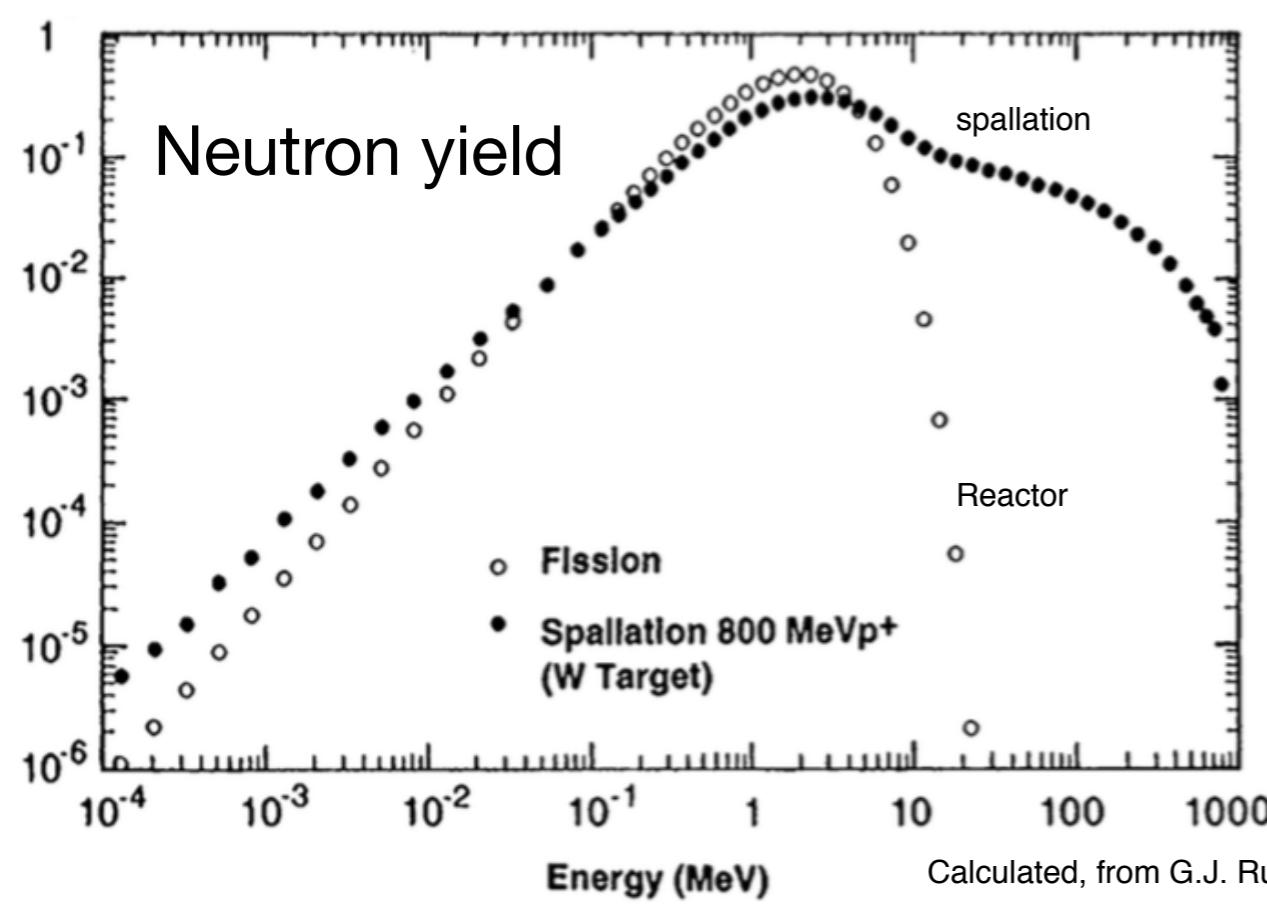
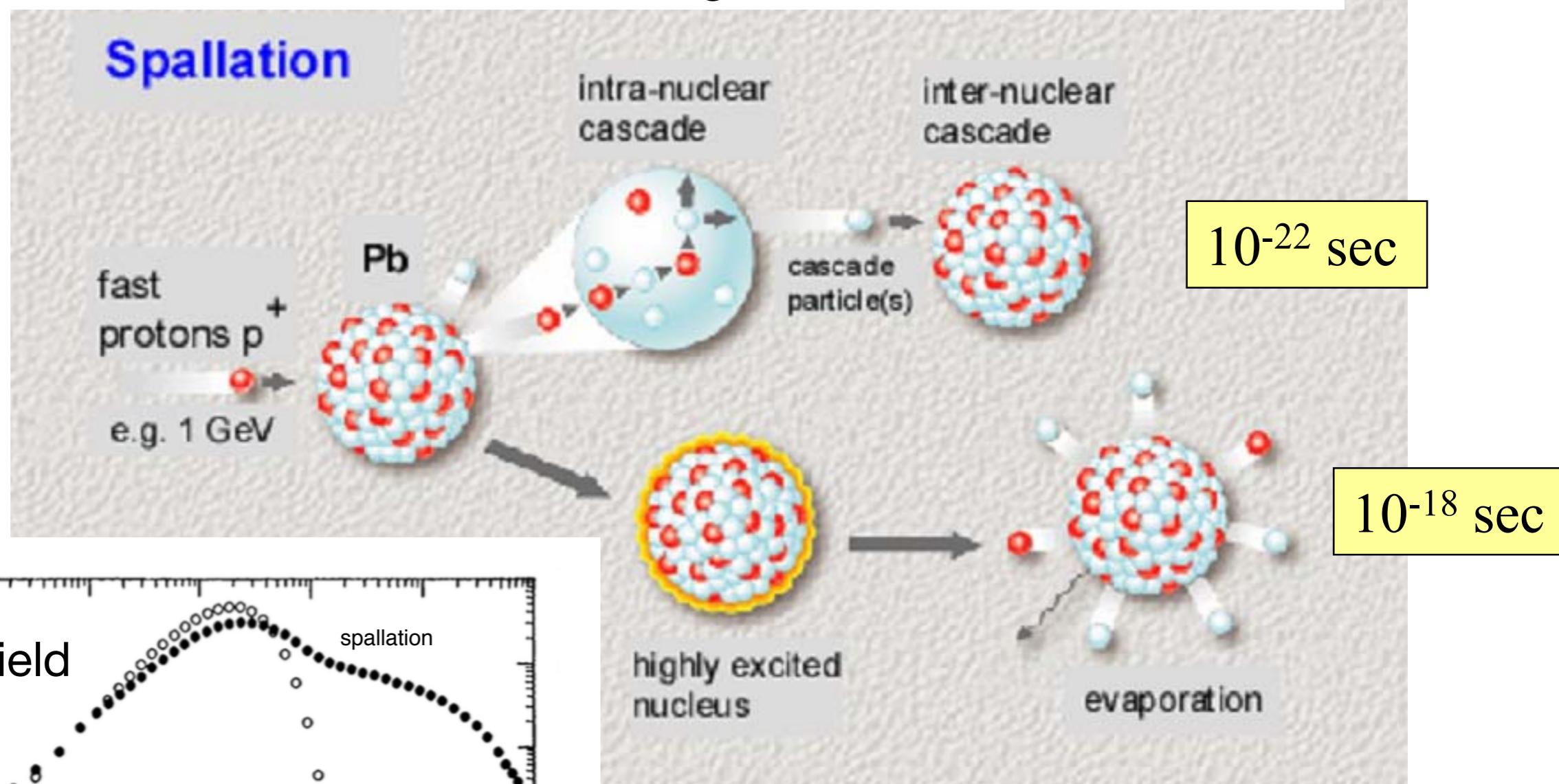
SINQ hall

The spallation neutron source

SINQ is a continuous source - the first and the only of its kind in the world - with a **flux of about 10^{14} n/cm²/s**. Beside thermal neutrons, a cold moderator of liquid deuterium (cold source) slows neutrons down and shifts their spectrum to lower energies.

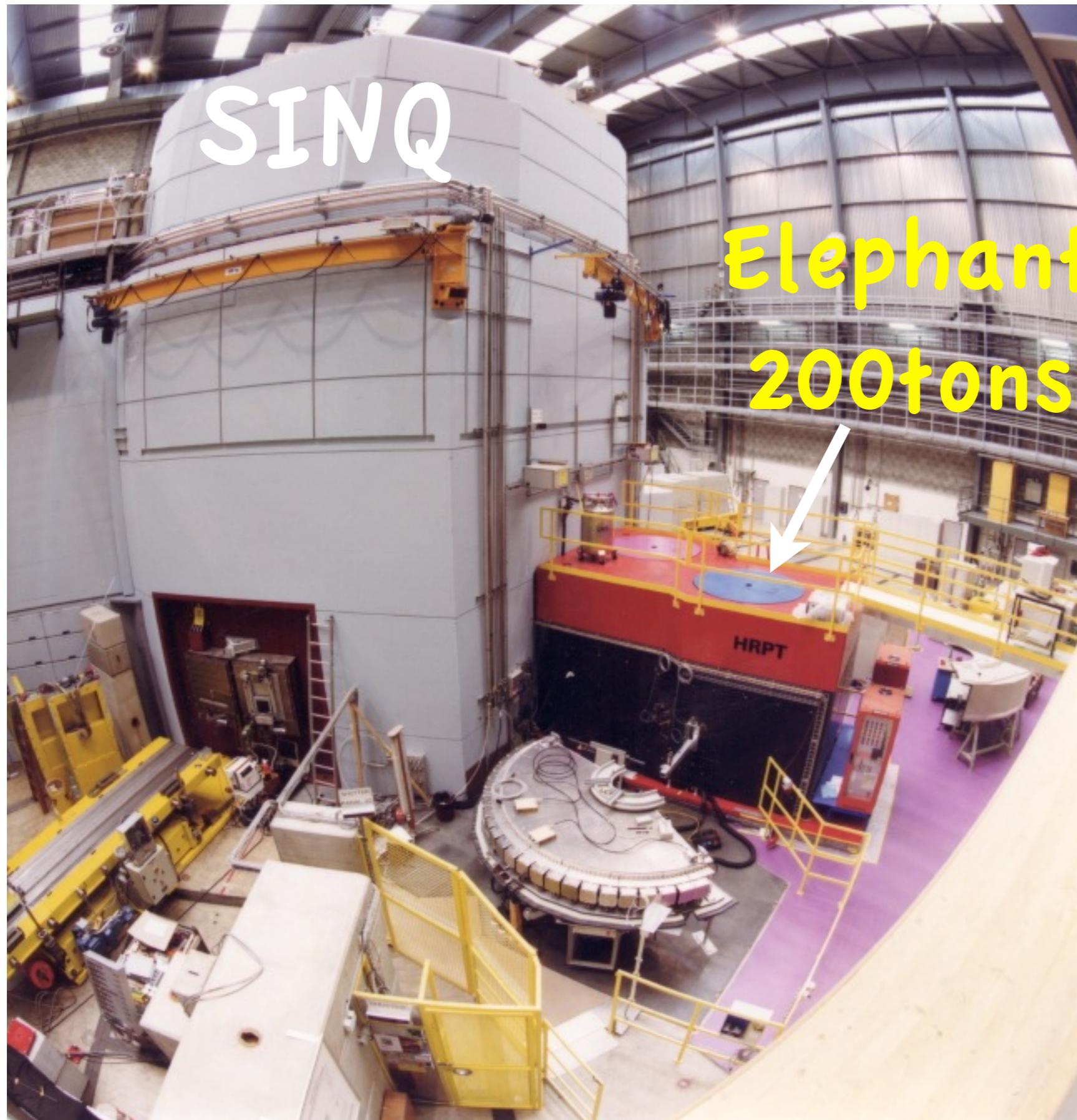


Spallation, SINQ 590MeV protons, Pb target



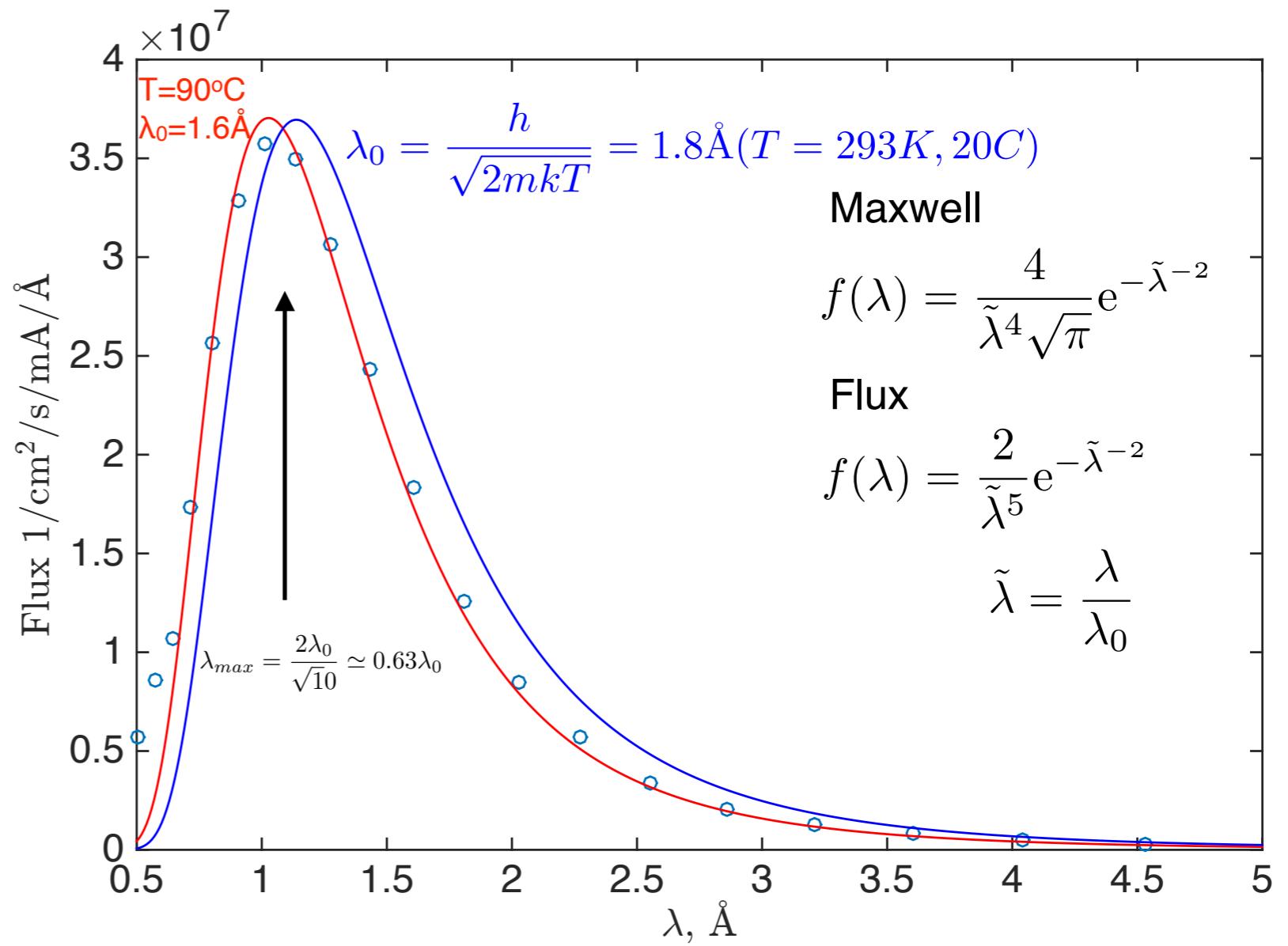
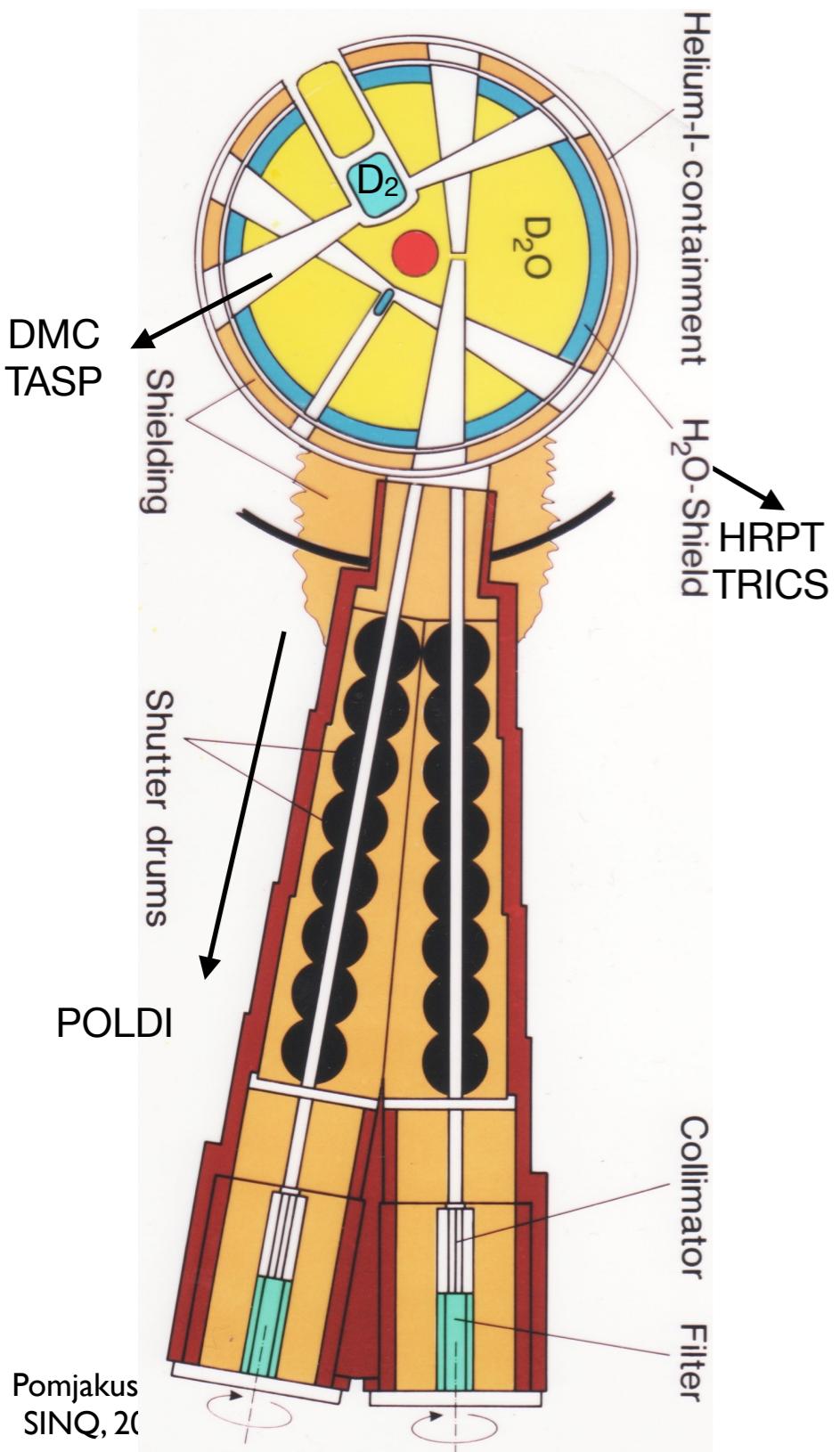
Calculated, from G.J. Russell, Spallation physics—an overview, Proceedings of ICANS-XI

SINQ hall



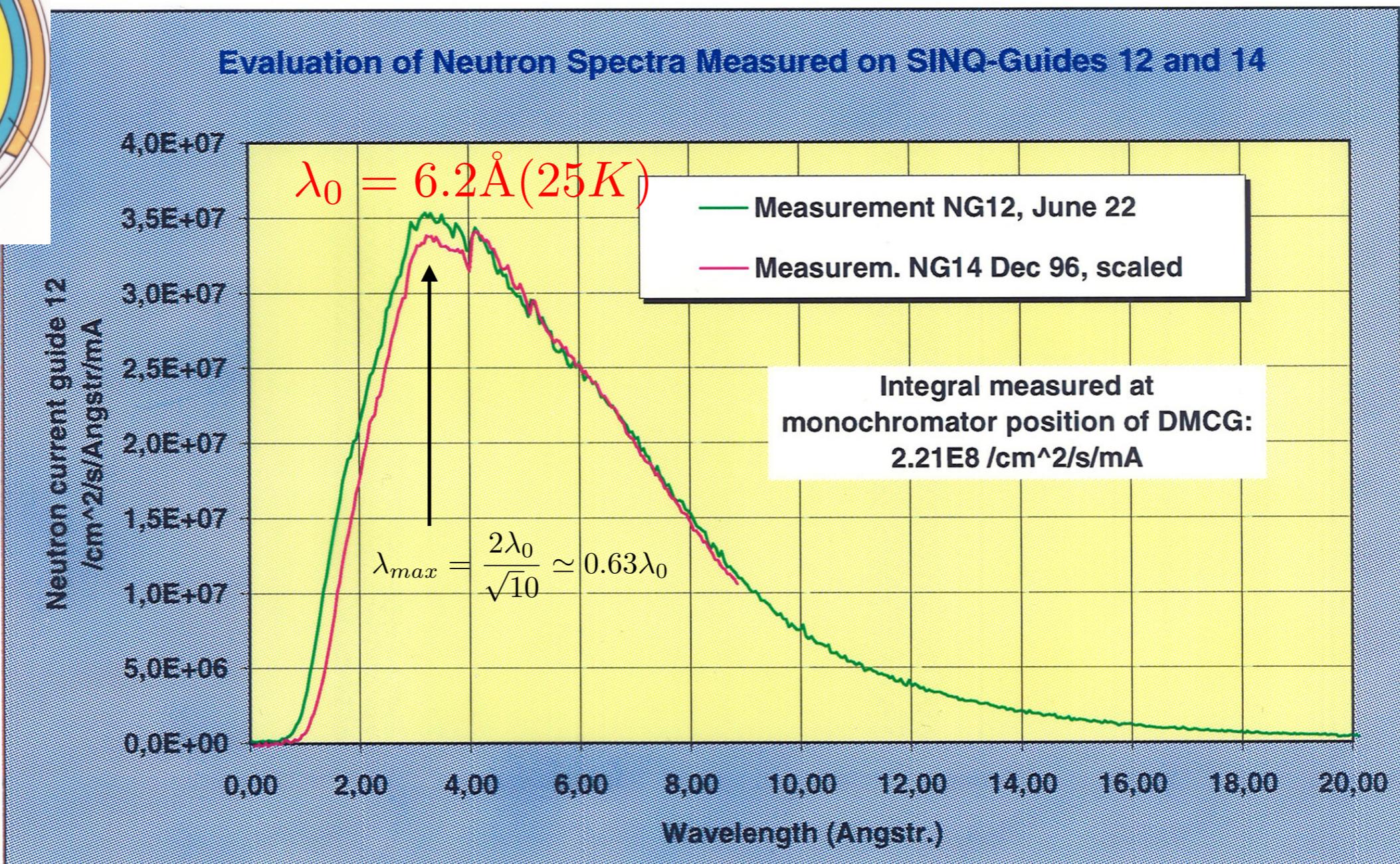
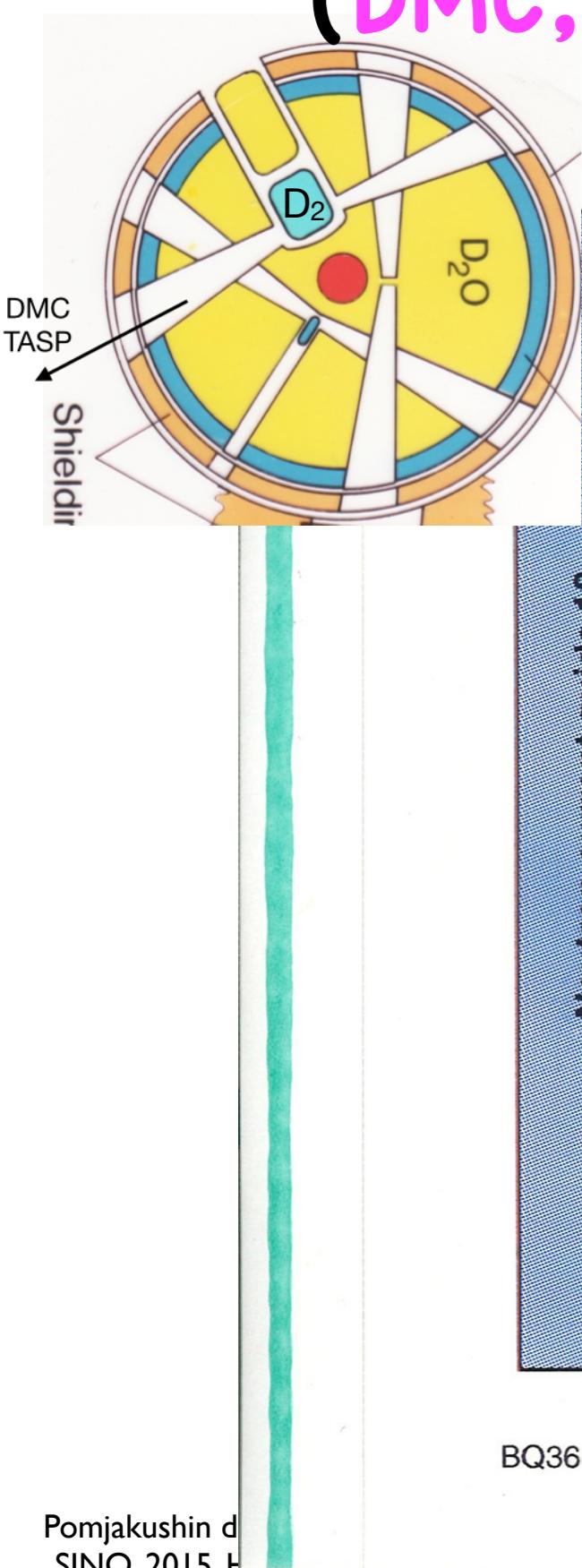
Elephant is:
Shielding of the direct
neutron beam also from
fast neutrons for
diffraction instruments

Neutron (thermal) flux from the D₂O moderator, Maxwellian at 90°C (HRPT,TRICS)



Total: $5 \cdot 10^7$ 1/cm²/s/mA
at SINQ current 2mA: 10^8

Neutron flux from cold moderator (DMC,TASP), liquid D₂, T=25K or -248C



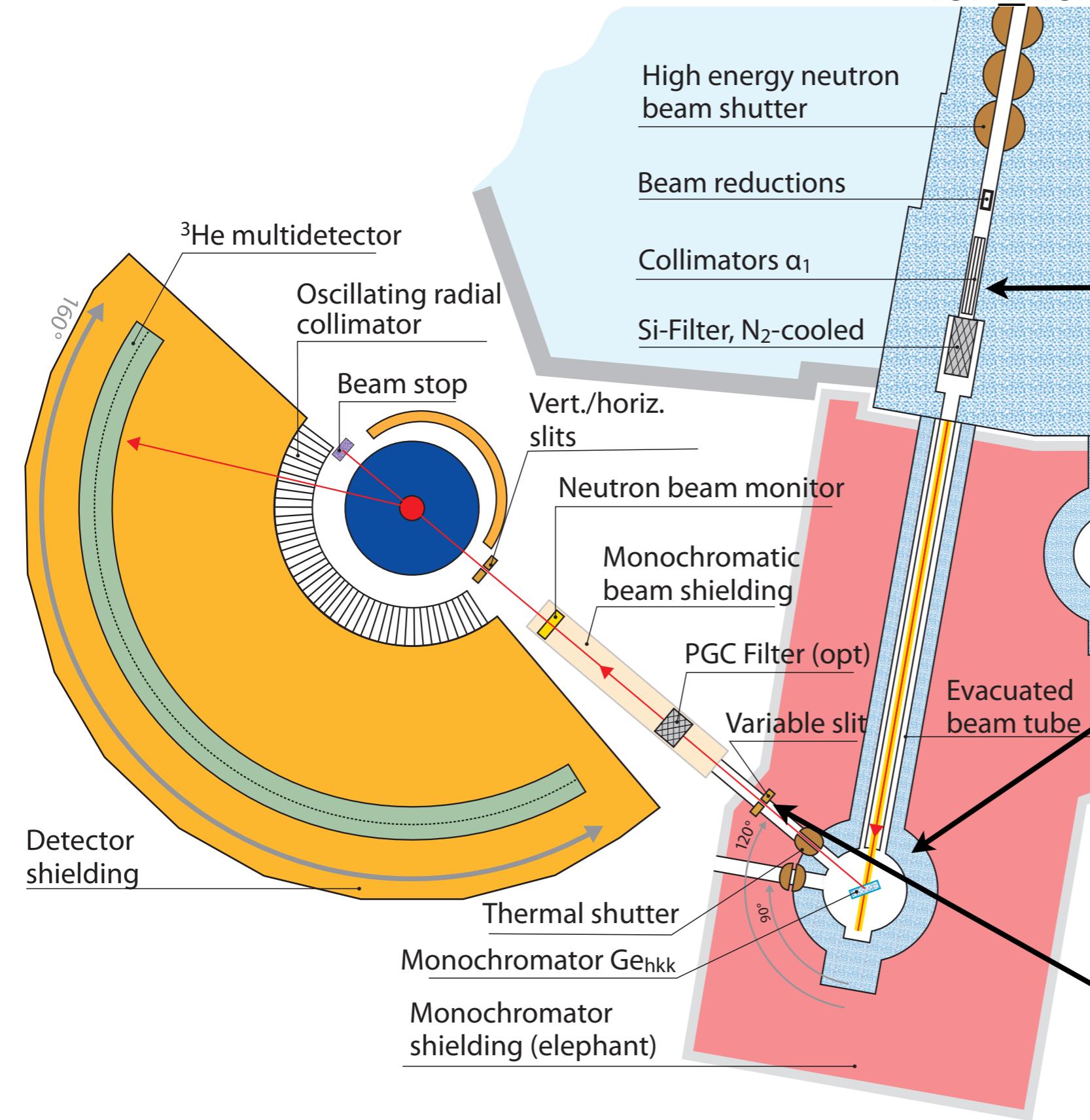
BQ36 / 23.07.1997

SINQ-NL12_tof.xls

Diagramm4

HRPT layout

High Resolution Powder Diffractometer for Thermal Neutrons



horizontal angular divergence control

α_1

primary beam collimator(s):
 $6'$, $12'$, $24'$, $30'$

α_2

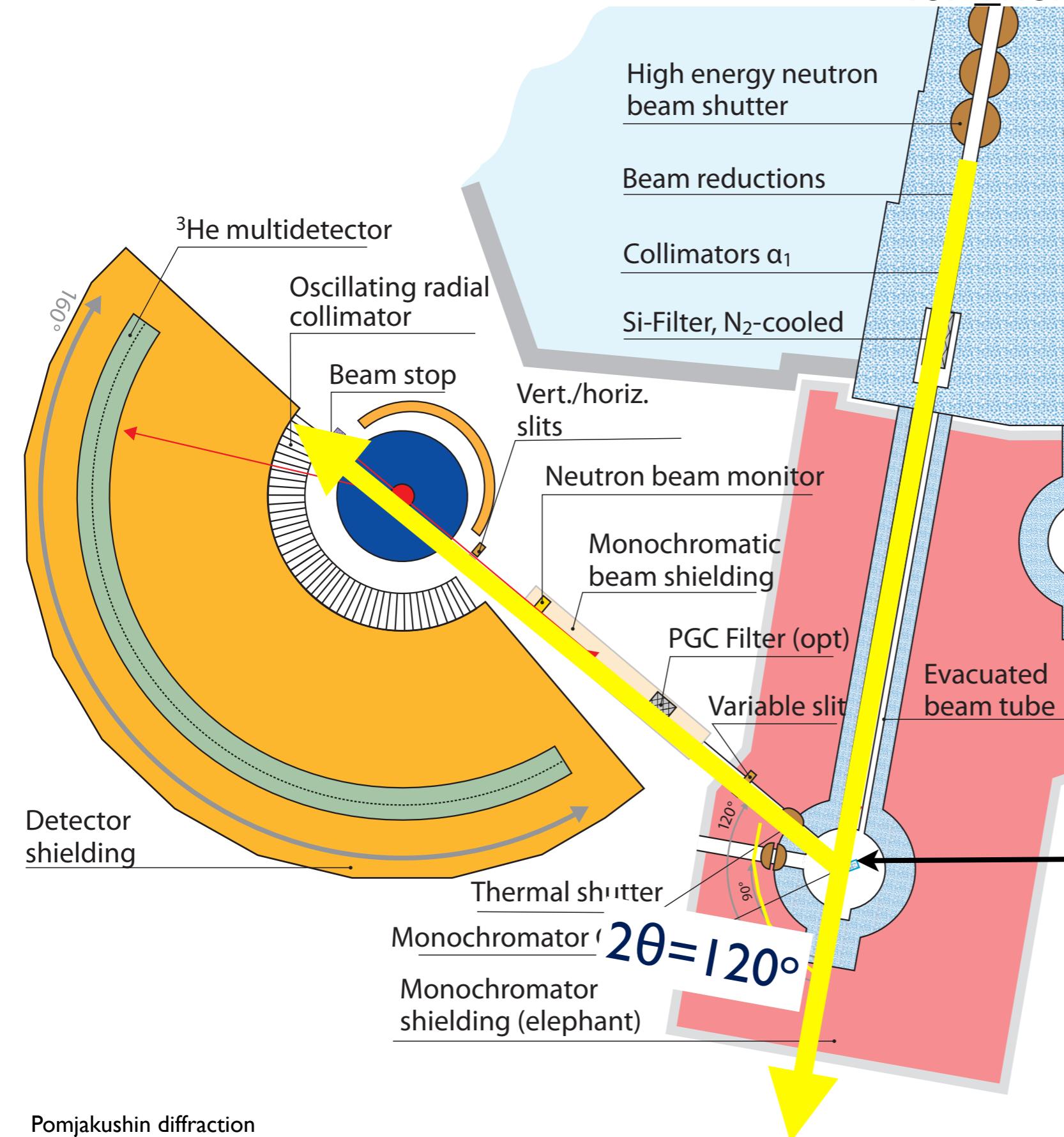
mosaic spread of the
monochromator $15'$

α_3

slit system for
monochromatic beam
and
sample diameter

HRPT layout

High Resolution Powder Diffractometer for Thermal Neutrons

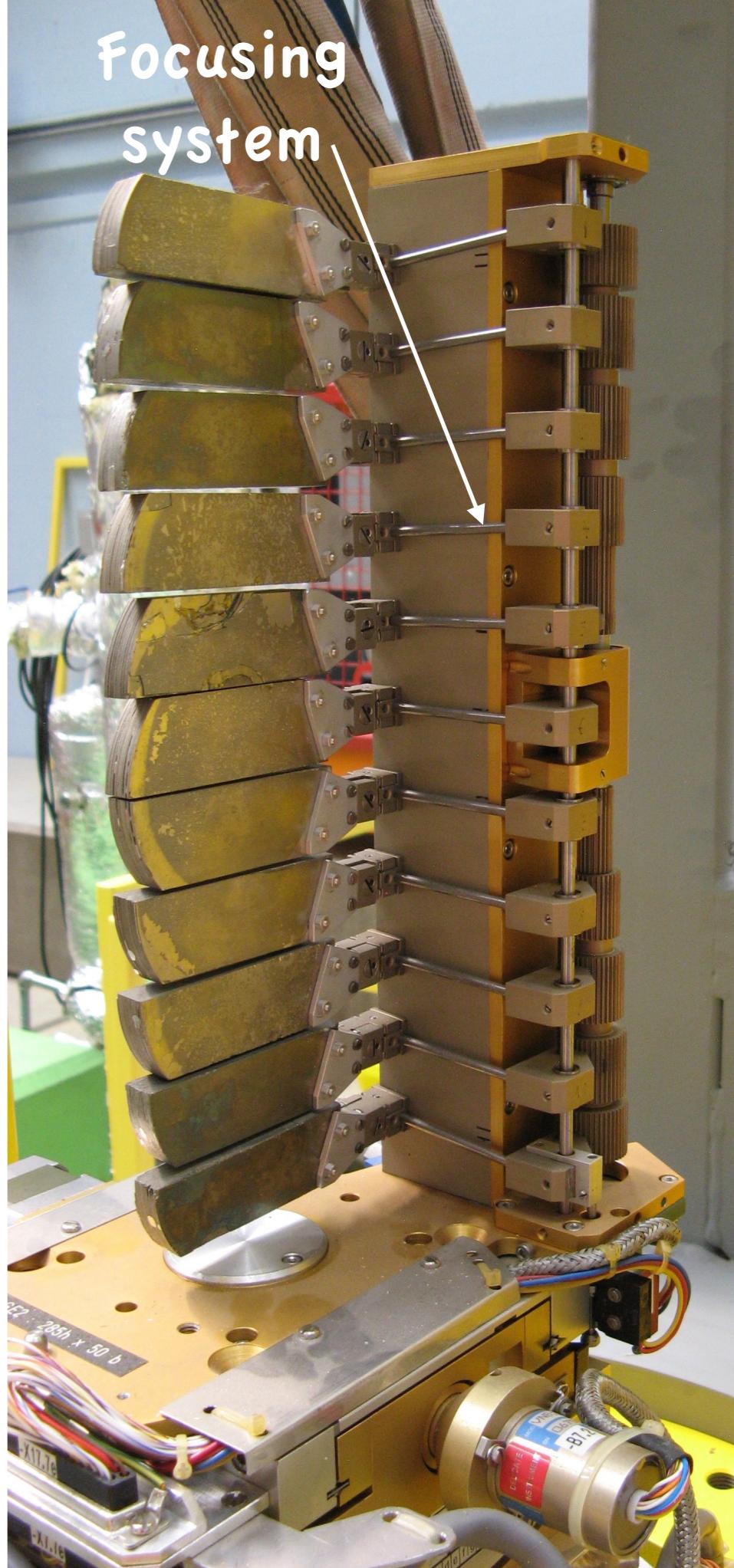
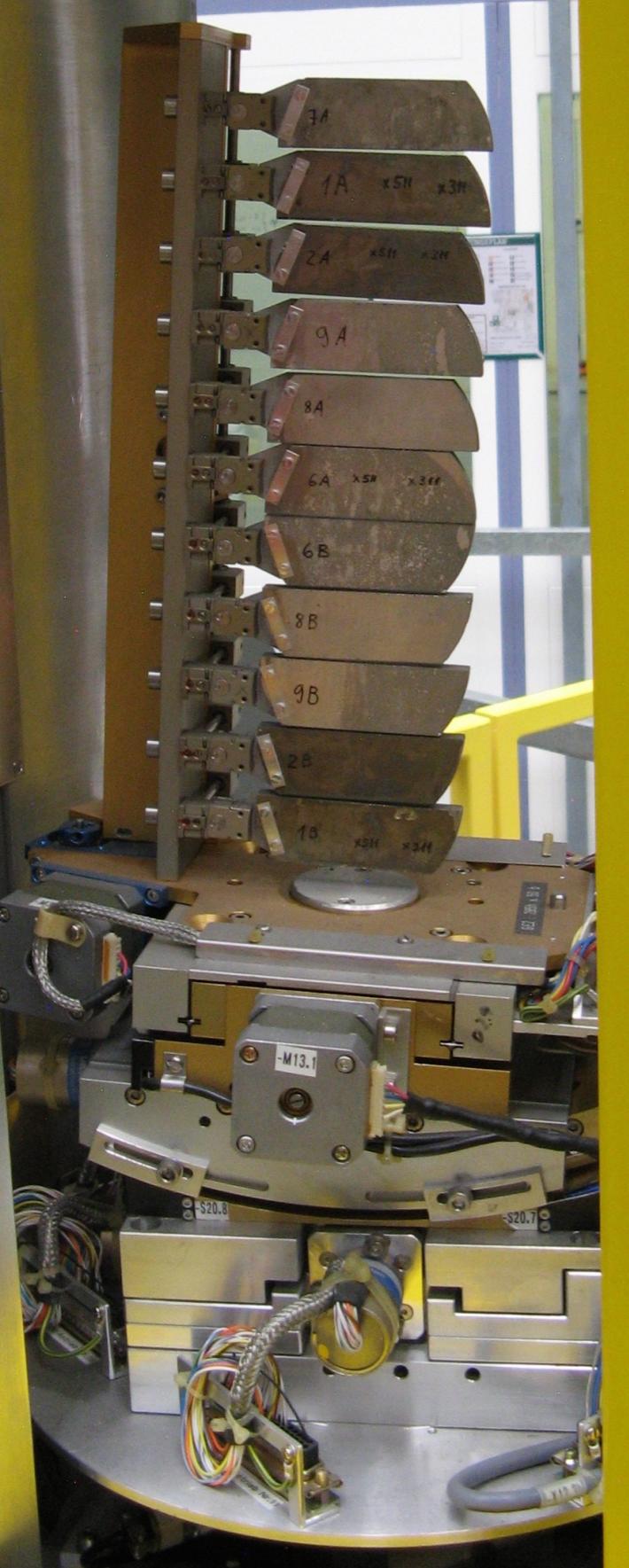


neutron monochromator
fixed 120° take off angle

$$\lambda = 2 d \sin (\theta)$$

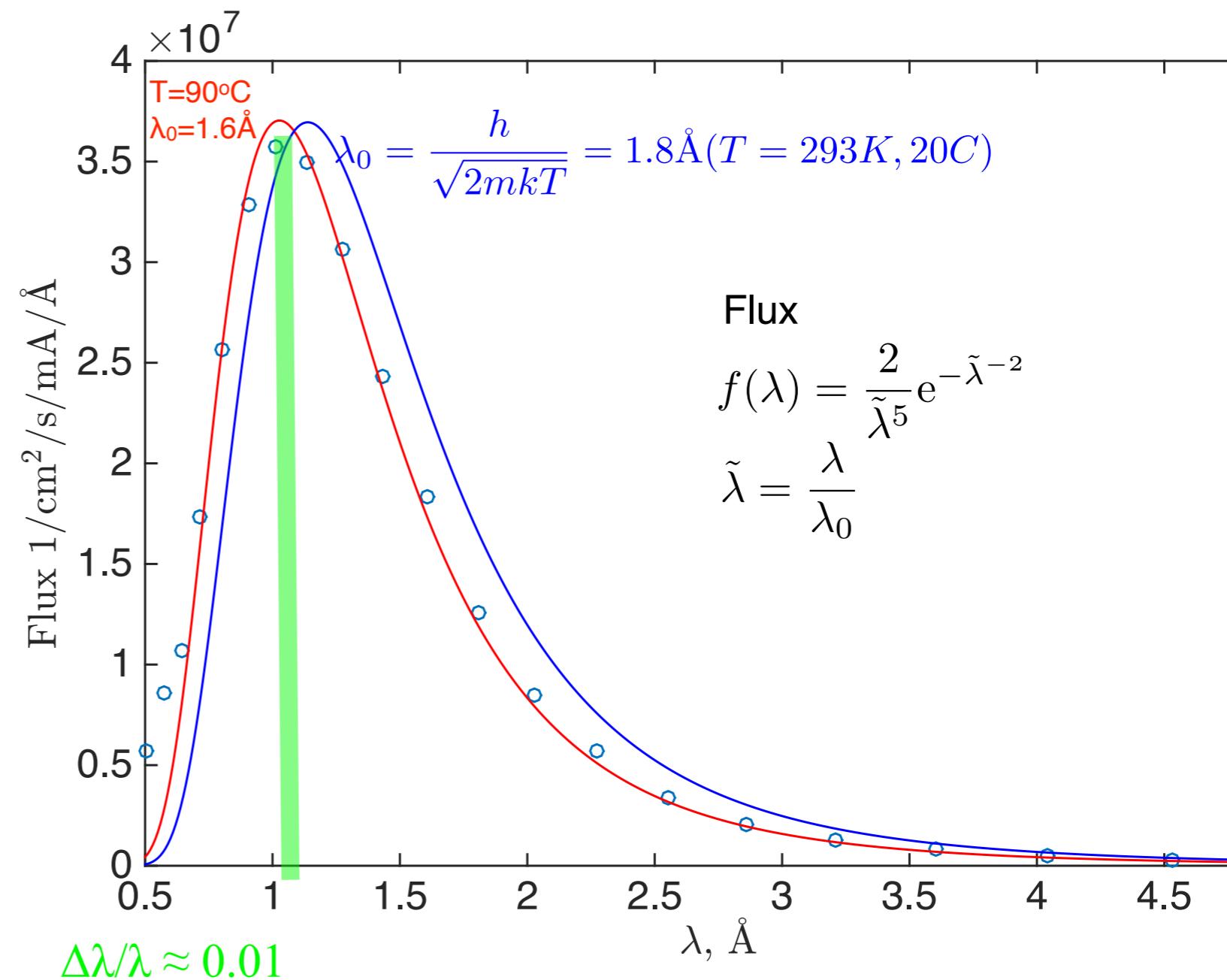
$$\lambda = 2 d \sin (60^\circ)$$

Ge single crystal monochromator, 7 motors



Focusing system

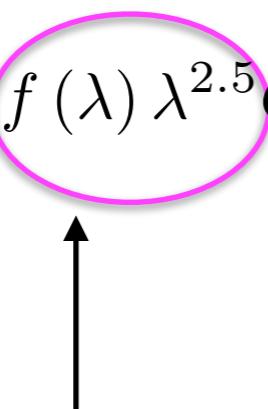
Monochromator cuts narrow wavelength range from the “white” flux. HRPT $\lambda=0.94 - 2.96 \text{ \AA}$



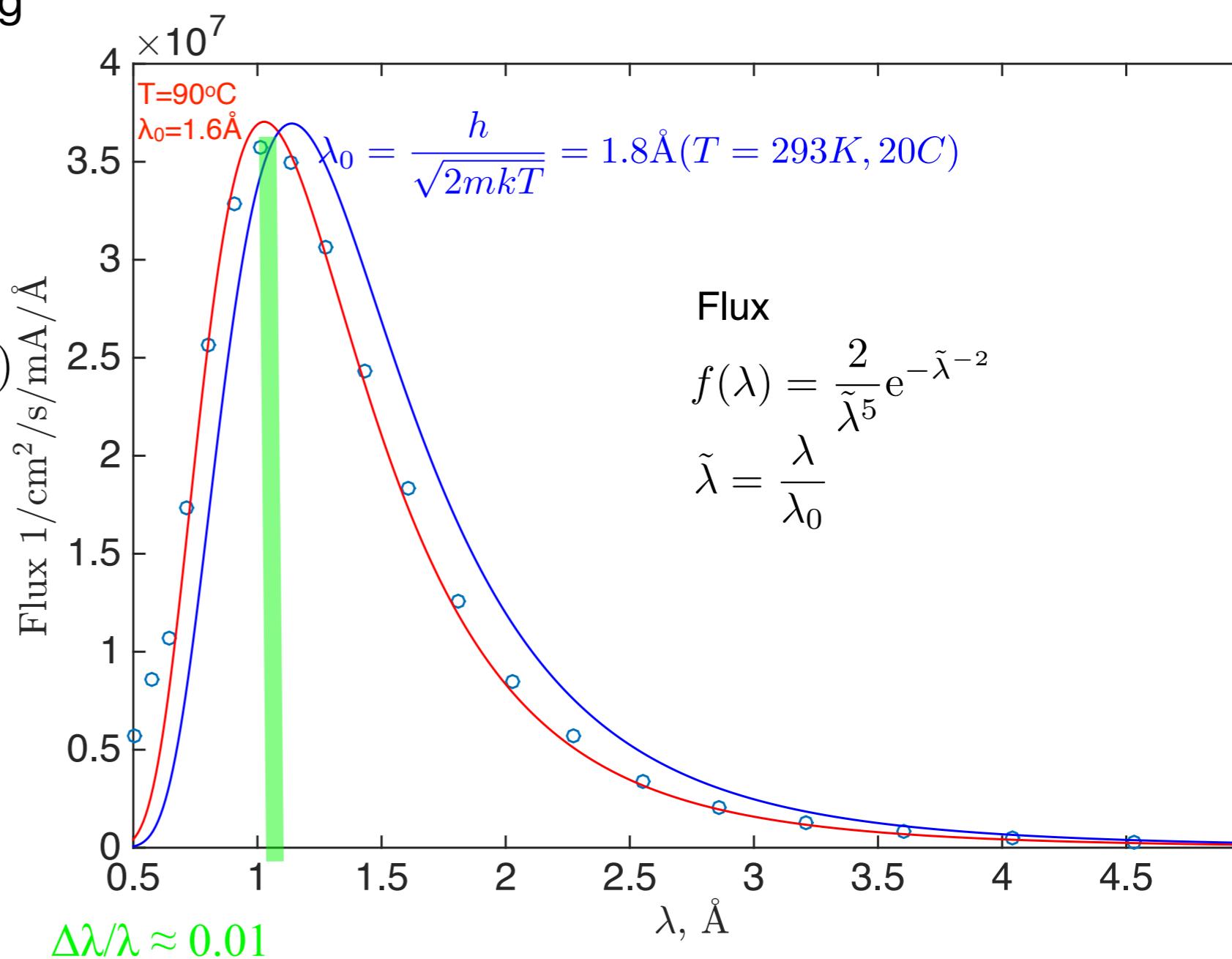
Monochromator cuts narrow wavelength range from the “white” flux. HRPT $\lambda=0.94 - 2.96 \text{ \AA}$

Intensity of Bragg scattering from big single crystal: Lorentz factor, extinction, geometry, ...

$$I \sim f(\lambda) \Delta\lambda C(\lambda, \theta) \sim f(\lambda) \lambda^{2.5} C'(\theta)$$



for fixed monochromator take-off 2θ for HRPT

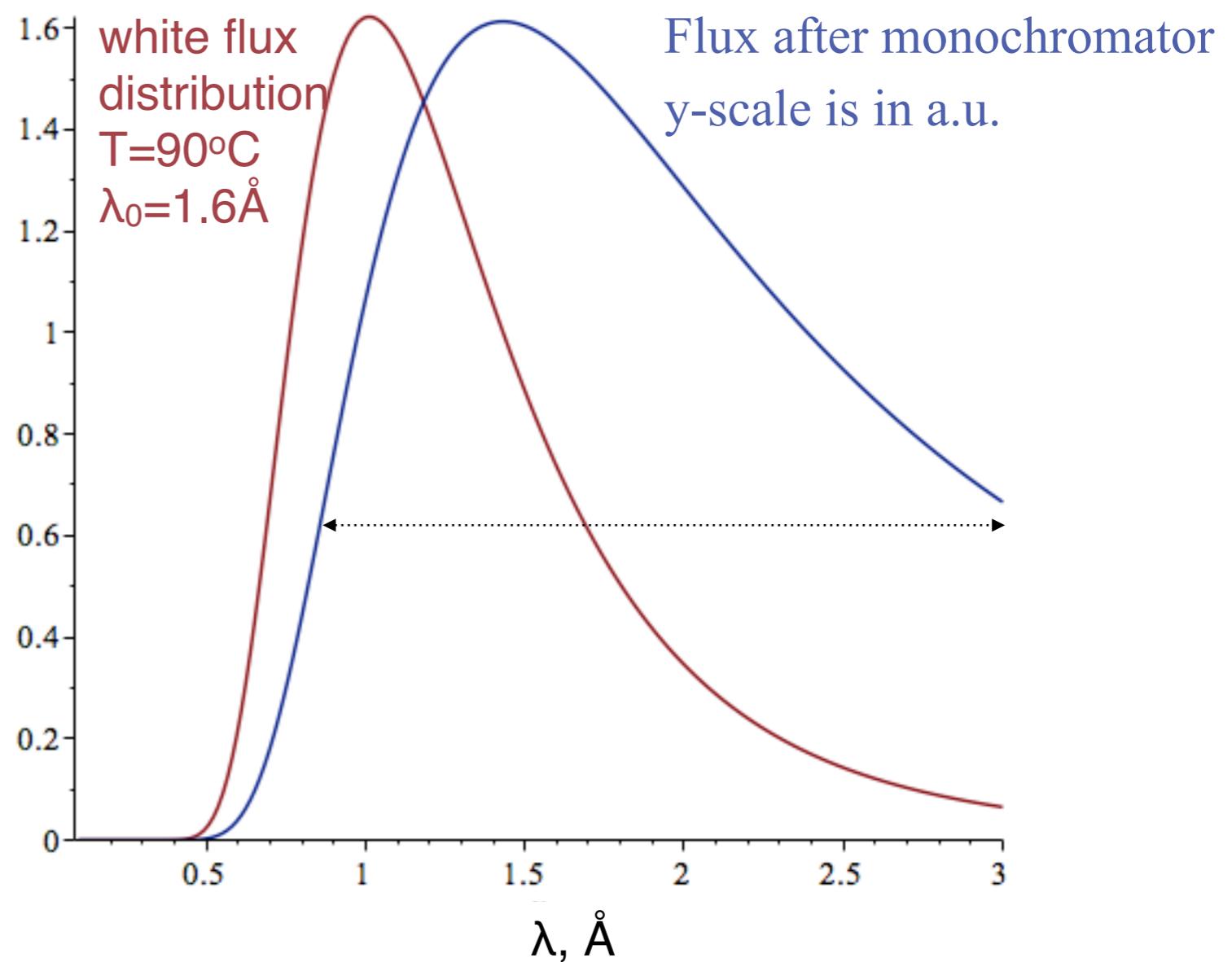


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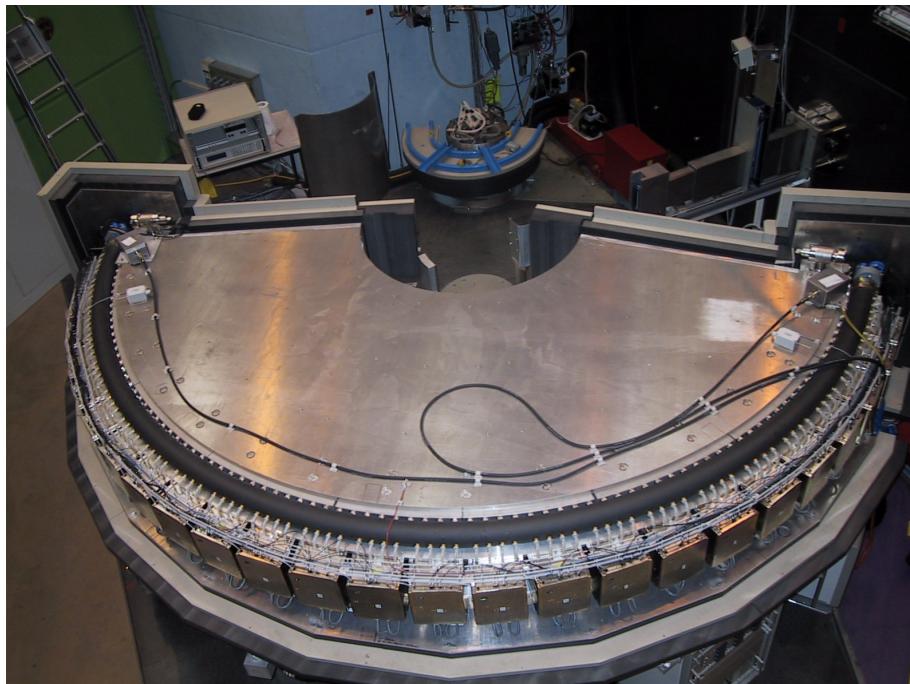
for fixed monochromator take-off 2θ for HRPT



Powder ND at SINQ/PSI

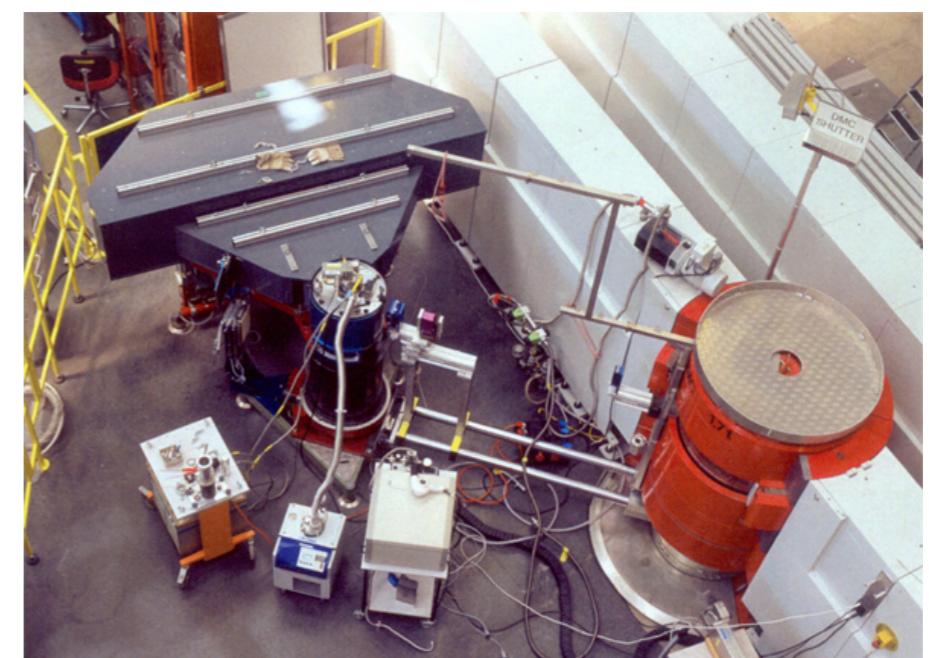
HRPT - High Resolution Powder Diffractometer for Thermal Neutrons. linear detector with 1600 channels, 0.1°

Responsible: Vladimir Pomjakushin, Denis Sheptyakov

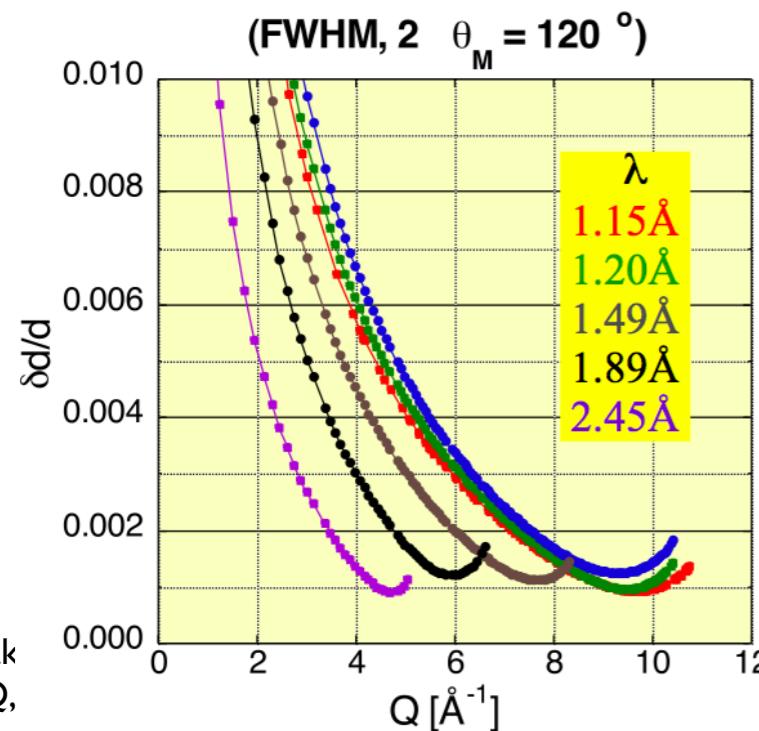


DMC - cold neutron powder diffractometer linear detector with 400 channels, 0.2°

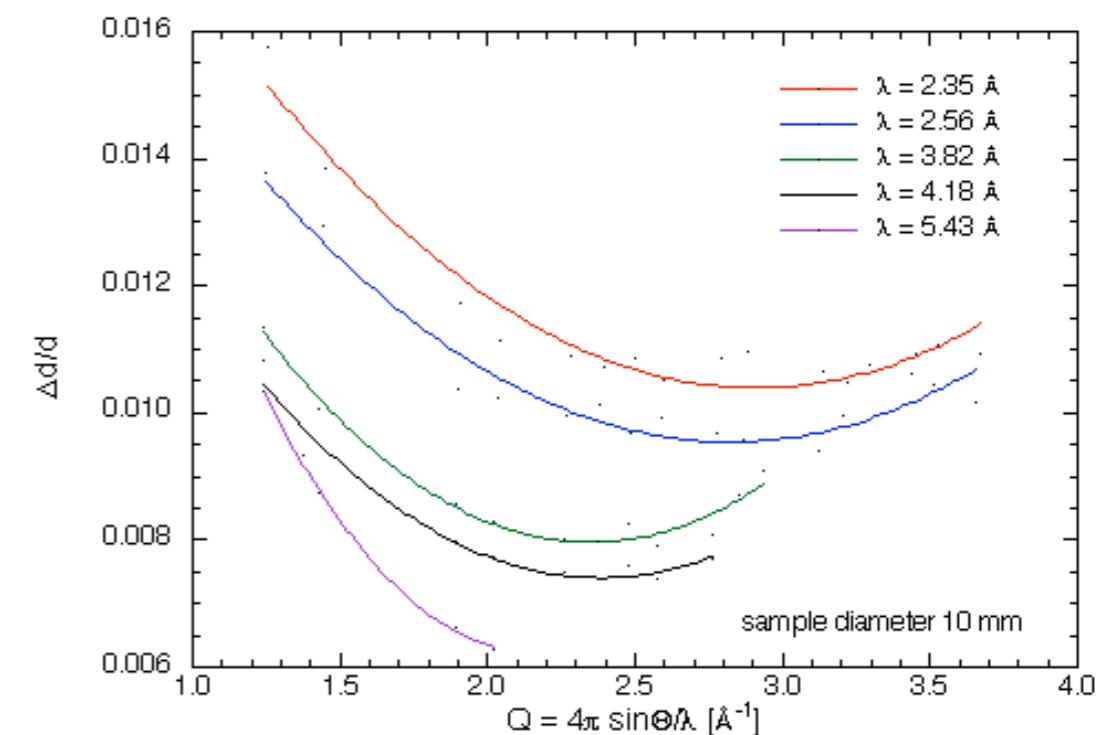
Responsible: Lukas Keller, Matthias Frontzek



HRPT RESOLUTION FUNCTIONS



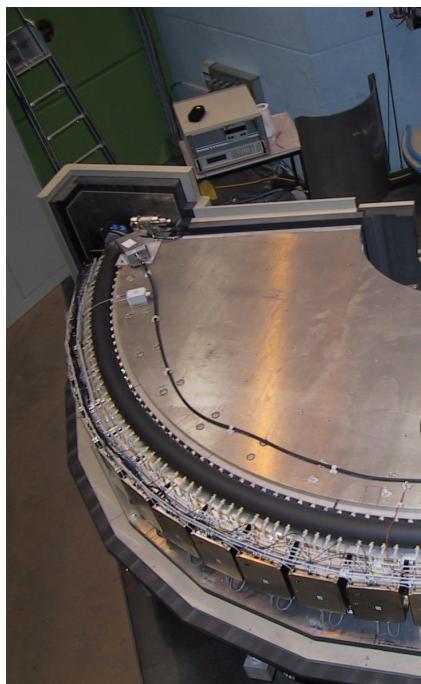
DMC: experimental resolution functions $\Delta d/d(Q, \lambda)$



Powder ND at SINQ/PSI

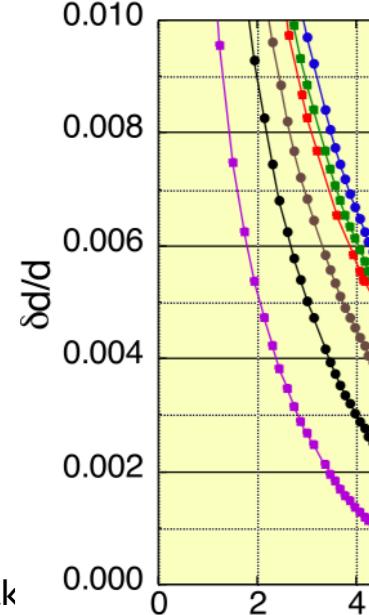
HRPT - High Resolution Powder Diffractometer for ^{Thermal} Neutrons
linear detector wi

Responsible: Vladimir Pomjak



HRPT RESOLU

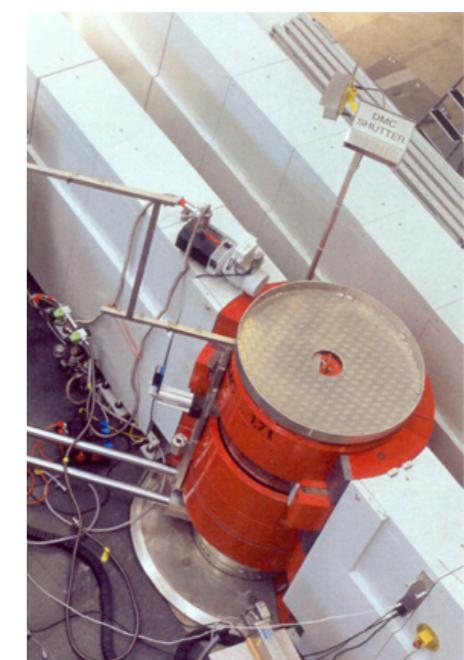
(FWHM)



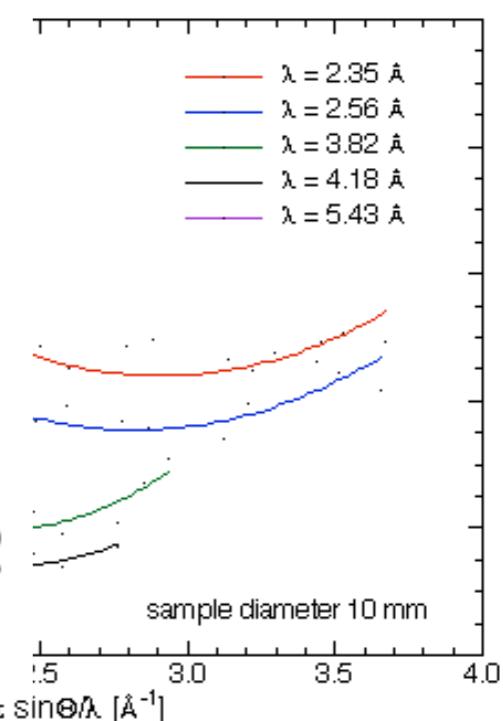
Pomjak
SINQ,

DMC - cold neutron powder diffractometer
hannels, 0.2°

Mias Frontzek



ution functions $\Delta d/d (Q, \lambda)$

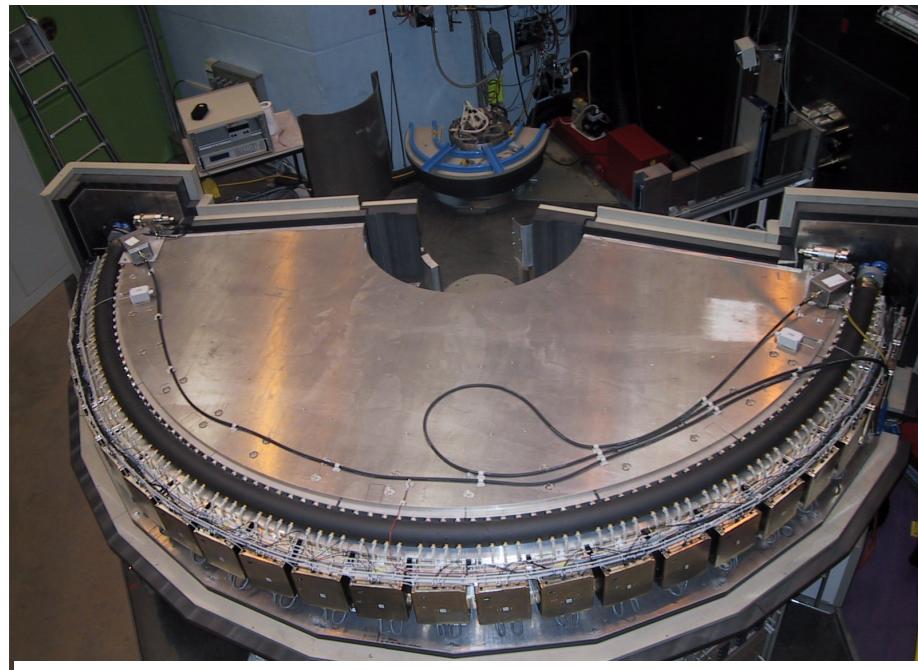


$Q [\text{\AA}^{-1}]$

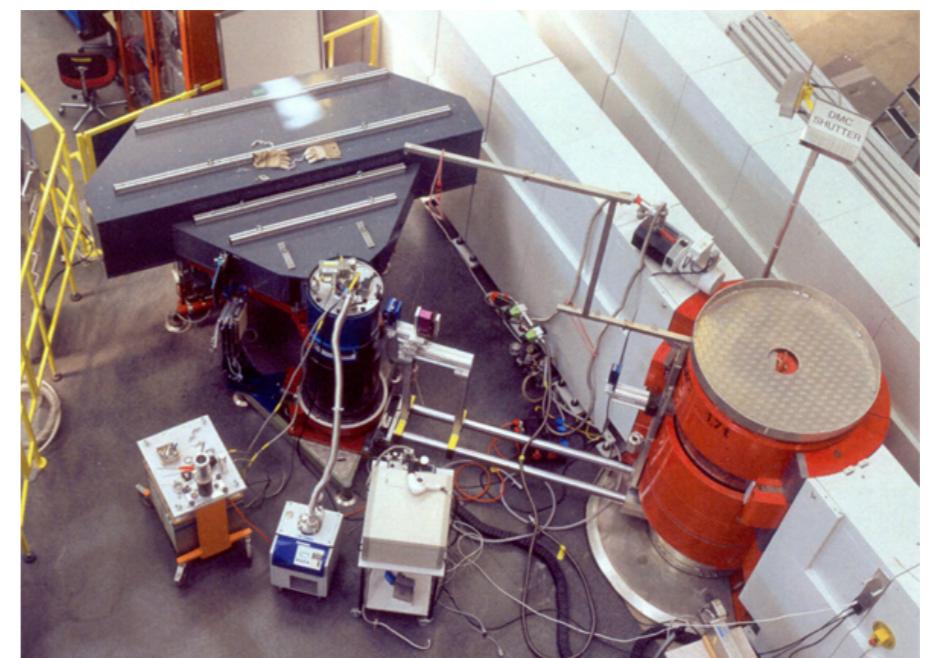
$Q = 4\pi \sin \theta / \lambda [\text{\AA}^{-1}]$

Powder ND at SINQ/PSI

HRPT - High Resolution Powder
Diffractometer for Thermal Neutrons at SINQ

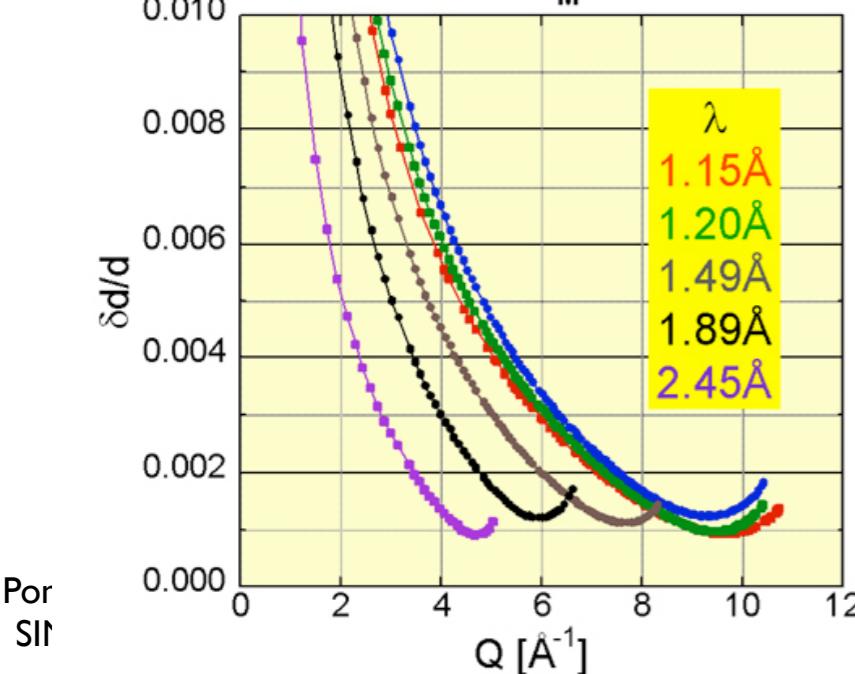


DMC - cold neutron powder diffractometer

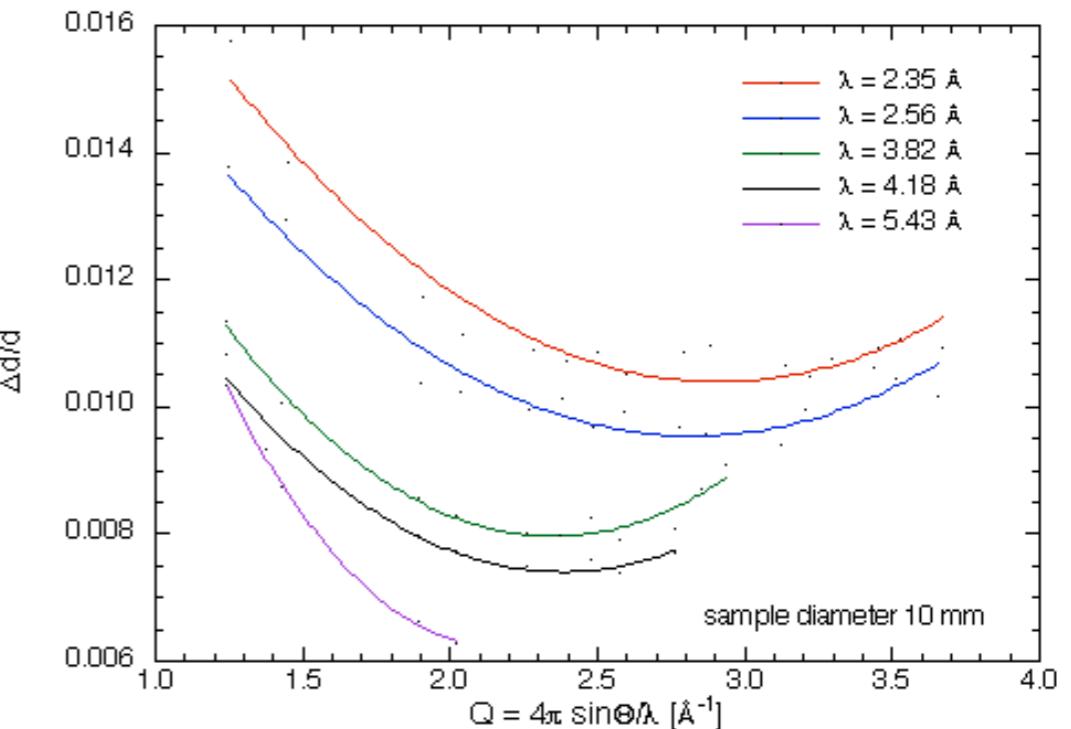


HRPT RESOLUTION FUNCTIONS

(FWHM, $2\theta_M = 120^\circ$)



DMC: experimental resolution functions $\Delta d/d$ (Q, λ)

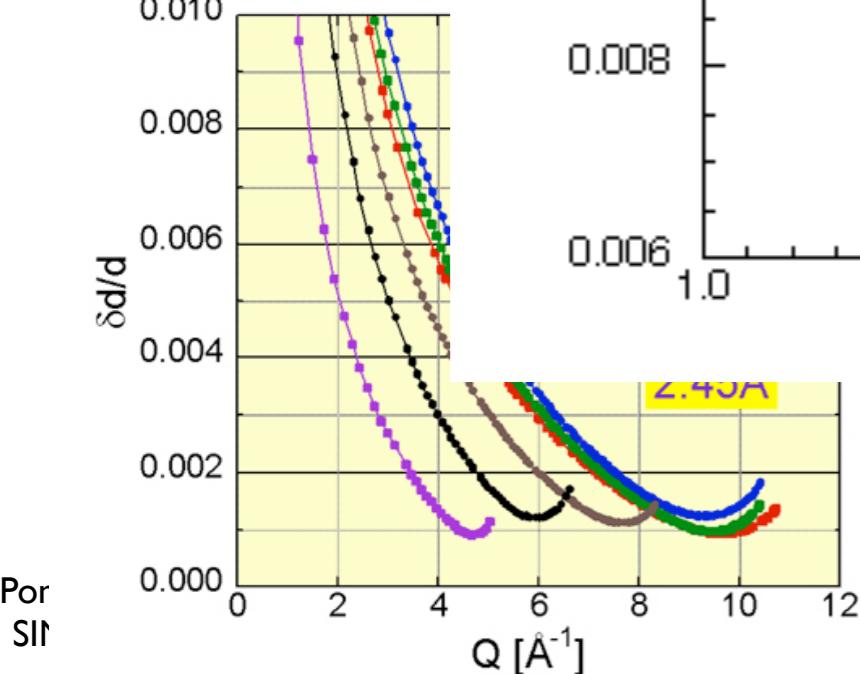


Powder ND at SINQ/PSI

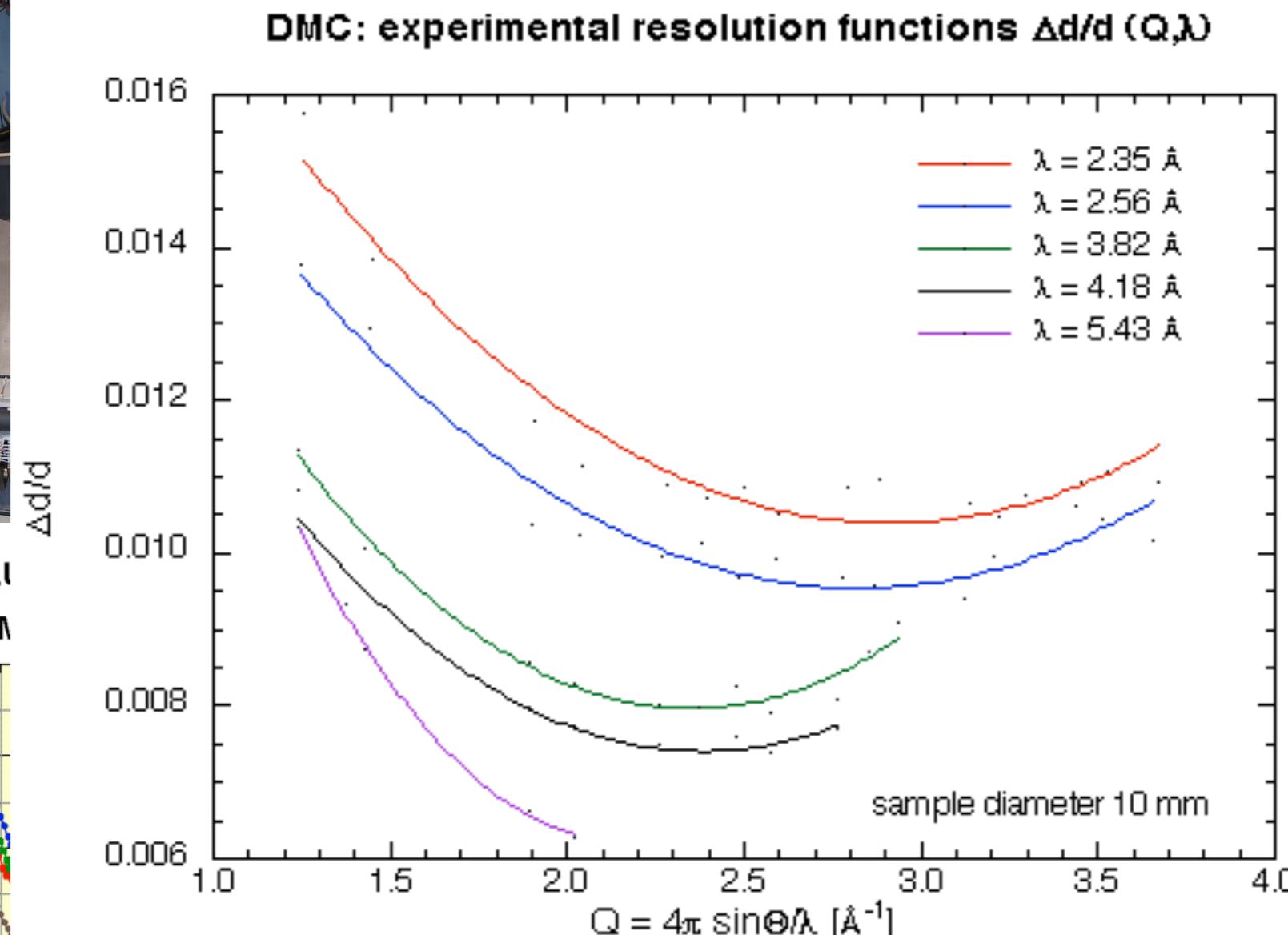
HRPT - High Resolution Powder Diffractometer for Thermal Neutrons at SINQ



HRPT RESOLU
(FWHM)

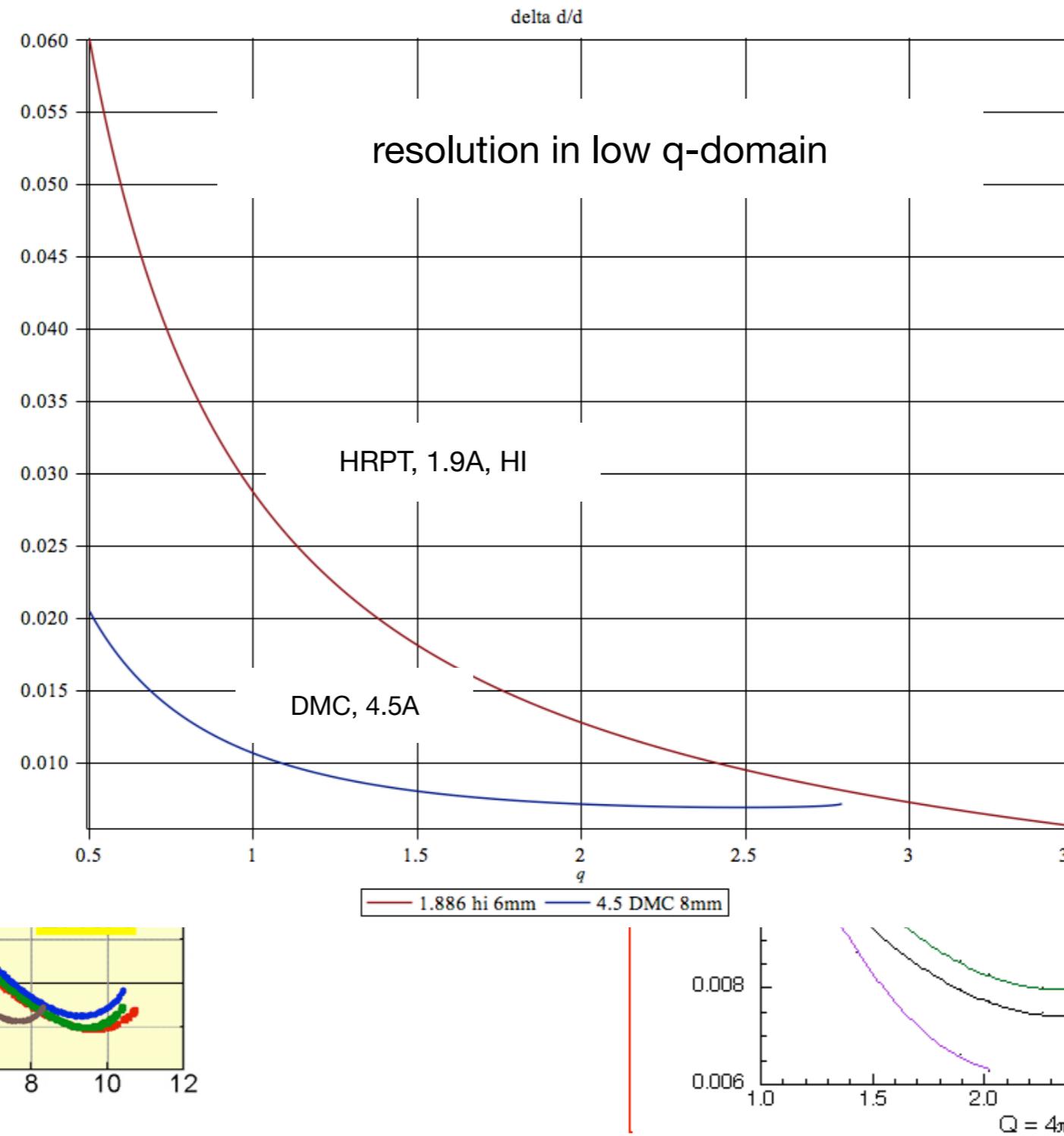
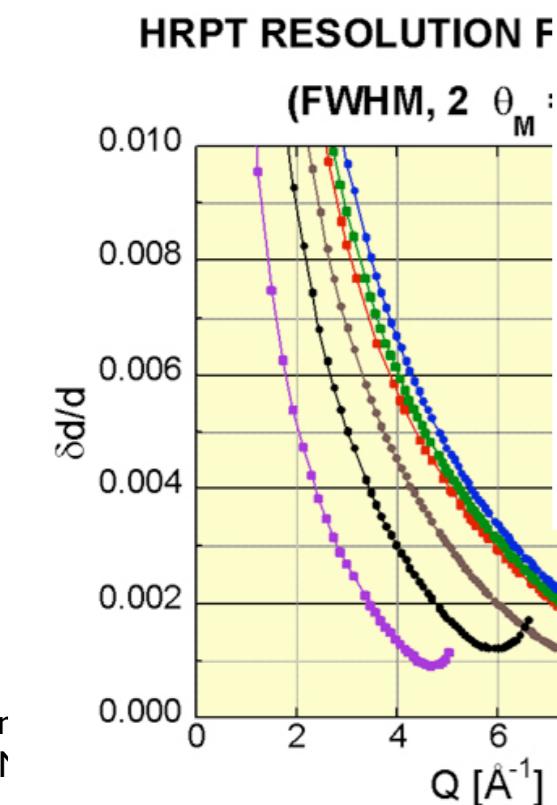
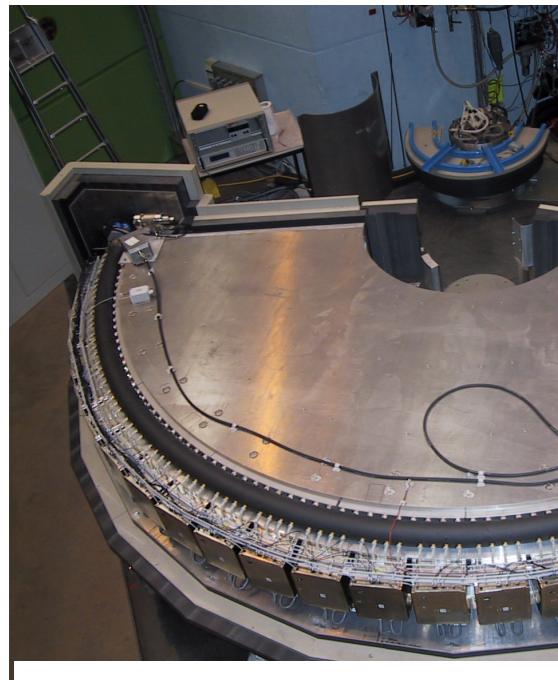


DMC - cold neutron powder diffractometer

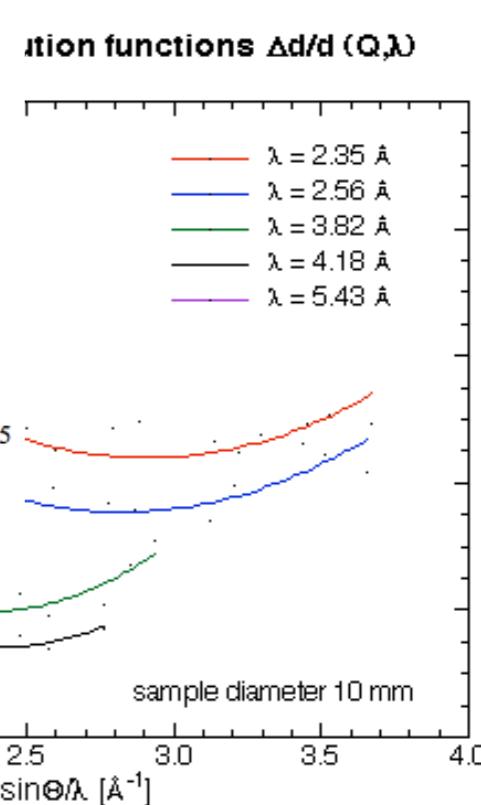
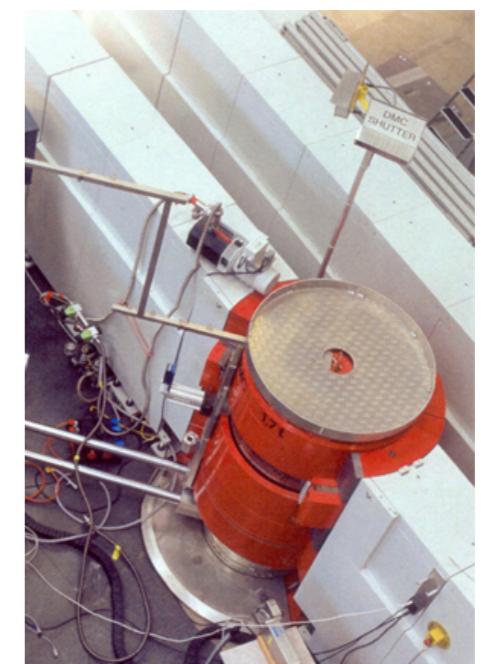


Powder ND at SINQ/PSI

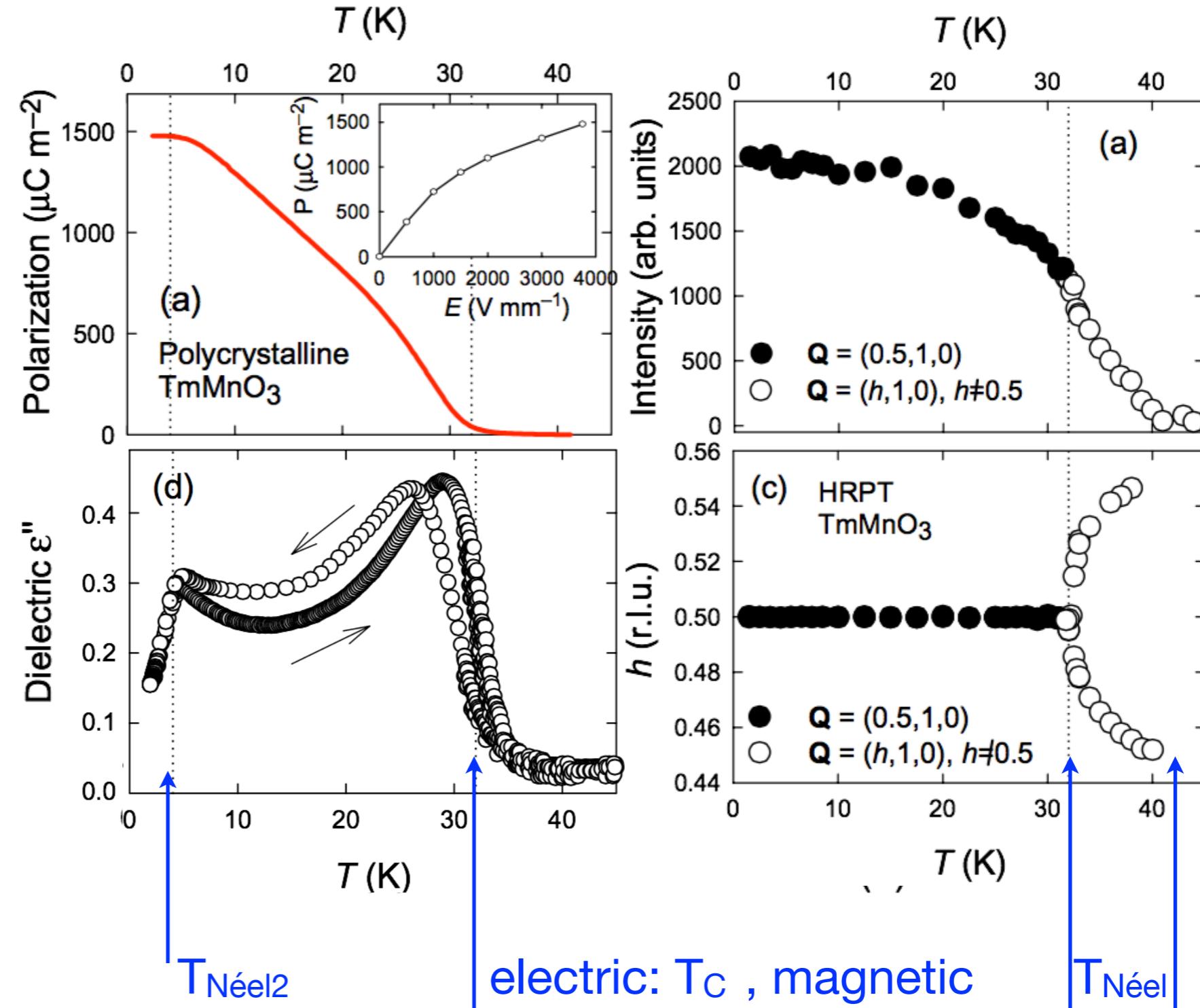
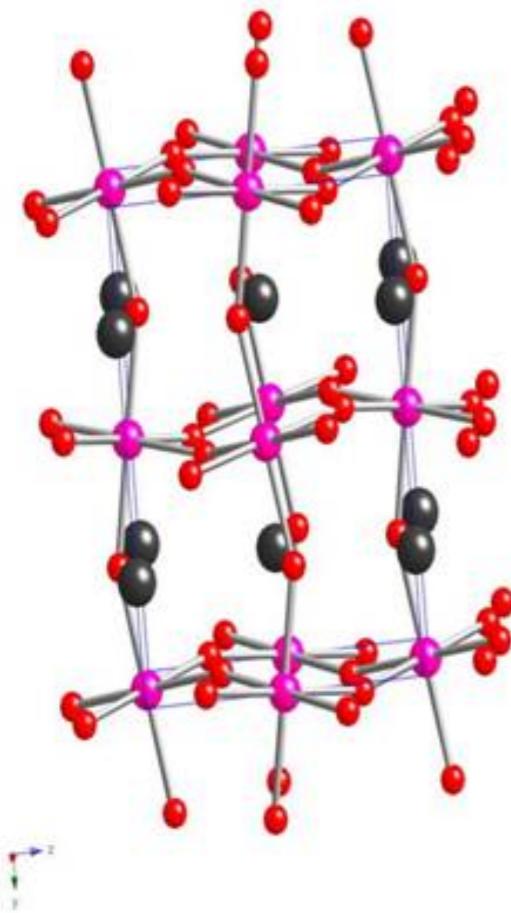
HRPT - High Resolution Powder
Diffractometer for Thermal Neutrons at SINQ



DMC - cold neutron powder diffractometer



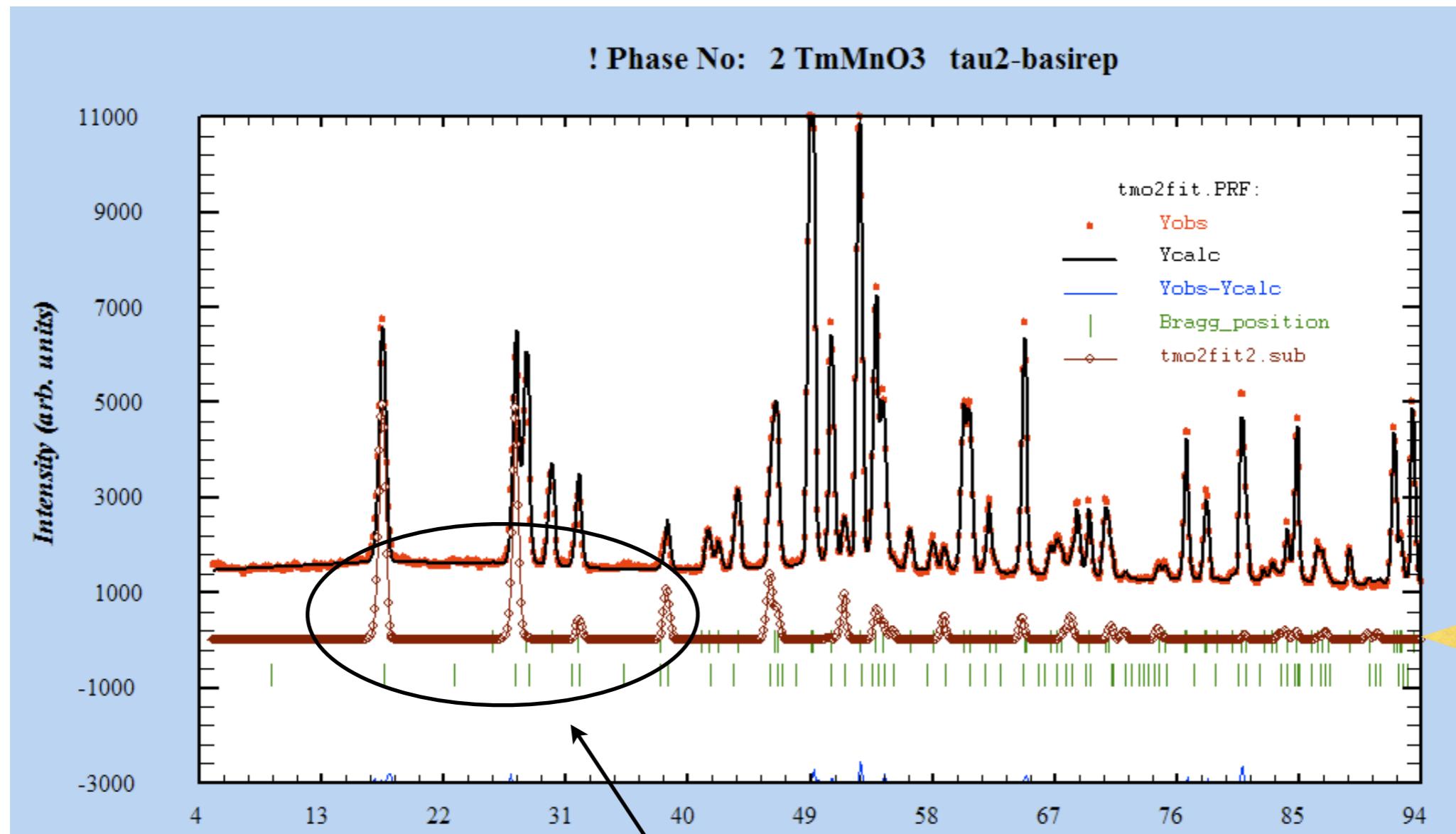
Spin-lattice coupling and antiferromagnetic order in orthorhombic multiferroic* $TmMnO_3$



* materials that have coupled electric, magnetic and structural order parameters

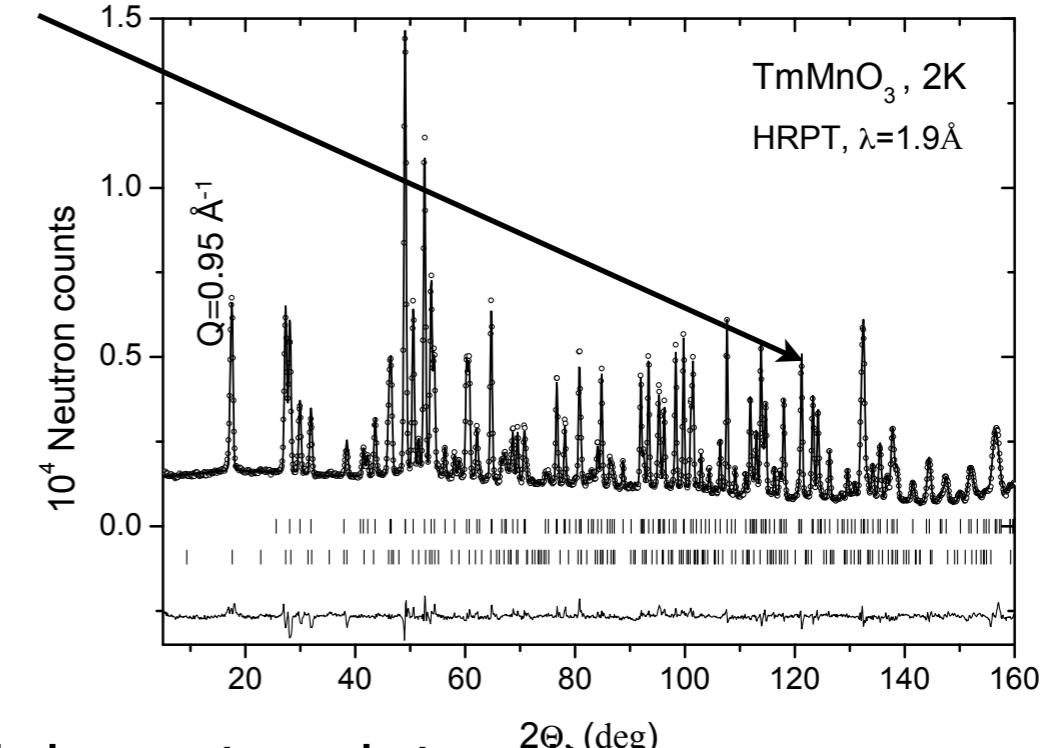
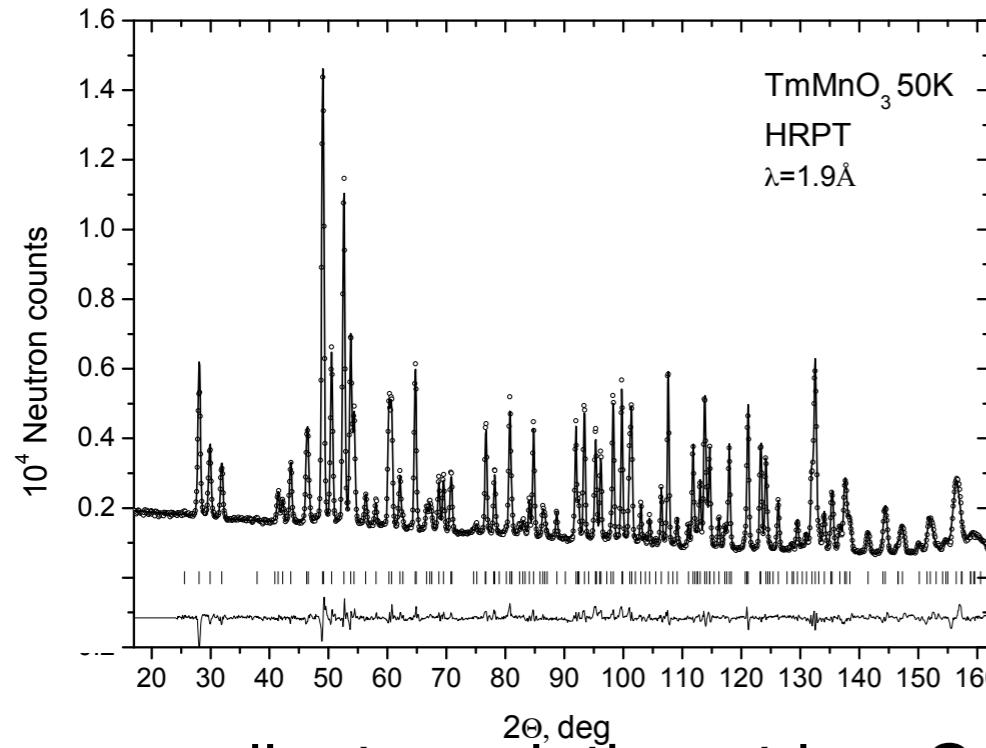
cf. resolution/q-range

HRPT 1.9Å

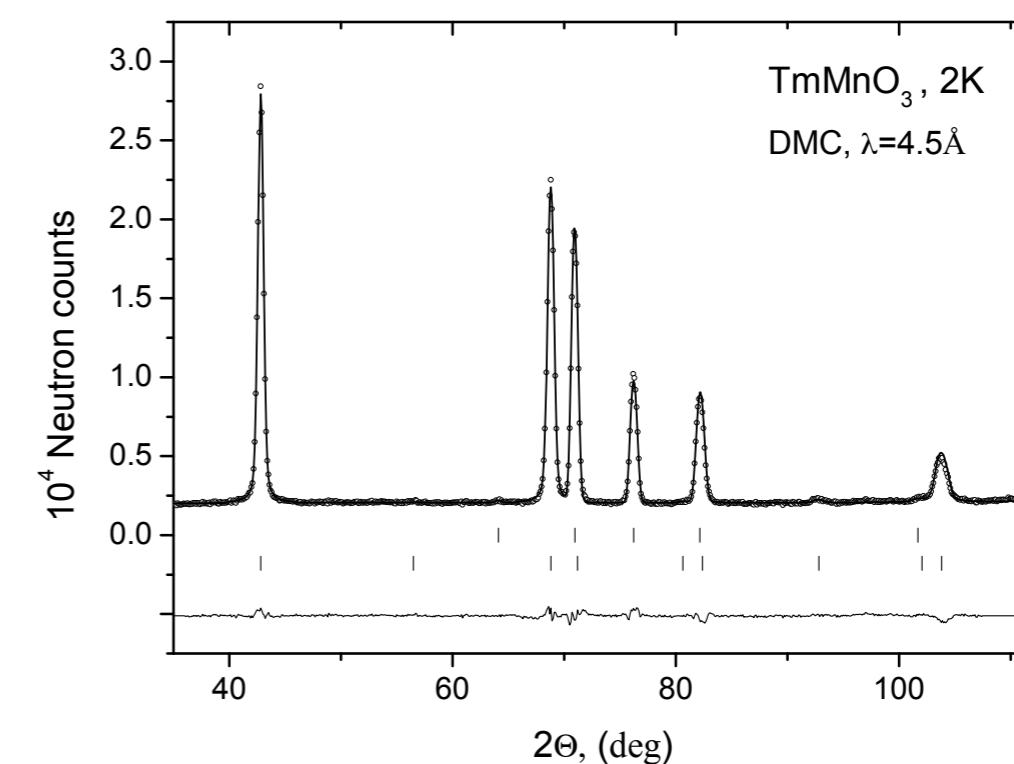
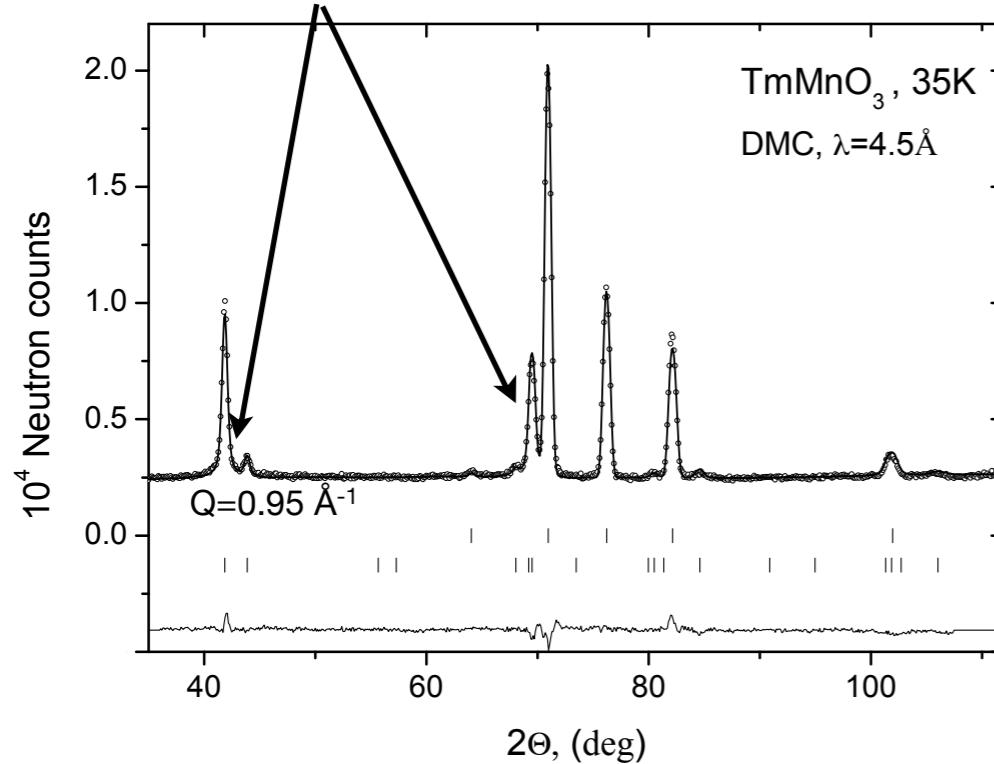


Complementarity 1.9Å HRPT and 4.5Å DMC

excellent resolution and high Q-range

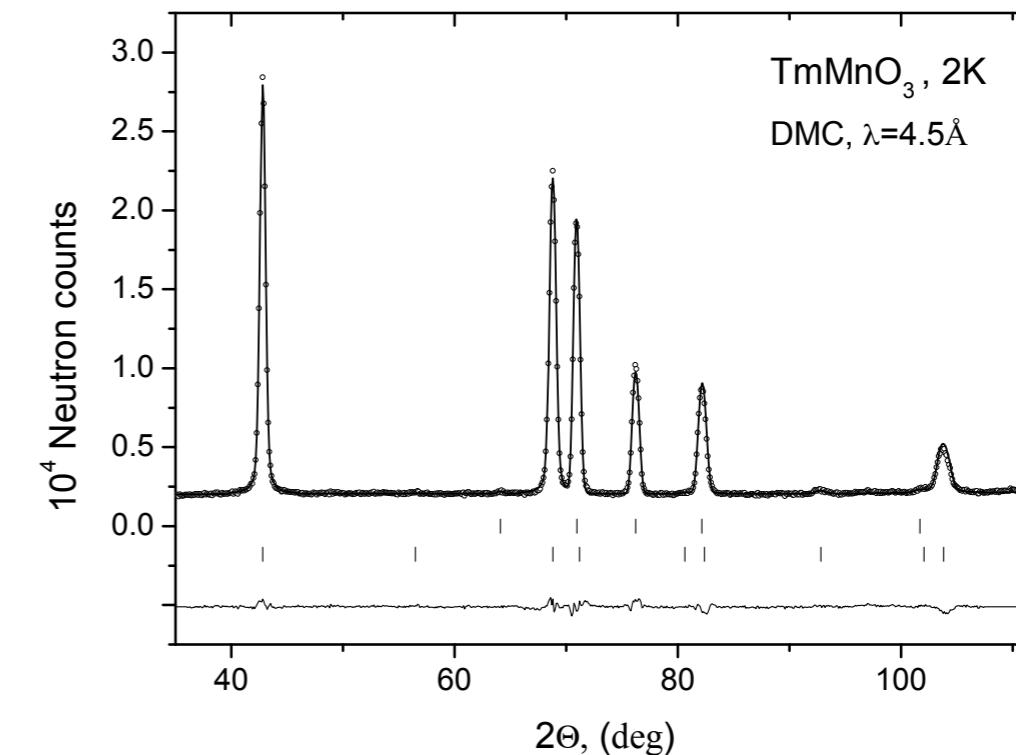
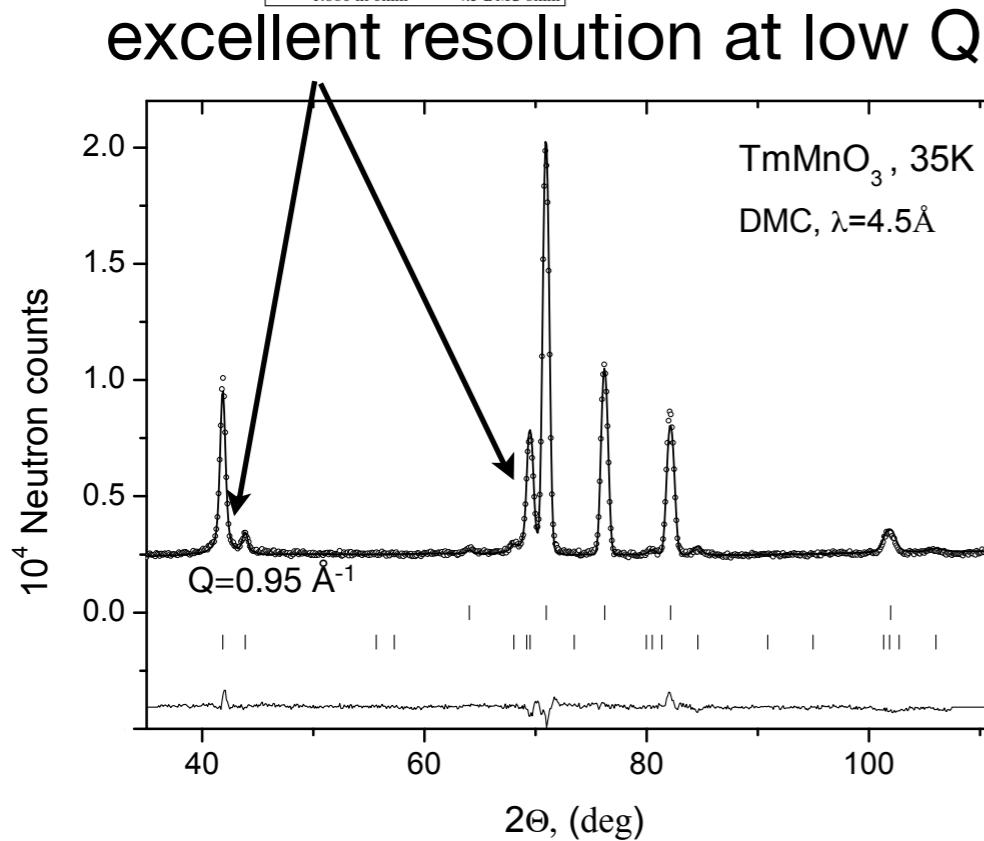
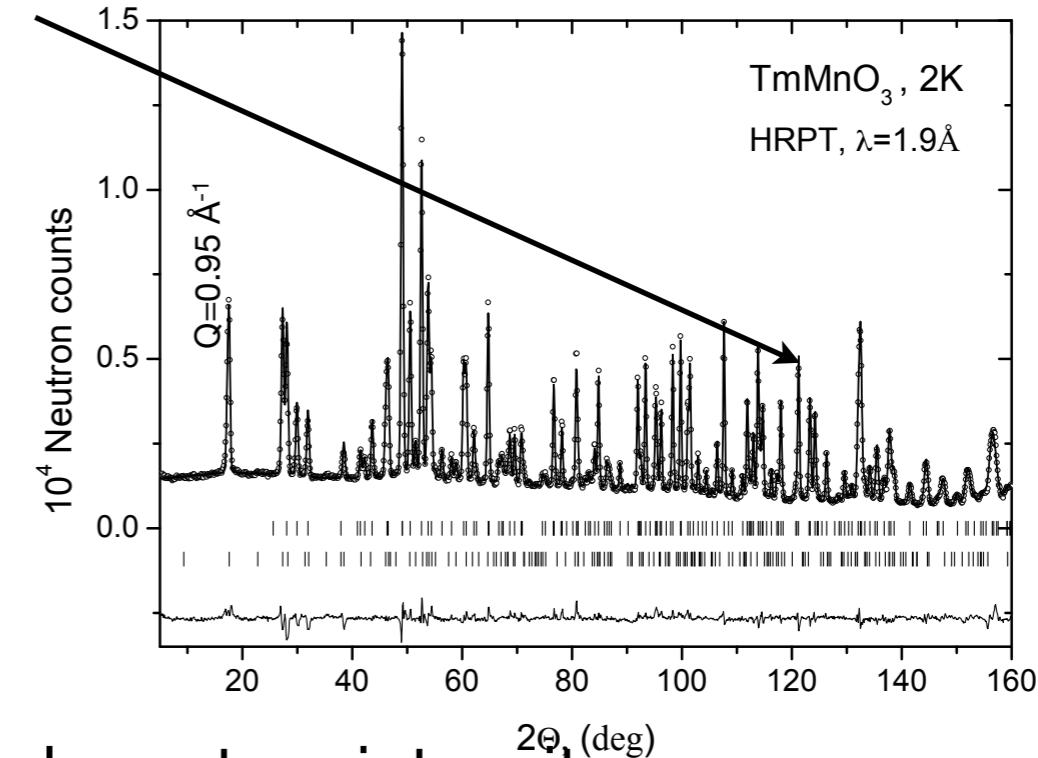


excellent resolution at low Q and high neutron intensity

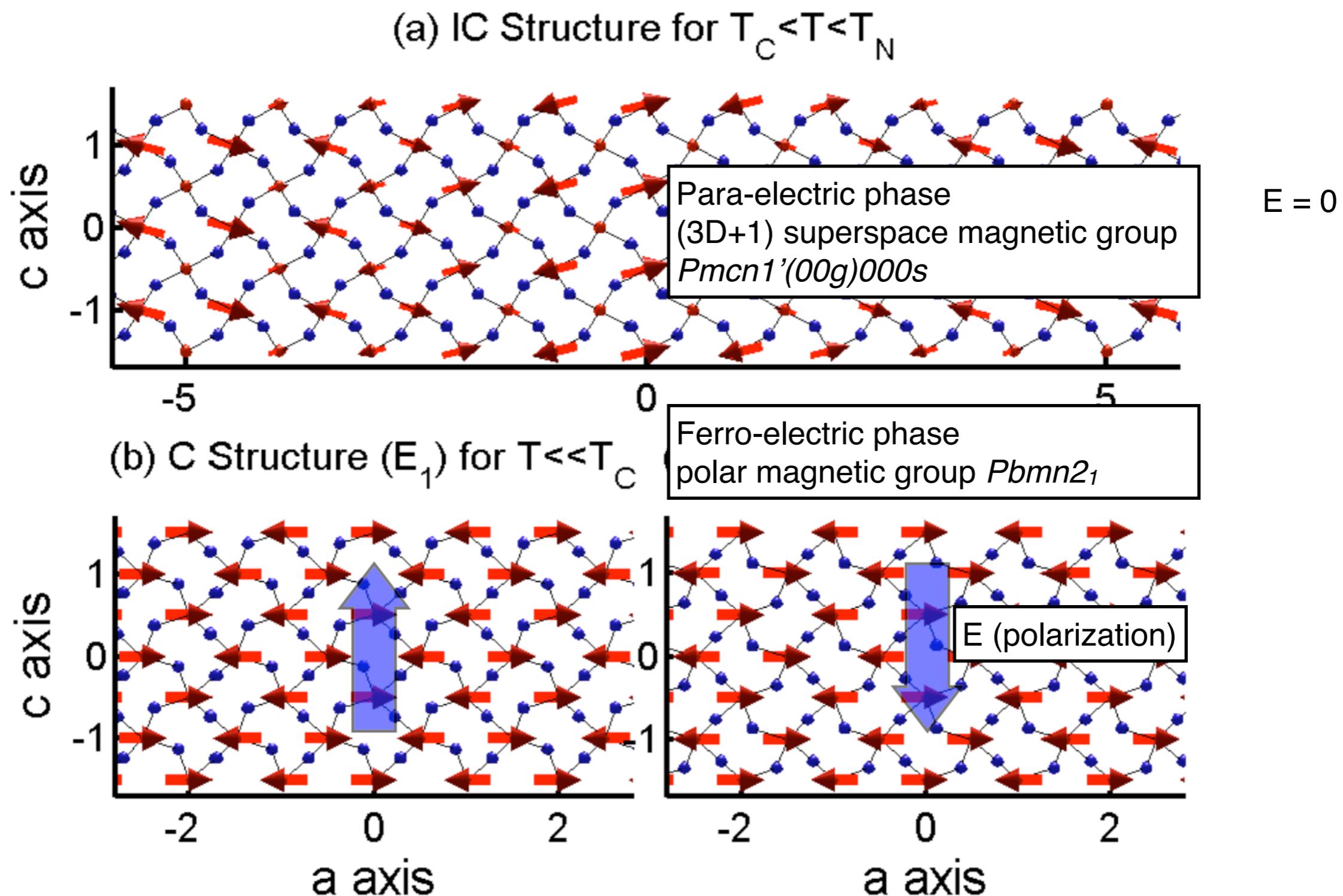


Complementarity 1.9Å HRPT and 4.5Å DMC

excellent resolution and high Q-range



Magnetic structure $TmMnO_3$

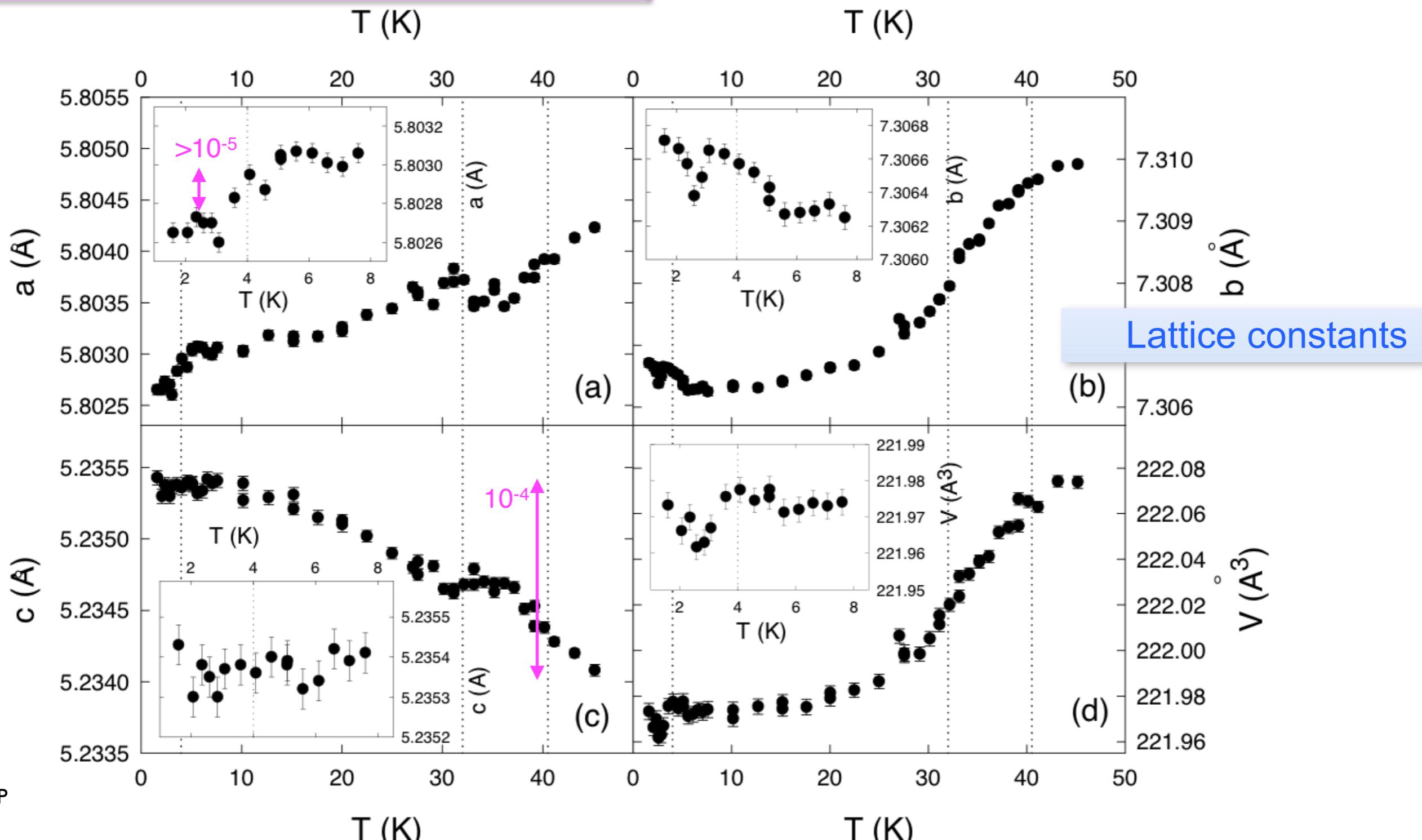


Example of accuracy on metric: orthorhombic **multiferroic** TmMnO_3

$\sim 0.0001 \text{\AA} = 10 \text{ fm}$ (proton radius 2fm)

TmMnO_3

material that have coupled electric,
magnetic and structural order



ECM-2016: August 28 – Sept. 1 European Conference on Crystallography

<http://ecm30.ecanews.org/>



Thank you