## **PSI Electrochemistry Resources**

## **Derivation of Expression for Concentration Overpotential**

We consider the generic electrochemical reaction

$$Ox + z \cdot e^- \rightarrow Red$$

The Nernst equation (for a half-cell reaction) states:

$$E = E^{\circ} + \frac{RT}{zF} \ln(\frac{a_{\rm ox}}{a_{\rm red}})$$
(1)

The reactant 'Ox' is characterized by its concentration c at the electrode surface. We consider now the Nernst potential of the electrode for case 1 when the concentration at the electrode corresponds to the concentration in the bulk  $c^{\infty}$ :

$$E_1 = E^\circ + \frac{RT}{zF} \ln(\frac{c^\circ / c_0}{a_{\rm red}})$$
<sup>(2)</sup>

where we have replaced the activity *a* by the concentration  $c / c_0$  ( $c_0 = 1 \text{ mol/L}$ ). In case 2, the concentration of the reactant 'Ox' at the surface of the electrode is  $c_{x=0}$ :

$$E_{2} = E^{\circ} + \frac{RT}{zF} \ln(\frac{c_{x=0} / c_{0}}{a_{\text{red}}})$$
(3)

The concentration overpotential  $\eta_c$  is given by the difference in equilibrium potential between the two cases 1 and 2:

$$\eta_{\rm c} = E_1 - E_2 = \frac{RT}{zF} \ln(\frac{c^{\infty}/c_0}{a_{\rm red}}) - \frac{RT}{zF} \ln(\frac{c_{x=0}/c_0}{a_{\rm red}}) = \frac{RT}{zF} \ln(\frac{c^{\infty}}{c_{x=0}}) = -\frac{RT}{zF} \ln(\frac{c_{x=0}}{c^{\infty}})$$
(4)

Rearrangement yields

$$\frac{c_{x=0}}{c^{\infty}} = \exp(-\frac{zF}{RT}\eta_{\rm c}) \tag{5}$$

From the lecture slides we note that the current of the reaction is given by

$$i = zFD(\frac{c^{\infty} - c_{x=0}}{\delta})$$
(6)

Inserting the expression for  $c_{x=0}$  from equation 5, we obtain:

$$i = zFD(\frac{c^{\infty}}{\delta} - \frac{c^{\infty}}{\delta} \cdot \exp(-\frac{zF}{RT}\eta_{c}))$$
(7)

The limiting current density is (cf. lecture slides)

$$i_{\rm lim} = zFD\frac{c^{\infty}}{\delta}$$
(8)

Hence, insertion of (8) in (7) yields

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$$i = i_{\rm lim} (1 - \exp(-\frac{zF}{RT}\eta_{\rm c})) \tag{9}$$

We solve for the concentration overpotential  $\eta_c$  and obtain:

$$\eta_{\rm c} = -\frac{RT}{zF} \cdot \ln(1 - \frac{i}{i_{\rm lim}}) \tag{10}$$

Since  $i < i_{\text{lim}}, \eta_c > 0$ .