



Research Proposal for an Experiment to Search for the Decay $\mu \rightarrow eee$

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EXECUTIVE SUMMARY

We propose an experiment (*Mu3e*) to search for the lepton flavour violating (LFV) decay $\mu^+ \rightarrow e^+e^-e^+$. We aim for an ultimate sensitivity of one in 10^{16} μ -decays, four orders of magnitude better than previous searches. This sensitivity is made possible by exploiting modern silicon pixel detectors providing high spatial resolution and hodoscopes using scintillating fibres and tiles providing precise timing information at high particle rates.

Existing beamlines available at PSI providing rates of order 10^8 muons per second allow to test for the decay $\mu^+ \rightarrow e^+e^-e^+$ in one of 10^{15} muon decays. In a first phase of the experiment, we plan to make use of this and establish the experimental technique whilst at the same time pushing the sensitivity by three orders of magnitude.

The installation of a new muon beamline at the spallation neutron source is currently under discussion at PSI. Such a *High Intensity Muon Beam* (HiMB) will provide intensities in excess of 10^9 muons per second, which in turn are required to reach the aimed sensitivity of $B(\mu^+ \rightarrow e^+e^-e^+) \sim 10^{-16}$.

The proposed experiment is highly complementary to other LFV searches for physics beyond the standard model, i.e. direct searches performed at the Large Hadron Collider (LHC) and indirect searches in the decay of taus and muons, such as the decay $\mu^+ \rightarrow e^+\gamma$, which is the subject of the *MEG* experiment currently in operation at PSI. The proposed experiment for the search $\mu^+ \rightarrow e^+e^-e^+$ will test lepton flavour violating models of physics beyond the Standard Model with unprecedented sensitivity.

This sensitivity is experimentally achieved by a novel experimental design exploiting silicon pixel detectors based on High Voltage Monolithic Act-

ive Pixel Sensors (HV-MAPS). This technology provides high granularity, important for precision tracking and vertexing, and allows one to significantly reduce the material budget by thinning down the sensors and by integrating the hit digitisation and readout circuitry in the sensor itself. The detector geometry is optimized to reach the highest possible momentum resolution in a multiple Coulomb scattering environment, which is needed to suppress the dominating background from the radiative muon decay with internal conversion, $\mu \rightarrow eee\nu$. The time information of the decay electrons¹, obtained from the pixel detector is further improved by a time-of-flight system consisting of a scintillating fiber hodoscope and tiles with Silicon Photo-Multipliers (SiPM) for light detection. By combining both detector systems accidental background can be reduced below the aimed sensitivity of $B(\mu^+ \rightarrow e^+e^-e^+) \sim 10^{-16}$.

We will complete the sensor development and start constructing the detector in 2013, in order to be ready for first exploratory data taking at an existing beam line with a first minimal detector setup in 2015. A detector capable of taking data rates of order 10^8 muons per second and capable of reaching a sensitivity of $B(\mu^+ \rightarrow e^+e^-e^+) \sim 10^{-15}$ will be available in 2016. This *Phase I* detector is the main focus of this proposal.

In *Phase II*, beyond 2017, the experiment will reach the ultimate sensitivity by exploiting a possible new high intensity muon beamline with an intensity of $> 2 \cdot 10^9$ muons per second. In the absence of a signal, LFV muon decays can then be excluded for $B(\mu^+ \rightarrow e^+e^-e^+) < 10^{-16}$ at 90% confidence level.

¹Here and in the following, the term “electron” denotes generically both decay electrons and positrons.

PART I



INTRODUCTION



MOTIVATION

In the Standard Model (SM) of elementary particle physics, the number of leptons of each family (lepton flavour) is conserved at tree level. In the neutrino sector, lepton flavour violation (LFV) has however been observed in the form of neutrino mixing by the Super-Kamiokande [1], SNO [2], KamLAND [3] and subsequent experiments. Consequently, lepton flavour is a broken symmetry, the standard model has to be adapted to incorporate massive neutrinos and lepton flavour violation is also expected in the charged lepton sector. The exact mechanism and size of LFV being unknown, its study is of large interest, as it is linked to neutrino mass generation, CP violation and new physics beyond the SM (BSM).

The non-observation of LFV of charged leptons in past and present experiments might at a first glance be surprising, as the mixing angles in the neutrino matrix have been measured to be large (maximal). This huge suppression of LFV effects is however accidental and due to the fact that (a) neutrinos are so much lighter than charged leptons and (b) the mass differences between neutrinos (more precisely the square of the mass differences) are very small compared to the W-boson mass.

The situation completely changes if new particles beyond the SM are introduced. If e.g. SUSY is realized at the electroweak scale, the scalar partners of the charged leptons (sleptons) will have large masses, and if not fully degenerate, induce LFV interactions via loop corrections. These LFV effects from new particles at the TeV scale are naturally generated in many models and are therefore considered to be a prominent signature for new physics.

In many extensions of the SM, such as grand unified models [4–6], supersymmetric models [7] (see Figure 2.2), left-right symmetric models [8–10], models with an extended Higgs sector [11] and models where electroweak symmetry is broken dynamically [12], an experimentally accessible amount of LFV is predicted in a large region of the parameter space.

Seesaw and Left-Right symmetric (supersymmetric) models are good candidates for realising grand unification, which also unify quark and lepton mass matrices. Moreover, it has been shown that LFV effects in the low energy limit can be related to mixing parameters at the GUT scale or to heavy Majorana masses in these models [17, 18]. Seesaw models are therefore very attractive in the context of LFV as they are also able to naturally explain the smallness of the masses of the left handed neutrinos. In this context the recent results from neutrino oscillation experiments are very interesting, as they measured a large mixing angle θ_{13} , which enhances the LFV-muon decays in most models which try to explain the small neutrino masses and the large mixing.

Currently the most accurate measurement is provided by the *Daya Bay* reactor neutrino experiment [19] yielding $\sin^2(2\theta_{13}) = 0.089 \pm 0.010(\text{stat}) \pm 0.005(\text{syst})$, excluding the no-oscillation hypothesis at 7.7 standard deviations. The *Daya Bay* measurement is in good agreement with measurements by the *RENO* [20], *Double Chooz* [21] and *T2K* [22] experiments. These results are very encouraging, as large values of $\sin^2(2\theta_{13})$ lead to large LFV effects in many BSM models.



DECAY CHANNEL	EXPERIMENT	BRANCHING RATIO LIMIT	REFERENCE
$\mu \rightarrow e\gamma$	<i>MEGA</i>	$< 1.2 \cdot 10^{-11}$	[13]
	<i>MEG</i>	$< 2.4 \cdot 10^{-12}$	[14]
$\mu \rightarrow eee$	<i>SINDRUM</i>	$< 1.0 \cdot 10^{-12}$	[15]
$\mu Au \rightarrow eAu$	<i>SINDRUM II</i>	$< 7 \cdot 10^{-13}$	[16]

Table 1.1: Experimental limits on LFV muon decays

The observation of LFV in the charged lepton sector would be a sign for new physics, possibly at scales far beyond the reach of direct observation at the large hadron collider (LHC). Several experiments have been performed or are in operation to search for LFV in the decays of muons or taus. Most prominent are the search for the radiative muon decay $\mu \rightarrow e\gamma$ [13, 14, 23, 24], the decay $\mu \rightarrow eee$ [15], the conversion of captured muons to electrons [16] and LFV tau decays [25–43].

The recent search performed by the *MEG*-Collaboration yields $B(\mu \rightarrow e\gamma) < 2.4 \cdot 10^{-12}$ [14] and sets currently the most stringent limit on many LFV models. The *MEG* collaboration plans to continue operation into 2013 in order to increase the number of stopped muons and to reach a sensitivity of a few times 10^{-13} . Plans to up-

grade the experiment to further improve the sensitivity are currently under discussion.

In the near future the *DeeMe* experiment [44] at J-PARC plans to improve the current muon-to-electron conversion limit of $B(\mu Au \rightarrow e Au) < 7 \cdot 10^{-13}$ [16] by almost two orders of magnitude. By the end of the decade this limit could be improved by even four orders of magnitude by *COMET* at J-PARC [45] and *Mu2e* at Fermilab [46, 47].

Selected limits for lepton flavour violating muon decays and muon-to-electron conversion experiments, which are of high relevance for the proposed experiment, are shown in Table 1.1. A search for the LFV decay $\mu \rightarrow eee$ with an unprecedented sensitivity of $< 10^{-16}$ as proposed here would provide a unique opportunity for discoveries of physics beyond the SM in the coming years.



THEORY

In the SM, charged lepton flavour violating reactions are forbidden at tree level and can only be induced by lepton mixing through higher order loop diagrams. However, the dominant neutrino mixing loop diagram, see Figure 2.1, is strongly suppressed in the SM with $B \ll 10^{-50}$ and thus giving potentially high sensitivity to LFV reactions in models beyond the Standard Model (BSM).

Such an example is shown in Figure 2.2, where a γ/Z -penguin diagram is shown with new supersymmetric (SUSY) particles running in a loop. These loop contributions are important basically for all models, where new particle couplings to electrons and muons are introduced. Lepton flavor violation can also be mediated by tree couplings as shown in Figure 2.3. These couplings could be mediated by new particles, like Higgs particles or doubly charged Higgs particles, R-parity violating scalar neutrinos or new heavy vector bosons, the latter being motivated by models with extra dimensions [48, 49]. These models usually

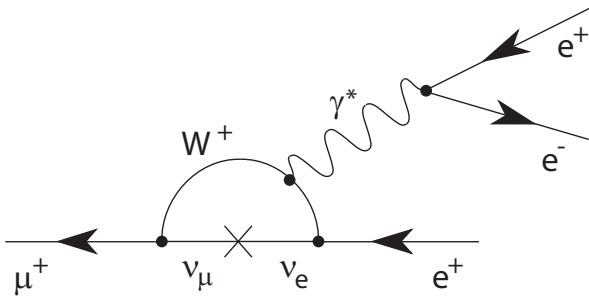


Figure 2.1: Feynman diagram for the $\mu \rightarrow eee$ process via neutrino mixing (indicated by the cross).

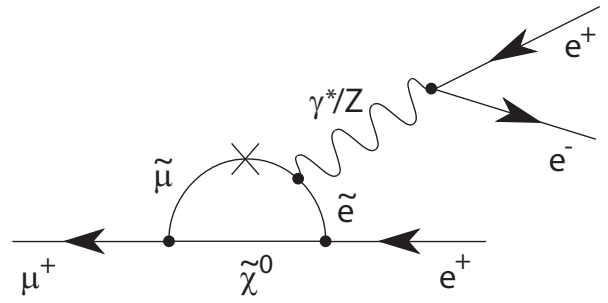


Figure 2.2: Diagram for lepton flavour violation involving supersymmetric particles.

also predict semihadronic decays of tau leptons or the muon conversion process $\mu q \rightarrow e q'$, which is experimentally best tested in muon capture experiments.

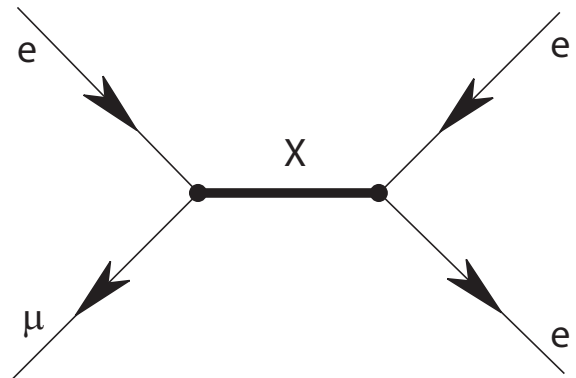


Figure 2.3: Diagram for lepton flavour violation at tree level.



The lepton flavor violating three electron decay of the muon can be mediated, depending on the model, via virtual loop (Figure 2.2) and box diagrams or via tree diagrams (Figure 2.3). The most general Lagrangian for this decay can be parameterized as [50]¹:

$$\begin{aligned}
 L_{\mu \rightarrow eee} = & \frac{4G_F}{2} [m_\mu A_R \overline{\mu}_R \sigma^{\mu\nu} e_L F_{\mu\nu} \\
 & + m_\mu A_L \overline{\mu}_L \sigma^{\mu\nu} e_R F_{\mu\nu} \\
 & + g_1 (\overline{\mu}_R e_L) (\overline{e}_R e_L) \\
 & + g_2 (\overline{\mu}_L e_R) (\overline{e}_L e_R) \\
 & + g_3 (\overline{\mu}_R \gamma^\mu e_R) (\overline{e}_R \gamma_\mu e_R) \\
 & + g_4 (\overline{\mu}_L \gamma^\mu e_L) (\overline{e}_L \gamma_\mu e_L) \\
 & + g_5 (\overline{\mu}_R \gamma^\mu e_R) (\overline{e}_L \gamma_\mu e_L) \\
 & + g_6 (\overline{\mu}_L \gamma^\mu e_L) (\overline{e}_R \gamma_\mu e_R) + H.c.] \quad (2.1)
 \end{aligned}$$

The form factors $A_{R,L}$ describe tensor type (dipole) couplings, mostly acquiring contributions from the photon penguin diagram, whereas the scalar-type ($g_{1,2}$) and vector-type ($g_3 - g_6$) form factors can be regarded as four fermion contact interactions, to which the tree diagram contributes in leading order. In addition also off shell form factors from the penguin diagrams, which are not testable in the $\mu \rightarrow e\gamma$ decay contribute to $g_1 - g_6$ [51]. In case of non-zero dipole and four-fermion couplings also interference effects have to be considered, which can be exploited to investigate violation of time reversal (T -invariance).

By neglecting higher order terms in m_e , the total branching ratio of the decay can be expressed by:

$$\begin{aligned}
 B(\mu \rightarrow eee) = & \frac{g_1^2 + g_2^2}{8} + 2(g_3^2 + g_4^2) + g_5^2 + g_6^2 \\
 & + 32 e A^2 \left(\ln \frac{m_\mu^2}{m_e^2} - 11/4 \right) \\
 & + 16 \eta e A \sqrt{g_3^2 + g_4^2} \\
 & + 8 \eta' e A \sqrt{g_5^2 + g_6^2} \quad , \quad (2.2)
 \end{aligned}$$

where the definition $A^2 = A_L^2 + A_R^2$ is used. The term proportional to A^2 is logarithmically enhanced and can be assigned to the photon penguin

¹A representation of Lagrangian containing explicitly the contributions from the loop and box diagrams can be found in [51].

diagram. The constants η and η' are T -violating mixing parameters. In case of a signal, the different terms can be measured from the angular distribution of $\mu \rightarrow eee$ decay particles using a polarized muon beam.

2.1 Comparison $\mu \rightarrow eee$ versus $\mu \rightarrow e\gamma$

In the decay $\mu \rightarrow e\gamma$ physics beyond the SM is only tested by photon penguin diagrams, in contrast to $\mu \rightarrow eee$ where also tree, Z -penguin and box diagrams contribute. To compare the new physics mass scale reach between the processes $\mu \rightarrow eee$ and $\mu \rightarrow e\gamma$ a simplified model is chosen; it is assumed that the photon penguin diagram Figure 2.2 and the tree diagram Figure 2.3 are the only relevant contributions. The Lagrangian then simplifies to²:

$$\begin{aligned}
 L_{LFV} = & \left[\frac{m_\mu}{(\kappa + 1)\Lambda^2} \overline{\mu}_R \sigma^{\mu\nu} e_L F_{\mu\nu} \right]_{\gamma\text{-penguin}} \\
 & + \left[\frac{\kappa}{(\kappa + 1)\Lambda^2} (\overline{\mu}_L \gamma^\mu e_L) (\overline{e}_L \gamma_\mu e_L) \right]_{\text{tree}} \quad (2.3)
 \end{aligned}$$

where for the contact interaction (“tree”) term exemplarily a left-left vector coupling is chosen. In this definition a common mass scale Λ is introduced and the parameter κ describes the ratio of the amplitudes of the vector-type (tree) term over the tensor (γ -penguin) term.

Limits on the common mass scale Λ as obtained from the experimental bounds on $B(\mu \rightarrow e\gamma) < 2.4 \cdot 10^{-12}$ (90% CL *MEG* 2011) and $B(\mu \rightarrow eee) < 1.0 \cdot 10^{-12}$ (90% CL *SINDRUM*) are shown in Figure 2.4 as function of the parameter κ . Experimentally, for small values of κ (dipole coupling) the mass scale Λ is best constrained by the *MEG* experiment whereas the four fermion contact interaction region with $\kappa \gtrsim 10$ is best constrained by the *SINDRUM* experiment.

For comparison also a hypothetical ten times improved limit is shown for the *MEG* experiment (post-upgrade) and compared to the sensitivities of the proposed $\mu \rightarrow eee$ experiment of 10^{-15} (phase I) and 10^{-16} (phase II). It can be seen that in this simple model comparison high mass scales Λ will be best constrained by the proposed

²A similar study was presented in [52]

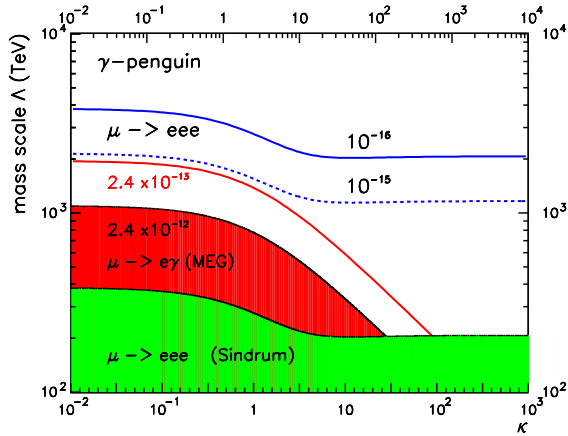


Figure 2.4: Experimental limits and projected limits on the LFV mass scale Λ as a function of the parameter κ (see equation 2.3) assuming negligible contributions from Z^0 penguins; based on [52].

$\mu \rightarrow eee$ experiment for all values of κ already in phase I.

In case of dominating tensor couplings ($A \neq 0$, $\kappa \rightarrow 0$) a quasi model independent relation between the $\mu \rightarrow eee$ decay rate and the $\mu \rightarrow e\gamma$ decay rate can be derived:

$$\frac{B(\mu \rightarrow eee)}{B(\mu \rightarrow e\gamma)} \approx 0.006 \quad (2.4)$$

This ratio applies for many supersymmetric models, where LFV effects are predominantly mediated by gauge bosons and where the masses of the scalar leptons or gauginos are of electroweak scale. In these models, which are already heavily constrained or even excluded by the recent LHC results, the sensitivity of the proposed *Mu3e* experiment in terms of branching ratio has to be two orders of magnitude higher than that of the *MEG* experiment in order to be competitive.

2.1.1 Z-PENQUIN CONTRIBUTION

However, besides the tree and γ -penguin diagrams also the Z -penguin diagram can significantly contribute to the process $\mu \rightarrow eee$. The Z -penguin diagram is of particular importance if the new physics scale is higher than the electromagnetic scale, as can be easily derived from a dimensional analysis. The enhancement of the Z -penguin contribution over the γ -penguin contribution and its non-decoupling behaviour when

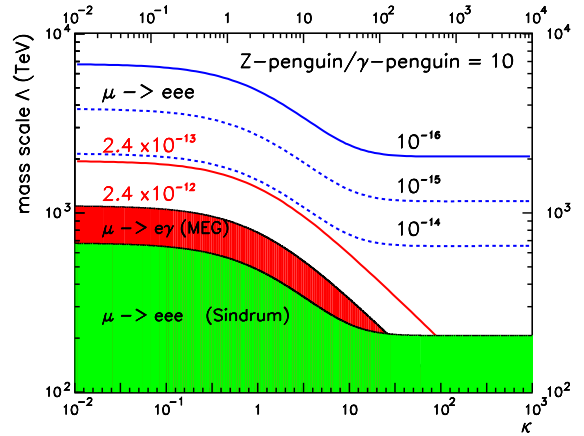


Figure 2.5: Experimental limits and projected limits on the LFV mass scale Λ as a function of the parameter κ (see equation 2.3) assuming contributions from Z^0 penguins ten times larger than the photon contribution.

going to high mass scales was discussed for Little Higgs models [53, 54] as well as for several SUSY models [55–59]. SUSY models with R -parity violation and right handed neutrinos received recently quite some attention in this context, as approximate cancellations of different Z -diagram contributions are not present in extended Minimum Supersymmetric Standard Models (MSSM).

The effect of such an enhanced Z -penguin coupling, where the LFV contribution to the $\mu \rightarrow eee$ process is exemplarily enhanced by a factor of ten relative to the photon-penguin contribution, is shown in Figure 2.5. It can be seen that the sensitivity of the $\mu \rightarrow eee$ process to new physics is significantly enhanced at small values of κ and that in such a case a sensitivity of 10^{-14} is already sufficient to be competitive with the $\mu \rightarrow e\gamma$ process with a sensitivity of a few times 10^{-13} .

2.2 Discussion of Specific Models

In the following, selected models are discussed in more detail in the context of the proposed experiment.

2.2.1 INVERSE SEESAW SUSY MODEL

Despite the fact that the most simple supersymmetric models with light squarks and gluinos were

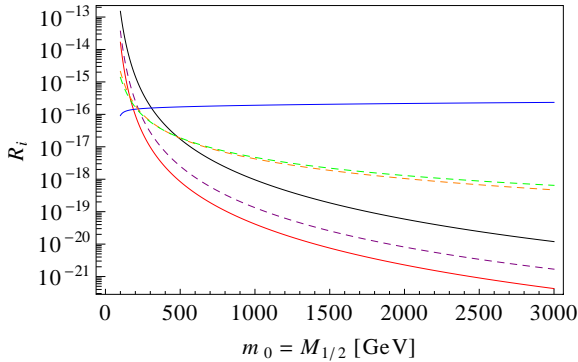


Figure 2.6: Inverse Seesaw SUSY Model: Contributions to $B(\mu \rightarrow eee)$ as a function of $m_0 = M_{1/2}$ for a degenerate singlet spectrum with $\hat{M}_R = 10$ TeV and $M = 10^{11}$ GeV. The rest of the cMSSM parameters are set to $A_0 = -300$ GeV, $B_0 = 0$, $\tan \beta = 10$ and $\text{sign}(\mu) = +$. Solid lines represent individual contributions, γ (black), Z (blue) and h (red) whereas the dashed lines represent interference terms, $\gamma - Z$ (green), $\gamma - h$ (purple) and $Z - h$ (orange). Note that in this case h includes both Higgs and box contributions. Taken from [58].

recently excluded by LHC experiments [60–84] supersymmetry can still exist in nature, just at higher mass scales or in more complex realisations. In many of these realisations with a non-minimal particle content the Z -penguin contribution discussed above gets significantly enhanced.

As a first example results obtained by a supersymmetric model with an inverse seesaw mechanism [58] are discussed here. The inverse seesaw model [85] constitutes a very appealing alternative to the standard seesaw realization and can be embedded in a minimal extension of the MSSM by the addition of two extra gauge singlet superfields, with opposite lepton numbers. Similar to other models, e.g. flavour violating Higgs decays in the MSSM, the Z -penguin exhibits here a non-decoupling behaviour, which is shown in Figure 2.6 for an effective right-handed neutrino mass of $M = 10^{11}$ GeV and degenerate sterile neutrino masses of $\hat{M}_R = 10$ TeV. At small mass scales $m_0 = M_{1/2}$ of the constrained MSSM (cMSSM) the photon-mediated penguin contribution clearly dominates over the other contributions from Higgs-mediated penguin and Z -mediated penguin diagrams. This picture completely changes at higher mass scales above 200-

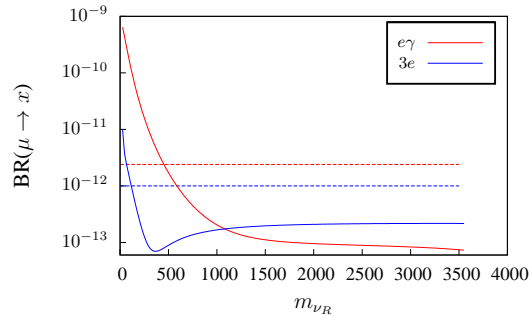


Figure 2.7: Supersymmetric $SU(3)_c \times SU(2)_L \times U(1)_{B-L} \times U(1)_R$ Model: Branching ratios of lepton flavour violating processes as a function of m_{ν_R} for $m_0 = 800$ GeV, $M_{1/2} = 1200$ GeV, $\tan \beta = 10$, $A_0 = 0$, $v_R = 10$ TeV, $\tan \beta_R = 1.05$, $\mu_R = -500$ GeV, $m_{A_R} = 1000$ GeV. The dashed red line is the predicted branching ratio for $\mu \rightarrow e\gamma$ and the dashed blue line for $\mu \rightarrow eee$. Taken from [59].

300 GeV, where the Z -mediated penguin diagram becomes dominant. The non-decoupling behaviour of the Z -penguin is clearly visible which will allow to test this model at any SUSY mass scale for the seesaw parameters given in this example at phase II of the proposed experiment.

2.2.2 SUPERSYMMETRIC $SU(3)_c \times SU(2)_L \times U(1)_{B-L} \times U(1)_R$ MODEL

This model represents a supersymmetric version of the SM, minimally extended by additional $U(1)_{B-L} \times U(1)_R$ symmetry groups [86,87]. This model includes the generation of light neutrino masses by the seesaw mechanism, can explain the observed large neutrino mixing angles and can be easily embedded into a $SO(10)$ grand unified theory. This model predicts an additional light Higgs particle, which is expected to mix with the lightest MSSM Higgs particle, and has been recently studied also in the context of LFV processes [59]. Also in this study it is found that at high SUSY mass scales the photon-mediated LFV penguin diagrams are more suppressed than the Z -mediated LFV penguin diagrams and that this suppression scales with m_Z^4/m_{SUSY}^4 as naively expected from a dimensional analysis. Branching ratio predictions for the processes $\mu \rightarrow eee$ and $\mu \rightarrow e\gamma$ are shown in Figure 2.7 as function of the right-handed neutrino mass m_{ν_R} for



the SUSY model parameters as given in the figure caption. Also here it can be seen that for high masses $m_{\nu_R} > 300$ GeV the Z -mediated penguin diagram starts to contribute dominantly to the $\mu \rightarrow eee$ process and that for $m_{\nu_R} > 1000$ GeV the $\mu \rightarrow eee$ process is expected to have an even higher branching fraction than $\mu \rightarrow e\gamma$. For even higher masses the non-decoupling behaviour is visible in the $\mu \rightarrow eee$ prediction.

2.2.3 OTHER MODELS

The above discussed enhancement of the Z -mediated penguin diagram appears also in Little Higgs Models with T-parity (LHT) where ratios $B(\mu \rightarrow eee)/B(\mu \rightarrow e\gamma) \approx 0.02 - 1$ have been predicted [53, 54, 88, 89], or in Left-Right Symmetric models with additional Higgs triplets. LFV interactions in Higgs-triplet models can be also generated directly in tree diagrams, see Figure 2.3.

In [11], these LFV violating effects are studied in a model where the Higgs triplet is responsible for neutrino mass generation. Figure 2.8 shows the predicted branching ratios for each of the three LFV muon processes and for different realisations of the neutrino mass hierarchy. Note that the absolute value of the branching ratios depends on the mass scale M and can vary. For the hierarchical case, Figure 2.8 b), all branching ratios are expected to be of similar size whereas for the degenerate, Figure 2.8 a), and the inverted case, Figure 2.8 c), the $\mu \rightarrow eee$ branching ratio dominates in the allowed region of U_{e3} . As the LFV-mediating Higgs triplet boson does not couple to quarks, the $\mu \rightarrow eee$ decay is enhanced compared to the $\mu \rightarrow e\gamma$ decay and the muon-to-electron conversion processes, which are both loop suppressed.

This enhancement of the LFV tree diagram is also found to be large in extra dimension models [48, 90] or models with new heavy Z bosons. In Randall-Sundrum (RS) models [48], flavor changing neutral currents (FCNCs) arise already at the tree level. This is caused by the flavor-dependent couplings of these gauge bosons, due to their non-trivial profiles in the extra dimension. Moreover, FCNCs arise through the exchange of the Higgs boson, as due to the contribution to the fermion masses from compactification, there is a misalignment between the masses and the Yukawa couplings.

Electroweak precision observables suggest that for RS models featuring the Standard Model gauge group, the new-physics mass scale M_{KK} (the scale of the Kaluza Klein excitations) should not be lower than $\mathcal{O}(10 \text{ TeV})$ at 99% CL [91–93]. Thus, without additional structure/symmetries, the experimental situation suggests that it could be challenging to find direct signals from RS models at the LHC. In such a situation, precision experiments, like the measurement of the decay $\mu \rightarrow eee$, will furnish the only possibility to see the impact of warped extra dimensions.

2.3 Theory Summary

The search for the decay $\mu \rightarrow eee$ is in itself of fundamental interest and might reveal surprises not foreseen by any of the models discussed above. This search is largely complementary to other LFV searches, in particular to the decay $\mu \rightarrow e\gamma$ and to the $\mu \rightarrow e$ conversion in muon capture experiments. In a wide range of models for physics beyond the standard model, highest sensitivity in terms of branching ratio is expected for the $\mu \rightarrow eee$ decay process.

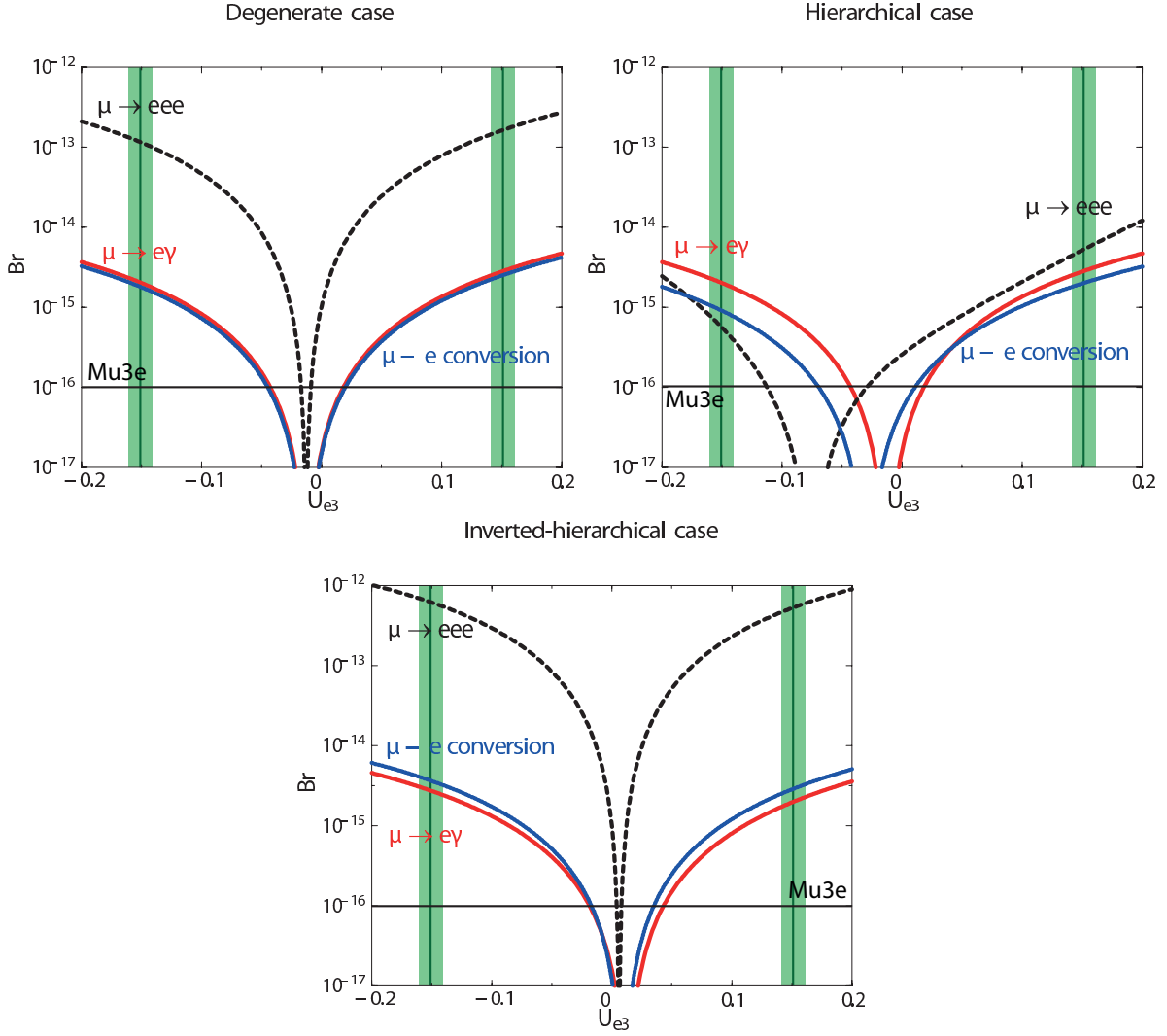


Figure 2.8: Branching ratios of $B(\mu \rightarrow eee)$, $B(\mu \rightarrow e\gamma)$ and muon conversion $B(\mu \rightarrow e)$ in different Higgs triplet scenarios with a degenerated, hierarchical or inverted mass hierarchy of the neutrinos as function of the neutrino mixing matrix element U_{e3} and for the model parameters: $M = 200$ GeV, $A = 25$ eV, and $m_\nu = 0.1$ eV for the degenerate case. These plots were taken from [11] and the U_{e3} constraints (green bands) as obtained from [19] were added posterior.



EXPERIMENTAL SITUATION

3.1 *SINDRUM* Experiment

The *SINDRUM* experiment was in operation at PSI from 1983-86 to search for the process $\mu \rightarrow eee$. No signal was found and the limit $B(\mu \rightarrow eee) < 10^{-12}$ was set at 90% CL [15], assuming a decay model with a constant matrix element.

The main components of the experiment were a hollow double-cone shaped target of dimension $58 \times 220 \text{ mm}^2$ to stop surface muons of 28 MeV/c in a solenoidal magnetic field of 0.33 T, five layers of multiwire proportional chambers and a trigger hodoscope. The main tracking parameters which were most relevant for the search sensitivity of the experiment are shown in Table 3.1.

The time resolution obtained by the hodoscope of less than 1 ns was, together with the achieved momentum resolution, sufficient to suppress the accidental background completely.

After all selection cuts, no candidate event was seen by the *SINDRUM* experiment. The sensitivity of the experiment was mainly determined by the $\mu \rightarrow eee\nu\nu$ background process and estimated as $5 \cdot 10^{-14}$ [94]; the obtained limit was basically given by the limited number of muon stops.

3.2 *MEG* Experiment

The *MEG* experiment at PSI is in operation since 2008 and is searching for the LFV decay $\mu \rightarrow e\gamma$. The main components used for event reconstruction are drift chambers for positron detection and a liquid xenon calorimeter for photon detection.

In the first running period in the year 2008 about 10^{14} muons were stopped on target [24]. No signal was found and a limit on the decay of $B(\mu \rightarrow e\gamma) < 2.8 \cdot 10^{-11}$ (90% C.L.) was set.

After upgrading the detector the search sensitivity and the limit was improved using data taken in the years 2009/2010 to $B(\mu \rightarrow e\gamma) < 2.4 \cdot 10^{-12}$ (90% C.L.) [14].

The dominant background contribution for $\mu \rightarrow e\gamma$ comes from accidentals where a high energy photon from a radiative muon decay or from a bremsstrahlung process is recorded, overlaid with a positron from the upper edge of the Michel spectrum. This accidental background mainly determines the final sensitivity of the experiment.

The amount of background is predominantly determined by the timing, tracking and energy resolution. Selected resolution parameters as achieved in the 2009 run are summarized in Table 3.2. The *MEG* experiment will continue operation until middle of 2013. The final sensitivity is expected to be a few times 10^{-13} . The collaboration has started to discuss possible upgrades to further improve the sensitivity by about one order of magnitude. These numbers are to be compared to the bound from the earlier *MEGA* experiment of $B(\mu \rightarrow e\gamma) < 1.2 \cdot 10^{-11}$ [13].

The study of the $\mu \rightarrow e\gamma$ decay sets stringent bounds on models predicting new heavy particles mediating LFV dipole couplings. These dipole couplings can also be tested in the process $\mu \rightarrow eee$, where the sensitivity is reduced by a factor of $\frac{\alpha}{3\pi}(\ln(m_\mu^2/m_e^2) - 11/4) = 0.006$ (note however that for $\mu \rightarrow eee$ also box diagrams, Z^0 -mediated penguin diagrams and tree diagrams contribute as



SINDRUM PARAMETER	VALUE
rel. momentum resolution σ_p/p	5.1 % ($p = 50 \text{ MeV}/c$)
rel. momentum resolution σ_p/p	3.6 % ($p = 20 \text{ MeV}/c$)
polar angle σ_θ	28 mrad ($p = 20 \text{ MeV}/c$)
vertex resolution σ_{dca}	$\approx 1 \text{ mm}$
MWPC layer radiation length in X_0	0.08 % - 0.17 %

 Table 3.1: *SINDRUM* tracking parameters taken from [15].

described in chapter 2). In the case that the LFV dipole couplings are dominant, the projected sensitivity of 10^{-13} of the *MEG* experiment corresponds accordingly to a sensitivity of about 10^{-15} in the search for the $\mu \rightarrow eee$ decay and the envisaged sensitivity of $B(\mu \rightarrow eee) = 10^{-16}$ corresponds to more than one order of magnitude higher sensitivity compared to the *MEG* experiment.

3.3 Muon Conversion Experiments

Muon to electron conversion experiments $\mu \rightarrow e$ on nuclei exploit the clear signature of monochromatic electrons. Differently to the search for LFV muon decays, which are performed using DC anti-muon beams in order to reduce accidental backgrounds, muon conversion experiments are performed using pulsed muon beams to reduce the rapidly decaying pion background. A limitation of this type of experiment is the background from ordinary decays of captured muons with large nuclear recoil and from pions.

The most stringent limits for muon-electron conversion on various nuclei have been obtained by the *SINDRUM II* collaboration [16,97,98]. The

<i>MEG</i> PARAMETER 2011 PUBL.	VALUE
rel. momentum resolution σ_p/p	0.7 % (core)
polar angle σ_θ	9 mrad
azimuthal angle σ_ϕ	7 mrad
radial vertex resolution σ_R	1.1 mm
long. vertex resolution : σ_Z	1.5 mm

 Table 3.2: Best *MEG* tracking parameter resolutions achieved in the year 2009/2010. The resolutions are given for positrons of 53 MeV/c momentum. Values taken from [14].

strongest limit has been set using a gold target $B(\mu \text{ Au} \rightarrow e \text{ Au}) < 7 \cdot 10^{-13}$ [16].

Similar to the $\mu \rightarrow eee$ process, the sensitivity to dipole couplings in muon conversion is reduced by about α_{em} compared to the more direct $\mu \rightarrow e\gamma$ search. However, new experiments planned at Fermilab (*Mu2e* [46,99,100]) and at J-PARC (*COMET* [45,101,102] and *PRISM* [103,104]) aim for branching ratios of 10^{-16} or smaller relative to the captured muon decay and have a higher sensitivity to LFV dipole couplings than the running *MEG* experiment. Similar to the $\mu \rightarrow eee$ process, also four-fermion couplings are tested in $\mu \rightarrow e$ conversion experiments. These couplings involve light quarks and are thus complementary to all other LFV search experiments.

The *Mu2e* and *COMET* experiments are ambitious projects and are expected to come into operation at earliest by the end of this decade. In a few years time the *DeeMe* experiment at J-PARC [44] will start taking data, aiming for a sensitivity for muon-to-electron conversions of 10^{-14} .

At Osaka university, the *MuSIC* project [105, 106] aims for a very high intensity DC muon beam using a high-field capture solenoid around a thick conversion target. One of many possible users of that beam is a $\mu \rightarrow eee$ experiment. However, an experimental concept has not yet been presented.

3.4 LFV in τ Decays

A wide variety of LFV decay channels are open in τ decays. These decay modes have been extensively explored at the *B*-factories, producing limits on branching ratios of a few 10^{-8} , see Table 3.3 and Figure 3.1. The next generation of *B* experiments at e^+e^- colliders could push these limits down by one to two orders of magnitude. For certain channels such as $\tau \rightarrow \mu\mu\mu$, the LHCb exper-

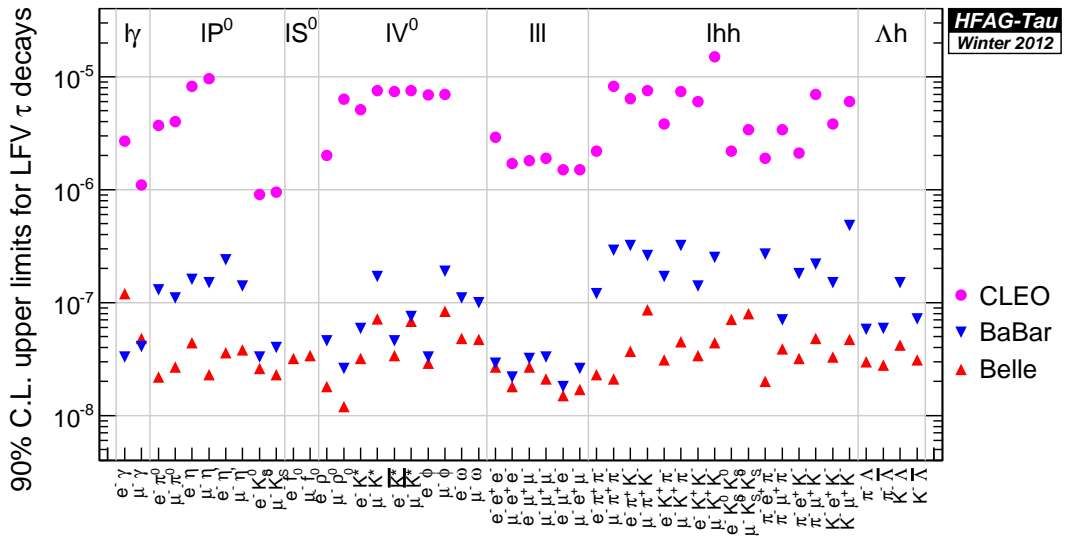


Figure 3.1: Limits on LFV τ decays. Taken from [95]

iment could also be competitive given the luminosity expected in the coming years [107, 108].

3.5 LFV at the Large Hadron Collider

LFV signatures might be observed at the LHC if e.g. supersymmetric particles are discovered, which naturally generate LFV couplings in slepton mass mixing. Consequently, if sleptons are light enough to be produced in pairs, different lepton flavors might show up in decay chains such as: $\tilde{\ell}^+ \tilde{\ell}^- \rightarrow \ell^+ \ell'^- \chi^0 \chi^0$.

Known and new scalar or vector particles could also have lepton violating tree couplings and might be directly reconstructed from resonance peaks: $H \rightarrow \ell \ell'$ or $Z' \rightarrow \ell \ell'$. Due to the existing bounds on flavor changing processes, these LFV decays are small and difficult to detect above

the large background from WW -production with subsequent leptonic decays. It seems however, that with high enough luminosities, the LHC can e.g. go beyond the LEP bounds [109–112] on LFV Z decays [113].

If new particles exist at the TeV mass scale, i.e. in the discovery reach of the LHC, it is very likely that precision experiments will discover lepton flavor violation via radiative loops. Dedicated LFV search experiments like the proposed $\mu \rightarrow eee$ experiment would then allow one to measure the LFV couplings of the new particles, complementary to the TeV scale experiments at the LHC.

Conversely, in the case that no new physics (excluding the SM Higgs boson [114, 115]) were discovered at the LHC, the discovery of LFV in precision experiments is not excluded as e.g. rare muon decays are testing the mass scale > 1 PeV, three orders of magnitude higher than at LHC.



DECAY CHANNEL	BELLE LIMIT	BABAR LIMIT	BELLE II PROJ. (5 ab ⁻¹)	BELLE II PROJ. (50 ab ⁻¹)	SUPERB PROJ. ¹ (75 ab ⁻¹)
$\tau \rightarrow \mu\gamma$	$4.5 \cdot 10^{-8}$ [26]	$4.4 \cdot 10^{-8}$ [27]	$10 \cdot 10^{-9}$ [42, 43]	$3 \cdot 10^{-9}$ [42, 43]	$1.8 \cdot 10^{-9}$ [96]
$\tau \rightarrow e\gamma$	$12 \cdot 10^{-8}$ [26]	$3.3 \cdot 10^{-8}$ [27]			$2.3 \cdot 10^{-9}$ [96]
$\tau \rightarrow \mu\mu\mu$	$2.1 \cdot 10^{-8}$ [34]	$3.3 \cdot 10^{-8}$ [28]	$3 \cdot 10^{-9}$ [42, 43]	$1 \cdot 10^{-9}$ [42, 43]	$2 \cdot 10^{-10}$ [96]
$\tau \rightarrow eee$	$2.7 \cdot 10^{-8}$ [34]	$2.9 \cdot 10^{-8}$ [28]			$2 \cdot 10^{-10}$ [96]
$\tau \rightarrow \mu\eta$	$2.3 \cdot 10^{-8}$ [25]	$15 \cdot 10^{-8}$ [33]	$5 \cdot 10^{-9}$ [42, 43]	$2 \cdot 10^{-9}$ [42, 43]	$4 \cdot 10^{-10}$ [96]
$\tau \rightarrow e\eta$	$4.4 \cdot 10^{-8}$ [25]	$16 \cdot 10^{-8}$ [33]			$6 \cdot 10^{-10}$ [96]
$\tau \rightarrow \mu K_S^0$	$2.3 \cdot 10^{-8}$ [35]	$4.0 \cdot 10^{-8}$ [31]			$2 \cdot 10^{-10}$ [96]
$\tau \rightarrow e K_S^0$	$2.6 \cdot 10^{-8}$ [35]	$3.3 \cdot 10^{-8}$ [31]			$2 \cdot 10^{-10}$ [96]

Table 3.3: Measured and projected limits on selected lepton flavour violating τ decays (90% *C.L.*).

¹ The SuperB projections assumed a polarized electron beam; they also assumed that all backgrounds except initial state radiation can be suppressed to the desired level. The SuperB project was canceled in November 2012.



THE DECAY $\mu \rightarrow eee$

4.1 Kinematics

The decay $\mu \rightarrow eee$ proceeds promptly. For discriminating signal and background, energy and momentum conservation can be exploited. The vectorial sum of all decay particle momenta should vanish:

$$|\vec{p}_{tot}| = \left| \sum \vec{p}_i \right| = 0 \quad (4.1)$$

and the total energy has to be equal to the muon mass.

The energies of the decay electrons (positrons) are in the range (0 – 53) MeV. All decay particles must lie in a plane and the decay is described by two independent variables in addition to three global rotation angles, which describe the orientation in space.

4.2 Detector Acceptance

The acceptance of the proposed $\mu \rightarrow eee$ experiment is determined by its geometrical acceptance and energy coverage. For various coupling assumptions about the LFV amplitude, see also equation 2.1, the energy spectrum of the highest energy, E_1 , and lowest energy decay particles, E_{min}^e , are shown in Figures 4.1 and 4.2, respectively. In order to achieve a high acceptance, the detector must be able to reconstruct tracks with momenta ranging from half the muon mass down to a few MeV with large solid angle coverage. The proposed experiment should cover the energy range > 10 MeV to provide acceptances of 50 % or more for all models.

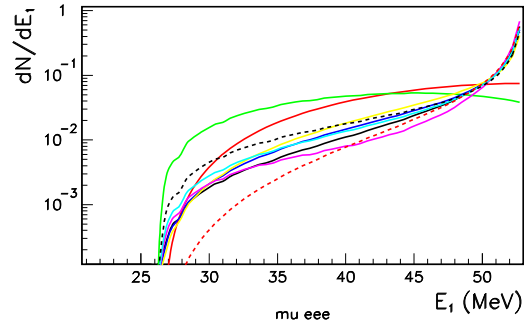


Figure 4.1: Energy distribution of the highest energy positron in the decay $\mu^+ \rightarrow e^+e^-e^+$ for different effective LFV models. The solid red and the green lines correspond to pure four-fermion contact interaction models (no penguin) contribution.

4.3 Backgrounds

The final sensitivity of the proposed experiment depends on the ability to reduce backgrounds from various sources. Two categories of backgrounds are considered; irreducible backgrounds, such as $\mu^+ \rightarrow e^+e^+e^-\nu\bar{\nu}$, which strongly depend on the granularity and resolution of the detector, and accidental backgrounds that scale linearly or with the square of the beam intensity.

In the following sections, the main background sources considered are discussed.

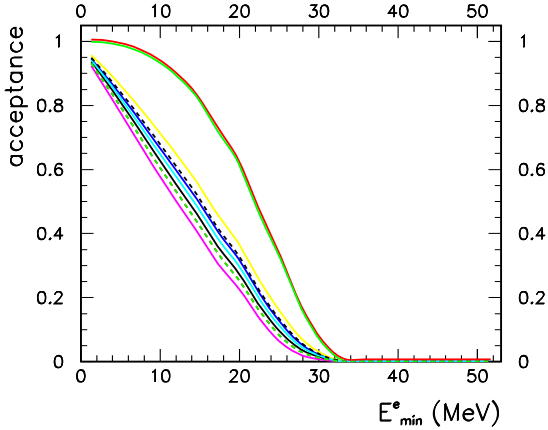


Figure 4.2: Acceptance of the lowest energy decay electron (positron) for different effective LFV models as function of the minimum transverse momentum. The solid red and green lines correspond to pure four-fermion contact interaction models (no penguin) contribution.

4.3.1 INTERNAL CONVERSIONS

The decay $\mu \rightarrow eee\nu\nu$ occurs with a branching fraction of $3.4 \cdot 10^{-5}$ [117]. It can be distinguished from the $\mu \rightarrow eee$ process by making use of energy and momentum conservation to reconstruct the undetected neutrinos; in order to separate the $\mu \rightarrow eee$ events from $\mu \rightarrow eee\nu\nu$ events, the total momentum in the event is required to be zero and the energy equal to the muon rest energy. The branching fraction as a function of the energy cut of the $\mu \rightarrow eee\nu\nu$ process [116] is shown in Figure 4.3. Figures. 4.4 and 4.5 show the energy spectrum of all and the lowest energy electron from internal conversion decays, Figs. 4.6 and 4.7 the invariant masses of e^+e^- combinations calculated with the matrix element from [116]. This process is the most serious background for the $\mu \rightarrow eee$ search and can only be resolved by a very good energy resolution.

4.3.2 MICHEL DECAYS

Using a beam of positive muons, one of the main processes contributing to accidental background is that of the ordinary Michel decay $\mu^+ \rightarrow e^+\nu\bar{\nu}$. This process does not produce a negatively charged particle (electron), which is one of

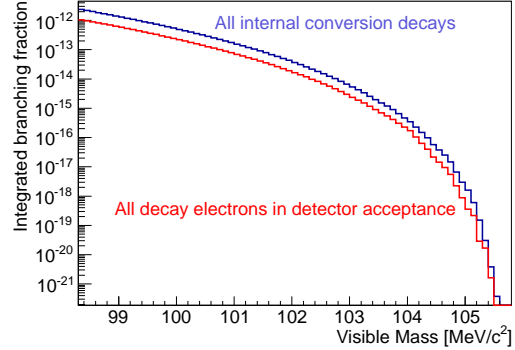


Figure 4.3: Integrated branching fraction for the decay $\mu \rightarrow eee\nu\nu$ in dependence of the visible mass for all internal conversion decays and those with all three decay particles in the detector acceptance. The matrix element was taken from [116].

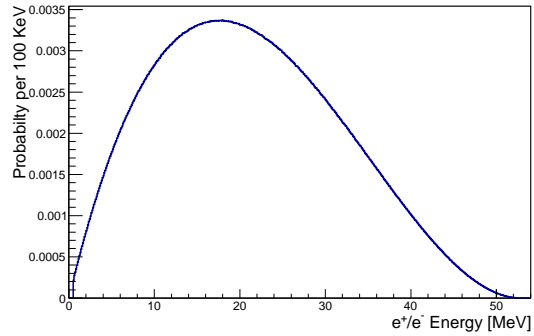


Figure 4.4: Spectrum of electrons from internal conversion decays.

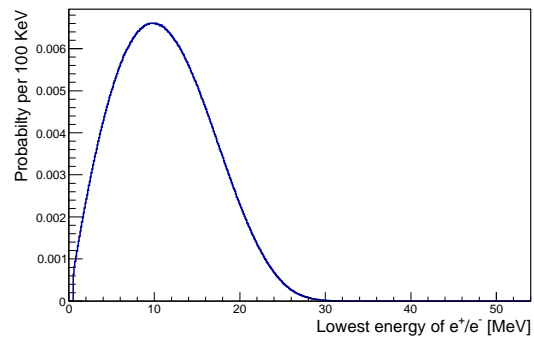


Figure 4.5: Spectrum of the electron with minimum energy from internal conversion decays.

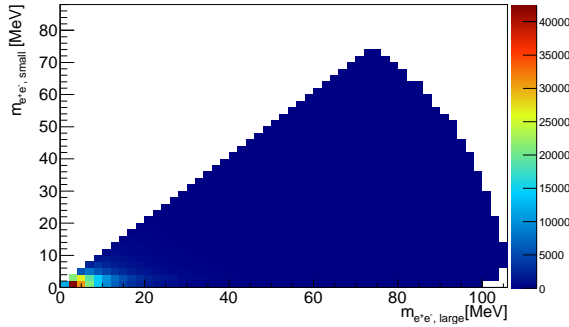


Figure 4.6: Invariant masses of the two possible e^+e^- combinations for internal conversion decays.

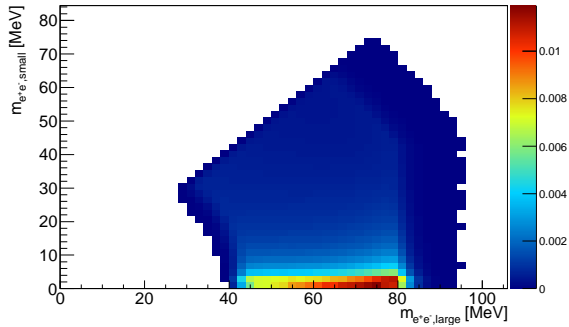


Figure 4.7: Invariant masses of the two possible e^+e^- combinations for internal conversion decays with a visible mass above 90 MeV and the electrons and positrons in the detector acceptance ($E > 10$ MeV, $|\cos\theta| < 0.8$).

the main characteristics of the $\mu^+ \rightarrow e^+e^+e^-$ decay, and can therefore only contribute as potential background if a track is wrongly reconstructed. Other processes which “naturally” provide negatively charged tracks (electrons) are radiative decays with internal or external photon conversions or Bhabha scattering.

4.3.3 RADIATIVE MUON DECAYS

The process $\mu^+ \rightarrow e^+\gamma\nu\nu$ (branching fraction $1.4 \cdot 10^{-2}$ for photon energies above 10 MeV [117]) can deliver an oppositely charged electron if the photon converts either in the target region or in

the detector. Contributions from conversions outside of the target are greatly suppressed if a vertex constraint is applied and by minimizing the material in both the target and detector. Photon conversion in the target generates an event topology similar to the radiative decay with internal conversion: $\mu \rightarrow eee\nu\nu$, which is discussed above.

Due to the missing energy from the neutrinos, this process mainly contributes to the accidental background in combination with an ordinary muon decay.

4.3.4 BHABHA SCATTERING

Positrons from the ordinary muon decay or beam-positrons can undergo Bhabha scattering with electrons in the target material, leading to an electron-positron pair from a common vertex. Due to the missing energy, this process mainly contributes to the accidental background in combination with an ordinary muon decay.

4.3.5 PION DECAYS

Certain decays of pions, especially $\pi \rightarrow eee\nu$ (branching fraction $3.2 \cdot 10^{-9}$ [117]) and $\pi \rightarrow \mu\gamma\nu$ (branching fraction $2.0 \cdot 10^{-4}$ [117]) with subsequent photon conversion are indistinguishable from signal events if the momenta of the final state particles fit the muon mass hypothesis; a low pion contamination of the primary beam (estimated to be in the order of 10^{-12} for the high intensity beamline), the small branching fraction and the small slice of the momentum is assumed to lead to negligible rates in the kinematic region of interest.

4.3.6 SUMMARY OF BACKGROUND SOURCES

First simulation studies have been performed to calculate the different background contributions. Their results indicate that purely accidental backgrounds for $\sim 10^9$ muons stops per second are small for the proposed high resolution detector.

The main concern are irreducible backgrounds, such as the process $\mu \rightarrow eee\nu\nu$, which can only be reduced by a very good tracking resolution resulting in total energy resolution of $\sigma_E < 1$ MeV for the aimed sensitivities $< 10^{-15}$.

PART II



THE MU3E EXPERIMENT



REQUIREMENTS FOR MU3E

5.1 Goals of the Experiment

The goal of the Mu3e experiment is to observe the process $\mu \rightarrow eee$ if its branching fraction is larger than 10^{-16} or otherwise to exclude a branching fraction of $> 10^{-16}$ at the 90% certainty level. In order to achieve these goals, $> 5.5 \cdot 10^{16}$ muon decays have to be observed¹ and any background mimicking the signal process has to be suppressed to below the 10^{-16} level. The additional requirement of achieving these goals within a reasonable measurement time of one year of data taking dictates a muon stopping rate of $2 \cdot 10^9$ Hz and a high geometrical acceptance and efficiency of the experiment.

We plan to perform the experiment in two phases. The exploratory phase I will make use of existing muon beams at PSI and serve to commission the detectors, gain experience with the new technologies and validate the experimental concept, whilst at the same time producing a competitive measurement. The goal for this first phase is to reach a sensitivity of 10^{-15} , thus pushing the existing limit by three orders of magnitude. For this level of sensitivity, the demands on the detector are somewhat relaxed, thus allowing for cross-checks between detectors also on analysis level or running without the full instrumentation. The lower data rates also will not require the full read-out and filter farm system. The second phase of the experiment on the other hand will aim for the ultimate sensitivity and thus require that the detector works as specified and a new beamline delivers $> 2 \cdot 10^9$ Hz of muons.

¹Assuming a total efficiency of 30%.

The expected rate at an existing beamline is $1 - 1.5 \cdot 10^8$ Hz of muons on target. In order to have a safety margin, we usually assume $2 \cdot 10^8$ Hz for phase I background studies, except where the running time is concerned.

This proposal discusses the phase I experiment in detail and shows the path leading to full rate capability. We also discuss alternative approaches.

5.2 Challenges for the Experiment

5.2.1 BACKGROUNDS

There are two kinds of backgrounds: Overlays of different processes producing three tracks resembling a $\mu \rightarrow eee$ decay (*accidental background*) and radiative decays with internal conversion (*internal conversion background*) with a small energy fraction carried away by the neutrinos. Accidental background has to be suppressed via vertexing, timing and momentum measurement, whereas momentum measurement is the only handle on internal conversion.

5.2.2 GEOMETRIC ACCEPTANCE

For a three-body decay with a priori unknown kinematics such as $\mu \rightarrow eee$, the acceptance has to be as high as possible in order to test new physics in all regions of phase space. There are two kinds of acceptance losses, losses of tracks downstream or upstream, where beam entry and exit prevent instrumentation, and losses of low transverse momentum tracks, which do not transverse

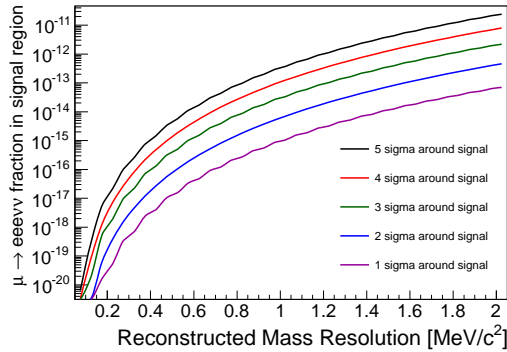


Figure 5.1: Contamination of the signal region (one sided cut) with internal conversion events as a function of momentum sum resolution.

a sufficient number of detector planes, and are not reconstructed.

5.2.3 RATE CAPABILITY

The Mu3e detector should be capable of running with $2 \cdot 10^9$ Hz of muon decays. This poses challenges for the detectors, the data acquisition and the readout.

5.2.4 MOMENTUM RESOLUTION

The momentum resolution directly determines to what level internal conversion background can be suppressed and thus to which level the experiment can be ran background free. In order to reach a sensitivity of 10^{-16} with a 2σ cut on the reconstructed muon mass, the average momentum resolution has to be better than 0.5 MeV. For the phase I experiment aiming at 10^{-15} , this requirement is relaxed to 0.7 MeV, see Figure 5.1.

5.2.5 VERTEX RESOLUTION

Keeping apart vertices from different muon decays is a key tool in suppressing accidental background. The vertex resolution is essentially determined by the amount of multiple scattering (and thus material) in the innermost detector layer. Ideally the vertex resolution is sufficient to eliminate almost all combinatorial backgrounds; for the phase I rates, this appears achievable, whereas in the phase II experiment, very good timing is needed in addition.

5.2.6 TIMING RESOLUTION

Good timing is essential for reducing combinatorial background at rates which lead to more than about 10 muon decays per frame on average.



EXPERIMENTAL CONCEPT

The Mu3e detector is aimed at the background free measurement or exclusion of the decay $\mu \rightarrow eee$ at the level of 10^{-16} . As discussed in more detail in the preceding chapter 5, these goals require to run at high muon decay rates, an excellent momentum resolution in order to suppress background from the internal conversion decay $\mu \rightarrow eee\nu\nu$ and good vertex and timing resolution in order to efficiently suppress combinatorial background.

We intend to measure the momenta of the muon decay electrons in a solenoidal magnetic field using a silicon pixel tracker. At the electron energies of interest, multiple Coulomb scattering in detector material is the dominating factor affecting momentum resolution. Minimizing this material in the active detector parts is thus of utmost importance.

The proposed detector consists of an ultra thin silicon pixel tracker, made possible by the High-Voltage Monolithic Active Pixel (HV-MAPS) technology (see chapter 10). Just four radial layers around a fixed target in a solenoidal magnetic field allow for precise momentum and vertex determination. Two timing detector systems guarantee good combinatorial background suppression and high rate capabilities.

The Mu3e experiment is designed to have a sensitivity four orders of magnitude better than the current limit on $\mu \rightarrow eee$ (10^{-12}), so it is reasonable to plan for a staged detector design, with each stage roughly corresponding to an order of magnitude improvement.

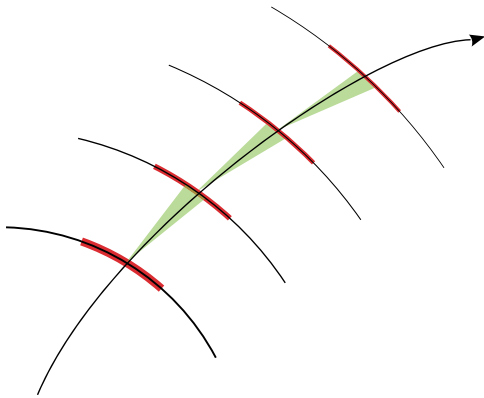


Figure 6.1: Tracking in the spatial resolution dominated regime

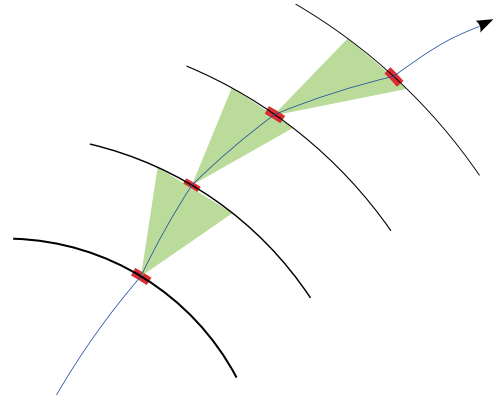


Figure 6.2: Tracking in the scattering dominated regime



6.1 Momentum Measurement with Recurlers

Due to the low momenta of the electrons from muon decay, multiple scattering is the dominating effect on momentum measurement. With our fine-grained pixel detector, we are thus in a regime where scattering effects dominate over sensor resolution effects, see Figs. 6.1 and 6.2. Thus adding additional measurement points does not necessarily improve the precision.

The precision of a momentum measurement depends on the amount of track deflection Ω in the magnetic field B and the multiple scattering angle Θ_{MS} , see Figure 6.3; to first order:

$$\frac{\sigma_p}{p} \propto \frac{\Theta_{MS}}{\Omega}. \quad (6.1)$$

So in order to have a high momentum precision, a large lever arm is needed. This can be achieved by moving tracking stations to large radii, which however compromises the acceptance for low momentum particles. In the case of muon decays, all track momenta are below 53 MeV and all tracks will thus curl back towards the magnet axis if the magnet bore is sufficiently large. After exactly half a turn, effects of multiple scattering on momentum measurement cancel in first order, see Figure 6.4. To exploit this feature we optimized the experimental design specifically for the measurement of re-curling tracks, leading to a narrow, long tube layout.

Measuring the momentum from bending outside of the tracker also allows us to place timing detectors inside, without strongly affecting the resolution.

6.2 Baseline Design

The proposed Mu3e detector is based on two double layers of HV-MAPS around a hollow double cone target, see Figures 6.5 and 6.6. The outer two pixel sensor layers are extended upstream and downstream to provide precise momentum measurements in an extended region with the help of re-curling electrons. The silicon detector layers (described in detail in chapter 10) are supplemented by two timing systems, a scintillating fibre tracker in the central part (see chapter 11) and scintillating tiles (chapter 12) inside the recurl layers. Precise timing of all tracks

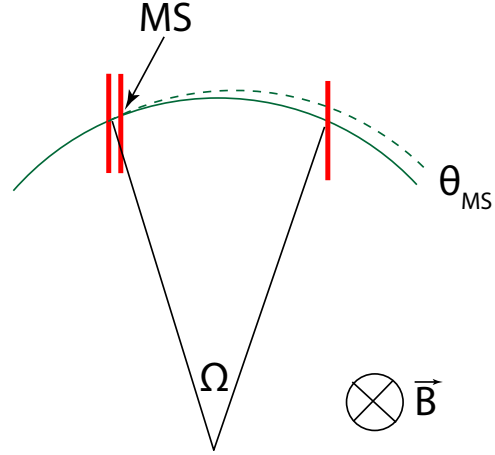


Figure 6.3: Multiple scattering as seen in the plane transverse to the magnetic field direction.

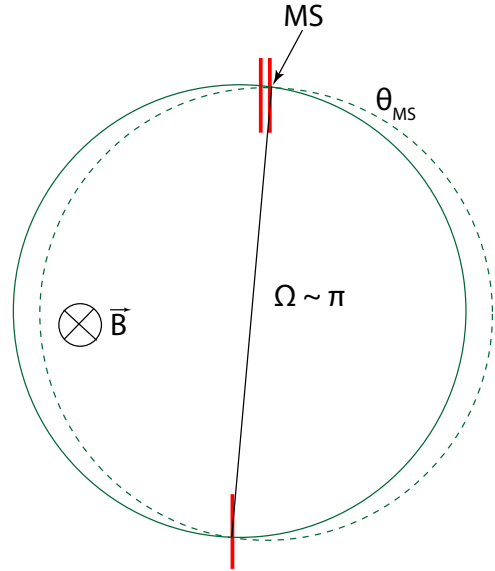


Figure 6.4: Multiple scattering for a semi-circular trajectory.



is necessary for event building and to suppress accidental combinatorial background.

The entire detector is built in a cylindrical shape around a beam pipe, with a total length of approximately 2 m, inside a 1 T solenoid magnet with 1 m inside diameter and 2.5 m total length (chapter 8). In the longitudinal direction the detector is sub-divided into five stations, the central detector with target, inner silicon double layer, fibre tracker and outer silicon double layer, and two forward and backward recurl stations with two silicon recurl layers surrounding a tile timing detector. In order to separate tracks coming from different muon decays, the target has a large surface with 10 cm length and 2 cm diameter. The target shape is a hollow double cone, see chapter 9. Around the target the two inner silicon pixel layers, also referred to as the vertex layers, cover a length of 12 cm. The innermost layer will have 12, the second one 18 sides of 1 cm each, corresponding to an average radius of 1.9 cm and 2.9 cm, respectively. The inner silicon layers are supported by two half cylinders made from 25 μm thin Kapton foil mounted on plastic end pieces. All silicon sensors are thinned to 50 μm , resulting in a radiation length of $X/X_0 \leq 0.1\%$ per layer. The detector will be cooled with gaseous helium.

The hit information from the silicon sensors is read out at a rate of 20 MHz using timestamps providing a time resolution of 20 ns.

The fibre tracker sits inside silicon pixel layer three at around 6 cm, providing timing information for decay positrons and electrons. It is composed from three to five layers of 250 μm thick 36 cm long scintillating fibres, see Figure 6.6. The fibre tracker is read out by fast silicon photo multipliers and can provide timing information with ≤ 1 ns accuracy.

The silicon pixel layers three and four are just outside the fibre tracker at a mean radius of 7.6 cm and 8.9 cm. The active area has a cylindrical shape of 36 cm length. The layer three has 24 sides, layer four 28 sides of 1.9 cm width each. Both outer layers are constructed as modules of 4 sides, six modules for layer three and seven modules for layer four. Similar to the inner two layers the mechanical frames of these modules are build from 25 μm Kapton foil with plastic end pieces.

Copies of silicon pixel layer three and four are also used in the recurl stations. Two recurl stations each are covering the upstream and downstream regions. These recurl stations add fur-

ther precision to the momentum measurement of the electrons, see section 6.1. While the silicon layer design is (almost) identical to the central part, the timing detector in the recurl region can be much thicker compared to the fibre tracker, as the particles can and should be stopped here. This is done by using scintillating tiles of about $7.5 \times 7.5 \times 5 \text{ mm}^3$ size. These tiles provide a much better time resolution than the thin fibre tracker in the center. Following the dimensions of the recurl silicon layers, the tile station have a active length of 36 cm and a cylindrical shape with a radius of ≈ 6 cm. All central detector components are mounted on spokes providing a light stiff support. The recurl silicon layers and tiles are mounted on the beam pipe support. In addition to the silicon and scintillating tile sensors the beam pipe support also carries the services and the PCBs equipped with the front-end electronics (chapter 13). Signal and power connection to the silicon layers is provided by flex prints which are also part of the mechanical support of the silicon sensors.

6.3 Building up the Experiment

One of the advantages of the design concept presented is its modularity. Even with a partial detector, physics runs can be taken. The full instrumentation is only required for achieving the final sensitivity of 10^{-16} at muon rates above $1 \cdot 10^9$ Hz. On the other hand, in an early commissioning phase at smaller muon stopping rates, the detector could run with the central silicon detector only (see Figure 6.7). The silicon detectors of the recurl stations are essentially copies of the central outer silicon detector; after a successful commissioning of the latter, they can be produced and added to the experiment as they become available together with the connected tile detectors. The fibre tracker can also be added later, since it is only needed to resolve combinatorial background at higher event rates and track multiplicities. The loss of momentum resolution due to multiple scattering at the additional material of the fibre tracker will be fully compensated by the improved momentum measurement with re-curlers. The configuration with two recurl stations (Figure 6.8) defines a medium-size setup, well suited for phase I running. The configuration with four

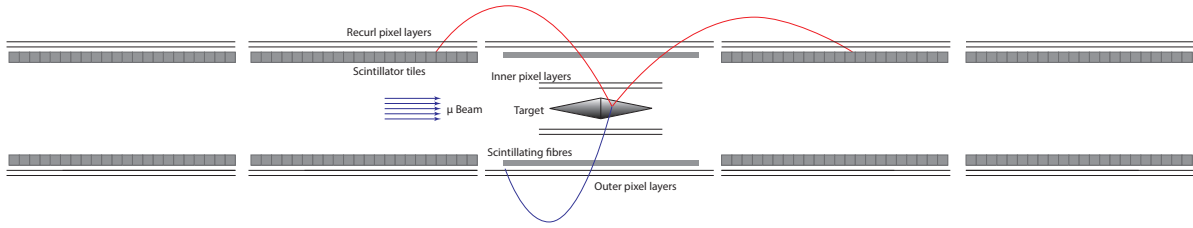


Figure 6.5: Schematic view of the experiment cut along the beam axis in the phase II configuration.

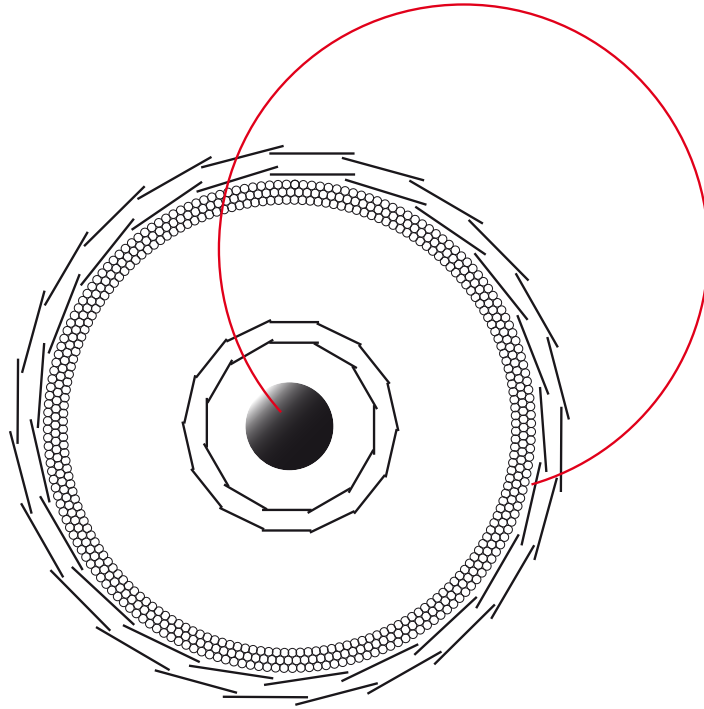


Figure 6.6: Schematic view of the experiment cut transverse to the beam axis. Note that the fibres are not drawn to scale.

recurl stations (Figure 6.9) defines the full setup for phase II running.

In the following sections, the experimental configurations for running at the existing $\pi E5$ beam-line (the *Phase I Experiment*) and the final detector for running at $> 1 \cdot 10^9$ Hz muon stopping rate (the *Phase II Experiment*) are outlined.

6.4 The Phase I Experiment

The phase I of the Mu3e experiment will start with a minimum configuration (phase IA detector) with the target regions surrounded by double layers of inner and outer silicon pixel detectors, see Figure 6.7. This configuration defines the minimal configuration as it allows to determine the momentum, the vertex position and the time of the decay pre-



AN EXPERIMENT TO SEARCH FOR THE DECAY $\mu \rightarrow eee$



Figure 6.7: Minimum detector configuration for early commissioning with central silicon only (phase IA).

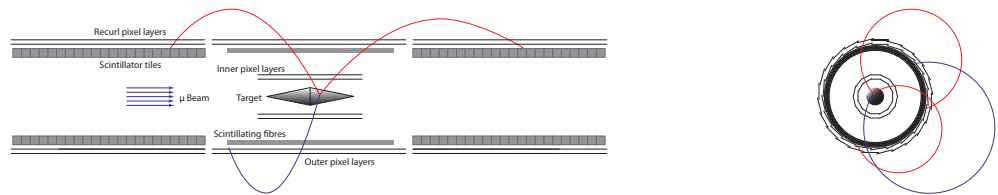


Figure 6.8: Detector with one set of recurl stations for physics runs and tile detector commissioning (phase IB).

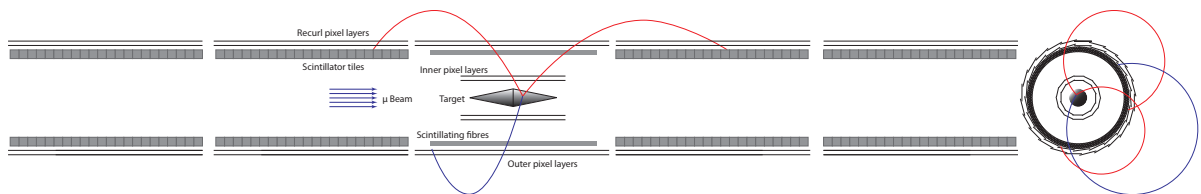


Figure 6.9: Final detector with two sets of recurl stations for high intensity physics runs (phase II).



cise enough to produce very competitive physics results with a sensitivity down to $\mathcal{O}(10^{-14})$. It is foreseen to run in the first year in this configuration at a muon stopping rate on target at around $2 \cdot 10^7$ Hz. The number of decays in one readout frame of the pixel tracker of 50 ns will be around one on average and combinatorial background can be suppressed with the help of the vertex reconstruction. The precision of the momentum resolution will be somewhat limited, as most tracks do not recur within the instrumented volume, see chapter 17.

In the phase IB the detector will be complemented by the first pair of recur stations, the corresponding tile detectors and the fibre tracker, see Figure 6.8. Adding the recur stations will significantly enhance the momentum resolution and thus improve the suppression of internal conversion background. The insertion of the fibre tracker and the tile detector stations gives a much better time resolution in comparison to the silicon pixel only. The fibre tracker will deliver a time resolution of about 200-300 ps, while the tile detector will have < 100 ps resolution for the tracks passing the recur stations. The high time resolution will

allow running at the highest possible rate at the π E5 muon beam line at PSI of $\approx 1 \cdot 10^8$ Hz. The sensitivity reach in this phase of the experiment of $\mathcal{O}(10^{-15})$ will be limited by statistics only, limited by the available muon decay rate.

6.5 The Phase II Experiment

A new high intensity muon beam line [118] delivering $\approx 2 \cdot 10^9$ Hz muon stops is crucial for the phase II of the proposed experiment. To fully exploit the new beam facility the limited detector acceptance at phase IB will be further enhanced by adding another a second pair of recur and tile detector stations, see Figure 6.9. These extra stations will allow to measure precisely the momentum of all particles in the acceptance of the inner tracking detector. At the same time the extra tile detector stations with their high time resolution and small occupancy will help to fight the increased combinatorics at very high decay rates. The combined performance of the final detector setup together with the high stopping rate will allow to search for the $\mu \rightarrow eee$ decay with a sensitivity of $B(\mu \rightarrow eee) \leq 10^{-16}$.



MUON BEAM

7.1 General Beam Requirements

The general beam requirements for a high intensity, low-energy, stopped muon coincidence experiment such as Mu3e are six-fold: an abundant supply of low-energy surface muons (from stopped pion decay at rest, at the surface of the production target [119]) capable of being stopped in a thin target; high transmission optics at 28 MeV/c, close to the kinematic-edge of stopped pion decay and hence close to the maximum production rate of such muons, as shown in Figure 7.1; a small beam emittance to minimize the stopping-target diameter; a momentum-byte of less than

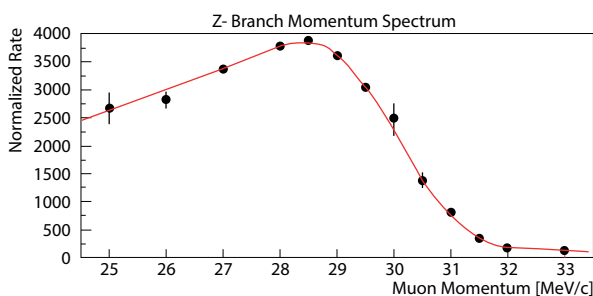


Figure 7.1: π E5 measured muon momentum spectrum with fully open slits. Each point is obtained by optimizing the whole beam line for the corresponding central momentum and measuring the full beam-spot intensity. The red-line is a fit to the data, based on a theoretical $p^{3.5}$ behaviour, folded with a Gaussian resolution function corresponding to the momentum-byte plus a constant cloud-muon background.

10% with an achromatic final focus, allowing an almost monochromatic beam with a high stopping density, to be stopped in a minimally thick target; minimization and separation of beam-related backgrounds such as beam e^+ originating from π^0 -decay in the production target, or decay particles produced along the beam line and finally minimization of material interactions in the beam, for example such as those in windows, thus requiring vacuum or helium environments to keep the multiple scattering under control.

7.2 Beam for phase I running

As previously outlined, a multi-staged detector configuration will be sought for phase I running, this in turn requires muon beam intensities ranging between (10^7-10^8) muons/s for the initial phase IA (central detectors), while for phase IB a maximal intensity close to $1 \cdot 10^8$ muons/s will be sought. The quoted maximum beam intensity which includes a phase space reduction factor due to collimation in the central region of the Mu3 magnet is based on measured intensities at the centre of the MEG detector, without a degrader and normalized to a proton beam current of 2.3 mA. This demand for the highest intensities necessitates the selection of only one possible facility in the world, namely the π E5 channel at PSI. Based on the experience gained in the design of the MEG beam line, a similarly developed concept is also envisaged for phase I of Mu3e. This should allow the required muon intensity to be achieved. However, since the area is likely to be shared with

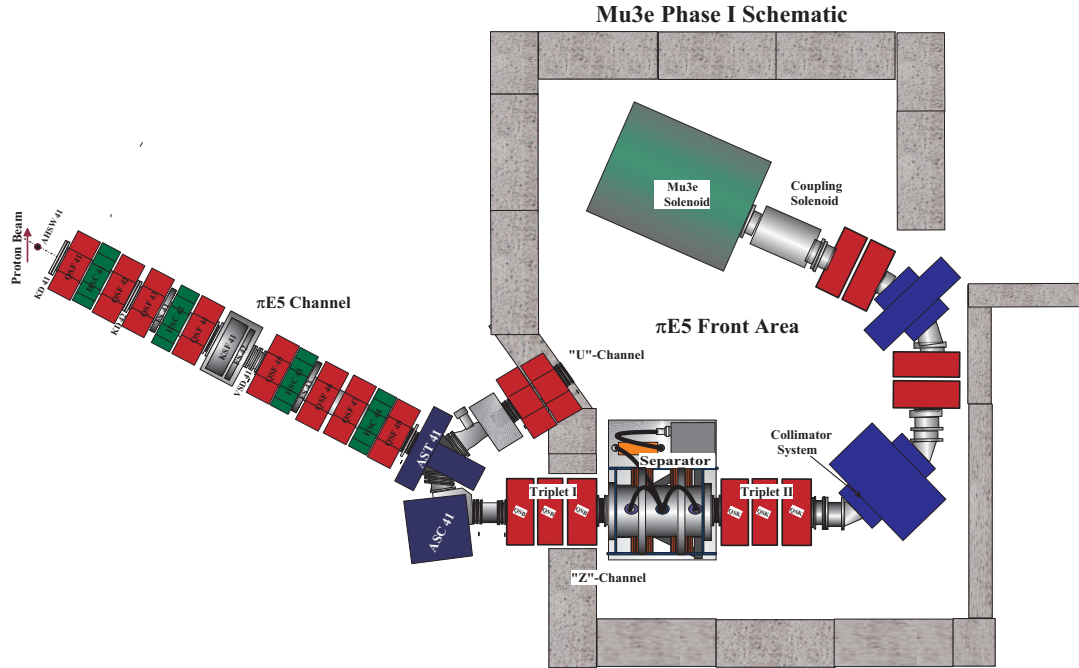


Figure 7.2: Mu3e potential beam line layout in the front-part of the $\pi E5$ area.

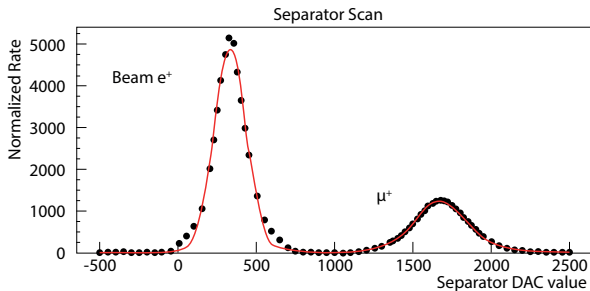


Figure 7.3: Separator scan plot, measured post collimator system. The black dots represent on-axis, low-threshold intensity measurements at a given separator magnetic field value during the scan, for a fixed electric field value of -195 kV. The red curve represents a double Gaussian fit to the data points, with a constant background. A separation of 8.1 muon beam σ_μ is found, corresponding to more than 12 cm separation of beam-spot centres at the collimator.

other experiments, that of MEG (R-99-05), and the Lamb-shift experiment (R-98-03) a compact muon beam line designed specifically to fit into the front-part of the $\pi E5$ area is under design. This would not only allow the beam line elements, such as the Wien-filter, triplet I and II, plus the MEG collimator system to be used by this experiment, but would also allow access to the MEG detector during running periods, by means of placing a shielding wall just upstream of the MEG detector, as previously adopted during the run periods of experiment R98-03.

Figure 7.2 shows the potential area layout adopted. Surface muons of 28 MeV/c will be extracted from the $\pi E5$ “Z-channel” and the initial part of the current MEG beam line, including: Triplet I, the 200 kV crossed-field Wien-filter, Triplet II and the collimator system. This combination of elements allows for an optimal beam correlated background suppression, as demonstrated in Figure 7.3, which shows the separation quality post collimator, between muons and beam positrons for the above mentioned section of beam line. Due to the severe restrictions imposed by space, a matching section, including two dipole magnets of 90° and 66° bending angles respectively, with an intermediate quadrupole doublet or triplet, is en-



visaged. A final doublet/triplet or intermediate transport solenoid would in turn couple the beam line to the Mu3e superconducting magnet. The beam line vacuum is currently planned to end close to the centre of the target and includes collimation to match the beam-spot to the target size and prevent beam interactions from occurring directly in the small radii inner silicon layers. The expected usable muon intensity at the Mu3e target is between $0.7\text{-}1.0 \cdot 10^8$ muons/s.

Although it is understood that simultaneous running of prospective $\pi E5$ experiments is not possible, it is nevertheless clear that the Mu3e phase I beam line will in fact benefit from the availability of MEG beam elements upstream of the detector and that this option, together with provision of the available standard PSI magnets currently in storage or potentially sharable, would cover most of the beam line requirements, except that of a short coupling solenoid, for which a potential solution is also currently under study and possible dipole vacuum chamber modifications.

7.3 High intensity muon beamline for phase II running

In order to reach the ultimate sensitivity goal of $\mathcal{O}(10^{-16})$ for the phase II experiment, an unpulsed muon stopping rate in the GHz region is required. As demonstrated in Table 7.1, there are no such (pulsed or unpulsed) high-intensity sources of muons currently available world-wide. Future intensity frontier facilities are however in the planning in the US and Japan and are also associated with LFV-experiments, more specifically Mu2e and Project X in the U.S. [46, 99] and the COMET and PRIME/PRISM experiments in Japan [45, 101]. To meet the needs of such experiments a totally new concept is therefore necessary. One such concept, which is still in its infancy, though is proving to be a promising candidate, is the HiMB project at PSI [118], a next-generation high-intensity muon beam, currently under study. A detailed feasibility study is due to start at PSI in 2013. This concept would provide the basis for a new Mu3e beam line for the phase II measurements, based on the production of surface muons from the Swiss Spallation Neutron Source's (SINQ) spallation target window.

The layout of the source in the SINQ hall [120], together with a schematic diagram of the source

with the proton beam injected from below is shown in Figure 7.4. The characteristics of the source, which resembles a medium-flux reactor, are that the protons are injected from below and defocussed onto a double-layered aluminium window separated by a D_2O cooling layer, before being stopped in the target, a ‘‘cannelloni’’ construct of lead-filled zircaloy tubes.

The HiMB project plans to extract the downward travelling muons produced in the aluminium window via a two-stage channel, the first stage, a solenoidal one, which uses the same beam-tube as the upward travelling protons and extracts the muons, in the opposite direction, to a large collection solenoid connecting to the second stage, a conventional dipole and quadrupole channel planned for the empty service cellar under the SINQ target. The general layout of both the proton channel and the service area are shown in Figure 7.5

There are several advantages of this concept, which would lead to a substantial enhancement compared to target E, namely: the increased number of primary proton interactions since 70% of the beam stops in the target; a much larger pion energy range of up to 150 MeV can be exploited in the case of SINQ, above which the high energy tail of the pion production cross-sections becomes negligible, in the case of Target E this limit is around 45 MeV [121, 122]; a substantially larger pion-production volume contribution compared to Target E and finally a significantly larger surface muon production volume.

Realistic Monte-Carlo studies were undertaken together with M. Wohlmuther (Head of the Target Development Group at PSI) using the Los Alamos Laboratory MCNPX code (Monte Carlo n-particle extended code), used also to design the SINQ target. A simulation of the surface muon production rate was made using the complete model of the SINQ target environment. Based on a total of $4 \cdot 10^8$ generated upward moving protons, corresponding to the measured 2D beam profile at SINQ, a complete particle tracking was done using three different event generators. For surface muons, the simulated fluences were determined for the conditions of a particle leaving the target with the correct energy, travelling downwards within the beam-pipe and crossing a horizontal plane 25 cm below the window. This is shown schematically in Figure 7.6. The calculated fluences from the three event generators agreed to within 35%

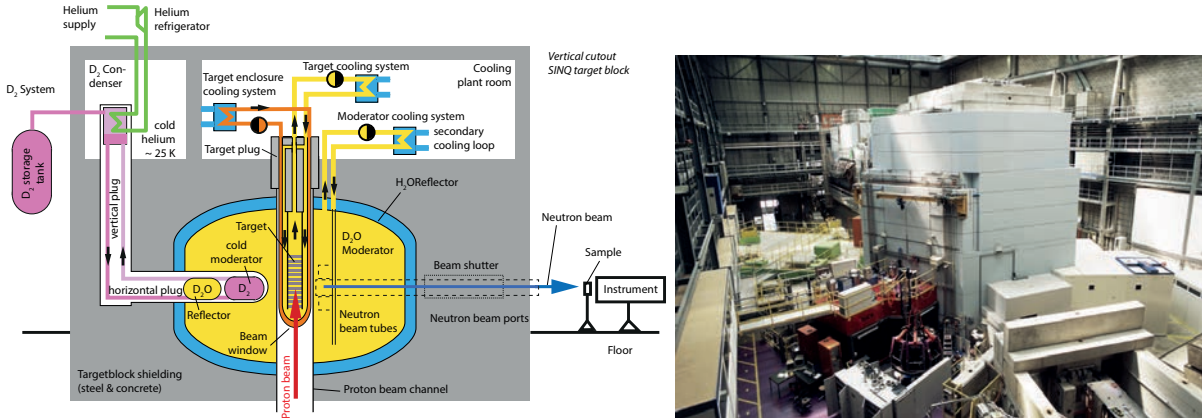


Figure 7.4: (Right) The SINQ spallation neutron source as seen in the experimental hall. The tower in the foreground, shown in section with the proton beam incident from below. (left) contains the main neutronics components, the spallation source, a Pb/Zr/Al structure cooled using D₂O, the D₂O moderator tank and reflector shield and a cold-source of solid deuterium. The upper-part of the tower deals with the cryogenic connections of the source.

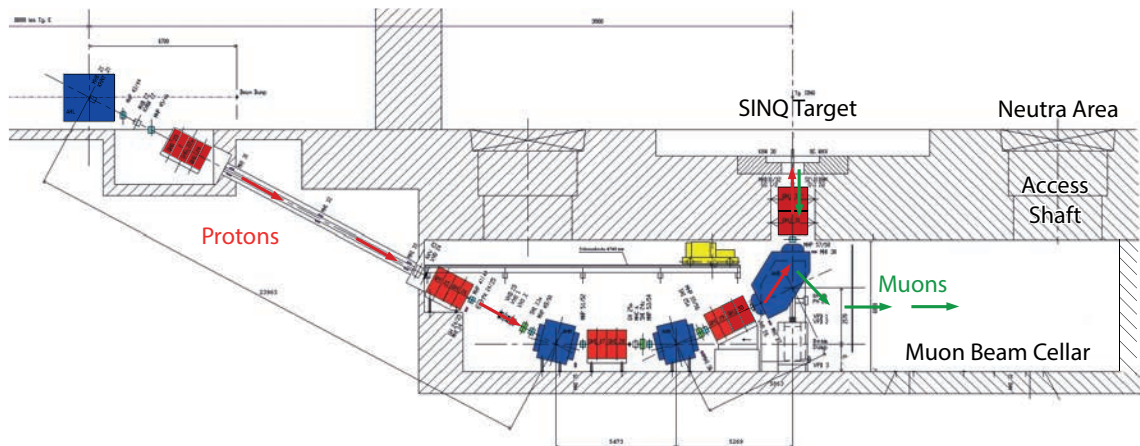


Figure 7.5: Shows the layout of the proton beam line at SINQ as well as showing the possibility for extracting the muons into the empty cellar region below the SINQ target. The blue elements are dipole bending magnets and the red elements focussing quadrupole magnets. Since the proton and muons are like-sign charged particles but travelling in opposite directions they will be bent in opposite directions, allowing the muons to access the empty cellar region shown. This is where a muon beam line could be placed.



Laboratory/ Beam line	Energy/ Power	Present Surface μ^+ rate (Hz)	Future estimated μ^+/μ^- rate (Hz)
PSI (CH)	(590 MeV, 1.3 MW, DC)		
LEMS	"	$4 \cdot 10^8$	
$\pi E5$	"	$1.6 \cdot 10^8$	
HiMB	(590 MeV, 1 MW, DC)		$4 \cdot 10^{10}(\mu^+)$
J-PARC (JP)	(3 GeV, 1 MW, Pulsed)		
	currently 210 KW		
MUSE D-line	"	$3 \cdot 10^7$	
MUSE U-line	"		$2 \cdot 10^8(\mu^+)$ (2012)
COMET	(8 GeV, 56 kW, Pulsed)		$10^{11}(\mu^-)$ (2019/20)
PRIME/PRISM	(8 GeV, 300 kW, Pulsed)		$10^{11-12}(\mu^-)$ (> 2020)
FNAL (USA)			
Mu2e	(8 GeV, 25 kW, Pulsed)		$5 \cdot 10^{10}(\mu^-)$ (2019/20)
Project X Mu2e	(3 GeV, 750 kW, Pulsed)		$2 \cdot 10^{12}(\mu^-)$ (> 2022)
TRIUMF (CA)	(500 MeV, 75 kW, DC)		
M20	"	$2 \cdot 10^6$	
KEK (JP)	(500 MeV, 2.5 kW, Pulsed)		
Dai Omega	"	$4 \cdot 10^5$	
RAL -ISIS (UK)	(800 MeV, 160 kW, Pulsed)		
RIKEN-RAL		$1.5 \cdot 10^6$	
RCNP Osaka Univ. (JP)	(400 MeV, 400 W, Pulsed)		
MUSIC	currently max 4W		$10^8(\mu^+)$ (2012) means $> 10^{11}$ per MW
DUBNA (RU)	(660 MeV, 1.65 kW, Pulsed)		
Phasatron Ch:I-III		$3 \cdot 10^4$	

Table 7.1: Currently running muon beam facilities around the world used for particle physics experiments and materials science μ SR investigations. Also shown are the planned next-generation facilities designed for cLFV experiments, together with an estimate of the starting date. The PSI HiMB solution is currently only under study and is included purely for completeness.

of each other. Based on the standard event generator, which also has the smallest statistical uncertainty, a summed fluence ($E \leq 4.12$ MeV) of surface and sub-surface muons of $1 \cdot 10^{11}$ muons/s is calculated at a proton current of 3 mA on target E, which corresponds to 2.1 mA on SINQ. However, on the assumption that the proton current on Target E will only rise to a maximum of 2.4 mA in the future, a value that has already been achieved during routine test periods since 2010 and taking into account the variation of event generators in the simulation, a conservative estimated fluence of $(3 \pm 1) \cdot 10^{10}$ good surface muons within a 10 %

FWHM momentum-byte could clearly be extracted from the SINQ target (c.f. Table 7.2).

Conclusions seen from the source point of view look very promising and providing the beam can indeed be transmitted without significant losses, the phase II rates of 2 GHz muons could be realized. Finally, the current extraction principle, to be studied extensively in the feasibility study, is demonstrated in Figure 7.7. Muons originating from the target window are to be guided in a downward direction using a low-field guiding solenoid. Since the muon momentum is about a factor of 42 times smaller than that of the protons, the low-field for the muons should not dramat-

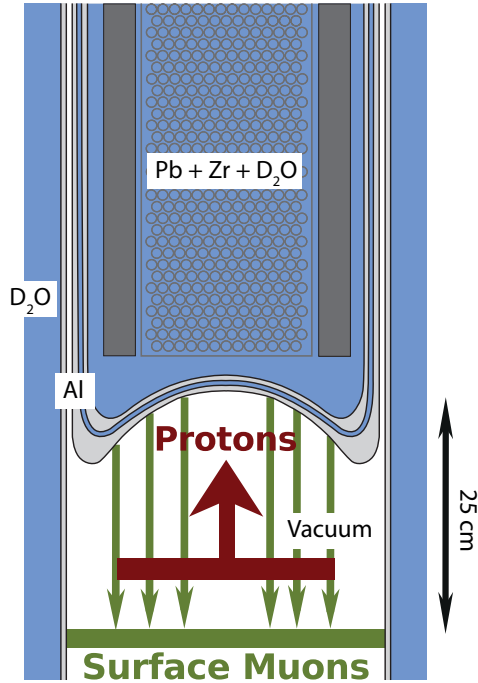


Figure 7.6: The Monte-Carlo model for the SINQ target with all components taken into account. Light grey is the aluminium window, with the D_2O cooling channel in the middle. Protons are generated according to a measured 2-D distribution at the dark red plane. Surface muons leaving the target at the correct energy and crossing the light-green plane, 25 cm below the window and moving downwards within the beam-pipe, are counted.

P_0 MeV/c	$\Delta P/P$ % FWHM	Rate Hz
28	Full	$(7 \pm 1) \cdot 10^{10}$
28	10	$(3 \pm 1) \cdot 10^{10}$
26	10	$(3 \pm 1) \cdot 10^{10}$

Table 7.2: Estimated surface and sub-surface muon rates based on a proton current of 2.4 mA on Target E and full transmission efficiency.

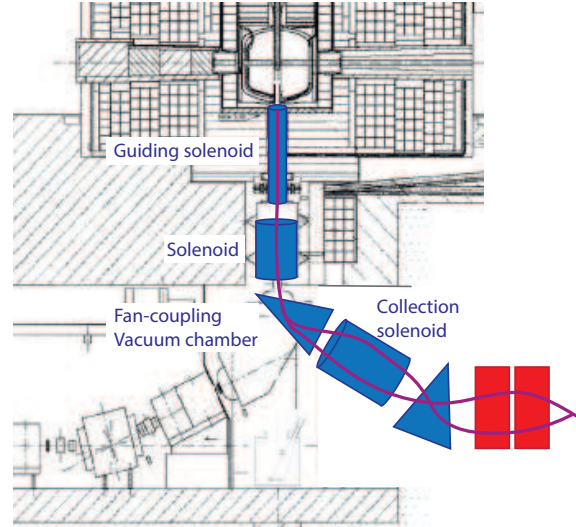


Figure 7.7: Schematic of HiMB muon extraction principle, with a guiding solenoid, followed by a focussing solenoid to satisfy proton and muon transmission. The extraction is done in the fringe-field of the AHO magnet, with a strong-focussing collection solenoid. This is followed by a conventional beam line consisting of a dipole magnet and quadrupole channel.

ically affect the protons. The present radiation-hardened, defocusing quadrupoles QTH 31 and 32, just below the SINQ target, must be replaced by a rotationally symmetric element such as a solenoid, since the muons will not traverse a set of quadrupoles which only focus alternately in the horizontal and vertical planes but have field strengths that are 42 times too high for the muons. The extraction will be done in the fringe-field of the last dipole magnet AHO, which means that the following strong-focussing collection solenoid must be placed close to the “fan-coupling” in order to fully collect the beam. Following this solenoid is a dipole magnet whose function is to bend the beam onto the horizontal plane, where a conventional secondary beam line quadrupole channel could be constructed. As the current cellar ends within just a few meters of the above SINQ hall wall, one could envisage bending the beam upwards again at the end of the cellar and extracting to a hall, exterior to SINQ, on the East-side. This would imply a relatively long beam line of order (30-35) m, which is not too problematic from the muon loss (decay-in-flight) point-of-view where 80% transmission for 28 MeV/c muons is

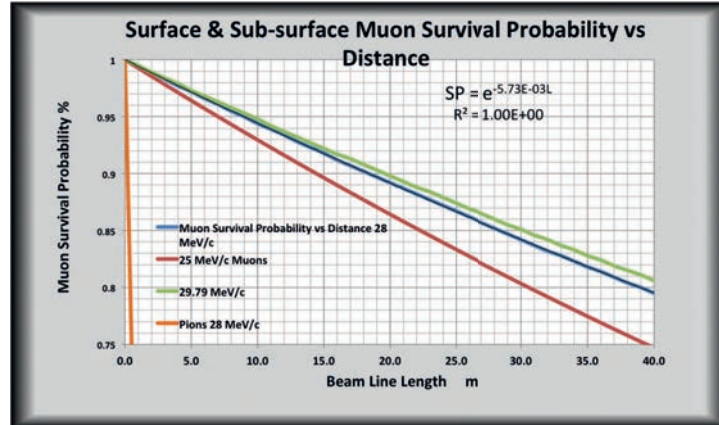


Figure 7.8: Survival probability for muons at the kinematic edge of 29.79 MeV/c (green curve), surface muons of 28 MeV/c (blue curve) and sub-surface muons of 25 MeV/c (red curve). Also shown (orange curve) is the survival probability for pion contamination at 28 MeV/c, which is at the 10^{-12} level.

expected at 40 m, as shown in Figure 7.8. Also shown are similar plots for the maximum momentum at the kinematic edge of pion-decay, as well as for a lower momentum sub-surface muon beam. Finally, the beam would naturally be free of pion contamination to a level of about 10^{-12} , which is also important for backgrounds relevant to the $\mu \rightarrow eee$ decay such as $\pi \rightarrow eee\nu$ and $\pi \rightarrow \mu\nu\gamma$.

The HiMB project is in its infancy at present and there are many aspects that will be studied in detail within the scope of the planned feasibility study, to show the feasibility of this next

generation high-intensity beam line. The initial step taken concerning the muon source intensity, the basis for the HiMB feasibility study, has been shown to be very promising. The next major steps to be studied are the optical extraction of the muons from the proton beam and the solenoidal replacement of the final proton defocussing quadrupole doublet in front of the SINQ target, while still maintaining the safety restraints on the SINQ target. The implementation of such a concept into the SINQ environment could only coincide with a major SINQ shutdown, which is currently planned for the period of 2016-2017.



The magnet for the Mu3e experiment has to provide a homogeneous solenoidal magnetic field for the precise momentum determination of the muon decay products. In addition it will also serve as beam optical element guiding the muon beam to the target. The basic parameters of the superconducting solenoid magnet, which are currently being specified for the preparation of order placements, are given in Table 8.1. The outer dimensions include also an iron field shield.

The nominal magnetic field strength is 1 T in the central part, providing the optimum bending radius in terms of resolution for the proposed experimental design. A higher magnetic field would lead to a loss of acceptance as the low momentum particles would not reach the central outer pixel layers (see Figure 8.1). A lower magnetic field would lead to less magnetic deflection at constant multiple scattering, leading to worse momentum resolution (see Figure 8.2). For systematic studies and to allow for possible reuses of the magnet for other experimental measurements, the field can be varied between 0.8 and 2 T.

The dimensions of the cylindrical warm bore of the magnet are 1 m in diameter and > 2 m in length. The minimum diameter is given by four times the bending radius of the highest momentum ($53 \text{ MeV}/c$) decay products at the lowest possible field of $B = 0.8 \text{ T}$ plus the target diameter. In addition the detector support and extraction rail system has to be taken into account when choosing the warm bore diameter.

The total length is a compromise between geometric acceptance for recurling particles and the very tight space constraints for the phase I exper-

imental area at $\pi E5$. In principle a longer solenoidal magnet would provide an intrinsically more homogenous field. At both ends of the magnet it is foreseen to have full access by means of removable flanges.

While the ideal magnet would have a constant field throughout the inner volume, real solenoid magnets show a drop in field to 50% at the end of the coil. The simplest solution would be a longer magnet, which however does not fit inside the phase I area. Another possibility is to introduce correction coils at both ends of the magnet, such that the high field region can be extended. The insertion of several compensating coils would make the magnet system more complex both in construction and operation due to the need of additional current settings and power supplies. At present the baseline magnet concept foresees three equal coils with a single power supply. The field change along the z-axis has to be taken into account for the reconstruction of tracks in the recur-

MAGNET PARAMETER	VALUE
field for experiment	1 T
field range	$0.8 < 1 < 2 \text{ T}$
warm bore diameter	1 m
warm bore length	$> 2 \text{ m}$
field description $\Delta B/B$	$\leq 10^{-4}$
field stability $\Delta B/B$ (100 days)	$\leq 10^{-4}$
outer dimensions: length	$< 2.5 \text{ m}$
width	$< 2.5 \text{ m}$
height	$< 3.5 \text{ m}$

Table 8.1: Properties of the Mu3e magnet

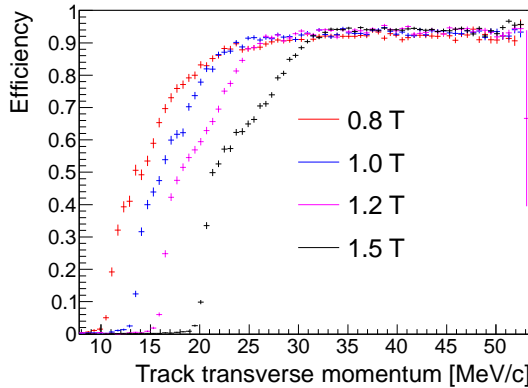


Figure 8.1: Reconstruction efficiency as a function of track transverse momentum for different magnetic fields, with recurl stations and without fibre detector.

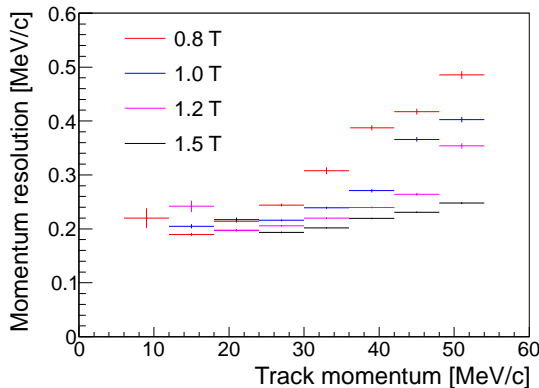


Figure 8.2: Momentum resolution as a function of track momentum for different magnetic fields, with recurl stations and without fibre detector.

stations by using a look up table for the field map plus interpolation between these points. Choosing the right granularity for the look-up table a linear interpolation of the field will be enough to reach an approximation of $\Delta B/B \leq 10^{-4}$. For the fast online selection of events the assumption of a constant field in the active part of the experiment will be sufficient. Though the assumption

of a constant (maximum) field leads to a systematic bias towards larger momenta and an increase of online selected background events from internal radiative muon decays with internal conversions, no signal events would be lost.

The superconducting magnet is made from three coils of equal size, which has advantages over one long coil in terms of mechanical stability. The small dips in the magnetic field can be treated numerically in the same way as the roll-off of the field to the ends of the magnet. The choice for the superconducting wires or conductors will be driven by commercial availability, since standard components allow for the desired 2T maximum field strength. A warm normal conducting magnet is no option because of size, cost (copper price) and operational stability. Superconducting magnets have an intrinsic immunity against absolute field changes, as they have to run at a constant (low) temperature. If feasible in terms of number of cooling compressors, a dry cooled system will be chosen.

There will be a magnetic shielding around the magnet. The shielding is required since the experimental hall is densely populated with other experiments and infrastructure. Also for the read-out of the proposed experiment it will be much easier to work in a low field environment. A beneficial side effect of the shielding is a gain of field homogeneity inside the magnet and less field dependence on variation of outside parameters.

The long term stability of the magnetic field should be $\Delta B/B \leq 10^{-4}$ over each 100 day data taking period. This can be achieved by using state of the art magnet power supplies and by permanent measurement of the absolute field with a hall probe inside the experiment.

The cool-down time for a system of the projected size will be one week and the ramp time will be in the order of one hour. The number and power of the dry compressors will be chosen to fulfill these requirements, in the case of a dry cooled magnet.

The D0 Magnet [123] fulfills most requirements of the future Mu3e magnet and serves as a prototype for the magnet design process.



STOPPING TARGET

The main challenge for the design of the stopping target is to optimize the stopping power on one hand and to minimize the impact on the track measurement on the other hand. Therefore the stopping target should contain just enough material in the beam direction to stop most of the 29 MeV surface muons but should be as thin as possible in the flight direction of decay electrons measured in the detector acceptance. Usage of a low Z material is advantageous as tails from large angle Coulomb scattering are suppressed. In addition, the decay vertices should be spread out as widely as possible in order to reduce accidental coincidences of track vertices and to produce a more or less even occupancy in the innermost detector layer.

9.1 Baseline Aluminium Design

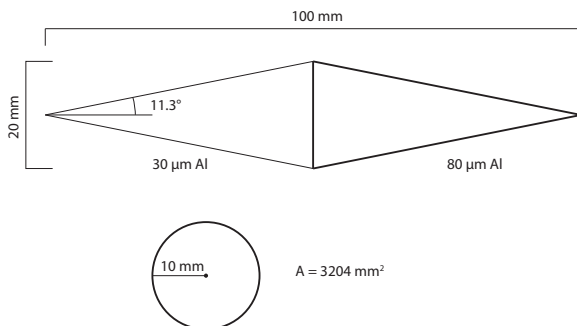


Figure 9.1: Dimensions of the baseline design target. Note that the material thickness is not to scale.

These requirements can be met by a hollow double cone target à la SINDRUM [15,94]. In our baseline design (see Figure 9.1), the target is made from 30 μm of aluminium in the front part and 80 μm aluminium in the back part, with a total length of 100 mm and a radius of 10 mm. This results in an total area of 3204 mm² and an effective target thickness in beam direction of 560 μm corresponding to 0.063 radiation lengths X_0 of Aluminium. The target can be suspended from the innermost tracking layer by e.g. nylon fishing wire (which we assume in the simulation) and which does not significantly add material in the beam line.

In the Geant4 [124] simulation (see 15), about 83.3% of the muons¹ that reach the target are stopped. Obviously, this fraction can be increased by adding material, which will however lead to additional multiple scattering and thus a reduced momentum resolution. For the phase I experiment, where muon rates rather than momentum resolution is limiting the sensitivity, a thicker target could be envisaged.

Stopping $2 \cdot 10^9$ Hz muons in the target corresponds to about 1 mW of power. Compared with the power dissipation of the sensor chips, this is negligible and easily taken care of by the helium cooling.

¹Muons are generated with an energy spectrum modeling the one observed in MEG.



9.2 Vertex distribution

The distances between tracks on the target can be reconstructed already online and used by the event filter farm to reject frames containing only background, see section 14. The only physics process exhibiting three tracks from the same vertex is the radiative muon decay with an internal conversion at a rate of $3.5 \cdot 10^{-5}$.

The simulated distribution of vertices (more precisely: intersections of simulated particles with the target) is shown in Figures 9.2 and 9.3. In the longitudinal direction, the effect of the thicker material in the back part can be clearly discerned, whereas for the transverse view, the “shadows” of the target suspension are visible in the projected beam profile.

Figure 9.4 shows the shortest distance between two vertices in a frame for $2 \cdot 10^8$ Hz muon stop rate. Less than 10% of the frames have tracks that come within 1 mm of each other on the target. Figure 9.5 shows the shortest distance within which three tracks approach on the target surface; one of the tracks has to be assigned negative charge, either because it is a true electron or a recurling positron track. Figures 9.6 show the same distributions for $2 \cdot 10^9$ Hz muon stop rate. Here all frames have two tracks approaching to closer than a millimeter, but a three track coincidence requirement still has a considerable suppression power, which can surpass a factor of 10^{-3} , if recurlers can be identified with high efficiency (see also chapter 14).

9.3 Alternative Designs

9.3.1 MATERIAL ALTERNATIVES

If the aluminium foil design proves unworkable or not mechanically stable enough, it could be replaced by an equivalent design in carbon fibre reinforced plastic (CFRP), where the material thickness would be approximately double. 200 μm thin CFRP structures were built e.g. for the CMS pixel detector upgrade [125].

Another material option would be the use of a low density foam-like material such as Rohacell, as used in the SINDRUM experiment [126].

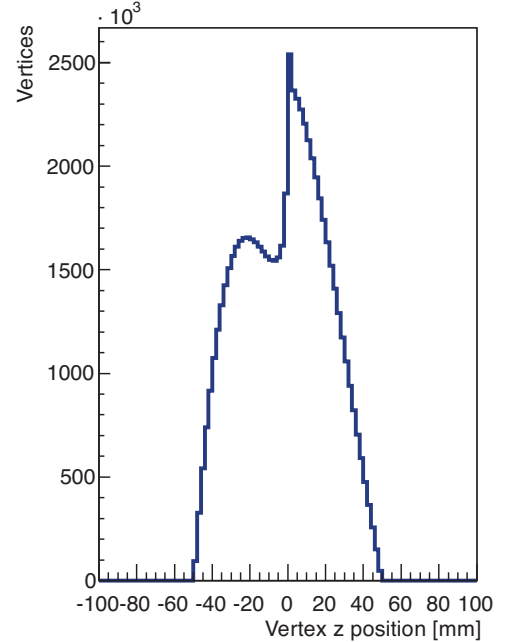


Figure 9.2: Vertex distribution along the beam direction.

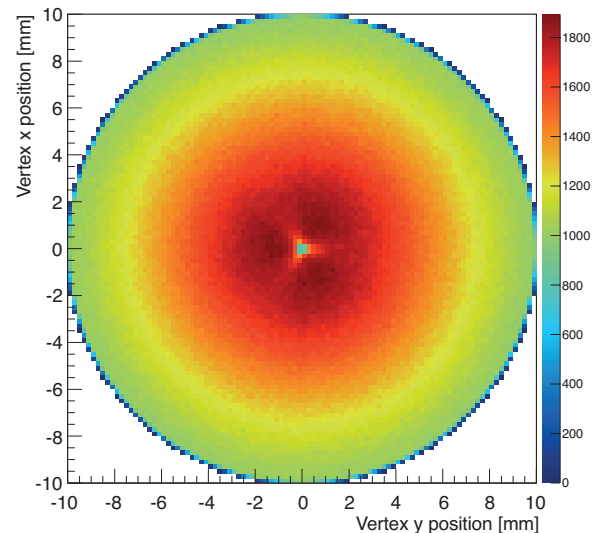


Figure 9.3: Vertex distribution transverse to the beam direction.

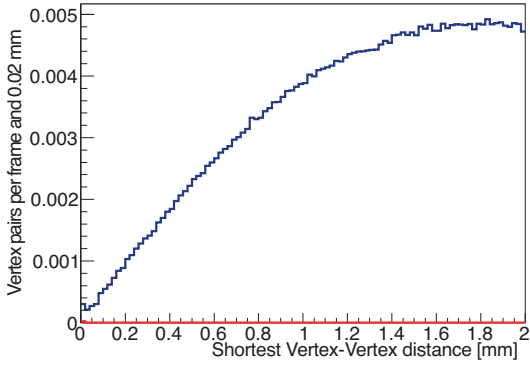


Figure 9.4: Shortest vertex-vertex distance inside a readout frame with 10 tracks on average (phase IB). Note that every crossing of a simulated electron/positron track is counted as a vertex. The red histogram shows the contribution from internal conversion decays.

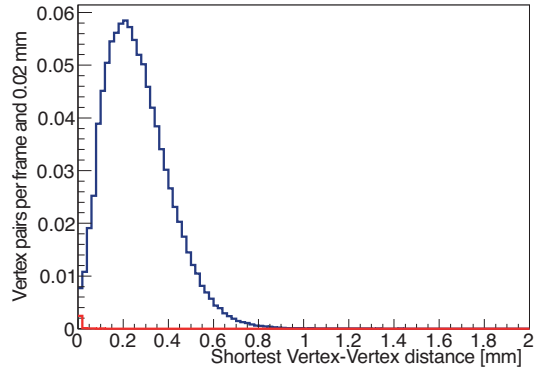


Figure 9.6: Shortest vertex-vertex distance inside a readout frame with 100 tracks on average (phase II). Note that every crossing of a simulated electron/positron track is counted as a vertex. The red histogram shows the contribution from internal conversion decays.

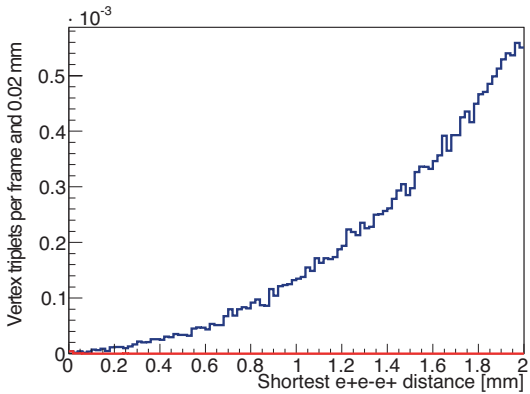


Figure 9.5: Shortest distance containing three vertices consistent with $e^+e^-e^+$ inside a readout frame with 10 tracks on average (phase IB). Note that every crossing of a simulated electron/positron track is counted as a vertex; charge assignments are made purely on the apparent curvature, i.e. recurling positrons are counted as electrons. The red histogram shows the contribution from internal conversion decays.

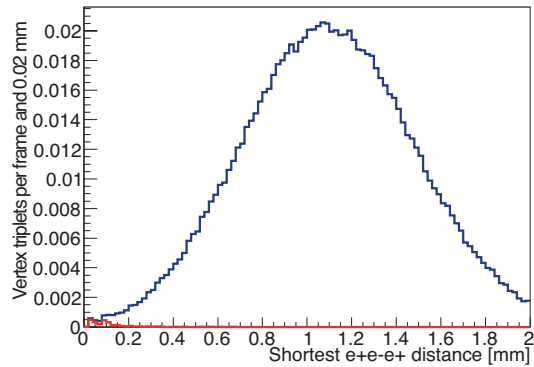


Figure 9.7: Shortest distance containing three vertices consistent with $e^+e^-e^+$ inside a readout frame with 100 tracks on average (phase II). Note that every crossing of a simulated electron/positron track is counted as a vertex; charge assignments are made purely on the apparent curvature, i.e. recurling positrons are counted as electrons. The red histogram shows the contribution from internal conversion decays.



9.3.2 ACTIVE TARGET

We have also considered the use of our Kapton-sensor assemblies (see chapter 10) as an active target. This would lead to a vertex separation ability in the order of the pixel size ($80\ \mu\text{m}$), as opposed to the $\approx 200\ \mu\text{m}$ expected from track extrapolation. At an appropriate inclination angle, a wedge of two chips with $6 \times 2\ \text{cm}^2$ active area and $50\ \mu\text{m}$ thickness presents a comparable amount of material to the beam (however, the cabling and cooling required would add significant additional material

at least in the downstream direction). Such an arrangement would sacrifice ϕ -symmetry.

The hit rate expected in an active target exceeds $3\ \text{GHz}$ for high intensity running, corresponding to about $8\ \text{kHz}$ per pixel, or $500\ \text{MHz}$ per reticle, far beyond the $80\ \text{MHz}$ expected in the innermost sensor layer. This in turn would necessitate the development of a completely new read-out block for the sensor chips. The gain in selectivity when going from $\approx 200\ \mu\text{m}$ vertex resolution to $80\ \mu\text{m}$ does not justify the cost and technical risks associated with the active target.



THE MU3E PIXEL DETECTOR

The Mu3e pixel tracker is to be built from High-Voltage Monolithic Active Pixel Sensors (HV-MAPS) thinned to $50\ \mu\text{m}$. Signal and power lines are aluminum traces on a Kapton flex-print, which, together with a Kapton prism, also serves as a support structure. The detector should be cooled with gaseous helium.

10.1 HV-Maps Sensor

We propose to use Monolithic Active Pixel Sensors (MAPS) as tracking detectors as they integrate sensor and readout functionalities in the same device and thus greatly reduce the material budget. Classical concepts like hybrid designs have usually a higher material budget due to additional interconnects (bonds) and extra readout chips, which compromise the track reconstruction performance especially at low track momentum.

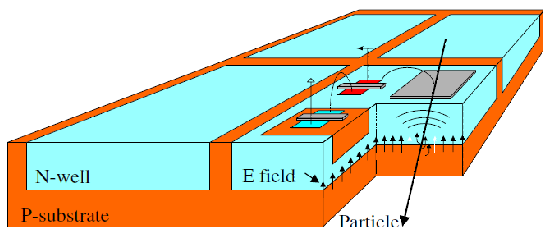


Figure 10.1: Sketch of the MAPS detector design from [127].

In the first MAPS designs ionization charges were collected mainly by diffusion with a timing constant of several hundreds of nanoseconds.

MAPS designs with high bias voltages exceeding $50\ \text{V}$, however overcome this problem by collecting charges via drift and provide timing resolutions of better than $10\ \text{ns}$.

We propose to use the High Voltage MAPS design with the amplifier electronics completely implemented inside the deep pixel N-well, which was first proposed in [127] and since successfully tested [128, 129], see also section 10.4.

Figure 10.1 shows a sketch of a Monolithic Pixel Detector. The readout circuitry allows an efficient zero suppression of pixel information and the implementation of timestamps to facilitate the assignments of hits between different pixel layers.

For readout designs providing $50 - 100\ \text{ns}$ timing resolutions power consumptions of about $150\ \text{mW}/\text{cm}^2$ are expected [130].

Because of the small size of the active depletion zone, the detectors can be thinned down to $50\ \mu\text{m}$ or less. By thinning, the material budget can be significantly reduced and becomes, averaged over the tracking volume comparable to ordinary gaseous detectors.

A further advantage is that HV-MAPS can be implemented in a “cheap” commercial process. We use the AMS/IBM $180\ \text{nm}$ HV-CMOS process [131], which was developed mainly for the automotive industry, and thus offers long-term availability as well as being specified for a very wide range of operating conditions. The process offers a maximum reticle size of $2 \times 2\ \text{cm}^2$. One of the few disadvantages of the process is the fact that the first metalization layer is in copper, thus introducing a small amount of medium Z material. There are however plans for replacing also



	Small Sensor	Large Sensor
Pixel Size [μm^2]	80×80	80×80
Sensor Size [cm^2]	1.1×2	2×2
Assembly	1×3	1×3
Assembly size [cm^2]	1.1×6	2×6
Max. LVDS links	4	2
Bandwidth [Gbit/s]	3.2	1.6

Table 10.1: Sensor specifications

that layer with an aluminium metalization in a future version of the process.

Radiation-tolerance studies of the HV-MAPS sensors in 180 nm technology are ongoing also on other projects (e.g. ATLAS pixel R&D). Several test chips with similar pixel electronics as MUPIX have been irradiated at PS (CERN) up to doses between 80 and 430 MRad (the latest corresponds to a fluence of nearly $1 \cdot 10^{16}$ neq/ cm^2). The results are promising. Despite of the use of standard NMOS layouts, the chip irradiated to 80 MRad still detects the particles radiated by a ^{90}Sr source. The setup irradiated to 430 MRad is strongly activated, and no accurate detection of ^{90}Sr signals is possible. The chip was able to detect particles from the beam up to 410 MRad dose. The main radiation effect is that the electronics suffers from ionizing effects such that it is difficult to find a proper operation point for the pixel amplifier. As the Mu3e experiment is performed at a muon beam-line the requirements on radiation hardness are not comparable to those at hadron colliders like the LHC. The radiation tests of the HV-MAPS sensors done so far all indicated that there will be no radiation damage even at highest muon rates at phase II.

10.2 Sensor specification

We plan to use two types of sensors in the Mu3e experiment, a smaller one for the inner layers and a larger one for the outer layers, see Table 10.1. The pixel size is $80 \times 80 \mu\text{m}^2$, much smaller than the multiple scattering contribution.

The wafers are to be thinned to $50 \mu\text{m}$. If the yields permit it, we will cut strips of three subsequent sensors from the wafers and mount them in one piece.

The sensor output is zero suppressed and consist of time-stamps and addresses of hit pixels,

serialized on a 800 Mbit/s low voltage digital signaling (LVDS) link. The sensor is configured via a JTAG interface [132]. Including supply voltages, we expect about 30 pads (and thus bond wires) to connect the chip to the Kapton flex-print.

10.3 Path towards the Full Sensor

10.3.1 THE MUPIX PROTOTYPES

First purpose-built sensor prototypes (the MUPIX series of chips) became available in 2011.

MUPIX1 and 2

The MUPIX 1 and 2 are small demonstration prototypes with a matrix of 42×36 pixels of $30 \times 39 \mu\text{m}^2$ size for an active area of approximately 1.8mm^2 , see Figures 10.2 and 10.4. Each pixel consists of the sensor diode, a charge-sensitive amplifier and a source follower to drive the signal to the chip periphery. In addition there is a capacity allowing to inject test charges. On the periphery, a comparator turns the analog signal into a digital time-over-threshold (ToT) signal. The threshold of the comparators is set globally for the chip and adjusted pixel-per-pixel with a 4-bit tune digital to analog converter (DAC). See Figure 10.3 for an overview of the pixel electronics. In the test chips, the comparator output of an individual pixel can be observed via a dedicated output line. Alternatively, the whole chip can be read out via a shift register, where all the available information is whether a particular pixel saw a signal during an active gate.

The MUPIX 1 chip had an issue with feedback in the comparator that occasionally led to double pulses. This issue has been fixed in MUPIX 2, which in addition contains temperature sensors.

MUPIX3

In August 2012, we submitted the MUPIX 3 chip, a major step towards the final sensor. The new chip has 40×32 pixels of $92 \times 80 \mu\text{m}^2$ size for an active area of approximately 9.4mm^2 , see Figure 10.5. It implements the full digital column logic, allowing for address generation and serial readout of zero-suppressed data. In addition, MUPIX3 has faster signal shaping.

The main differences with the final sensor are the lack of a high-speed LVDS output, buffers in

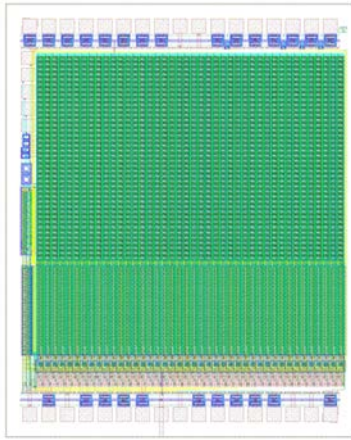


Figure 10.2: Design view of the MUPIX2 chip (actual size about 1.8 by 2.5 mm).

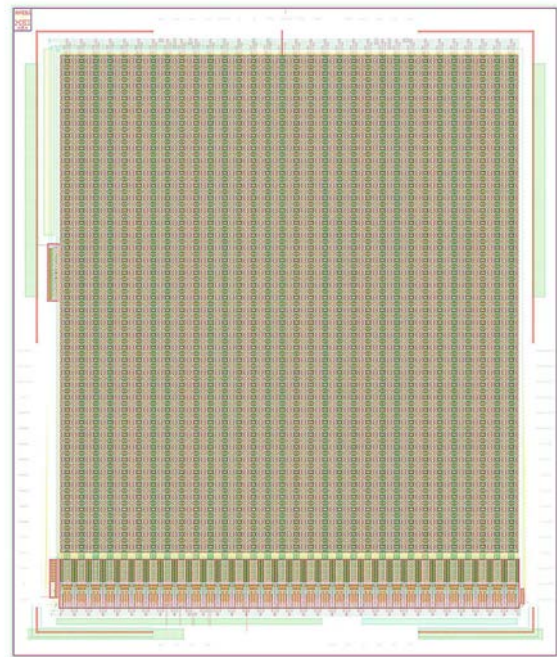


Figure 10.5: Design view of the MUPIX3 chip (actual size about 4 by 5 mm).

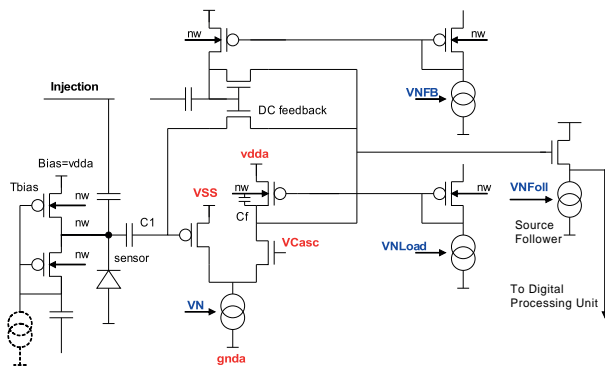


Figure 10.3: Schematic of the pixel cell analog electronics in the MUPIX chips. *nw* stands for n-well.

the columns and the chip-wide hit collection logic. For this prototype, the corresponding logic will be emulated off-chip in an FPGA. Also several control voltages which should be generated on-chip in the final version are currently produced on a test printed circuit board (PCB) in order to allow for easier debugging.

We have just received the first MUPIX 3 samples. First test results will become available early 2013.

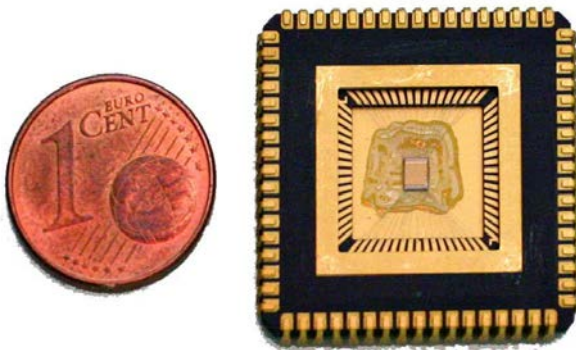


Figure 10.4: MUPIX2 sensor on ceramic carrier with one Euro-cent for scale comparison.

10.3.2 PLANS FOR 2013

As soon as the first results from the MUPIX 3 sensor are available, we will prepare another multi-project-wafer (MPW) run, implementing the remaining digital logic and addressing potential issues discovered with MUPIX 3. This should clear the path for an engineering run in the second half of 2013, opening up the possibility to build a full scale tracker prototype.



10.4 Characterization of the Prototypes

We have studied the properties of the MUIPX 1 and 2 prototypes using injection pulses, LEDs, laser diodes, X-rays, radioactive sources and test beam measurements. In the following, we will outline the core results; details of the findings can be found in a master [133] and a bachelor thesis [134].

The test setup was based on a test board housing the chip itself and a logic interface card. The chip test board has voltage regulators for the supply voltages, digital to analog converters for the threshold and injection pulse height and a flat ribbon connector to the logic interface card. This interface card uses a FPGA both to program and readout the MUIPX chip and to communicate with a PC via USB. These two boards together with a C++ control software have been used for all tests described here.

10.4.1 SIGNAL TO NOISE RATIO

Injection pulses can simulate the charge deposition of ionizing particles. A scan of the injection pulse height at constant threshold would deliver a step function if no noise were present. Due to the additional noise on top of the injection pulse the step function is transformed to an error function with a finite slope. In turn the width of the step function can be used to determine the noise as a function of the applied threshold. A ^{55}Fe source has been used as reference signal for the determination of the signal to noise ratio (SNR). The injection pulse height corresponding to the ^{55}Fe signal is found by matching the time over threshold of both signals at a given threshold. For the MUIPX 2 chip the signal to noise ratio as a function of threshold ranges between 21.5 and 35.7, see Figure 10.6. Any signal to noise ratio >9 is considered good.

10.4.2 PIXEL TO PIXEL UNIFORMITY

Using a similar method as for the measurement of the signal to noise ratio, the pixel to pixel uniformity can be determined and optimized. At a constant injection pulse height a scan of the threshold setting for the entire pixel matrix is carried out. For each pixel the error function fit is performed and the 50% value of the error function rising edge plotted, see Figure 10.7a). As can

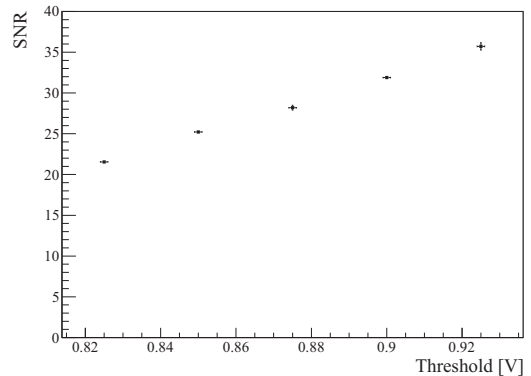


Figure 10.6: Signal to noise rate for the MUIPX 2 chip. The signal size is taken from measurements with a ^{55}Fe source, whilst the noise is measured in a injection pulse scan, see [133] for details.

be seen in Figure 10.7c) the distribution of the threshold values for the pixels of the same chip is quite broad. In order to compensate for these inequalities, a threshold offset, the so called tune DAC (TDAC) value can be set for each pixel. The best TDAC values for the pixels are found by running an automated procedure, see [133]. Figure 10.7b) and d) show that the threshold spread (reflecting the response uniformity) after tuning the threshold offsets has decreased by almost an order of magnitude from 19.6 mV to 2.3 mV RMS.

10.4.3 PIXEL RESPONSE TIME

The timing characteristics of the MUIPX chip is very important because of the requirement to run at high muon decay rates. A fast response of the MUIPX chip leads to precise timing of hits and helps suppressing combinatorial background. In the inner detector layers the double pulse resolution should be good as the hit rate is up to 2 kHz for each pixel.

Timing studies have been carried out using a LED driven by a pulse generator to stimulate the sensor. The discriminator output of a single pixel is then compared to the second output of the pulse generator on an oscilloscope. In this configuration it is possible to measure the latency between generator and pixel output and the time over threshold (ToT) of the pixel. By plotting latency and ToT for many threshold values one obtains the pulse shape, see Figure 10.8. The measured pulse shape reflects the RC-CR shaping

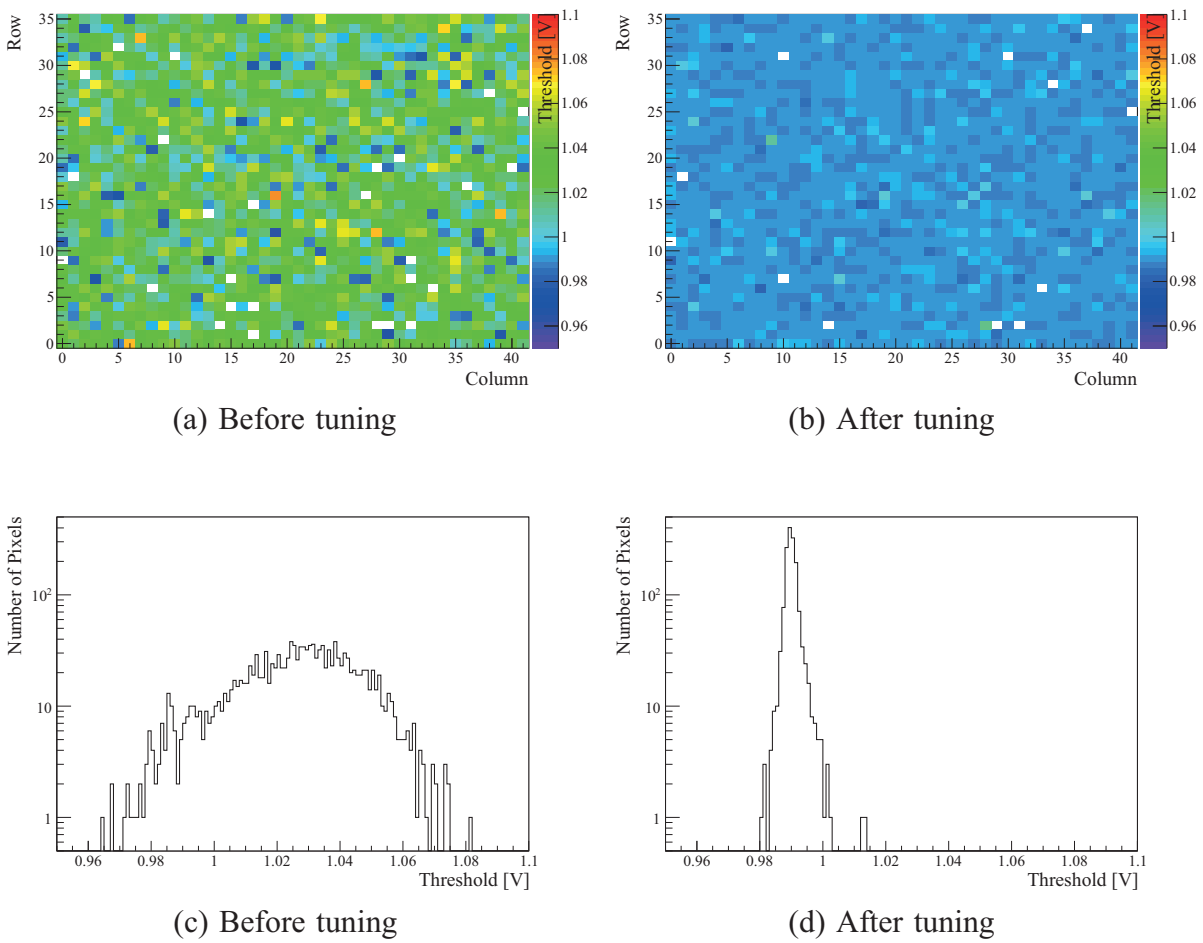


Figure 10.7: Uniformity of the pixel response before and after tuning of the pixel DAC values, from [133].

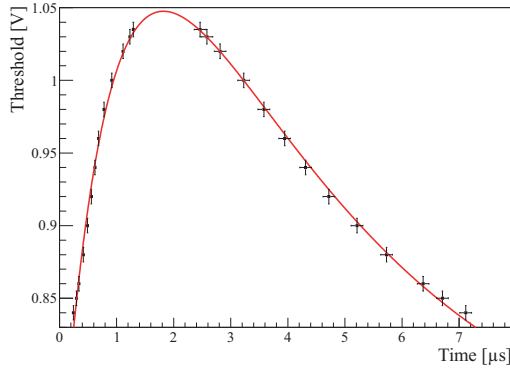


Figure 10.8: Measured pulse shape of a MUIPX pixel in response to an LED pulse, fitted with the expectation from $RC - CR$ shaping, from [133].

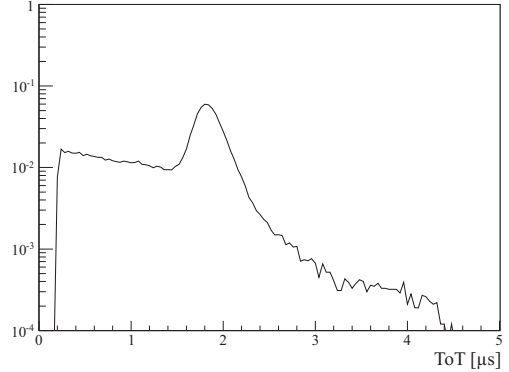


Figure 10.10: Time-over-threshold (corresponding to energy) spectrum of a ^{55}Fe radioactive source, from [133].

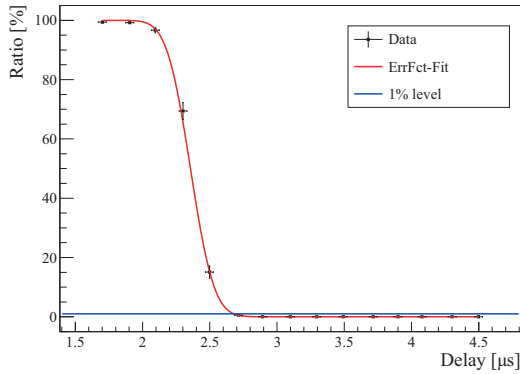


Figure 10.9: Double pulse resolution of the MUIPX2 chip, from [133].

characteristic of the pixel electronics. The charge collection process in the depletion zone is much faster and has little influence on the measured timing.

By generating double pulses and dividing the number of unresolved pulses at the pixel output by the number of all pulses, the double pulse resolution can be determined. Figure 10.9 shows this ratio as a function of pulse to pulse delay. An error function has been fitted and the point of 1% un-resolved pulses gives a double pulse resolution of $2.7 \mu\text{s}$ consistent with the expectation from the chosen shaper characteristics.

10.4.4 MEASUREMENTS WITH RADIOACTIVE SOURCES

Radioactive sources allow to test the MUIPX chips with real particles. For a ^{55}Fe source the time over threshold (ToT) distribution, which is an measure for the energy distribution, is shown in Figure 10.10. X-ray fluorescence in the range of 4 to 18 keV has been used to derive a relative energy resolution of 10 to 20 %.

The ^{55}Fe peak in the ToT spectrum has been used to study the influence high voltage (HV) and temperature on the pixel signal. Figure 10.11 shows the ^{55}Fe peak as a function of the HV, revealing first a steep rise as the depletion zone grows. Between 20 and 60 V, the ToT stays almost constant. At even higher voltages the electric field in the depletion zone becomes strong enough for the creation of secondary electron-hole pairs, which results in a signal amplification. The temperature dependence of the pixel sensor is important, because in the later experiment the different parts of the detector will operate at different temperatures varying by 30-40 °C. In Figure 10.12 the ^{55}Fe peak of the ToT spectrum is plotted as a function of temperature between 20 to 60 °C. As can be seen the ToT goes down from 1.6 to below $1 \mu\text{s}$, with a slope of $16.3 \text{ ns}/^\circ\text{C}$. Measurements with test pulse injection and simulation studies confirm that the observed temperature dependence is a feature of the charge sensitive amplifier of the pixel analog stage.

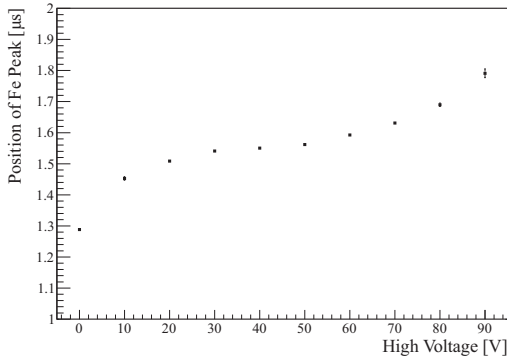


Figure 10.11: Position of the ^{55}Fe peak in dependence of the applied high voltage, from [133].

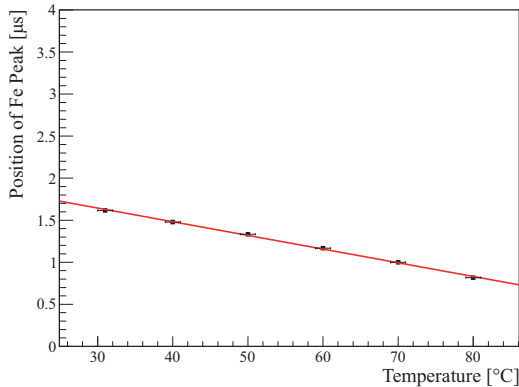


Figure 10.12: Temperature dependence of the position of the ^{55}Fe peak, from [133].

10.4.5 TESTBEAM RESULTS

In August 2012 the MUPIX2 chip was tested at the CERN SPS. The beam from the SPS was a 170 GeV pion beam, chosen for little multiple scattering effects due to the device under test (DUT). In two separate data taking periods the MUPIX2 was mounted inside the TimePix telescope [135]. This silicon pixel telescope has four layers before and four layers after the DUT, providing very precise pointing resolution of $5\ \mu\text{m}$. The MUPIX2 chip was tested facing the beam and under an angle of 45° . For both beam periods a threshold scan was performed in order to derive the efficiency as a function of threshold, but no threshold calibration to equalize the gain of the pixels was performed. Figure 10.13 shows the resolution in x and y direction of the MUPIX2 chip facing the

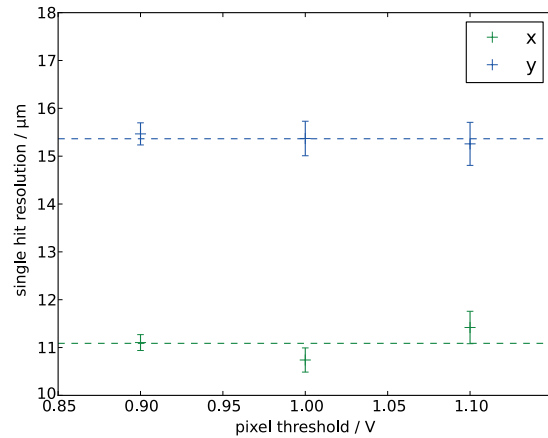


Figure 10.13: Resolution of the MUPIX 2 chip measured in a testbeam with 170 GeV pions and the TIMEPIX telescope. The measured resolutions correspond very well to the expectation from the $5\ \mu\text{m}$ resolution of the telescope and the pixel pitch in x and y direction, respectively.

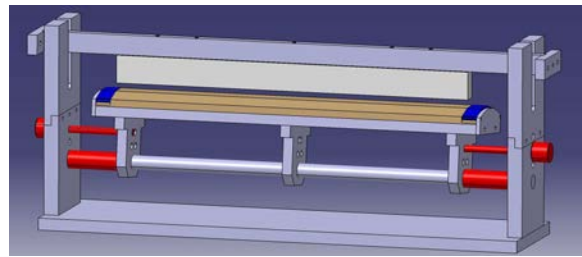


Figure 10.14: Tool for layer 3 segment assembly.

beam and tested at three different threshold values. The measured resolution of $11.2\ \mu\text{m}$ in x and $15.4\ \mu\text{m}$ in y corresponds to the expected resolution given the telescope resolution and the pixel size. Further results are still subject to studies and will follow soon.

10.5 Mechanics

The pixel detector mechanics has been optimized for very low material budget in the active detector region. Additional requirements are mechanical stability, resistance to temperatures over a wide range and a modular design for ease of assembly and repair. It is proposed to build the frame for the silicon pixel detector from thin Kapton foil. The sensors are glued and bonded on a flex-print and then mounted onto the Kapton frame.



Figure 10.15: Tool for layer 3 segment assembly.

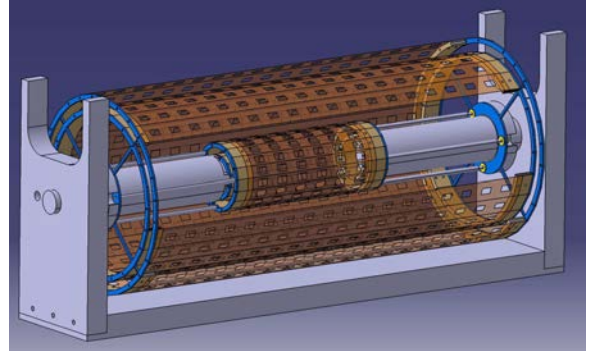


Figure 10.18: Mounting tool for the central pixel detector.

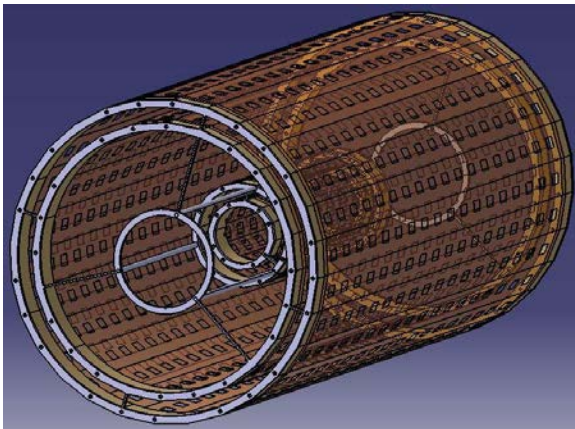


Figure 10.16: Mechanics of the central pixel detector

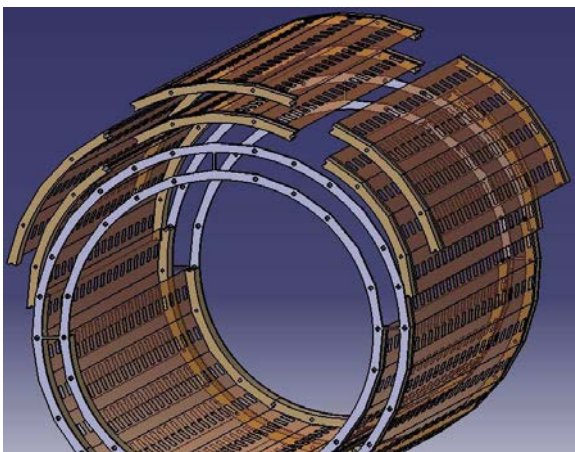


Figure 10.17: Segmentation of the central outer layers.

The Kapton foil used for the mechanical frame construction is $25\ \mu\text{m}$ thin. It gains in mechanical stability as it is folded around a prism-shaped template and glued to plastic end-pieces. For this process tools have been built, which support the detector modules until they are ready for full station assembly, see Figures 10.14 and 10.15. In a separate tool the $50\ \mu\text{m}$ thin pixel chips are glued on the single layer Kapton flex-print. Alignment grooves secure the correct position of the chips. In the next step the chips are wire bonded to the flex print. With a vacuum lift tool the flex-prints are then positioned and glued to the mechanical frames. The radiation length of a pixel detector layer is summarized in Table 10.2.

The pixel detector is built from layers of four different sizes and prism shapes, see Figure 10.16. As the digital readout circuits of the pixel chips create an approximately $0.5\ \text{mm}$ wide dead area, there is a $1\ \text{mm}$ overlap to the adjacent sensor. The inner double layers have $12\ \text{cm}$ active length. Layer 1 has 12 and layer 2 18 sides of $1\ \text{cm}$ width. Each inner layer is assembled from two half-modules. As a consequence the plastic end-pieces are half moon shaped. When all four half modules of the inner detector layers are produced and tested they are mounted to two thin rim wheels. A mechanical prototype for the inner double layer has been constructed from $25\ \mu\text{m}$ Kapton foil both for the frame and the flex-print layer, while the pixel chips have been simulated with $100\ \mu\text{m}$ thick glass plates. Glass of $100\ \mu\text{m}$ thickness is of comparable flexibility as thinned silicon, which is shown in Figure 10.19. The resulting mechanical unit is surprisingly sturdy and fully self supporting, as can be seen in Figure



COMPONENT	THICKNESS [μm]	X/X ₀ [%]
Kapton frame	25	0.018
Kapton flex-print	25	0.018
Aluminum traces (50 % coverage)	15/2	0.008
HV-MAPS	50	0.053
Adhesive	10	0.003
Full detector layer	125	0.100

Table 10.2: The pixel detector layer radiation length is dominated by the HV-MAPS chips.

10.20. Layer 3 and layer 4 have a three times larger active length of 36 cm. The sides of these outer layers are 19 mm wide. The layers 3 and 4 have 24 and 28 sides. An outer double layer module combines four sides, so layer 3 consists of 6 and layer 4 consists of 7 modules, see Figure 10.17. The station assembly is done in a special mounting frame, combining the inner two layers with the modules of the outer two layers on large rim wheels (Figure 10.18). Re-curl stations will be assembled accordingly.

10.6 Cooling

The cooling system for the pixel detector must be capable of keeping the temperatures at a reasonable level ($\leq 70^\circ\text{C}$) and should at the same time add very little extra material to the active volume of the detector. Cooling with gaseous helium has been chosen as it appears to offer a reasonable compromise between cooling potential and radiation length.

Given its size, the heat load introduced by the pixel detector is considerable. Table 10.3 details the contributions of the different parts of the pixel detector assuming a realistic heat load of 150 mW/cm^2 . It is worth mentioning that the heat load is strongly dependent on the clock speed at which the pixel chips are running. Pixel chips with very low occupancy, for example those installed in the recurl stations, could optionally be operated at half the clock speed which would largely reduce the total thermal power of the pixel detector.

In order to keep the temperature of the coolant equally low in all parts of the detector, it is fore-

DETECTOR PART	SIZE [cm^2]	power [W]
layer 1	158.4	23
layer 2	237.6	35
vertex layers (1+2)	396	59
layer 3	1728	259
layer 4	2016	302
outer layers (3+4)	3744	561
central detector (1-4)	4140	621
detector with 2 recurl stations	11628	1744
full detector	19116	2867

Table 10.3: Pixel detector heat load for 150 mW/cm^2

seen to place nozzles between the support structures pointing at different parts of the sensor layers.

In order to study the potential of gaseous helium cooling a bachelor thesis has been carried out [136]. In this thesis a thin sandwich of aluminum foil, Kapton and silicon was heated inductively and cooled with a helium flow. For the 8.5 cm long sample heated with 100 mW/cm^2 a flow of 0.4 m/s was necessary to maintain a temperature difference between helium and sensor of 32 K . Further studies using a full scale central detector prototype in a wind tunnel are on the way. This full scale prototype will be assembled from aluminized Kapton foil such that Ohmic heating can be applied. It is planned to run the upcoming tests with the helium heat exchanger acquired for phase I of the experiment.

10.7 Alternative Technologies

Since the Mu3e pixel detector plays the key role in the experiment, it is important to carefully compare the chosen HV-MAPS technology with alternatives. To do so one has to have the detector requirements in mind, see chapter 5. The goal of a branching ratio sensitivity of 10^{-16} leads to a high muon decay rate on target of $2 \cdot 10^9\text{ Hz}$. In order to suppress combinatorial background a very good vertex resolution of $\mathcal{O}(200\text{ }\mu\text{m})$ is needed. The suppression of the background from the conversion decay $\mu \rightarrow eee\nu\nu$ requires very precise momentum reconstruction of better than 0.5 MeV , for the 10^{-16} branching ratio sensitivity. The



Figure 10.19: A 50 μm thin silicon wafer.



Figure 10.20: Mechanical prototype of the inner pixel layers. Thin glass plates replace the silicon chips.



momentum resolution for the low energetic decay products of 10 MeV to 53 MeV will be governed by the multiple scattering in the detector. Only concepts with extremely low radiation length of $<1\%$ in total can achieve this.

In the following different technology options for the *Mu3e* tracking detector are compared. The result of this comparison is summarized in table 10.4.

10.7.1 TIME-PROJECTION CHAMBER

Time projection chambers are a very attractive concept for tracking detectors with good spacial resolution and very low radiation length. The example of the ALICE TPC [137] has demonstrated that very high track densities can be handled with such a detector. Over the last two decades many studies for TPCs with very low radiation length, i.e. 0.12% for a proposed chamber at SLAC [138], have been carried out. The drift time of an electron in a possible TPC for the *Mu3e* experiment with 2m total length would be in the order of $50\mu\text{s}$, using the proposed gas mixture of Helium:CO₂:Isobutane (83:10:7%). This time of $50\mu\text{s}$ at $2 \cdot 10^9$ Hz decay rate means that the DAQ and event filter farm would have to handle frames containing $>10^5$ muon decays, which is not realistic. Another problem would be strong space charge effects due to continuous very high track density, see [139]. These two aspects rule out the usage of a TPC in the phase IB and phase II of *Mu3e*, while it would be possible to use a TPC in phase IA.

10.7.2 OTHER PIXEL TECHNOLOGIES

The usage of pixel detectors in particle and heavy-ion physics has recently lead to a variety of thin detectors capable of dealing with high particle fluxes. It is worth to discuss the solutions developed for the upgrades of the STAR, BELLE and LHCb vertex detectors.

The STAR upgrade vertex detector [140] is based on Monolithic Active Pixel Sensors (MAPS), more precisely the MIMOSA 28 sensor [141]. The vertex detector under construction is located around the interaction point at $r=2.5$ cm, 8 cm and has an intrinsic hit resolution of $<6\mu\text{m}$. An ultralight carbon fibre support structure has been developed with a thickness of $200\mu\text{m}$. The radiation length is $X/X_0=0.079\%$ per layer in the active region. The power dissipation is about

$170\text{mW}/\text{cm}^2$ and forced air cooling at 10 m/s is used [142]. The charge collection for the MIMOSA chips is based on electron diffusion, resulting in charge collection times of 50 ns. This has to be compared to the charge collection times of drift based silicon detectors like silicon strip and hybrid silicon pixel detectors of a few ns. The signal integration of the MIMOSA 28 chip is $185.6\mu\text{s}$. This long integration time corresponding to $>10^5$ decay events rules out the usage of the MAPS developed for STAR vertex upgrade in *Mu3e*,

Belle2 is building a lightweight silicon vertex tracker based on DEPFET pixel sensors [43]. The Belle2 silicon vertex detector has two layers at $r=1.4$ cm, 2.2 cm. The monolithic sensors are only $75\mu\text{m}$ thick and self supporting, resulting in a radiation length of $X/X_0=0.18\%$ per layer [143]. The cooling system uses liquid CO₂ for the readout electronics and cold dry air with forced convection for the sensors. The sensor chip is equipped with an integrated read out amplification, the charge is then accumulated internally. The readout is enabled externally and done in a row wise rolling shutter mode. The readout time for the entire chip is $20\mu\text{s}$. As for the MIMOSA 28 sensor the relatively long readout time makes the Belle2 DEPFET sensor unsuitable for the *Mu3e* detector. On top of this the Belle2 DEPFET sensor produces analog output signals and requires further electronics for analog to digital conversion, baseline subtraction, discrimination and zero-suppression.

The proposed pixel detector for the LHCb vertex upgrade belongs to the TIMEPIX family of chips. The main goal of the LHCb upgrade is to move from a 1 MHz readout to a 40 MHz readout in order to make a track based L0-trigger possible. The power consumption per chip is $1.5\text{W}/\text{cm}^2$ [144], which is quite high. The sensor thickness is $150\mu\text{m}$ to $200\mu\text{m}$. The LHCb Velo upgrade pixel sensor is a hybrid design, so in addition to the sensor there is also the readout chip thickness, the solder bump bonds, aluminum traces and cooling elements summing up to $X/X_0=0.73\%$ per layer. In LHCb the vertex detector is inside a vacuum tank around the interaction point, so the cooling scheme relies on a high thermally conductive spine (diamond) in combination with a liquid CO₂ cooling outside the active area. Alternative cooling studies look at micro-channel cooling which would extend the CO₂ cooling to the pixel chips in the active area. The pixel sensor is designed to



PARAMETER	required	Mu3E		STAR	BELLE	LHCb
		HV-MAPS	He TPC	MIMOSA28	DEPFET	VELOPIX
sensor thickness X/X_0 [%]	≤ 0.1	0.075	-	0.079	0.18	0.73
readout cycle [μ s]	≤ 0.1	0.05	50	185.6	20	0.025
power [mW/cm^2]	≤ 200	150	-	170	100	1500

Table 10.4: Alternative technology comparison, only the crucial parameters are listed.

have less than 25 ns time-walk at 1000 electrons. The output bandwidth is > 12 Gbit/s with on-chip zero suppression. The readout is hit driven and asynchronous. While the readout speed would be ideal for the Mu3e detector, the radiation length per layer of $X/X_0=0.73\%$ is too high.

10.7.3 CONCLUSION

In the field of tracking detectors with good resolution, low radiation length and high rate capabilities there has been a very strong progress in the recent years, see Table 10.4. Time projection chambers with helium gas mixtures would provide excellent momentum resolution. Because of the very long drift times in a large TPC and the constantly high muon decay rates, it is not possible to do online track reconstruction in the event filter

farm for decay rates exceeding $1 \cdot 10^7$ Hz, which corresponds to phase IA of the Mu3e running. As a change of technology between phases IA and IB is not desirable, the TPC option can only be considered as a back-up solution.

The above discussed pixel alternatives can be grouped in two categories. The systems based on the MIMOSA chip for the STAR upgrade and the DEPFET chip for Belle 2 have little radiation length of $X/X_0=0.079\%$ and 0.18% per layer, but have long readout cycles. On the other hand the VeloPix based tracker for the LHCb upgrade can be read out at 40 MHz, but has a relatively large radiation length of $X/X_0=0.73\%$ per layer. In all three cases further R&D would be required to transform the existing designs into one fulfilling the requirements of all phases of the Mu3e experiment.



THE MU3E FIBRE DETECTOR

11.1 The time of flight detector

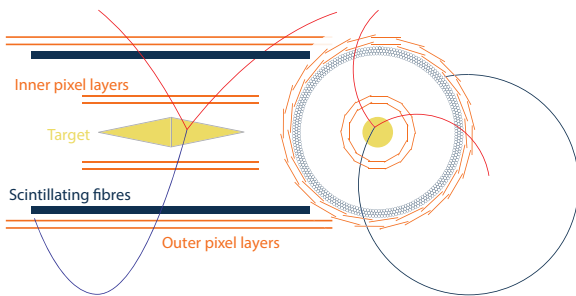


Figure 11.1: Schematic side view (*left*) and cross section (*right*) of the detector components. The Sci-Fi system is highlighted in blue.

A cylindrical time of flight (ToF) detector complements the central silicon tracking system. It consists of a scintillating fibre (Sci-Fi) hodoscope with a radius of 6 cm and a length of 36 cm. The expected time resolution is of several 100 ps and a detection efficiency close to 100 %. The main purpose of the ToF system is to measure very precisely the arrival time of particles in order to allow for the matching with hits detected in the silicon detectors. This will help to reject pile-up events (accidental backgrounds) and allow for a charge (direction of propagation) measurement for recurling tracks. The ToF system will operate at very high particle rates up to several MHz per channel.

A detailed R&D program is ongoing to prove the feasibility of the Sci-Fi detector and to help optimizing the design of the Sci-Fi detector. The R&D activity covers all the aspects of the ToF

detector development: scintillating fibres, SiPMs, amplifiers, and readout electronics. The challenging aspects of the ToF system are (i) the high rates per Sci-Fi readout channel and (ii) the large data flow generated by the readout digitizing electronics, which has to be handled in real time. Time resolutions of about 200 to 300 ps have been already achieved with Sci-Fi hodoscopes with single-ended readout using multi-anode PMTs [145]. We aim at a similar time resolution.

In the current design, the scintillating fibre detector is composed of 24 Sci-Fi ribbons, each 36 cm long and 16 mm wide, as illustrated in Figure 11.2. The ribbons will be supported by a carbon fibre mechanical structure. The use of 250 μm diameter multi-cladding scintillating fibres produced by Kuraray is envisaged. Three to five Sci-Fi layers (Figure 11.2 right) are staggered such as to minimize empty spaces between fibres. Figure 11.3 shows a Sci-Fi ribbon and its cross section. In the figure the uniform staggering of the Sci-Fi layers can be seen. The overall thickness of the Sci-Fi arrays varies depending on the number of layers between 0.6 to 1 mm. This thickness has to be kept as low as possible, to reduce the multiple scattering to a minimum compatible with the required performance (i.e. time resolution and efficiency). The empty space between adjacent ribbons will be minimized in order to guarantee continuous coverage.

The scintillating light produced in the fibres will be detected with SiPM arrays at both fibre ends. The choice of SiPMs as a photo-detection device is based on the fact that they are very compact ob-

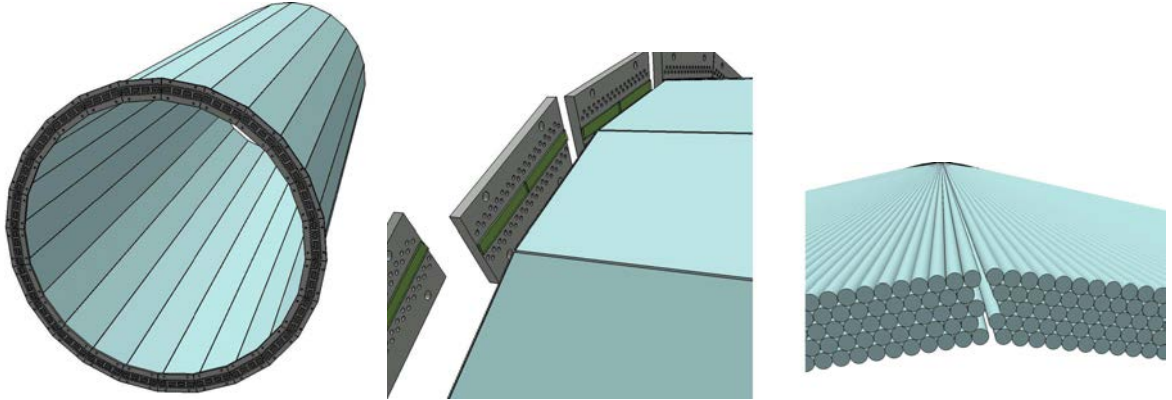


Figure 11.2: *Left*: Overall view of the Sci-Fi barrel ToF detector. The diameter of the detector is about 12 cm, the length about 36 cm. *Middle*: Detail showing the SiPM ceramic supports and the Sci-Fi arrays. *Right*: Details of the Sci-Fi ribbons. In this figure, the ribbons consist of five staggered Sci-Fi layers.

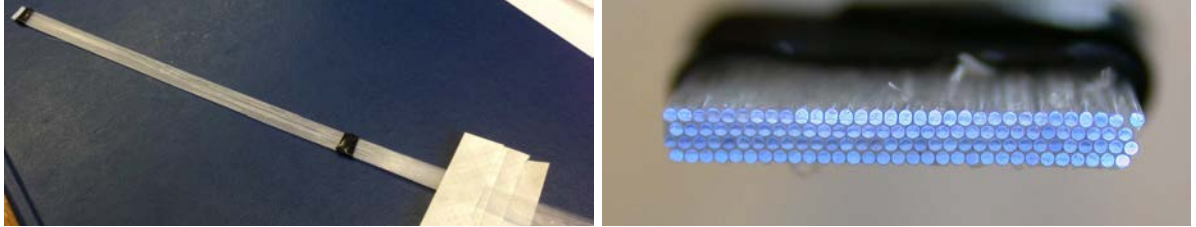


Figure 11.3: Photos of a Sci-Fi ribbon (*left*) and of its cross section (*right*). The uniform staggering of 4 Sci-Fi layers is clearly visible.

jects that can be operated in high magnetic fields with high gain ($\sim 10^6$) and at high counting rates.

Two different readout schemes for the fibres are being considered and investigated: 1) fibres are grouped in vertical columns (this is implemented by the structure of the readout photo-device), 2) each fibre is read out individually. In the first design we envisage to use the 32 channel SiPM arrays with $50 \times 50 \mu\text{m}^2$ pixels available from Hamamatsu [146, 147]. The active size of the sensor is $8 \times 1.1 \text{ mm}^2$ with a total surface of 9 mm^2 . The pixels are arranged in columns, corresponding to an effective pitch of $250 \mu\text{m}$. Two such SiPM sensors will be assembled side by side with almost no dead region, giving a 16 mm wide photosensitive region with 64 readout channels, and matching precisely the width of the Sci-Fi ribbons. The photo-detectors will be directly coupled to the Sci-Fi arrays to maximize the light collection efficiency, and consequently the timing performance. In total 96 SiPM arrays with 32 channels each will be required to readout the Sci-Fi tracker at each

end, for a total of $2 \times 24 \times 64$ (~ 3000) readout channels.

A detailed understanding of the expected occupancies in the the Sci-Fi detector is required. The rates depend also on the background in the detector generated by secondary interactions in the materials of the different components. A particle crossing the Sci-Fi ribbons at 90° , will excite one or two adjacent Sci-Fi columns, as sketched in Figure 11.4. A particle crossing the same Sci-Fi ribbon, for example at 45° , will excite 4 to 5 adjacent Sci-Fi columns for a 5 layer ribbon and 2 to 3 for a 3 layer ribbon, thus increasing significantly the overall occupancy of the detector. At an expected rate of $1.5 \cdot 10^9$ muon decays per second using 1500 Sci-Fi channels, the estimated rate in the Sci-Fi system is 5 MHz on average. At the same time the signal will be spread out over several SiPM channels. A well designed clustering algorithm will be required to reconstruct the timing and position of the crossing particle.

The lowest possible detector readout occupancy can be achieved by reading out each fibre indi-



vidually. In absence of dark current noise and background, the occupancy is given by the rate of detected electrons from muon decays and is expected to be 1 MHz per fibre. When reading out each multi-cladding fibre individually, one has to take into account that the scintillating light travels preferentially in the cladding of the fibre and exits the fibre in a cone with an aperture of about 45° . In order to collect all the scintillating light exiting the fibre, and thus ensure high detection efficiency, the photo-detector has to be wider than the fibre diameter, at least $100 \mu\text{m}$ around the fibre. This compensates also the misalignment, of the order of few tens of microns, between the fibres and the SiPMs. In order to avoid the light from one fibre to spill over to a neighboring photo-detector channel (optical cross-talk) the fibres and photo-detectors have to be separated by $500 \mu\text{m}$ center-to-center. To summarize, the estimated, optimal size of the photo-detector for reading out each $250 \mu\text{m}$ fibre individually is $400 \times 400 \mu\text{m}^2$ (for a square device), and a center-to-center separation of $500 \mu\text{m}$.

A transition region between the highly compact Sci-Fi ribbons and the photo-detectors of about 5 cm will be required to fan-out the Sci-Fis to the desired center-to-center separation of $500 \mu\text{m}$ before coupling the fibres to the SiPMs. To assure the precise alignment, the fibres will be glued in sockets with a precision of $10 \mu\text{m}$. The SiPMs will be coupled to the Sci-Fis using the same sockets. Reading out each fibre individually will require a total of about 9000 readout channels.

In case the SiPMs could not be coupled directly to the Sci-Fis (because of mechanical constraints inside the limited space), optical fibres coupled to the Sci-Fis will be used to transmit the scintillating light outside of the solenoid, where they will be coupled to the same type of SiPM arrays, however with some loss of light. In this case the use of multi-anode PMTs or multi-channel plate PMTs could be also envisaged as alternative photo-detector device to the SiPMs for the readout of the Sci-Fi ribbons.

Different manufacturers are also being investigated. The reported photo-detection efficiency of the Hamamatsu SiPMs is not that high (PDE $\sim 25\%$). Since the time resolution depends on the number of detected scintillating photons ($\sigma_\tau \sim 1/\sqrt{n_{\text{ph}}}$) in order to obtain the best timing performances we need to maximize the PDE of the SiPM arrays. Discussions with Hamamatsu to ex-

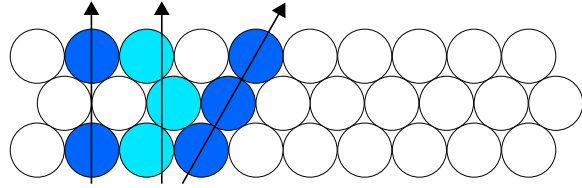


Figure 11.4: Sci-Fi occupancy vs. particle crossing angle and position. Dark fibres indicate higher energy deposit.

plore various possibilities to increase the PDE are ongoing. We will also discuss with other companies capable of producing such devices (we already contacted FBK in Italy and Ketek in Germany). Very likely it will be required to design SiPM sensors matching precisely the requirements of the Sci-Fi detector rather than using commercially available SiPMs.

Performance studies of Sci-Fi ribbons coupled to SiPM arrays will be carried out in test beams at PSI. The test beam activities will include the study of the time resolution, rate capabilities, detection efficiency, tracking resolution, and uniformity of the detector. Different readout electronics will be also tested.

11.2 Readout of photon detectors

For the readout of the SiPMs different options are being investigated. Details are given in chapter 13.

One possibility is to use the well-established waveform digitizing technology based on the DRS switched capacitor array chip developed at PSI. The advantage of this technology compared to traditional constant fraction discriminators and TDCs is that pile-up can be effectively recognized and corrected for. Due to the bulkiness of this readout electronics, the digitizing electronics cannot be located in the proximity of the Sci-Fi detector. To transmit the electrical pulses from the SiPMs to the digitizing electronics two options are being considered. In a first version the signals are transmitted without amplification on shielded low attenuation coaxial cables. Given the low amplitude of the pulses (1.5-2 mV per photo-electron) and potentially high noise from the digital readout electronics, the amplification of SiPM signals might be required. In this second version the pulses are first amplified about a factor

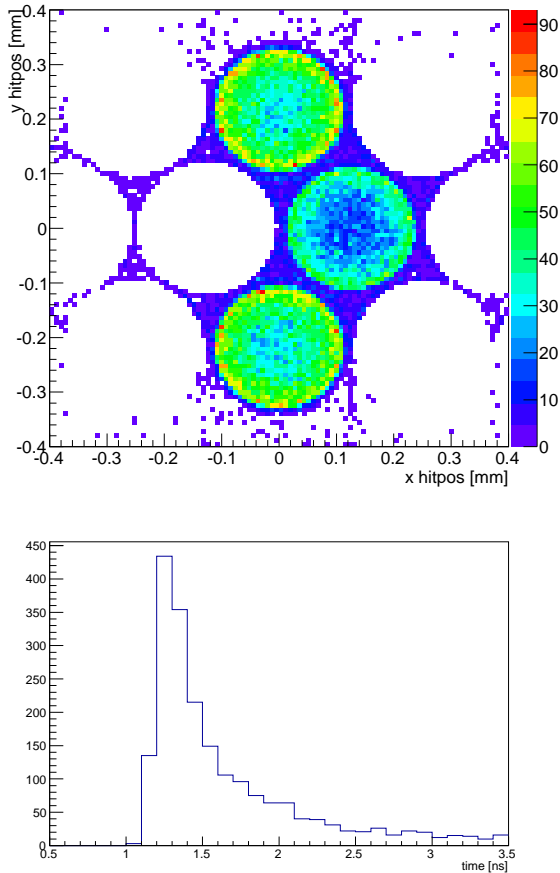


Figure 11.5: Simulated photon output integrated over 1000 positron crossing events for a specific fibre geometry (*top*) with the corresponding time distribution of the SiPM response using a constant fraction discriminator algorithm with a FWHM of about 300 ps (*bottom*).

of ten and then transmitted. Hybrid amplifier circuits will be installed on the other side of the SiPM mountings. We already developed fast amplifiers using transistors (rise time ~ 1 ns, decay time ~ 10 ns) matching the input characteristics of SiPMs for optimal time performance and high rates.

A second possibility is to use the STiC chip, which includes a fast discriminator and a TDC digitizing the time information. The advantage of this solution is the compactness of the chip that could be installed very close to the SiPMs, with no need to amplify and to transmit analog signals

outside of the solenoid. A third option could be offered by time to digital converters implemented in FPGAs.

11.3 GEANT simulations

To optimize the overall design of the detector and of the Sci-Fi sub-system in particular, extensive simulation studies are being carried out. We are exploring the propagation of scintillating light in the fibres in a dedicated simulation that allows to compare the optical properties for any possible fibre and ribbon geometry. Meanwhile a complete set of simulation tools is available which allows a profound analysis of the different possible layouts of the Sci-Fi system.

Ongoing simulation studies will help us to optimize and work out the details of the final Sci-Fi ToF design. Given that a crucial requirement of the experiment is to minimize all involved materials also a layer of reflecting paint or glue will add additional non active material to the detector and thus increase the overall material budget seen by the particles crossing the Sci-Fi ribbons, resulting in a deterioration of the overall momentum resolution of the tracking system. This and similar effects can now be studied easily with the available tools.

In combination with a simulation of the SiPM response [148], we are now able to estimate whether the aimed time resolution of a few hundred picoseconds is feasible with the fibre geometry and the SiPMs under investigation. First studies show that the resolution can be achieved with the baseline design (Figure 11.5). Further fibre geometries and readout combinations are currently being evaluated. In addition to the simulation test setups are being developed consisting of a complete ribbon with the SiPM detectors mounted on both ends to verify the simulation results and to get the prove whether the desired geometry can be constructed with reasonable effort. Furthermore the test stand will be used to evaluate readout electronics.

An additional source of concern is the cross talk and after pulsing observed in most APDs operated in Geiger mode. Both effects will lead to an increase of the occupancy of our electronics channels and thus have to be minimized. Since the Sci-Fi ribbons are read-out on both ends, this uncorrelated source of noise, in principle, can be rejected.



THE MU3E TILE DETECTOR

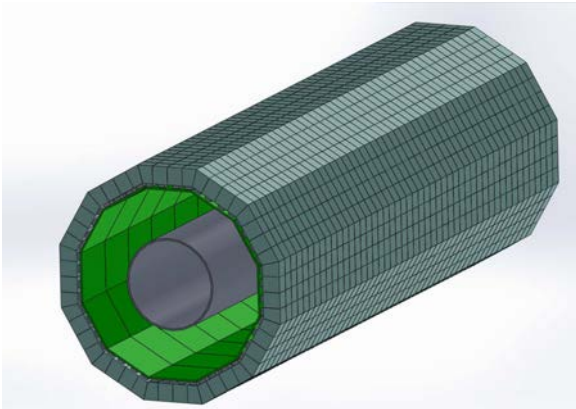


Figure 12.1: Drawing of a tile detector module with 48×48 tiles.

The second component of the Time-of-Flight hodoscope is a detector consisting of scintillating tiles which are, as in the case of the Sci-Fi tracker, read out by SiPMs. The tile detector is located in the recurl station on the inside of the recurl pixel layer (see Figure 6.5). The detector aims at a time resolution of below 100 ps and an efficiency close to 100% in order to effectively identify a coincident signal from three electrons and suppress combinatoric background. The main challenge of the detector design is to achieve these requirements under the high hit rate which is expected, especially in phase II.

12.1 Detector Design

The detector is divided into four modules (one for each recurl station) with a length of 36 cm and

diameter of ≈ 12 cm. Each module is segmented into small tiles with a size of $\mathcal{O}(1 \text{ cm}^3)$, which are individually wrapped in reflective foil in order to increase the light yield.

In the current design, each module consists of 48 rings with a thickness of 5 mm, and each ring consists of 48 tiles (see Figure 12.1). This results in a total number of 2304 tiles per station, and a tile geometry of roughly $7.5 \times 7.5 \times 5$ mm. For the outer two recurl stations, the number of tiles might be decreased to 36×36 due to the lower hit rate (see Figure 12.2), in order to reduce the costs. This detector geometry is the result of extensive simulation studies which will be continued in order to further optimize the detector performance.

The tiles are made of plastic scintillator material which provides a fast light response. The main requirements for the scintillator are a high light yield, fast rise and decay time and a scintillation spectrum which approximately matches the spectral sensitivity of the SiPM. Different scintillators have been compared using a Geant4 simulation in combination with a simulation of the SiPM response. The best suited scintillator was found to be BC420 from Bicron. However, the differences between the individual scintillating materials were found to be small, and thus also more inexpensive alternatives are feasible.

The scintillation light of each tile is read out by a SiPM which is directly attached on the inside of the tile. SiPMs are well suited for this application due to the compact size, insensitivity to magnetic fields, high photon detection efficiency (PDE) and excellent timing properties. The most important SiPM characteristics for this application are a high

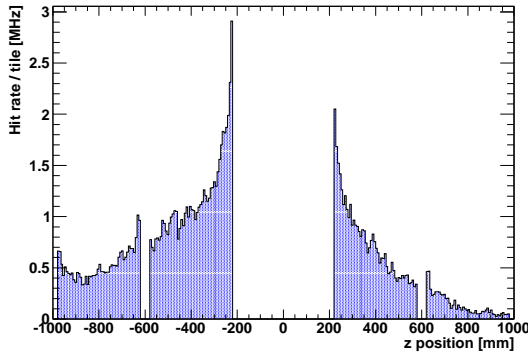


Figure 12.2: Hit rate per tile for phase II. The rate for phase I is a factor 10 to 20 smaller.

PDE and gain in order to obtain a large signal and therefore a good time resolution. Furthermore, a small signal decay time is desired in order to reduce signal pile up and thus increasing the signal efficiency. The S10362-33-050 MPPC from Hamamatsu with an active area of $3 \times 3 \text{ mm}^2$ and 3600 pixels is a suitable sensor for this application. A possible alternative sensor is the PM3350 from Ketek which offers a larger PDE and gain compared to the Hamamatsu device, but has a longer decay time. A further option is the SensL MicroFB series, which will be available in the first quarter of 2013. These sensors are a very promising alternative, as the devices will have an additional fast output providing signals with a width of $\mathcal{O}(\text{ns})$ and provide a high PDE and gain. Measurements and simulation studies comparing the different sensor types will be continued, in order to find the devices which is best suited for this application.

For the readout of the SiPMs, two different options are currently discussed. One solution is to digitize the SiPM waveforms using the DRS chip. The waveforms then have to be further processed externally, in order to determine the time-stamps. The second option is the STiC chip which includes a fast discriminator and a TDC digitizing the time information. Details on both chips can be found in chapter 13.

12.2 Simulation

Simulation studies using the full detector simulation described in section 15 have been carried out in order to determine the detector performance.

The optical properties of a tile are parameterized using a separate Geant4 simulation of a single tile. The SiPM simulation GosSiP [148] was used to generate the signal waveforms from the hit information of the full detector simulation. The simulation has been done for a detector design with 48×48 5 mm thick tiles per recur station with BC420 scintillator and S10362-33-050 MPPCs.

Figure 12.2 shows the hit rate per tile as a function of the position along the beam direction for phase II, including also tracks which pass several tiles, as well as background events e.g. from the collimators. These rates can be handled by the proposed readout electronics (see section 13). In order to further reduce the hit rate, and therefore the signal pileup, optimizations like adjusting the tile angle to match the mean incident angle of the tracks are currently studied.

The time-stamps for the individual hits are assigned using the signal waveforms generated by the SiPM simulation. A simple fixed threshold method is used which approximates the behaviour of the STiC chip. The same method can also be applied to the output of the DRS chip.

The optimal threshold was determined to be $\approx 10\%$ of the mean signal amplitude (≈ 350 pixels). Due to the varying signal amplitudes and the fixed threshold, the individual time-stamps have to be corrected for the timewalk effect. Figure 12.3 shows the timewalk as a function of the Time-over-Threshold.

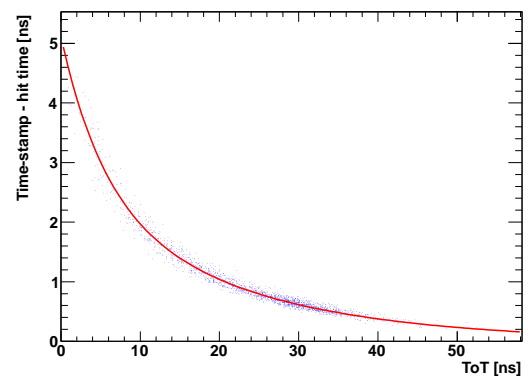


Figure 12.3: Timewalk correction.

Figure 12.4 shows the distribution of the time-stamps relative to the true hit time given by the simulation for phase II. A fit of a Gaussian function yields a time resolution of $\sigma_t = 45 \text{ ps}$. The

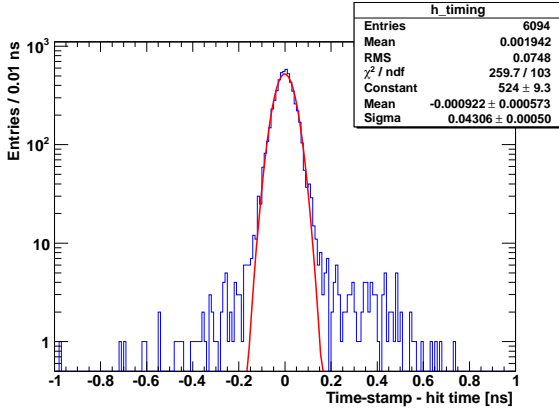


Figure 12.4: Timing for phase II. The timestamps have been corrected for timewalk.

non-Gaussian tails of the distribution come from signal pileup.

The efficiency for assigning a time-stamp to an isolated track within $\pm 3\sigma_t$ of the true hit time is $\approx 100\%$. Inefficiencies at the edge of a recurl station, where a track deposits too little energy in a tile to pass the threshold can be neglected.

However, the efficiency is also influenced by signal pileup. For the simple fixed threshold model used in this analysis, an overall efficiency of $\approx 99.5\%$ for phase I and $\approx 98.0\%$ for phase II is achieved. With a more sophisticated peak-finding algorithm, it should be possible to resolve pileup signals which occur within a time interval of a few nanoseconds and consequently achieve an efficiency of $\approx 100\%$. Also, using a SiPM with a fast output, like the SensL MicroFB series, will significantly reduce the pileup and thus increase the efficiency.

12.3 Time Resolution Measurements

First measurements of time resolution of a single $1 \times 1 \times 1 \text{ cm}^3$ tile and a Hamamatsu S10362-33-050 MPPC have been done using an oscilloscope with a bandwidth of 1 GHz. The scintillator material used in this measurements is NE110. Compared to BC420, this scintillator has a lower light yield and a slightly slower rise and decay time; using a more suited scintillator will thus improve the results. The scintillation light was triggered using a pulsed UV laser¹.

Figure 12.5 shows the measured time resolution as a function of the signal amplitude for a threshold of 10%. For a typical signal amplitude of ≈ 350 pixels, a time resolution of ≈ 45 ps is achieved, which is consistent with the simulation results. Figures 12.6 and 12.7 show the dependence on the applied threshold and SiPM bias voltage.

These results show, that a time resolution well below 100 ps can be achieved. It is expected, the resolution will not be degraded using the DRS or STiC readout chip, which will be verified in future measurements.

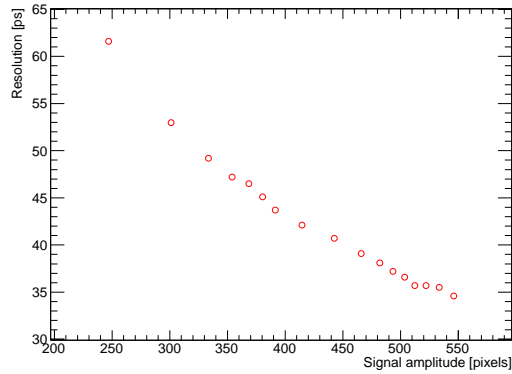


Figure 12.5: Time resolution as a function of the signal amplitude for a threshold of 10%. The amplitude expected in the tile detector is ≈ 500 pixels.

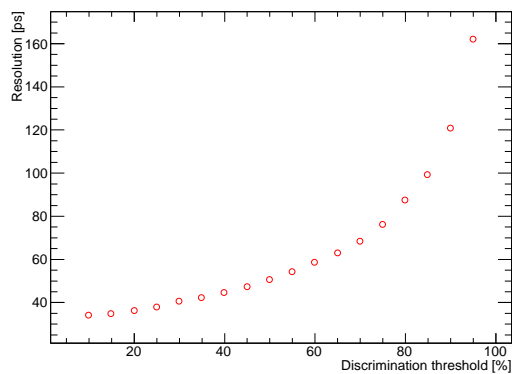


Figure 12.6: Time resolution as a function of the discrimination threshold for 500 pixel signal amplitude.

¹The scintillator response to the UV light is a good approximation of the response to electrons.



12.4 Detector Prototype

The design of a prototype of a tile detector module has been started (see Figure 12.1) and the construction is expected to be completed within 2013. In this prototype the mechanical design of the support structures and readout infrastructure will be tested and measurements of the detector performance will be carried out.

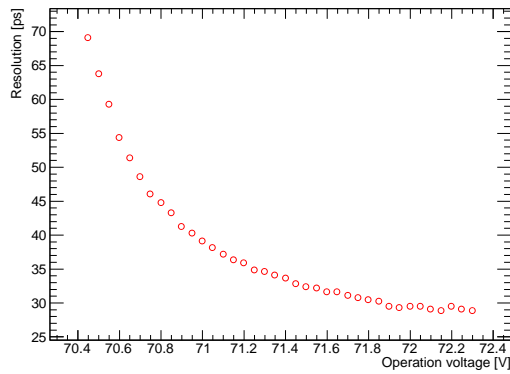


Figure 12.7: Time resolution as a function of the SiPM bias voltage for 500 pixel signal amplitude and a threshold of 10%.



Mu3e DATA ACQUISITION

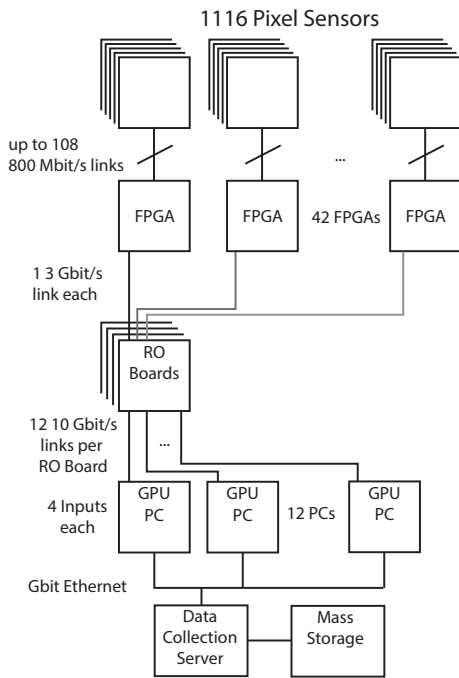


Figure 13.1: Mu3e readout scheme for the start-up detector.

13.1 Overview

The Mu3e data acquisition system works without a hardware trigger on a push basis, i.e. the detector elements continuously send hit information to the data acquisition (DAQ) system. The DAQ consists of three layers, namely front-end FPGAs, read-out boards and the filter farm. The topology of interconnects is built such that every farm PC

gets to see the complete detector information for a select time slice. See Figure 13.2 for an overview of the readout scheme and Figure 13.1 for the scheme at detector start-up.

13.2 Occupancy

The bandwidth requirements of the data acquisition are largely determined by the expected detector occupancy, as all the Mu3e sub-detectors produce zero-suppressed output.

The occupancies shown are obtained with the full simulation running at a muon stop rate of $2 \cdot 10^9$ Hz ($2 \cdot 10^8$ Hz for phase I) and pessimistically estimating the beam related background by loosing another $4 \cdot 10^9$ Hz ($4 \cdot 10^8$ Hz) of muons along the beam line. Figures 13.3 and 13.4 show the expected number of hits per 50 ns frame in the pixel detector. Figures 13.5 and 13.6 show the same for the fibre detector. The distribution of the occupancy over the pixel sensors is shown in Figures 13.7 and 13.8.

13.3 Front-end

13.3.1 PIXEL DETECTOR

The pixel sensors contain electronics for hit detection and time as well as address encoding. All hits assigned to the same (20 MHz) time-stamp constitute a *frame*. The sensors collect the data of 16 frames into a *superframe* and send it off chip via an 800 Mbit/s low-voltage differential signaling (LVDS) link. The signals travel over a max-

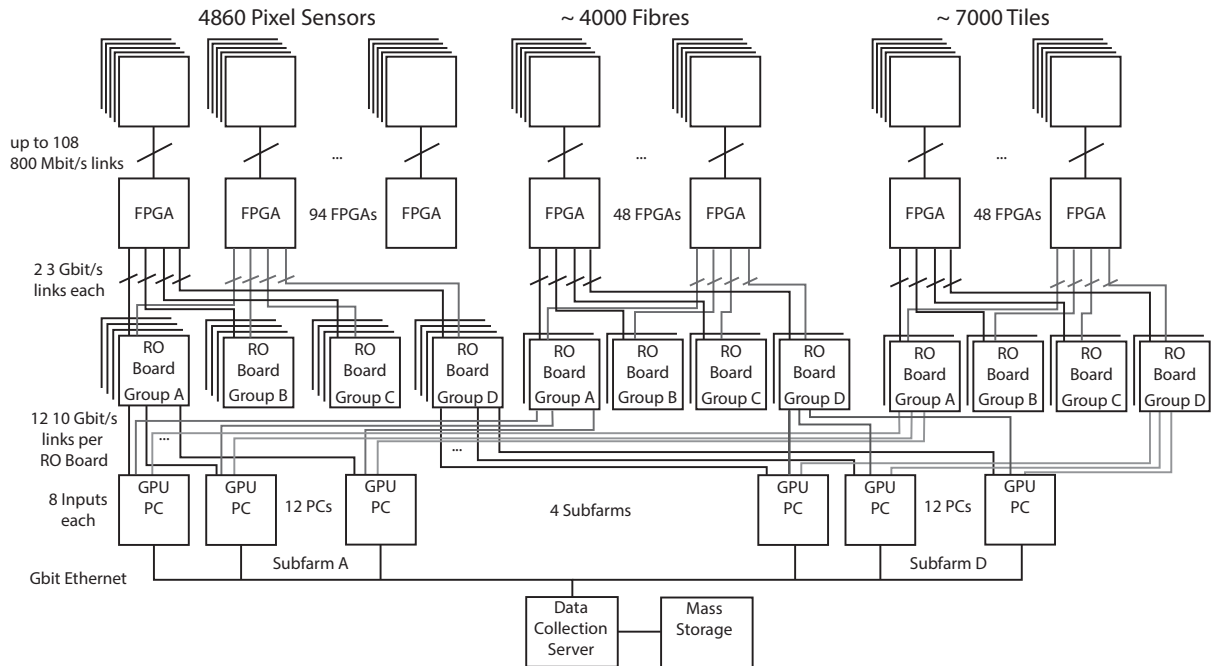


Figure 13.2: Overall Mu3e readout scheme

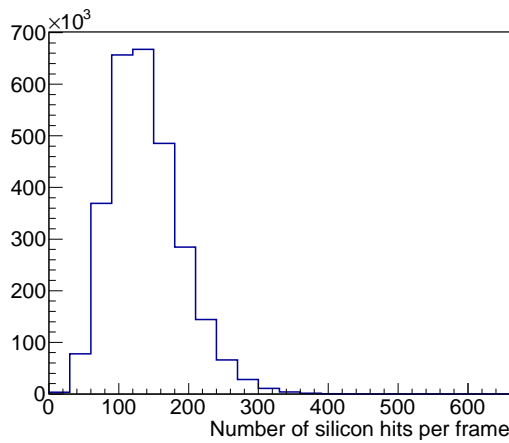


Figure 13.3: Number of pixel hits in the central detector per 50 ns frame in phase I running.

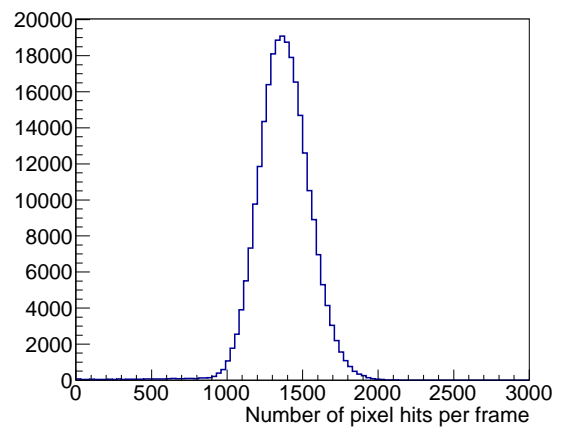


Figure 13.4: Number of pixel hits in the complete detector per 50 ns frame in phase II running.

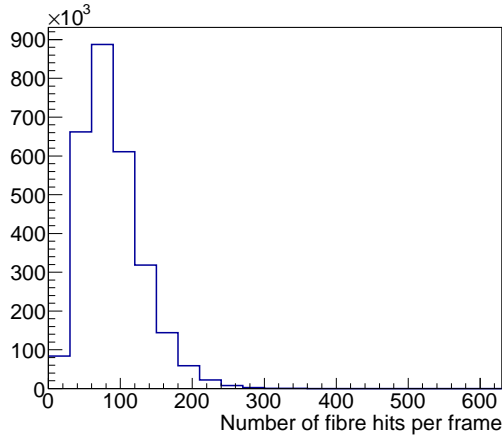


Figure 13.5: Number of fibre hits per 50 ns frame in phase I running.

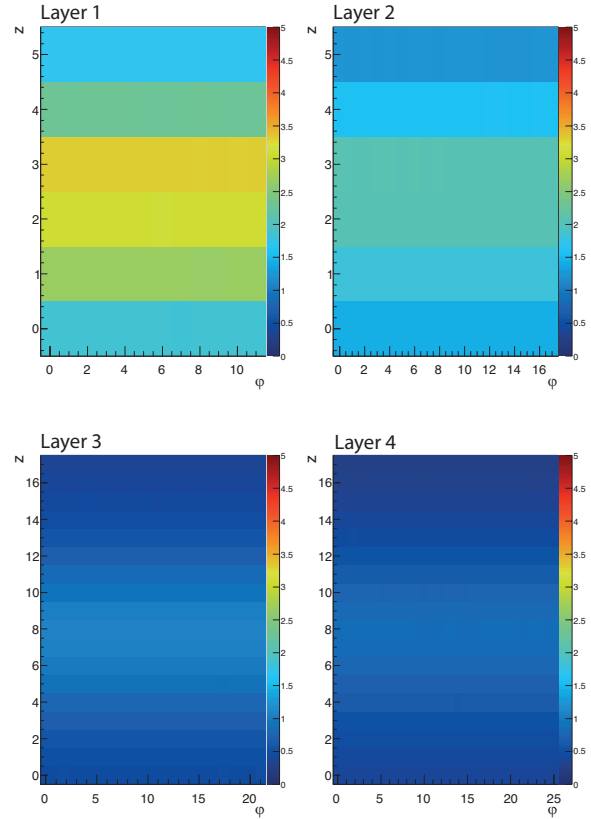


Figure 13.7: Occupancy in 50 ns frames of the central pixel sensors for phase II running. The axes enumerate sensor numbers. For phase I, the occupancy numbers have to be scaled down by a factor 10-20.

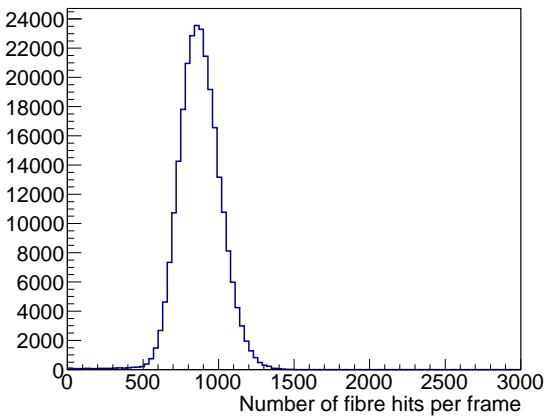


Figure 13.6: Number of fibre hits per 50 ns frame in phase II running.

imum of 18 cm on a Kapton flex-print to the edge of the sensitive area, where they are amplified by a driver chip. The Kapton prints then connects to a PCB located between the recur layers and the beam-pipe. On this PCB, up to 72 LVDS links are fed into a FPGA. The FPGA provides buffering and collects a long stream of frames (at least 1024) into a *frametrain*. The assembled data are then output to 8 3 Gbit/s links, such that the data of one frame-train are sent on two links. On the PCB, the signals are converted to optical and sent off-detector via fibres. An additional pair of optical links per FPGA is required for slow control and monitoring.

Hardware

The requirements for the on-detector FPGAs can be met by mid- or even low-price devices (such as



	Sensor Chips	Max Hits /Chip	Average Hits /Layer	Chip→FPGA link capacity Mbit/s	Chip→FPGA total in Layer Gbit/s	Front end FPGAs	FPGA→RO capacity Gbit/s
Layer 1	72	0.35	18.0	220	16	8	17
Layer 2	108	0.25	18.4	157	17	8	17
Layer 3	432	0.15	31.0	94	40	12	29
Layer 4	504	0.15	28.6	94	47	14	27
Total	1116		96		120	42	90

Table 13.1: Pixel readout requirements (Phase IB without recurl stations).

	Sensor Chips	Max Hits /Chip	Average Hits /Layer	Chip→FPGA link capacity Mbit/s	Chip→FPGA total in Layer Gbit/s	Front end FPGAs	FPGA→RO capacity Gbit/s
Layer 1	72	3.5	180	2203	155	8	166
Layer 2	108	2.5	184	1574	166	8	170
Layer 3	432	1.5	310	944	398	12	286
Layer 4	504	1.5	286	944	465	14	264
Recurl backward 1 inner	432	0.5		315	133	6	
Recurl backward 1 outer	504	0.5		315	155	7	
Recurl backward 2 inner	432	0.25		157	66	6	
Recurl backward 2 outer	504	0.25		157	77	7	
Recurl forward 1 inner	432	0.3		189	80	6	
Recurl forward 1 outer	504	0.3		189	93	7	
Recurl forward 2 inner	432	0.2		126	53	6	
Recurl forward 2 outer	504	0.2	$\Sigma=490$	126	62	7	$\Sigma=452$
Total	4860		1450		1903	86	1515

Table 13.2: Pixel readout requirements (Phase II), for the recurl stations only the sum of average hits per layer and FPGA→RO capacity is given.

the ALTERA Cyclone IV family or the XILINX Artix VII family). The FPGAs are to be mounted on PCBs that are placed between the recurl layers and the beam-pipe.

Firmware

The main task of the on-detector FPGAs is collecting the relatively short time slices of 16 clock cycles assembled on the pixel chips to the long intervals treated by the individual filter farm PCs. During this buffering, the hits can be time ordered inside a slice and the protocol overhead can be reduced. In addition, hits can be clustered.

A further task for the first line of FPGAs is the configuration and monitoring of the pixel chips. A 32 bit histogram of the hit counts in a single sensor however requires 256 kB of memory, thus exceeding the capacity of the devices; an ex-

ternal memory interface would significantly increase the pin count and the PCB complexity; the histogramming task is thus deferred to the readout boards.

These tasks are all fairly standard and FPGAs that fulfill the bandwidth requirements for the in- and output channels do provide enough logic for implementing them.

13.3.2 TIMING DETECTOR

For the timing detectors, three readout schemes are currently under investigation: One based on a further development of the DRS switched capacitor array developed at PSI, one based on the STiC chip developed at KIP, Heidelberg University and one with FPGA-based TDCs (mainly for the fibres).

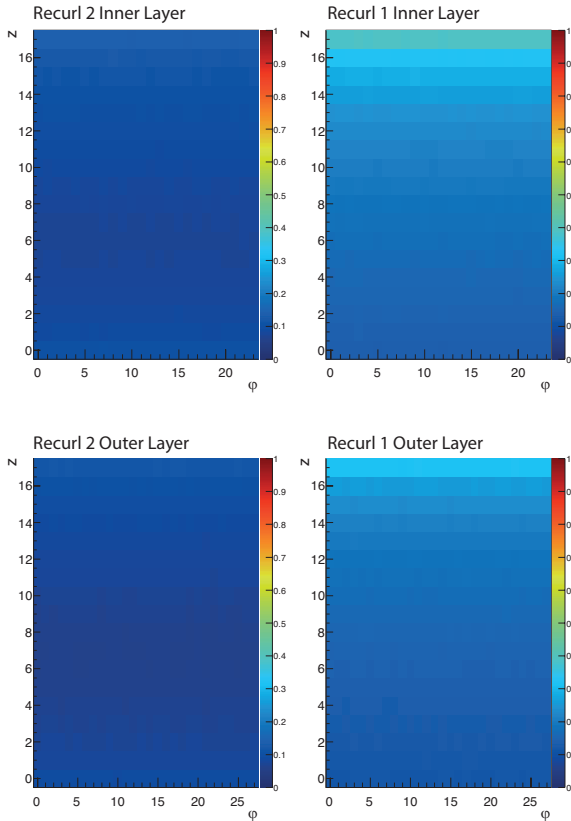


Figure 13.8: Occupancy in 50 ns frames of the recurl pixel sensors for phase II running. The axes enumerate sensor numbers.

DRS sampling readout

The readout of the tile and fibre detectors requires high rate capability and extremely good timing resolution. To achieve an overall detector timing accuracy below 100 ps, the associated electronics needs to be at least a factor of two better, i.e. 50 ps. The high rate environment causes significant pile-up, which limits the usage of conventional techniques such as discriminators and TDCs. Therefore one option to read out the tiles is with the well-established waveform digitizing technology developed at PSI, which is in use since many years in the MEG experiment. It is based on the DRS4 switched capacitor array, which is capable of sampling the SiPM signals with up to 5 Giga samples per second (GSPS) with a resolution close to 12 bits. It has been shown in the MEG experiment that this technology allows a timing accuracy in the order of 40 ps across many thousand channels. The knowledge of the exact wave-

form of an event is very well suited to detect and suppress pile-up.

The tile readout electronics could be placed outside the detector in special crates connected with a few meters of cable. This simplifies the design and maintainability, while not compromising the signal quality dramatically.

A principal limitation arises from the DRS4 chip, which is capable of only a limited event rate of about 100 kHz. While this will be sufficient for Phase IB, it has to be improved for Phase II. Therefore a new development has been started to design a new version of this chip. The DRS5 chip will use an internal analog memory (FIFO) to work in a dead-time less fashion up to an event rate of about 5 MHz. A critical part of the DRS5 chip which is the inverter chain operating the sampling circuitry has already been designed in the new 110 nm CMOS technology and submitted. First test results are expected beginning of 2013. The dead-time less operation of this chip will be combined with higher sampling speed (10 GSPS) and a better timing accuracy, allowing for a time measurement well below 10 ps.

In order to limit the amount of data to be read out, the FPGA connected to the DRS chip will already analyze the waveform and extract its major parameters like time and amplitude. Only a prescaled subset of events will contain the full detector waveform in order to cross-check the analysis algorithms in the FPGA. Methods have recently been published which obtain the timing information by cross correlation or cubic interpolation with an accuracy of about 1/10th of the sampling interval, which would be 10 ps in the case of 5 GSPS.

STiC readout

The STiC chip offers an alternative to the DRS5 readout. STiC is a mixed mode 16-channel ASIC chip in UMC 0.18 μm CMOS technology designed for SiPM readout with high time resolution. It is developed for Time-of-Flight measurements in high energy physics and medical imaging, in particular the EndoTOFPET-US project. The chip has a differential structure, however, it supports both differential and single-ended connection of SiPMs. A 6 bit DAC allows to tune the voltage at each input terminal within ≈ 1 V. In this way the SiPM operating voltage can be adjusted and

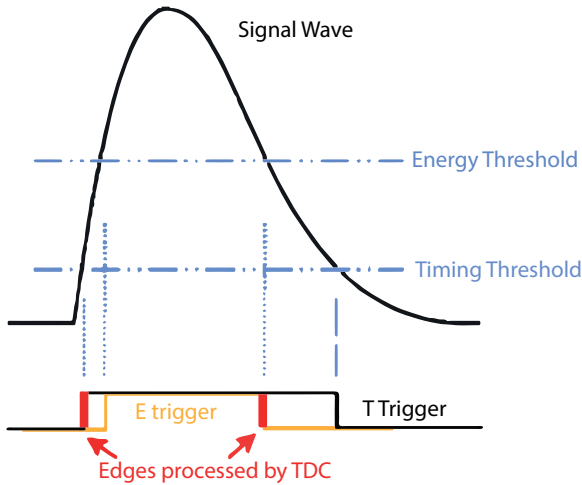


Figure 13.9: Dual threshold discrimination for energy and timing information.

temperature and device-to-device fluctuations can be compensated.

The time and charge information of the signal are encrypted into two time-stamps which are obtained by discriminating the signal with two different thresholds (see Figure 13.9). The thresholds can be tuned in a range of $\approx 0.2 - 15$ pixel signals for the timing and up to 200 pixel signals for the charge. The time-stamps are then processed by an embedded TDC module with a resolution of < 20 ps. A special linearization method is implemented to obtain a linear charge response in a very wide range. With the chip, a time-resolution of ≈ 50 ps was measured for a 10 pixel signal of a MPPC S10362-33-50 without scintillator. For typical signal amplitudes of $\mathcal{O}(100)$ pixels, which are expected in the tile detector, the timing jitter of the chip is negligible.

The data rate of the current chip is limited to ≈ 100 kHz per channel. However, the chip will be modified to allow for data rates of ≈ 500 kHz per channel within 2013/2014. Until 2016, the data rate will be further increased to several MHz in order to match the requirements for phase II.

FPGA based readout

A further alternative for the fibre readout is the use of time to digital converters implemented in FPGAs. Resolutions of $\mathcal{O}(1$ ns) can be achieved fairly cheaply; much better performance requires the use of carry chain techniques, which greatly reduces the number of channels per FPGA and

makes programming much more fickle. It has however been shown that resolutions of $\mathcal{O}(10$ ps) can be achieved with this technology [149]. Whilst definitely not the optimal solution, FPGA based timing could serve as a low-cost, low-risk solution for phase IB running.

13.4 Read-out links

In total there are three different types of read-out links in the Mu3e data acquisition system. The same type of links can be used for a small number of slow and fast control links in the opposite direction.

The data from the MUIPX chips will be transmitted to the front-end FPGAs via LVDS links at 800 Mbit/s, which is a quasi industry standard. The fast serializers and LVDS drivers for the MUIPX chip will be adopted from a similar chip design by a group from Bonn [150]. The link will be physically implemented as a matched differential pair of aluminum traces on the sensor flex-print, shielded by ground lines on both sides. It is foreseen to have a first set of LVDS repeaters just outside the acceptance of the detector. Very compact commercially available LVDS repeaters have already proven to be radiation tolerant. Outside the acceptance, the flex-print will then be of multilayer type, with differential signal inner layers, shielded by ground planes. The connection to the PCB housing the front-end FPGA is made by small form factor connectors, which support high bandwidth. Lastly the routing on the front-end FPGA PCB will be done with matched differential copper traces going to the pre-defined LVDS inputs of the FPGA itself.

There will be two types of optical high speed data links. The first one is going from the front-end FPGAs to the read-out boards, the second from the read-out boards to the FPGA PCIe boards in the event filter farm PCs. The optical links from the front-end FPGAs to the read out boards have a bandwidth of 3.125 Gbit/s, which fits well the FPGA specifications. Each FPGA has eight (or more) fast transceiver blocks. The optical interface can be implemented using radiation tolerant components developed by the Versatile Link group [151]. Especially the 12-way laser array with MTP/MPO standard connector would give a very compact form factor, the fall back solution would be a radiation hard dual laser transmit-



ter system, the VTTx module developed at CERN [152]. The data laser will have a wavelength of 850nm and the optical fibre is of 50/125 multi-mode type, since this is a standard both in industry and in particle physics detector readout. In the case of the 12-way emitter the fibres will go to a splitter and patch panel in order to combine fibres going to the same read-out board. In the case of dual transmitters the fibres can be combined in groups of 12 using break-out fibre cables. The fibres traveling from the experimental area to the filter farm counting house can be further combined in cables containing 8×12 fibres going to the same sub-farm. An optical patch panel for each sub-farm will allow to connect the long distance 96-fibre cables to 12 fibre patch cords going to the readout boards. The readout boards have 2 or 3 12-way optical inputs, which are populated with commercial receiver modules. The high-end FPGAs used on the read-out card have up to 66 high speed transceiver blocks, which will be used for the de-serialization of the data.

The last type of link connects the read-out cards to the FPGA PCIe boards in the event filter farm PCs. This optical link will be implemented as 10Gbit/s high speed link. Since each read-out board is connected to every sub-farm PC with one of the high speed links, they are point to point single fibre links. The fibres are of 50/125 multi-mode type operated at 850nm to stay compatible with the links from the detector. If 12-way optical transmitters and receivers running at 10Gbit/s can be purchased, they will be used for this high speed link. Otherwise single fibre transmitters and receivers will be used both on the read-out board and the FPGA PCIe board side. In practice the high speed optical receivers for the FPGA PCIe boards could be on optical mezzanines such as the 8 channel St. Luce card developed by TU Dortmund [153].

13.5 Read-out cards

The main tasks of the read-out cards is to act as switches between the front end and the on-line reconstruction farm and to act as buffers between the synchronous front end and the asynchronous back end. The board design and choice of FPGAs is dominated by the number of fast links required. We plan to adapt an existing development, e.g. LHCb TELL1 cards [154] or PANDA

compute nodes [155], which would both fulfill our needs.

13.6 Event filter interface

The filter farm PCs will be equipped with FPGA cards in PCIe slots and optical receiver daughter cards, as described in more detail in section 14.2.

13.7 Data collection

The filter farm will output selected events at a data rate in the order of 50 MBytes/s in total. This data rate is low enough to be collected by a single PC connected to the filter farm by common GBit Ethernet and written to local disks. Then the data will be transferred to the central PSI computing center, where it is stored and analyzed. For the central data acquisition the well established MIDAS (Maximum Integrated Data Acquisition System) [156] software package will be used. This software is currently used in several major experiments such as the T2K ND280 detector in Japan [157], ALPHA at CERN and the MEG experiment at PSI [158]. It can easily handle the required data rate, and contains all necessary tools such as event building, a slow control system including a history database and an alarm system. A web interface allows controlling and monitoring the experiment through the Internet. The farm PCs will use MIDAS library calls to ship the data to the central DAQ PC. The framework also offers facilities to send configuration parameters from a central database (the “Online DataBase” or ODB) to all connected farm PCs and to coordinate common starts and stops of acquisition (run control).

For the purpose of monitoring and data quality control of the experiment the MIDAS system offers taps to the data stream for connections of analysis and graphical display programs. The output of graphical user interface programs can be fed back into the web interface of the MIDAS system so the experiment can be monitored also remotely with just a Web browser.

13.8 Slow control

The slow control system deals with all “slow” data such as high voltages for the SiPMs and silicon sensors, ambient temperatures and pressures. For

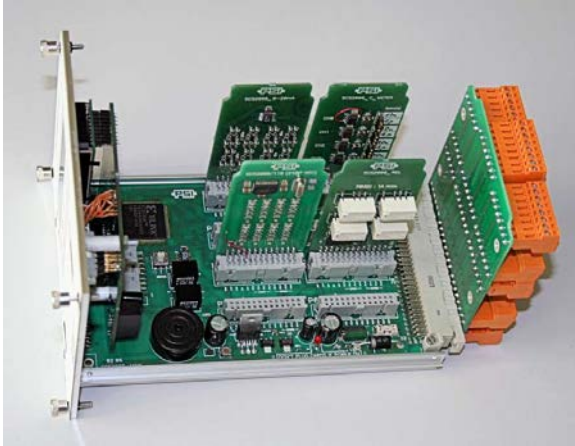


Figure 13.10: SCS-2001 unit as part of the MSCB slow control system. This unit has 64 input/output channels, which can be configured via plug-in boards as digital or analog channels. Many plug-in boards exist already such as PT100 temperature sensor readout cards, analog high resolution inputs (24 bit resolution), valve control outputs and many more.

the configuration and control of the silicon pixel sensors the JTAG standard [132] will be used. It is planned to use the MIDAS Slow Control Bus (MSCB) system [159] to link all distributed control and monitoring devices into a single system. The MSCB system is also well established at several laboratories. It uses a serial differential bus for communication, and simple micro controllers in all control devices. The micro controllers perform local control loops such as high voltage stabilization, and send measured values to the central DAQ system for monitoring. Many devices already exist for this system, such as the SCS-2001 unit shown in 13.10. Since the system was

developed at PSI, it can be quickly adapted to new hardware. The high voltage control for the SiPMs can for example be directly integrated into the carrier boards holding the SiPMs, thus eliminating the need for high voltage cables. The optimized protocol of the MSCB system allows the monitoring of many thousand channels with repetition rates in the 100 ms range, which will be more than enough for this experiment.

In addition to the MSCB system, the MIDAS slow control package contains interfaces to the PSI beamline elements via the EPICS system [160]. This allows monitoring and control of the beamline from the main DAQ system, which has been proven very versatile in other experiments using this scheme.

All slow control data will be stored in the history system of the MIDAS system, so that long term stabilities of the experiment can be effectively verified. The slow control data is also fed into the main event data stream, so that any off-line analysis of the event data has this data available.

A special case is the configuration of the pixel detectors, which require many million parameters, like the trim-DAC values for each pixel. Since the amount of data here is considerably larger than for all other systems, an extension of the slow control system is planned. A dedicated program manages, visualizes and exchanges the pixel detector configuration parameters between an optimized database and the pixel hardware. In this way the time required to configure the pixel detectors can be minimized, while this program is still connected to the main DAQ system. It can be synchronized with run starts and stops, and can inject pixel monitoring data periodically into the event data stream for offline analysis.



ONLINE EVENT SELECTION

14.1 Selection Algorithms

As in the final analysis, event selection in the filter farm can rely on the coincidence of three tracks in time and vertex and on their kinematics. Especially for high rate running, coincidence in time in the fibre detector is not sufficient to reduce the data rate by three to four orders of magnitude. Thus a track reconstruction will be required. The triplet based multiple scattering fit described in chapter 16 is well suited for online implementation and current GPUs can perform 10^9 triplet fits per second¹, thus already fulfilling the needs of Mu3e up to at least medium intensity (few 10^8 muons/s) running.

Triplets of the tracks thus reconstructed can then be fit to a common vertex. Even loose vertex requirements can give a 10^3 reduction factor at $2 \cdot 10^9$ Hz muon rate and $10^4 - 10^5$ for the phase I experiment (see Figures 14.1 and 14.2). Combining the vertexing with modest kinematic requirements (e.g. on the three-particle invariant mass or the planarity) should produce the required data reduction, leaving the timing information as a valuable offline cross-check (and obviating the need for online timing reconstruction).

14.2 Hardware Implementation

The data will arrive on the farm PCs via optical links on a PCIe FPGA board. The FPGA will perform the event building and buffering and

¹As tested on a AMD Radeon 6990 using OpenCL under Linux.

also allows to run simple clustering and sorting algorithms. The event data are then transferred via DMA over the PCIe 3 bus² to the memory of a graphics processing unit (GPU), where the selection algorithms are run. The GPU then posts selected events and monitoring data to the main memory of the PC, from where the CPU ships it via Ethernet to the central data acquisition computer running the MIDAS software. At that computer, the data streams from the farm PCs are combined into a single data stream, combined with various slow control data, compressed and stored.

For the receiver FPGA cards, evaluation boards from either XILINX [161], or ALTERA (Figure 14.3) [162,163] or similar hardware built by the collaboration could be used in conjunction with daughter boards with the optical receivers (similar to e.g. the optical receiver boards used in the LHCb readout electronics [164]). The maximum data rate over the PCIe 3.0 bus is 16 Gbyte/s, amply sufficient for phase I³. For the full phase II rate, the raw link speed is still sufficient, would however have to be fully and efficiently used. The PCIe 4.0 standard, doubling this rate, should become commercially available around 2017, compatible with phase II running; alternatively, the number of farm PCs could be increased.

²Note that PCIe is actually not a bus protocol, but offers switched point-to-point connections. The *bus* designation is due to the software-side backwards compatibility to the original PCI bus interface.

³For phase I running, the FPGA-GPU link can also be implemented on PCIe 2.0 (max. 8 Gbyte/s), which is better supported on currently available FPGAs.

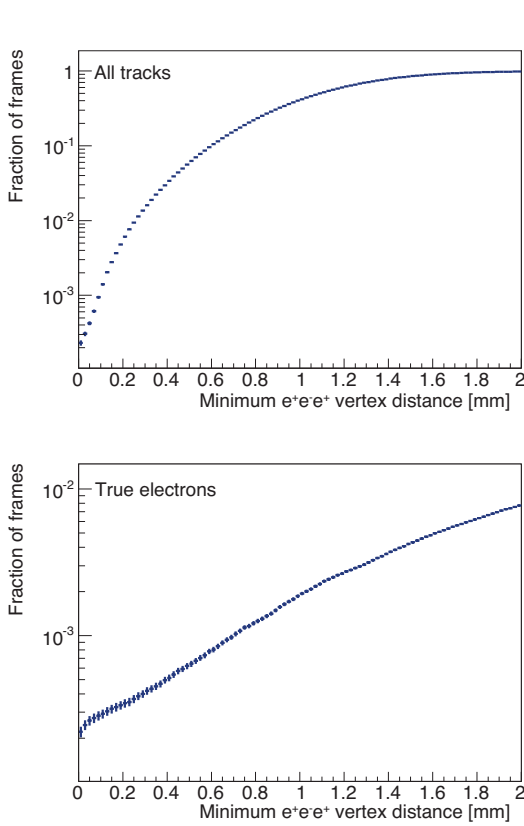


Figure 14.2: Fraction of 50 ns frames containing three vertices consistent with $e^+e^-e^+$ inside a given distance for a muon stop rate of $2 \cdot 10^9$ Hz for 680'000 simulated frames. In the top plot, every crossing of a simulated electron/positron track is counted as a vertex; charge assignments are made purely on the apparent curvature, i.e. recurling positrons are counted as electrons. In the bottom plot, only true electrons are counted.

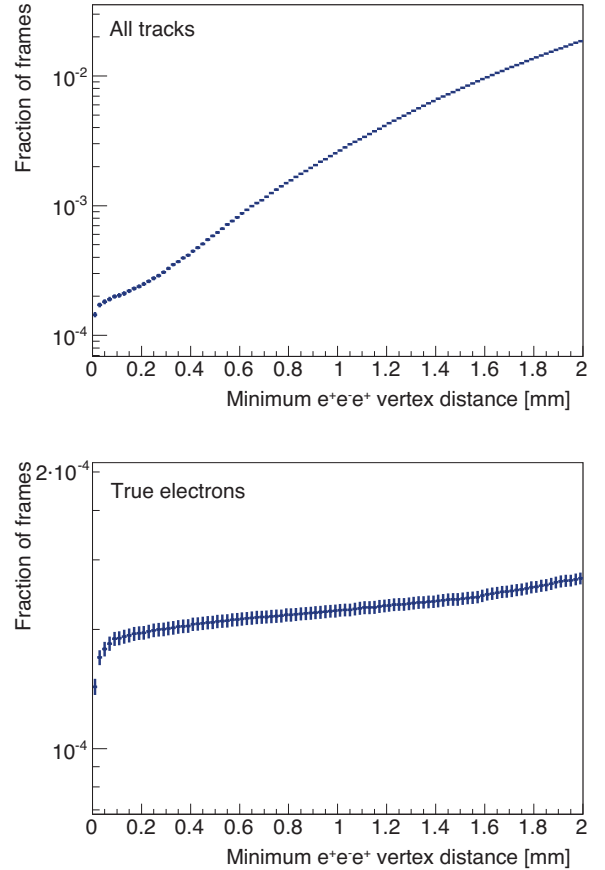


Figure 14.1: Fraction of 50 ns frames containing three vertices consistent with $e^+e^-e^+$ inside a given distance for a muon stop rate of $2 \cdot 10^8$ Hz for 3.15 million simulated frames. In the top plot, every crossing of a simulated electron/positron track is counted as a vertex; charge assignments are made purely on the apparent curvature, i.e. recurling positrons are counted as electrons. In the bottom plot, only true electrons are counted.



Figure 14.3: ALTERA Stratix IV PCIe development board.

The GPU boards will be obtained commercially as late as possible in order to profit from the fast developments and sinking prices. As far as raw floating point throughput is concerned, current high-end GPUs already pack enough power for high rate running [165,166]. Newer cards are however expected to offer higher memory bandwidth and better caching. Also the performance of the driver software (especially as far as the PCIe 3 bus is concerned) and the GPU compilers is expected to improve. The two GPU vendors AMD and NVIDIA offer fairly different architectures; which one performs better depends a lot on the details of the algorithm to be implemented; we are currently



AN EXPERIMENT TO SEARCH FOR THE DECAY $\mu \rightarrow eee$

performing tests with both architectures and will choose a vendor once we have a mature implementation.

We currently plan to host the farm PCs in individual tower casings, ensuring enough space for

the FPGA board and the high end GPU whilst allowing for air cooling. At load, each tower will consume around 0.5 KW, so adequate cooling of the counting house is essential.



SIMULATION

This chapter describes the Geant4 [124, 167] based simulation used to derive the figures and plots in this proposal.

15.1 Detector geometry

15.1.1 BEAM DELIVERY

In the simulation, the beam is started 3 m in front of the target inside a beam transport solenoid. Beam particles are generated with a profile and momentum spectrum like the one observed in MEG. 1.5 m before the target, the beam enters the main solenoid and shortly before the target it exits the beam vacuum through a thin window. Along the beamline, two thick lead collimators reduce the beam to the target size. For an overview of the simulated beamline elements, see Figure 15.2. In this simple setup, about a third of the generated muons decay in the target, which, whilst

not very efficient, gives a conservative estimate of beam-induced backgrounds.

15.1.2 TARGET

The target is simulated as a hollow aluminium double cone supported by three nylon strings at each end and a nylon string along its axis, see also chapter 9.

15.1.3 PIXEL DETECTOR

The pixel detector is simulated as 50 μm of silicon on top of 15 μm of aluminium representing the traces on the flexprint (covering half the available area) on top of 50 μm of Kapton, with the silicon offset such that an overlap with next sensor is created, see Figure 15.4. Half a millimeter of the pixel sensor at the edge is assumed to be inactive, the rest is divided into $80 \times 80 \mu\text{m}^2$ pixels. The simulated sensor layers are supported at their ends by plastic and aluminium structures modeled on those in the mechanical prototype shown in Figure 10.20.

15.1.4 SCINTILLATING FIBRES

The fibre detector is simulated as three circular layers of 250 μm scintillating fibres in the main simulation. A detailed simulation including optical transport and the effect of fibre cladding and coating also exists, see section 11.3. The results of the detailed simulation regarding light yield and propagation times will eventually be fed back into the main simulation in a parameterized form. The

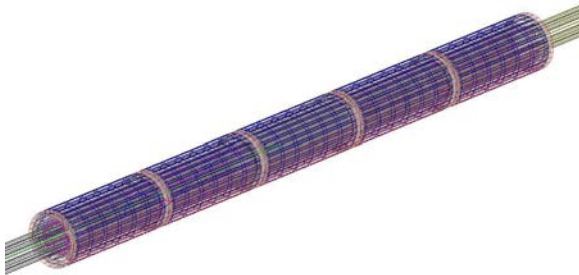


Figure 15.1: Wire frame view of the simulated detector.



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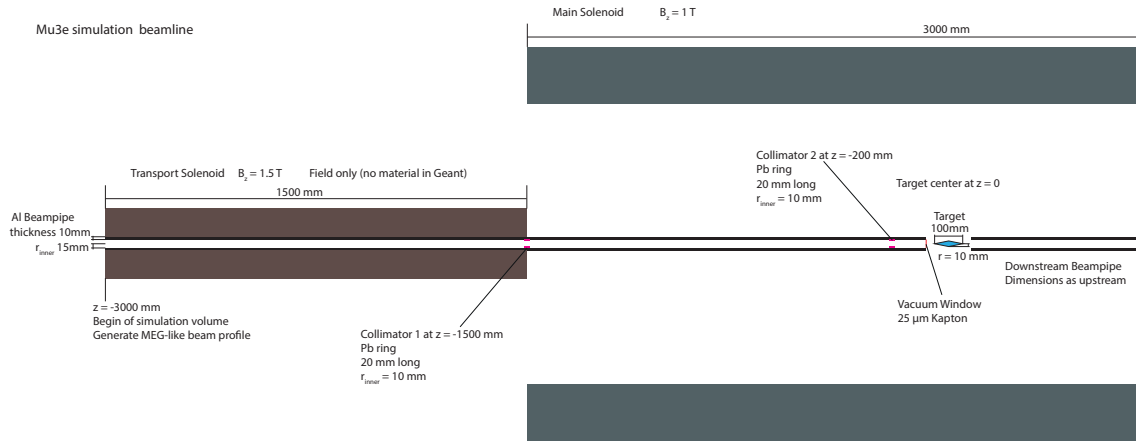


Figure 15.2: Beamline in the current simulation.

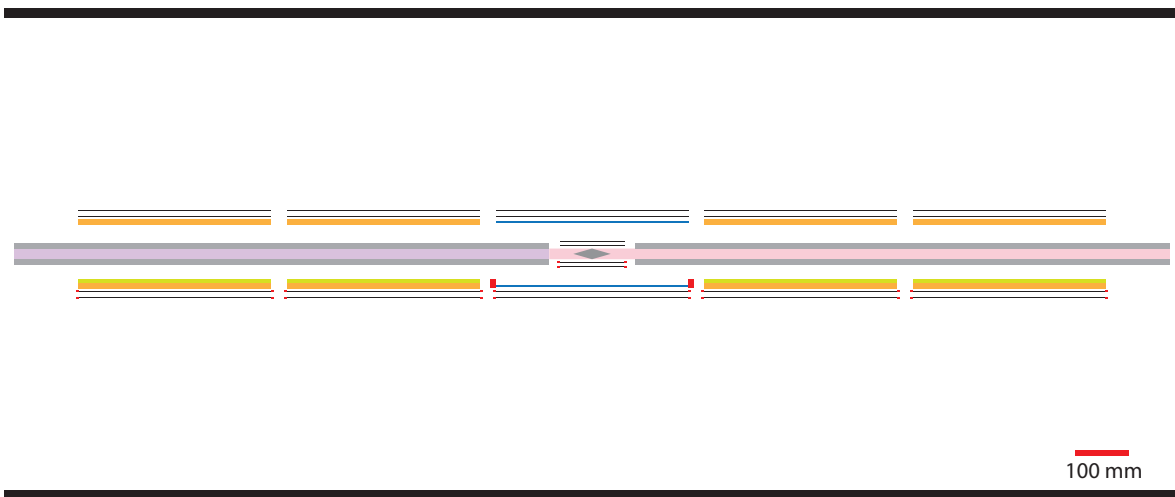


Figure 15.3: Geometry of the detector in the simulation. The top half only shows active (sensor) volumina, whereas the bottom half only shows support structures.

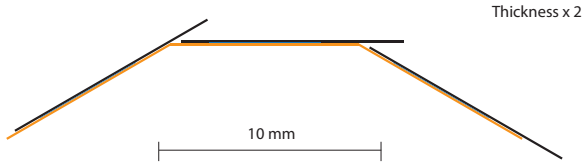


Figure 15.4: Pixel detector simulation geometry for the innermost layer. The sensor is shown in black, the aluminium traces in blue and the Kapton support in orange. Note that all thicknesses are stretched by a factor of 2.

response of the silicon photomultipliers is simulated by the GosSiP package [148]. In the simulation, the fibres are supported at both ends by massive aluminium rings.

15.1.5 TILE DETECTOR

The simulated tile detector consists of plastic scintillator tiles mounted on an aluminium tube. Also here, a separate detailed simulation including light transport and silicon photomultiplier response is available and will have to be fed back into the main simulation in a parameterized form.

15.2 Magnetic field

The simulated magnetic field can be read from arbitrary field maps or generated in the code via integration over current loops. The propagation of muons in the field includes spin tracking. For the simulations shown in this report, the field was generated from 100 current loops spaced equally over 3 m, with currents normalized such that the longitudinal component of the field in the center of the target is 1 T, supplemented by a 1.5 T field in the center of the beam transport solenoid, see section 15.1.1 and Figure 15.2.

15.3 Physics Processes

15.3.1 MULTIPLE COULOMB SCATTERING

Multiple coulomb scattering is the main limiting factor for the resolution of the experiment; an accurate simulation is thus crucial. The best results are obtained by simulating each individual scattering, which however results in prohibitively large computing times. A large selection of multiple scattering parameterizations are available in

Geant4; in a test setup they were compared to the single scattering model, see Figure 15.5. The best overall description is obtained from the Urbán-Model [168] at large step widths, which also has the shortest computation times. In the helium gas on the other hand, none of the parameterizations performs adequately, see Figure 15.6.

We plan to verify the simulation results with beam telescope measurements in 2013, which should also lead to a usable parameterization of multiple scattering in gases.

15.3.2 MUON DECAYS

Michel decay

Geant4 implements the Michel decay including polarization of both the muon and the positron based on [169] and [170]. The spectra of the neutrinos do not follow the physical distribution, this does however not affect the simulation for Mu3e. Somewhat more worrying is the fact that the Michel matrix element contains radiative corrections but is not clearly separated from the radiative decay matrix element.

Radiative decay

The radiative decay of the muon was implemented in Geant4 by the TWIST collaboration [171] based on [172]. The code does not describe the neutrino spectra and avoids the collinear and infrared singularities by sampling the matrix element assuming a finite integral.

Radiative decay with internal conversion

The radiative decay with internal conversion is simulated using the hit and miss technique on events generated evenly in phase space using the RAMBO code [173] and applying the matrix element from [116]. Unfortunately, there is currently no polarized version of the matrix element available and thus the simulation is unpolarized. The hit and miss technique is very expensive in terms of computation time, if the complete phase space is to be simulated (as the matrix elements varies by more than 16 orders of magnitude), this can however be overcome by restricting the simulation to regions of particular interest, e.g. high invariant masses of the visible particles.

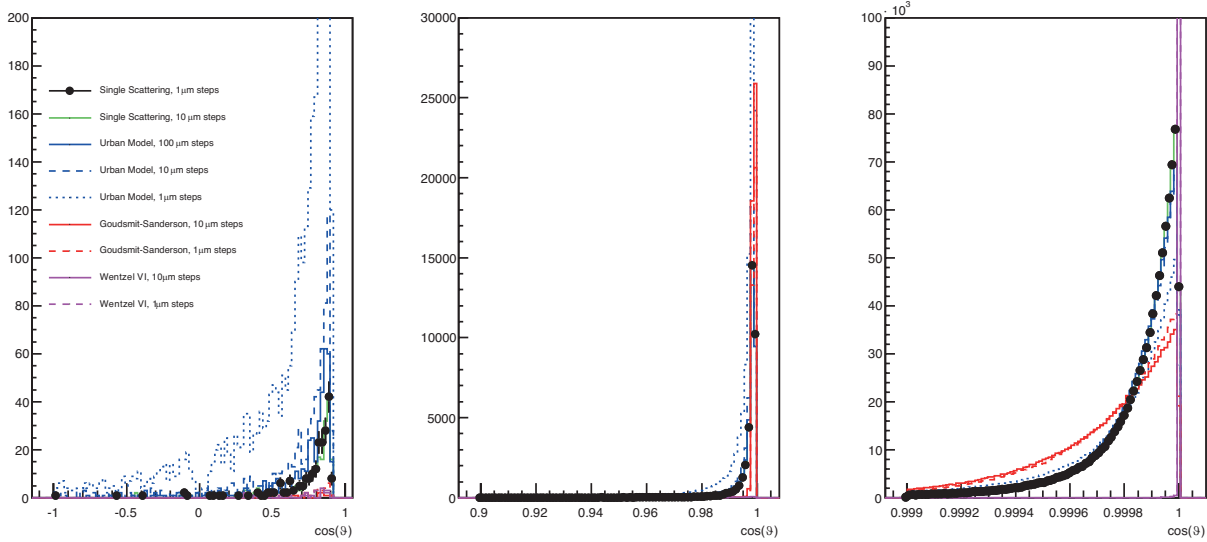


Figure 15.5: Comparison of multiple coulomb scattering models in different scattering angle ranges. The scatterer is a single silicon-Kapton assembly shot at a right angle with 30 MeV positrons. The black dots and the green line show the single scattering model which serves as a reference; as expected, the single scattering model is not affected by the Geant step size. Of all the parameterizations, the Urban model with a step size that treats each bit of material as a single volume performs best.

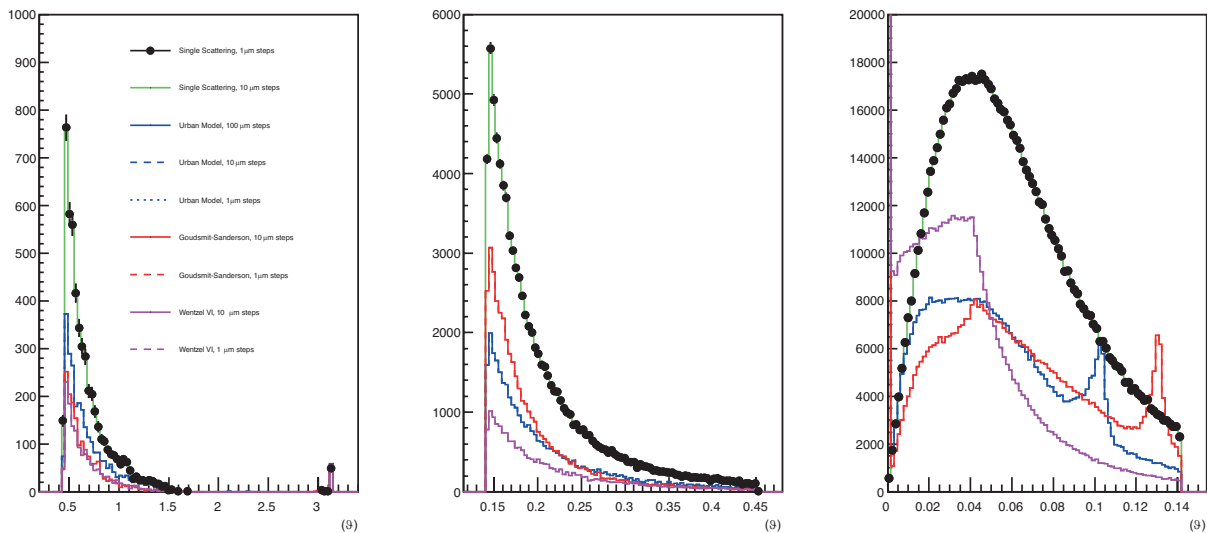


Figure 15.6: Comparison of multiple coulomb scattering models in m of helium gas for different scattering angle ranges. The test particles are 30 MeV positrons. The black dots and the green line show the single scattering model which serves as a reference. All the parameterizations are unfortunately inadequate.

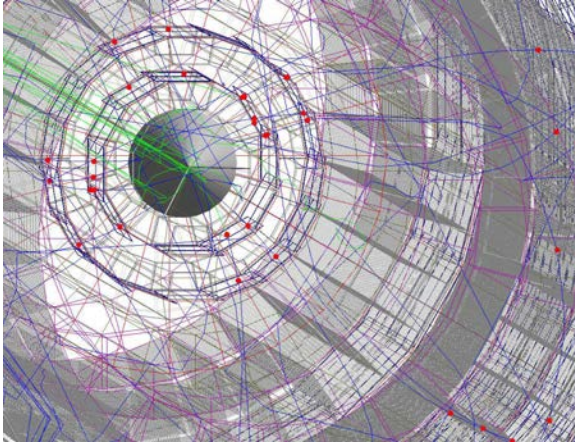


Figure 15.7: View of a simulated frame.

Signal

The signal kinematics are highly model-dependent, see chapter 4. If not otherwise noted, we have used three particle phase space distributions in the simulation, following the practice of SINDRUM and earlier experiments.

Special decays

The simulation allows the simulation of overlap decays, where we force more than one muon decay to happen at a single vertex. Thus we can simulate the accidental backgrounds arising e.g. from the overlap of an internal conversion decay and a Michel decay without having to generate in excess of 10^{16} frames.

15.4 Time structure

As the Mu3e experiment operates with a quasi continuous beam, the paradigms of *bunch crossing* and *event* from collider experiments do not apply; they have however informed the design of the Geant4 package. In our simulation, particles are assigned a 64 bit ID, which is unique over a run and thus conserves identities and mother-daughter relationships across the boundaries of read-out time frames. Before each step of tracking the particle through the detector, it is checked whether the particle has just crossed into the next time slice. If so, its information is stored, its time relative to the time slice adjusted and tracking deferred to the next slice. Thus we ensure that we correctly treat muons stuck in the target before decaying and decay products crossing read-out frame boundaries while traversing the detector. In order to simulate a steady state, where approximately the same number of muons enter the target and decay, the first 5 ms of simulation running, during which the target is loaded, are usually thrown away and not used in occupancy or efficiency studies.

Currently not simulated are effects of the 40 MHz structure of the primary proton beam on the time structure seen in the detector; if this would be needed, a measured structure could easily be superimposed on the generation of muons in the simulation framework.



RECONSTRUCTION

16.1 Track Reconstruction in the Pixel Tracker

A precise track reconstruction of electrons is of highest importance for the identification of the $\mu \rightarrow eee$ decay with a sensitivity of 1 out of 10^{15} (10^{16}) ordinary Michel decays in phase I (II), which have to be suppressed by 16 orders of magnitude.

Due to the high rate and the resulting high occupancy especially at phase II of the project with up to 100 tracks per readout frame, the reconstruction algorithm has to deal effectively with the combinatorial background in order to reduce the fake rate, i.e. the rate of wrongly reconstructed tracks, to an acceptable level. The combinatorial problem is not only due to the high rate but also due to the large bending of the low momentum electrons in the strong magnetic field of $B = 1$ T, which, depending on the position and flight direction can make several turns in the detector (recurlers). Hit combinations can span over distances of more than half a meter. Hits of recurling tracks are found on opposite sides of the detector and still have to be correctly combined by the reconstruction program. This is of particular importance for the determination of the flight direction and therefore charge of the particle. Only for a fully reconstructed track the time information provided by the time of flight system can be correctly applied.

As the full detector readout is triggerless, all muon decays have to be fully reconstructed already on filter farm level, setting high demands

on the speed of the online track reconstruction algorithm. A further complication comes from the fact that the track resolution is dominated by multiple scattering in the silicon pixel sensors and not by the pixel size, in contrast to most other experiments. Therefore, standard non-iterative circle fits of tracks [174] as used in high energy experiments can not be used here.

In order to reduce multiple scattering, the number of sensor layers are reduced to a minimum in the detector design which, unfortunately, also reduces redundancy for track reconstruction. Therefore, the track reconstruction also has to cope with a minimum of information provided by only four sensor layers.

16.2 Track Fitting and Linking

For the track reconstruction two different approaches are followed in the Mu3e experiment, the broken line fit [175, 176] and the fast linear fit based on multiple scattering [177]. The broken line fit determines hit positions and scattering angles simultaneously and was implemented in 2D [175, 178] and recently also in 3D [176, 179]. It is based on linearisation of a previous circle fit, works non-iteratively and provides the correlation between all fit quantities. The broken line fit, however, requires knowledge of the assignments of hits to tracks from a previous linking step. Therefore, the broken line fit can only be used in the final step of the track reconstruction, also because a previous track fit is required for the linearisation procedure.

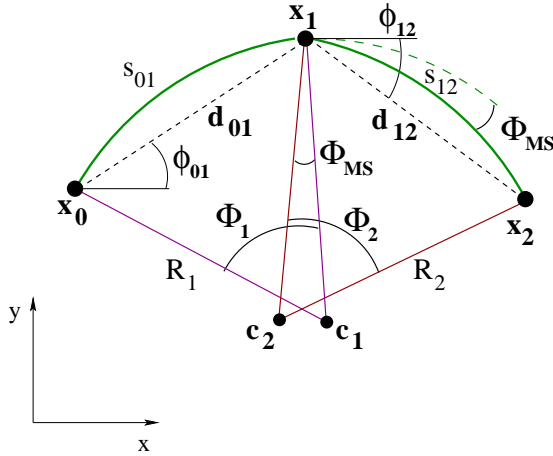


Figure 16.1: Sketch of the variables used in the multiple scattering fit.

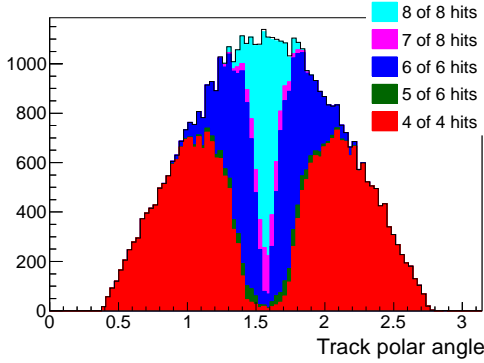


Figure 16.2: Track types versus track polar angle for Michel decays in phase IA.

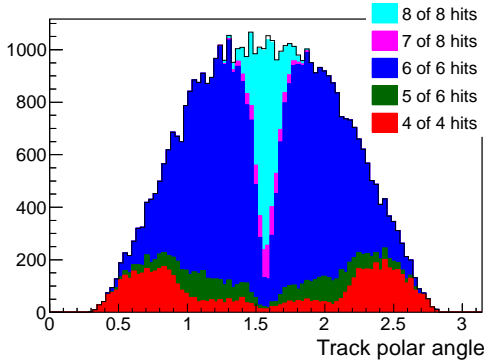


Figure 16.3: Track types versus track polar angle for Michel decays in phase IB.

The fast three-dimensional multiple scattering (MS) fit [177] is based on fitting the multiple scattering angles at the middle hit position in a hit triplet combination, see Figure 16.1. In this fit, spatial uncertainties of the hit positions are ignored. This is a very good approximation for the Mu3e experiment as the pixel resolution uncertainty given by $\sigma_{\text{pixel}} = 80/\sqrt{12} \mu\text{m}$ is much smaller than the uncertainty from multiple scattering in the corresponding sensor layer. The MS-fit requires a detailed knowledge of the material distribution in the detector for the calculation of the scattering angle uncertainty. It minimises the azimuthal and polar scattering angles at the sensor corresponding to the middle hit and exploits energy conservation¹. The hit triplet trajectory, represented by two connected helical curves, is described by the following two equations:

$$\sin^2 \frac{\Phi_1}{2} = \frac{d_{01}^2}{4R_{3D}^2} + \frac{z_{01}^2}{R_{3D}^2} \frac{\sin^2(\Phi_1/2)}{\Phi_1^2} \quad (16.1)$$

$$\sin^2 \frac{\Phi_2}{2} = \frac{d_{12}^2}{4R_{3D}^2} + \frac{z_{12}^2}{R_{3D}^2} \frac{\sin^2(\Phi_2/2)}{\Phi_2^2} \quad (16.2)$$

The quantities, also shown in the sketch of Figure 16.1, are the following: R_{3D} is the three dimensional track radius, which can be directly related to the momentum of the particle for a given magnetic field; Φ_1 (Φ_2) are the bending angles of the first (second) arc and d_{01} (d_{12}) and z_{01} (z_{12}) are the distances between the hits in the plane transverse and longitudinal to the solenoidal magnetic field between the first and second (second

¹the energy loss in the Mu3e experiment is only about 80 keV per sensor layer and can be neglected for track finding.

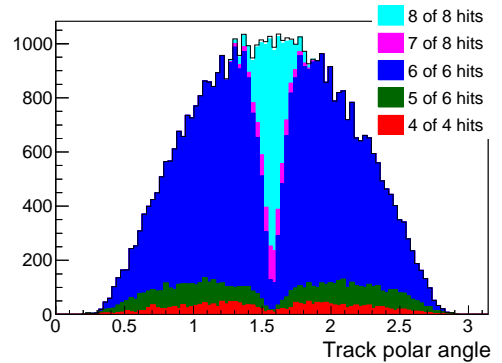


Figure 16.4: Track types versus track polar angle for Michel decays in phase II.

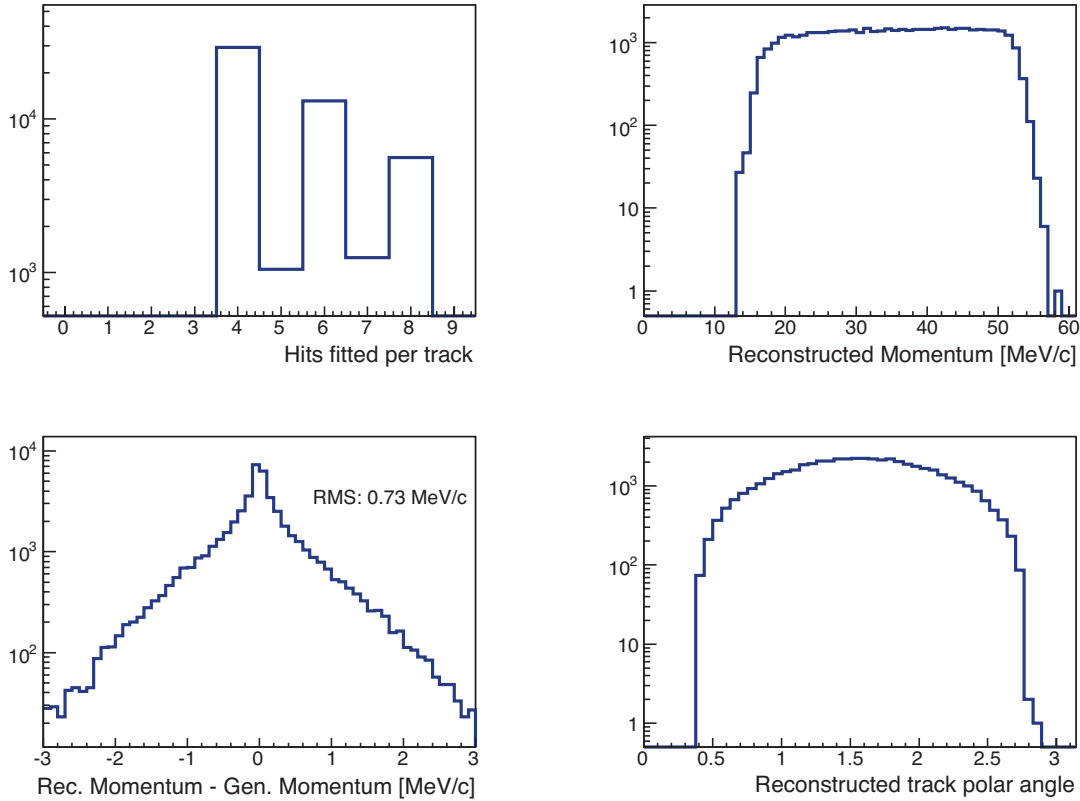


Figure 16.5: Tracking performance for Michel decays in phase IA.

and third) hit, respectively. These equations can be linearized and solved in a fast non-iterative procedure [177].

This linearized MS-fit is used as basis for the full reconstruction of tracks in the pixel detector. Tracks with more than three hits are fitted by subsequently combining several hit triplets. In the current reconstruction program [180], long tracks combining hits from several pixel layers are reconstructed first, then shorter tracks with fewer hit assignments are reconstructed. This procedure is repeated until no hits are left or no further tracks are found. Tracks with unresolved hit ambiguities are ignored in the following study to ensure high quality tracks with low fake rate. Also tracks with less than four hits combined are ignored.

The number of hits linked to tracks depends on the single hit efficiency, which is assumed to be 98% in the following studies, on the track direction (polar angle), the geometry of the pixel tracker and the geometrical acceptance of the detector,

which is largest in phase II with four recurl stations. The multiplicity of linked tracks as function of the polar angle is shown in Figures 16.2, 16.3 and 16.4 for the three different detector configurations. The multiplicity of linked hits is highest in the central region of the detector, where recurling tracks can be fully reconstructed. In the current version of the reconstruction program, only single turns of tracks are reconstructed, corresponding to a maximum of eight hits - four hits assigned to the outgoing trajectory and four hits assigned to the returning trajectory. In cases where one hit is missing, only seven hits are linked. For upstream or downstream going tracks the recurlers are not fully reconstructed, leading to tracks with mainly four linked hits or six linked hits depending on the detector setup and the number of implemented recurl stations. It should be noted here that there is a big qualitative difference between the four-hit tracks and tracks with more than 4 hits (recurlers). The bending radius of recurling tracks

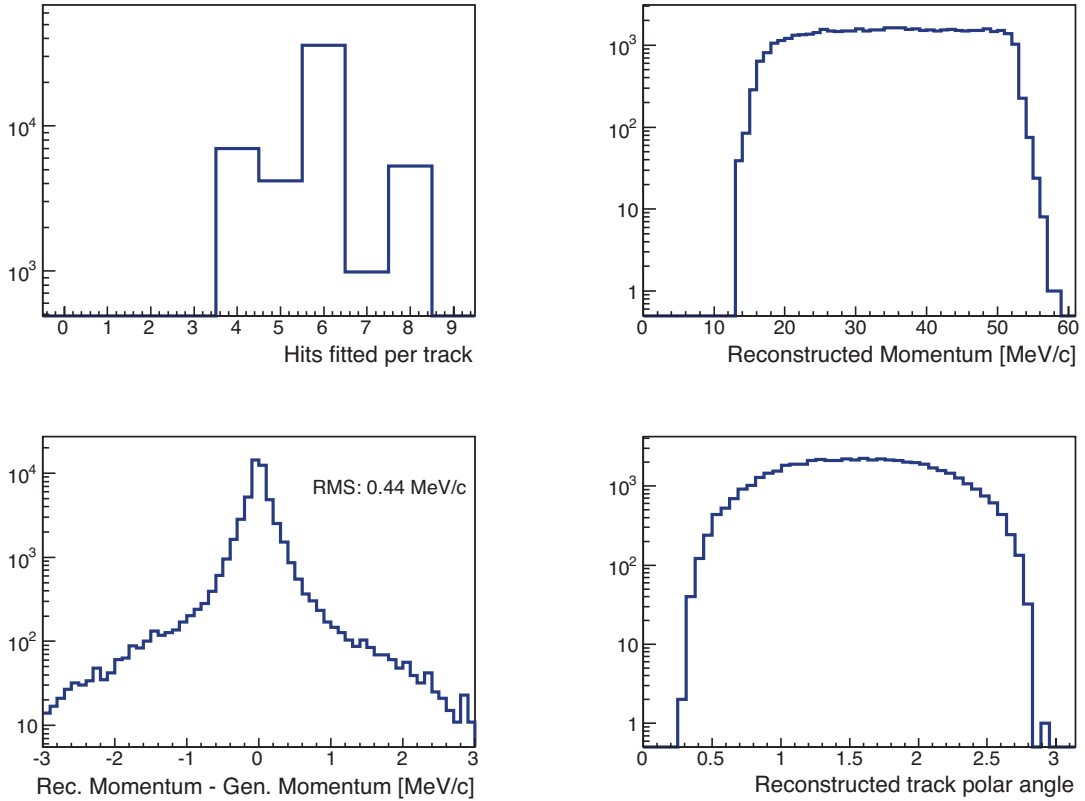


Figure 16.6: Tracking performance for Michel decays in phase IB.

can be measured with much higher precision due to the larger bending in the magnetic field. This leads to very different momentum resolutions for the different detector setups.

In phase IA without Recurl Stations most tracks are reconstructed with only four linked hits. This yields a momentum resolution for reconstructed Michel electrons of about $RMS(p) = 0.73 \text{ MeV}/c$, see Figure 16.5. This resolution improves considerably to $RMS(p) = 0.44 \text{ MeV}/c$ by adding two inner Recurl Stations in phase IB (Figure 16.6) and it improves further to $RMS(p) = 0.28 \text{ MeV}/c$ by adding two inner and two outer Recurl Stations in phase II (Figure 16.7). The reconstruction of the recurling tracks, which provide high resolution momentum information, is crucial for the success of the experiment.

16.3 Vertex Fitting

A vertex fit will be used to precisely reconstruct the position of the muon decay for signal events. The vertex fit intrinsically checks the consistency of the assumption that all three signal candidate tracks originate from the same vertex. A common vertex fit of the three candidate electrons allows a suppression of the combinatorial background of Michel decays by a factor of about $3 \cdot 10^8$ due to the very good pointing resolution of the pixel detector, which is mainly given by the multiple scattering at the first sensor layer. Instead of using a common vertex fit, also the distance between target impact points of reconstructed and extrapolated tracks can be used to discriminate signal against background. For simplicity the latter approach is used here for the following sensitivity study.

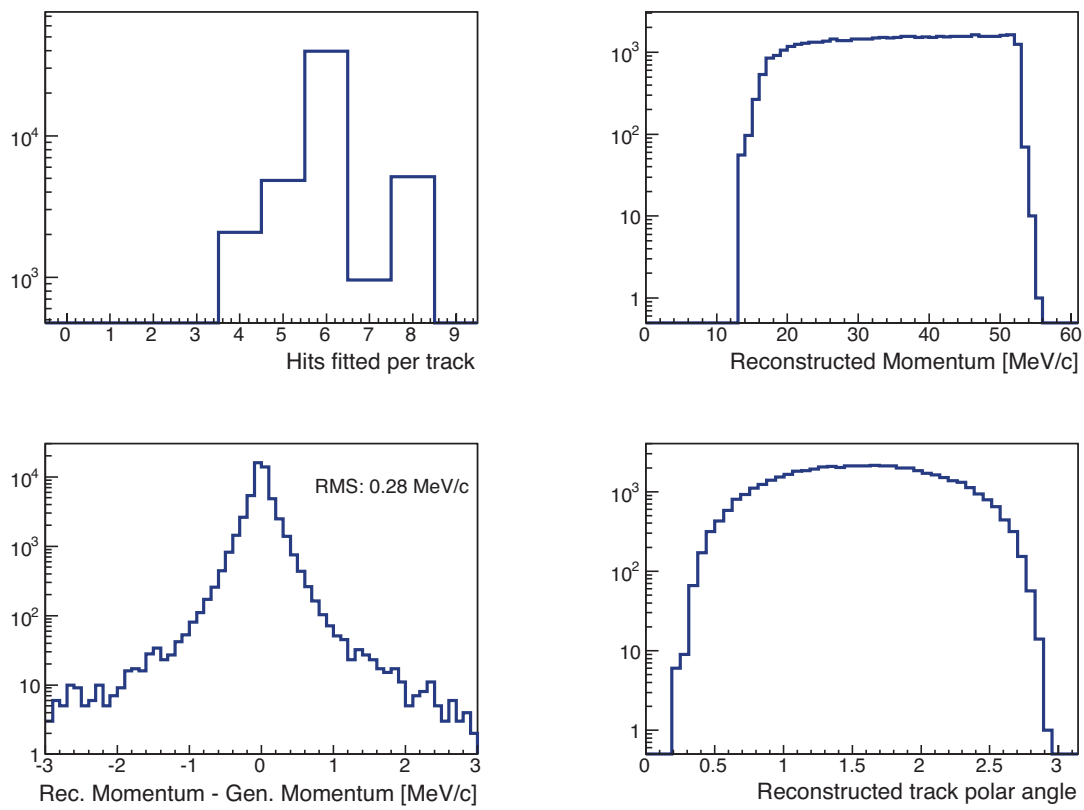


Figure 16.7: Tracking performance for Michel decays in phase II.



SENSITIVITY STUDY

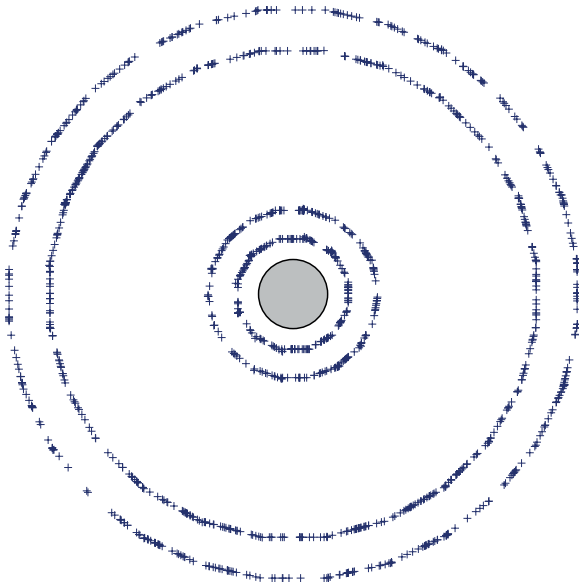


Figure 17.1: Hits in a simulated event at $2 \cdot 10^9$ Hz muon rate, viewed in the plane transverse to the beam.

A sensitivity study based on a full simulation of the pixel detector is performed to estimate the background contribution at the different phases of the Mu3e experiment. The simulation includes a first material description of the detector, which varies between the different detector phases. The increasing level of detector instrumentation at later stages of the experiment will provide more information for particle tracking on one hand. On the other hand, the scintillating fibre tracker, which will be added at a later stage of the experiment when running at high muon rates, will also

add multiple scattering and consequently increase confusion in the track linking step. In addition, the factor 10 and 100 higher increased particle rates at the Phase IB and II, respectively, will significantly increase the combinatorial background from Michel decays and other accidentals. A detailed simulation is therefore required to estimate the sensitivity reach of the different experimental phases. The simulated setups are summarized in Table 17.1.

17.1 Simulation and Reconstruction Software

In order to estimate the maximum achievable sensitivities at the different stages of the project the track reconstruction program [180] is interfaced to a) a full GEANT simulation of the detector and b) to a fast simulation program, which is mainly used for the following sensitivity studies. Both simulations were cross checked to give comparable values for the track parameter resolution.

In a first test it was proven that the track reconstruction program is relatively insensitive with regards to changes of the single hit efficiency. Using tight reconstruction criteria it is found that a 5% loss of signal hits corresponds to an about 5% loss of tracks and an about 10% loss of signal events.

Noise hits also affect the track reconstruction. From noise studies of the MUIX2 prototype chip it is known that the noise rate is very small (no noise hits were observed in an overnight run at a low threshold). To simulate the effect of noise



	Phase IA	Phase IB	Phase II
Recurl stations	0	2	4
Scintillating fibres	No	Yes	Yes
Charge measurement	No	Yes	Yes
Target stopping rate ¹ (Hz)	$2 \cdot 10^7$	$2 \cdot 10^8$	$2 \cdot 10^9$

Table 17.1: Mu3e configurations considered for the sensitivity studies. Note that the detector acceptance is about 50% for signal events, given by the geometry of the central pixel detector.

¹ Highest possible rates are assumed in the simulation in order to be conservative.

100 additional hits are randomly generated in the pixel detectors, corresponding to a noise rate of 10^{-6} Hz per pixel. This rate will be remeasured as soon as a first large scale detector including a full readout chain becomes available.

17.2 Signal Acceptance

Signal events are generated by using a constant matrix element in phase space. This choice is motivated by LFV models with effective four-fermion contact interactions, which predict a constant matrix element. The so generated signal events are used for the following efficiency studies.

The resulting signal efficiency is mainly given by the acceptance of the experiment, which is in total about 50% for the innermost detector layers being placed at radii of approximately 2.0 cm and 3.0 cm. The total acceptance consists of two contributions, one related to the orientation of the decay plane with respect to the instrumented regions of the experiment and one from the minimum bending radius (momentum), which can be reconstructed in the experimental setup.

By moving the inner pixel layers closer to the target, the total acceptance can be slightly increased to about 55%. Further improvements of the total acceptance to about 60% or more are only possible by using a longer inner barrel design and by reconstructing particles with a lower momentum threshold. The latter can be achieved in two ways - a) by including highly bent trajectories in the track reconstruction or b) by decreasing the strength of the magnetic field, which however also compromises the momentum resolution.

In the following, a conservative design is chosen with inner sensor layers placed at 2.0 and 3.0 cm and outer sensor layers placed at 7.0 and 8.0 cm, providing a signal acceptance of about 50%.

The resulting mass resolutions calculated from the reconstructed track parameters are shown in Figures 17.2-17.4 for the different phases. Compared to phase IA, the mass resolutions improve considerably by adding the recurl stations at phase IB and phase II and yield - despite the additional material from the scintillating fibre tracker - resolutions well below 1 MeV. Of special importance for the background suppression is the strong reduction of the tails in the phase II setup.

17.3 Selection

17.3.1 KINEMATIC SELECTION OF SIGNAL EVENTS

The mass resolution can be further improved by rejecting badly reconstructed signal events, where one or several tracks are either wrongly reconstructed or suffer from large multiple scattering. A wrong measurement of the track momentum or direction affects momentum balance and leads to a measurable missing momentum. In the following we follow the strategy of the SINDRUM experiment [15] and define an acoplanar momentum vector p_{acopl} , which is obtained by projecting the vectorial sum of all track momenta into the decay plane defined by the three tracks. The correlation between the reconstructed invariant mass and the variable p_{acopl} is shown in Figures 17.5. In addition to the main spot at small values of p_{acopl} , which originates from well measured signal events, two diagonal sidebands originating from wrongly measured signal events are visible. By applying the cut $p_{\text{acopl}} < 1.4 \text{ MeV}/c$, which will also be used to reject background events in the following, most of the wrongly measured signal events are rejected.

The resulting mass resolution plots are shown in Figure 17.6-17.8, which show by about 20% im-



proved resolutions and significantly reduced tails. The expected mass resolutions and signal efficiencies for the three stages of the experiment are summarized in Table 17.2.

The main criterion for the kinematic selection of signal events is the reconstructed invariant mass. In a final analysis the number of signal and background events will be determined by a fit of the invariant mass distribution, see also Figures 17.12-17.14 or by exploiting multivariate methods which include several estimators. For sake of simplicity the number of signal events is here determined from a 2-sigma mass window around the nominal muon mass.

17.3.2 REDUCTION OF THE $\mu \rightarrow eee\nu\nu$ BACKGROUND

The acoplanar momentum cut is also very effective in reducing the dominating background from radiative events with internal conversion $\mu \rightarrow eee\nu\nu$. These events are characterized by missing energy carried away by the two undetected neutrinos. Most of these background events have either a small value of the reconstructed three electron mass m_{eee} or show some momentum imbalance. In particular the class of dangerous background events, which have only little missing energy, carried away by the two neutrinos, and are wrongly reconstructed such that the reconstructed invariant mass matches the muon mass, show some significant momentum imbalance. Most of these background events are rejected by the cut $p_{\text{acopl}} < 1.4 \text{ MeV}/c$.

The separation of signal and background in the plane p_{acopl} versus m_{eee} is shown for the three stages of the experiments in Figures 17.9-17.11. A clear separation of signal and background events at a level of $10^{-17} - 10^{-16}$ muon decays is visible. This separation improves with the upgraded experiment at phase IB and II.

The projected invariant mass distribution of signal and background after applying the acoplanar momentum cut is shown in the Figures 17.12-17.14. These distributions are used as basis for the estimated sensitivity calculation.

17.3.3 REDUCTION OF ACCIDENTAL BACKGROUND

The dominant contribution to the accidental background comes from combinatorial background of

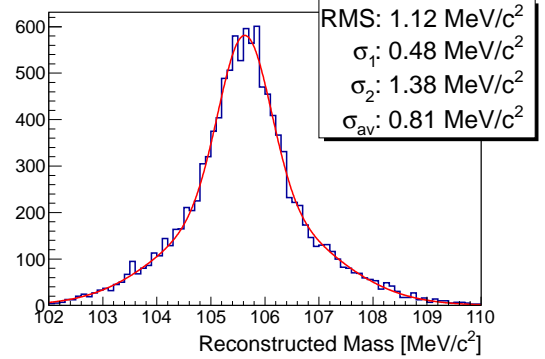


Figure 17.2: Reconstructed mass resolution for signal events in the phase IA configuration.

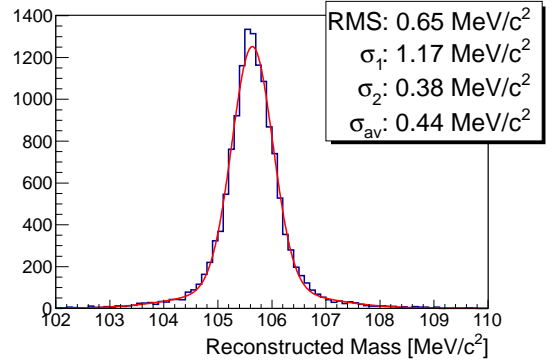


Figure 17.3: Reconstructed mass resolution for signal events in the phase IB configuration.

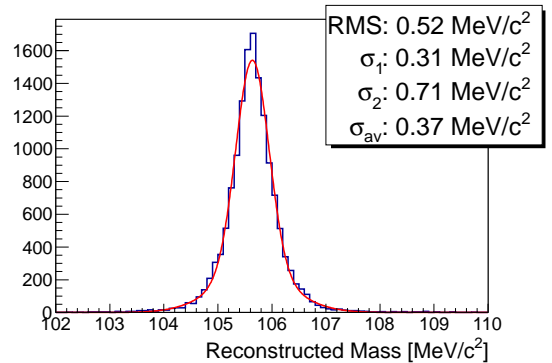


Figure 17.4: Reconstructed mass resolution for signal events in the phase II configuration.



	Phase IA	Phase IB	Phase II
Michel decays:			
Efficiency (unpolarized)	50.0 %	53.4 %	52.4 %
Momentum RMS	0.73 MeV/c	0.44 MeV/c	0.28 MeV/c
Wrong charge fraction	1.14 %	0.45 %	0.45 %
Signal:			
Reconstruction efficiency	39 %	46 %	48 %
Energy sum RMS (reconstructed)	1.12 MeV/c ²	0.65 MeV/c ²	0.52 MeV/c ²
Efficiency after selection	26 %	39 %	38 %
Energy sum RMS (selected)	0.91 MeV/c ²	0.47 MeV/c ²	0.42 MeV/c ²
Track d_{ca} resolution (σ)	190 μm	185 μm	185 μm

Table 17.2: Efficiencies and resolutions used in the sensitivity study. d_{ca} is the distance of closest approach of a track to the beam line. The drop in the efficiency after selection for phase II is due to the larger combinatorial background.

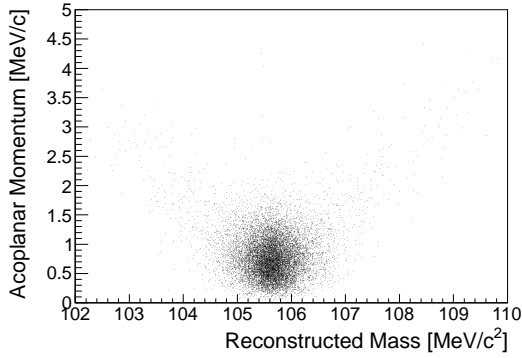


Figure 17.5: Reconstructed mass versus acoplanar momentum for the phase II detector.

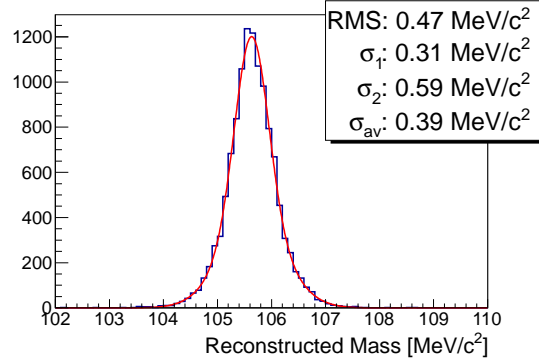


Figure 17.7: Reconstructed mass resolution for signal events after kinematic cuts in the phase IB configuration.

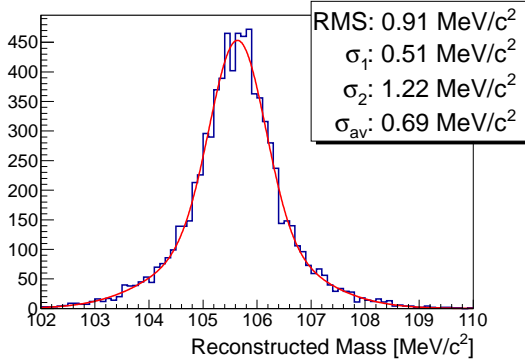


Figure 17.6: Reconstructed mass resolution for signal events after kinematic cuts in the phase IA configuration.

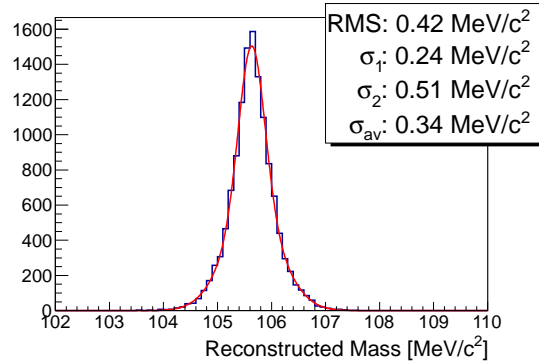


Figure 17.8: Reconstructed mass resolution for signal events after kinematic cuts in the phase II configuration.

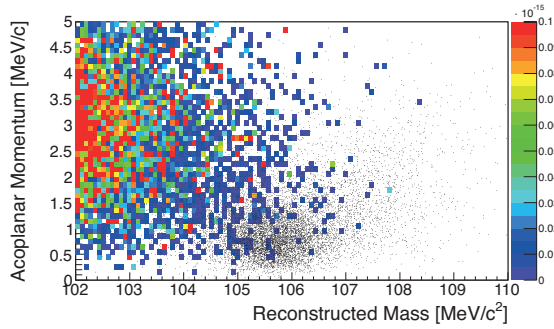


Figure 17.9: Internal conversion background (colours) and signal (black dots) in the acoplanar momentum - reconstructed mass plane for the phase IA detector configuration.

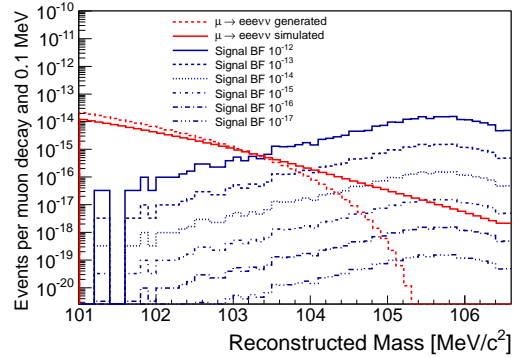


Figure 17.12: Tail of the internal conversion distribution overlaid with signal at different branching ratios for the phase IA detector. The resolution for the internal conversion decays was taken from 30 000 simulated signal decays.

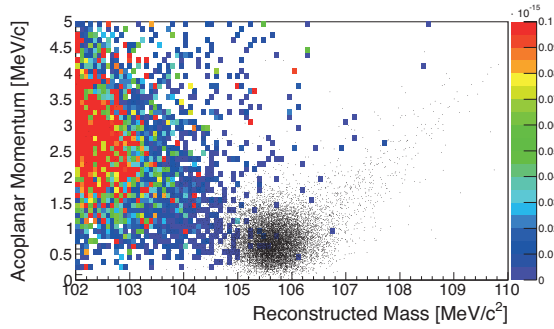


Figure 17.10: Internal conversion background (colours) and signal (black dots) in the acoplanar momentum - reconstructed mass plane for the phase IB detector configuration.

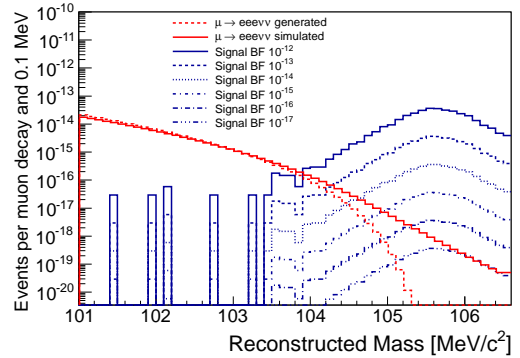


Figure 17.13: Tail of the internal conversion distribution overlaid with signal at different branching ratios for the phase IB detector. The resolution for the internal conversion decays was taken from 30 000 simulated signal decays.

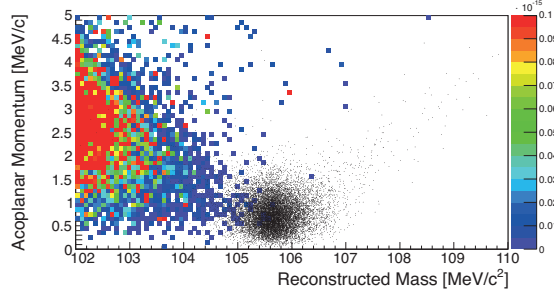


Figure 17.11: Internal conversion background (colours) and signal (black dots) in the acoplanar momentum - reconstructed mass plane for the phase II detector configuration.

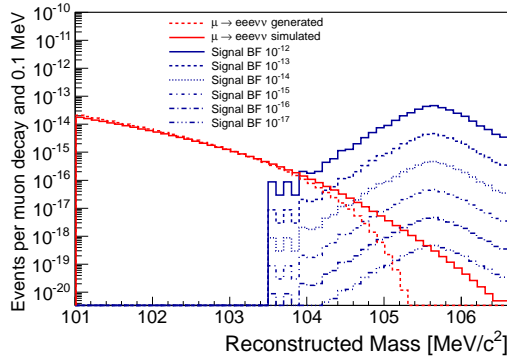


Figure 17.14: Tail of the internal conversion distribution overlaid with signal at different branching ratios for the phase II detector. The resolution for the internal conversion decays was taken from 30 000 simulated signal decays.

three Michel decays $3 \times (\mu \rightarrow e\nu\nu)$ and from coincidences of a radiative muon decay with internal conversion $\mu \rightarrow eee$ with a Michel decay $\mu \rightarrow e\nu\nu$. Both types of backgrounds are significantly reduced by applying vertex and time requirements. The combinatorial Michel background depends quadratically on the vertex and time resolution, whereas the coincidences $\mu \rightarrow eee \times \mu \rightarrow e\nu\nu$ coincidence rate scale linearly with the vertex and the time resolution.

The vertex resolution in the transverse direction can be represented by the distance of closest approach when the track is extrapolated to the muon decay position. This value is about 185 μm in all phases of the experiment and given in Table 17.2. For a target size of 10 cm in length and 2 cm in diameter a reduction factor of $1 \cdot 10^{-4}$ can be derived per coincidence.

The estimation of the reduction factor from the timing cut, relevant for phases Ib and II, is difficult as the design for the time of flight system has not been finalised yet. Another difficulty comes from the fact that the timing resolutions of the scintillating fibre detector and the scintillating tiles detector

are expected to be different and that particles depending on their flight direction will be measured in both detectors or by the scintillating fibre detector only if staying in the central region. In the latter case the particles will be measured many times in several turns, what also leads to an increase in precision. Preliminary studies indicate that timing resolutions of 200-300 ps in the scintillating fibre detector and < 100 ps in the Scintillating Tiles Detector can be achieved, see sections 11 and 12. For the sensitivity calculation it is assumed that all particles will be measured with a time resolution of better than 250 ps and that reduction factors of $5 \cdot 10^{-3}$ per coincidence can be obtained at a signal efficiency of 90 %.

17.4 Results

The signal efficiencies and the expected background reduction factors of the different selection cuts are summarized in Table 17.3. Single event sensitivities are calculated, which are defined as the branching ratio at which one background event is expected. The sensitivity of the experiment scales with one over the number of muons on target as long as the single event sensitivity is not reached and with one over the square root of the number of muons on target after. It can be seen that the single event sensitivity at phase IB is higher than at phase II. This comes from the fact that the combinatorial background increases at higher muon rates. However, the time to reach the aimed sensitivity of $1 \cdot 10^{-16}$ takes in phase IB ten years of running whereas at phase II this sensitivity can be reached in 180 days because of the higher muon rate, see Figure 17.15. Although the expected sensitivity at phase IA, even without the time of flight system, is quite high with $4 \cdot 10^{-16}$ it would take a long time of running to reach this sensitivity. However, about one month of running is sufficient to reach a sensitivity of $1 \cdot 10^{-13}$, which is factor ten smaller than the current experimental bound.



	Phase IA	Phase IB	Phase II
Backgrounds:			
Michel	0	$< 2.5 \cdot 10^{-18}$	$5 \cdot 10^{-18}$
$\mu \rightarrow eee\nu\nu$	$1 \cdot 10^{-16}$	$1 \cdot 10^{-17}$	$1 \cdot 10^{-17}$
$\mu \rightarrow eee\nu\nu$ and accidental Michel	0	$< 2.5 \cdot 10^{-21}$	$7.5 \cdot 10^{-18}$
Total Background	$1 \cdot 10^{-16}$	$1 \cdot 10^{-17}$	$2.3 \cdot 10^{-17}$
Signal:			
Track reconstruction and selection efficiency	26 %	39 %	38 %
Kinematic cut (2σ)	95 %	95 %	95 %
Vertex efficiency ($(2.5\sigma)^2$)	98 %	98 %	98 %
Timing efficiency ($(2\sigma)^2$)	-	90 %	90 %
Total efficiency	24 %	33 %	32 %
Sensitivity:			
Single event sensitivity	$4 \cdot 10^{-16}$	$3 \cdot 10^{-17}$	$7 \cdot 10^{-17}$
muons on target rate (Hz)	$2 \cdot 10^7$	$1 \cdot 10^8$	$2 \cdot 10^9$
running days to reach $1 \cdot 10^{-15}$	2600	350	18
running days to reach $1 \cdot 10^{-16}$	-	3500	180
running days to reach single event sensitivity	6500	11 700	260

Table 17.3: Signal efficiencies and estimated background reduction factors of the discussed selection cuts, which are used to determine the single event sensitivities for the three phases of the experiment. For the given muon on target rates running times are calculated to reach the given single event sensitivities.

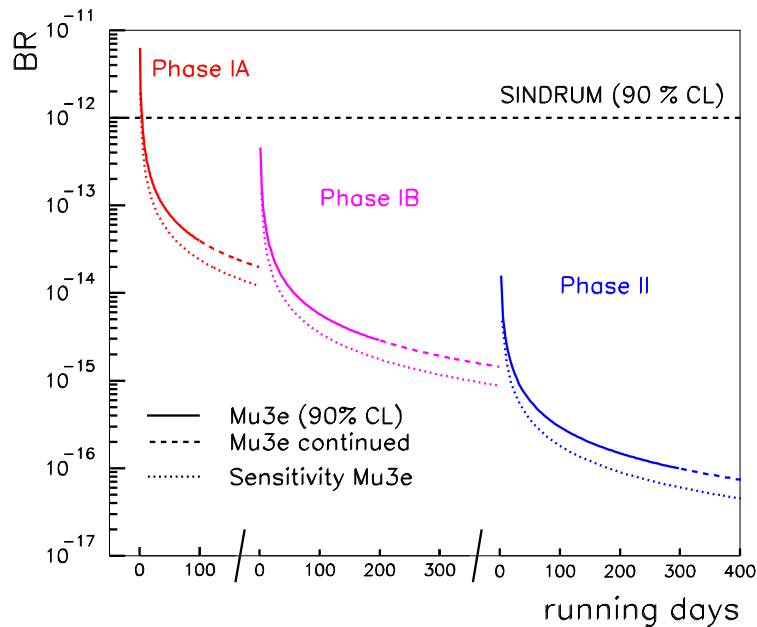


Figure 17.15: Projected sensitivity and projected limit (90% CL) of the *Mu3e* experiment for the three construction phases IA (red), IB (magenta) and II (blue) as function of the running time. The curves were obtained from the corresponding numbers in Table 17.3. For comparison also the (90% CL) obtained from the SINDRUM experiment is indicated (black dashed line).

PART III



THE MU3E COLLABORATION



THE INSTITUTES IN MU3E

18.1 Responsibilities

The responsibilities of the institutes participating in Mu3e are outlined in Table 18.1. This list concerns the phase I experiment and does not imply funding responsibilities.

18.2 Collaborators

18.2.1 UNIVERSITY OF GENEVA

Currently working on Mu3e:

Alain Blondel *Professor*

Alessandro Bravar *Professor*

Martin Pohl *Professor*

Antoaneta Damyanova *Master student*

Planned positions:

1 *Postdoc*

1 *Ph.D. candidate*

18.2.2 UNIVERSITY OF ZÜRICH

Currently working on Mu3e:

Ueli Straumann *Professor*

Peter Robmann *Senior scientist*

Roman Gredig *Ph.D. candidate*

18.2.3 PAUL SCHERRER INSTITUT

Currently working on Mu3e:

Felix Berg *Ph.D. candidate*

Malte Hildebrandt *Senior scientist*

Peter-Raymond Kettle *Senior scientist*

Angela Papa *Senior scientist*

Stefan Ritt *Senior scientist*

Alexey Stoykov *Senior scientist*

Funded open positions:

1 *Postdoc*

1 *Ph.D. candidate*

18.2.4 ETH ZÜRICH

Currently working on Mu3e:

Christophorus Grab *Professor*

Günther Dissertori *Professor*

Rainer Wallny *Professor*

Planned positions:

1 *Ph.D. candidate*

18.2.5 UNIVERSITY OF HEIDELBERG

Physikalisches Institut (PI)

Currently working on Mu3e:

André Schöning *Professor*

Dirk Wiedner *Senior scientist*

Sebastian Bachmann *Senior scientist*

Niklaus Berger *Junior research group leader*

Bernd Windelband *Mechanical engineer*

Moritz Kiehn *Ph.D. candidate*

Kevin Stumpf *Mechanical engineer*

Raphael Philipp *Master student*

Funded open positions:

1 *Postdoc*

4 *Ph.D. candidates*

Planned positions:

1 *Postdoc*

1 *Ph.D. candidate*



Kirchhoff Institut für Physik (KIP)

Currently working on Mu3e:

Hans-Christian Schultz-Coulon *Professor*

Wei Shen *Postdoc*

Patrick Eckert *Ph.D. candidate*

Carlo Licciulli *Master student*

Tobias Hartwig *Bachelor student*

Planned positions:

1 *Postdoc*

1 *Ph.D. candidate*

Zentralinstitut für Technische Informatik

Currently working on Mu3e:

Peter Fischer *Professor*

Ivan Péric *Senior scientist*

COMPONENT	RESPONSIBLE
Beam	PSI
Magnet	UGS Heidelberg PI
Target	Heidelberg PI PSI
Pixel chip	ZITI Mannheim Heidelberg PI Heidelberg NB
Pixel detector	Heidelberg PI
Mechanics and cooling	Heidelberg PI
Pixel on-detector electronics	Heidelberg NB Heidelberg PI
Read-out electronics	Heidelberg NB
Fibre detector	Geneva Zürich ETHZ PSI
Tile detector	Heidelberg KIP
Timing electronics	PSI Heidelberg KIP Geneva Zürich ETHZ
Filter farm	Heidelberg NB
Slow control	PSI
Infrastructure	PSI

Table 18.1: Institutional interests and responsibilities in phase I Mu3e. NB denotes the Emmy Noether junior research group at the *Physikalisches Institut* led by N. Berger. UGS is an external engineering consultancy tasked with magnet design and procurement. Note that especially for large common items such as the magnet, design and construction responsibility does not imply funding responsibility.



SCHEDULE

19.1 Phase I Schedule

Our goal is to take first data in 2015, with a pixel-only detector. Correspondingly, the timing critical items are the central pixel detectors and the magnet. Prototyping on the first is well underway and a first instrumented assembly corresponding to the vertex layers should be operational by late 2013. Magnet design has also started, however the tendering process will consume about half a year; we hope the actual magnet construction will be under way early in 2014.

For a second, longer run in 2016, we plan to integrate the fibre detector as well as the inner recurl stations complete with timing tiles. As the outer recurl stations are identical to the inner ones, we

plan to maintain the production capacities and manufacture them during 2016.

Depending on the outcome of the 2016 run and the schedule for the high intensity beam line, 2017 could either be spent for phase II preparations or with an extended run at the existing beamline.

19.2 Phase II Schedule

The phase II schedule is contingent on the schedule for the high intensity beamline. By 2017, we can have all required detector components ready. If the phase I experience shows that major parts of the detector will have to be rebuilt, earliest phase II startup would slip to 2018.



COST ESTIMATES

Item	Estimated cost (KCHF)	Item	Estimated cost (KCHF)
Beam line	< 50	Beam line	u.a.
Target	< 10	Target	< 10
Pixel detector (central)	400	Pixel detector (upgrade central)	200
Pixel detector (2 recurl stations)	200	Pixel detector (2 recurl stations)	200
Scintillating fibres	200	Scintillating fibres	200
Tile detector (2 stations)	110	Tile detector (2 stations)	110
Mechanics and cooling	200	Mechanics and cooling	100
DAQ pixel detector	50	DAQ pixel detector	50
DAQ fibres	200	DAQ fibres	200
DAQ tiles	190	DAQ tiles	190
Central DAQ	100	Central DAQ	100
Filter farm	50	Filter farm	50
Slow control	50	Slow control	50
Infrastructure	100	Infrastructure	u.a.
Total	1910	Total	1460

Table 20.1: Estimated costs of the phase I experiment. The magnet (estimated at 500 KCHF) will be loaned to Mu3e by PI Heidelberg for the run time of the experiment.

Table 20.2: Estimated costs of the phase II experiment. Items marked u.a. are under assesment; the new beam line required will be by far the most expensive item but also benefit many other users.



APPENDIX

A.1 Mu3e theses

Several theses involving the Mu3e project have been completed:

- M. Kiehn, diploma thesis *Track Fitting with Broken Lines for the Mu3e Experiment*, Heidelberg University, 2012.
- M. Zimmermann, bachelor thesis *Cooling with Gaseous Helium for the Mu3e Experiment*, Heidelberg University, 2012.
- H. Augustin, bachelor thesis *Charakterisierung von HV-MAPS*, Heidelberg University, 2012.
- A.-K. Perrevoort, master thesis *Characterisation of High Voltage Monolithic Active Pixel Sensors for the Mu3e Experiment*, Heidelberg University, 2012.

These theses are available in portable document format (PDF) from <http://www.psi.ch/mu3e/documents>. Several more theses are ongoing (thus titles are preliminary):

- R. Gredig, doctoral thesis *Fibre Tracker for the Mu3e Experiment*, Zürich University, started 2012.
- M. Kiehn, doctoral thesis *Track Reconstruction for the Mu3e Experiment*, Heidelberg University, started 2012.
- A. Damyanova, master thesis *Fibre and SiPM characterization for the Mu3e Experiment*, Geneva University, started 2012.
- R. Philipp, master thesis *Tests of High Voltage Monolithic Active Pixel Sensors for the Mu3e Experiment*, Heidelberg University, started 2012.

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