

# $g-2$ of the muon: the next round



Thomas Teubner



- Introduction
- $a_{\mu}^{\text{SM}}$ : overview and update on hadronic contributions
- Status of the new experiments
- BSM?

# Introduction & motivation:

SM `too' successful, but incomplete:

- $\nu$  masses (small) and mixing point towards some high-scale (GUT) physics
- Need to explain dark matter & dark energy
- Not enough CP violation in the SM for matter-antimatter asymmetry
- And:  $a_{\mu}^{\text{EXP}} - a_{\mu}^{\text{SM}}$  at  $\sim 3-4 \sigma$  plus other deviations e.g. in the flavour sector

Is there a common New Physics (NP) explanation for all these puzzles?

- Uncoloured leptons are particularly clean probes to establish and constrain/distinguish NP, complementary to high energy searches at the LHC
- No direct signals for NP from LHC so far:
  - some models like CMSSM are in trouble already when trying to accommodate LHC exclusion limits and to solve muon  $g-2$
  - is there any **TeV scale** NP out there? Or unexpected new **low scale** physics?

The key may be provided by **low energy observables** incl. precision QED, EDMs, LFV.

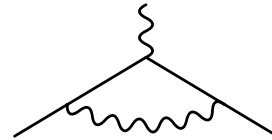
# Introduction

- Dirac equation (1928):  $g$  is 2 for fundamental fermions  $\vec{\mu} = g \frac{Qe}{2m} \vec{s}$
- 1947: small deviations from predictions in hydrogen and deuterium hyperfine structure; Kusch & Foley propose explanation with  $g_s = 2.00229 \pm 0.00008$

- 1948: Schwinger calculates the famous radiative correction:

that  $g = 2(1+a)$ , with

$$a = (g-2)/2 = \alpha/(2\pi) = 0.001161$$



“ If you can't join 'em, beat 'em “

This explained the discrepancy and was a crucial step in the development of perturbative QFT and QED

- The anomaly  $a$  (Anomalous Magnetic Moment) is from the Pauli term:

$$\delta \mathcal{L}_{\text{eff}}^{\text{AMM}} = -\frac{Qe}{4m} a \bar{\psi}(x) \sigma^{\mu\nu} \psi(x) F_{\mu\nu}(x)$$

This is a dimension 5 operator, non-renormalisable and hence not part of the fundamental (QED) Lagrangian. But it occurs through radiative corrections and is calculable in perturbation theory.

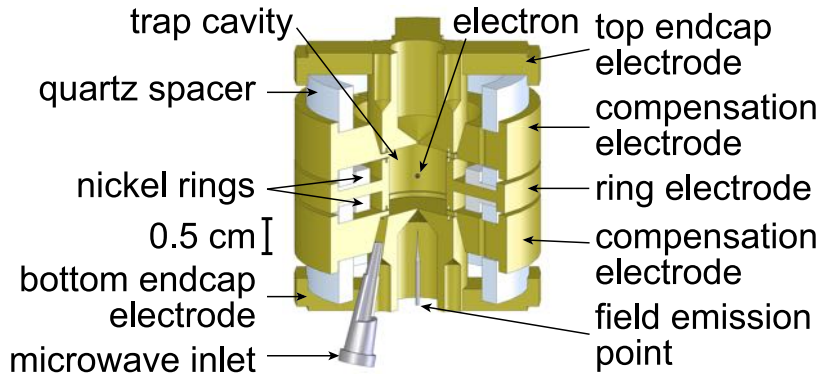
# Magnetic Moments: $a_e$ vs. $a_\mu$

$$a_e = 1\,159\,652\,180.73 (0.28) \cdot 10^{-12} \quad [0.24\text{ppb}]$$

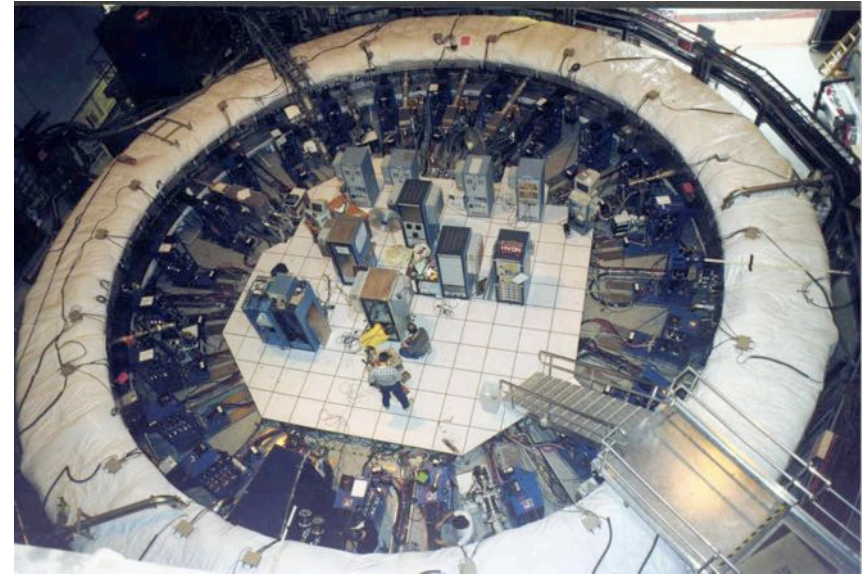
Hanneke, Fogwell, Gabrielse, PRL 100(2008)120801

$$a_\mu = 116\,592\,089(63) \cdot 10^{-11} \quad [0.54\text{ppm}]$$

Bennet et al., PRD 73(2006)072003



one electron quantum cyclotron



- $a_e^{\text{EXP}}$  more than 2000 times more precise than  $a_\mu^{\text{EXP}}$ , but for  $e^-$  loop contributions come from very small photon virtualities, whereas muon `tests' higher scales

- dimensional analysis: **sensitivity to NP** (at high scale  $\Lambda_{\text{NP}}$ ):  $a_\ell^{\text{NP}} \sim C m_\ell^2 / \Lambda_{\text{NP}}^2$

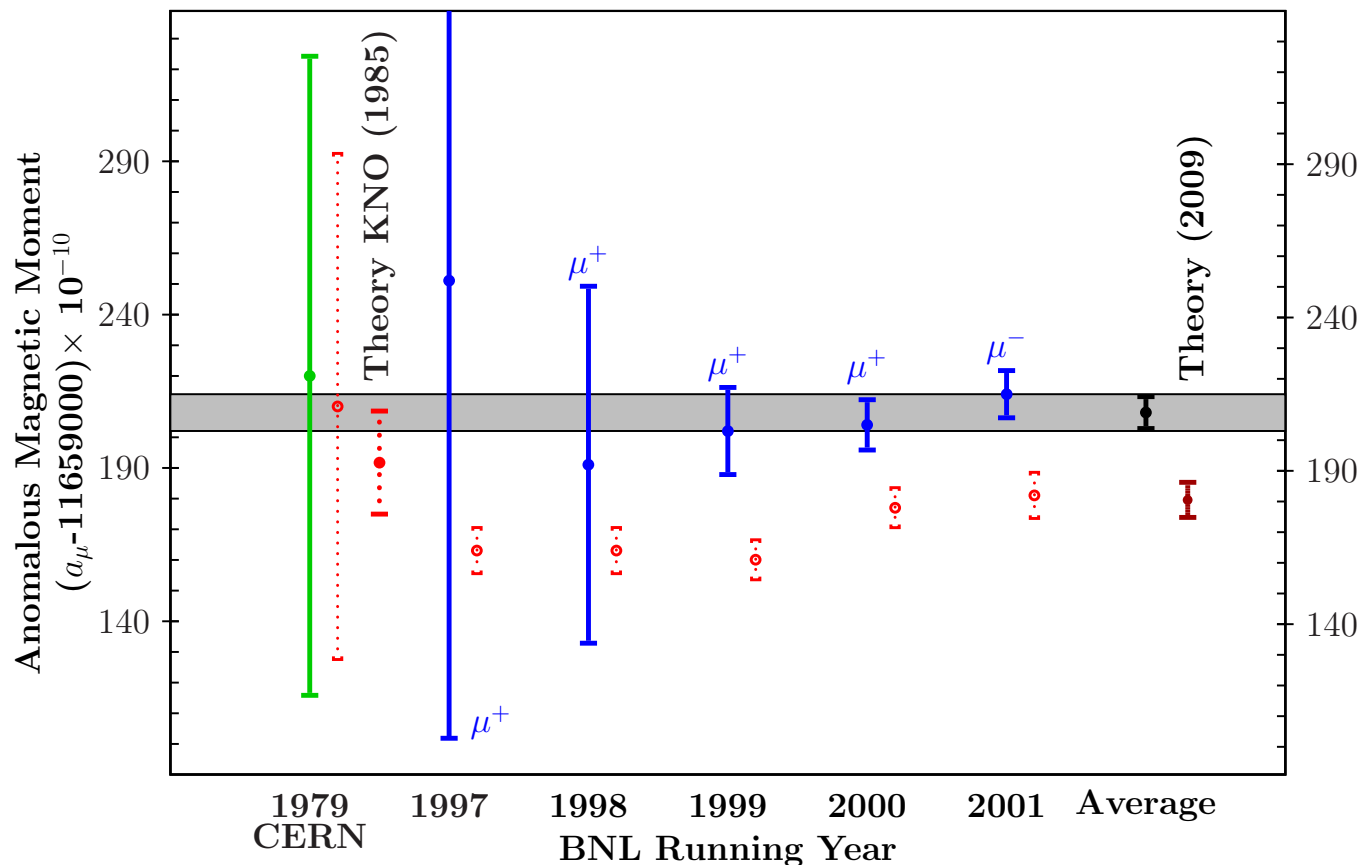
→  $\mu$  wins by  $m_\mu^2 / m_e^2 \sim 43000$  for NP, but  $a_e$  provides best determination of  $\alpha$

# $a_\mu$ : back to the future

- CERN started it nearly 40 years ago
- Brookhaven delivered 0.5ppm precision
- E989 at FNAL and J-PARC's g-2/EDM experiments are happening and should give us certainty

g-2 history plot and book motto from Fred Jegerlehner:

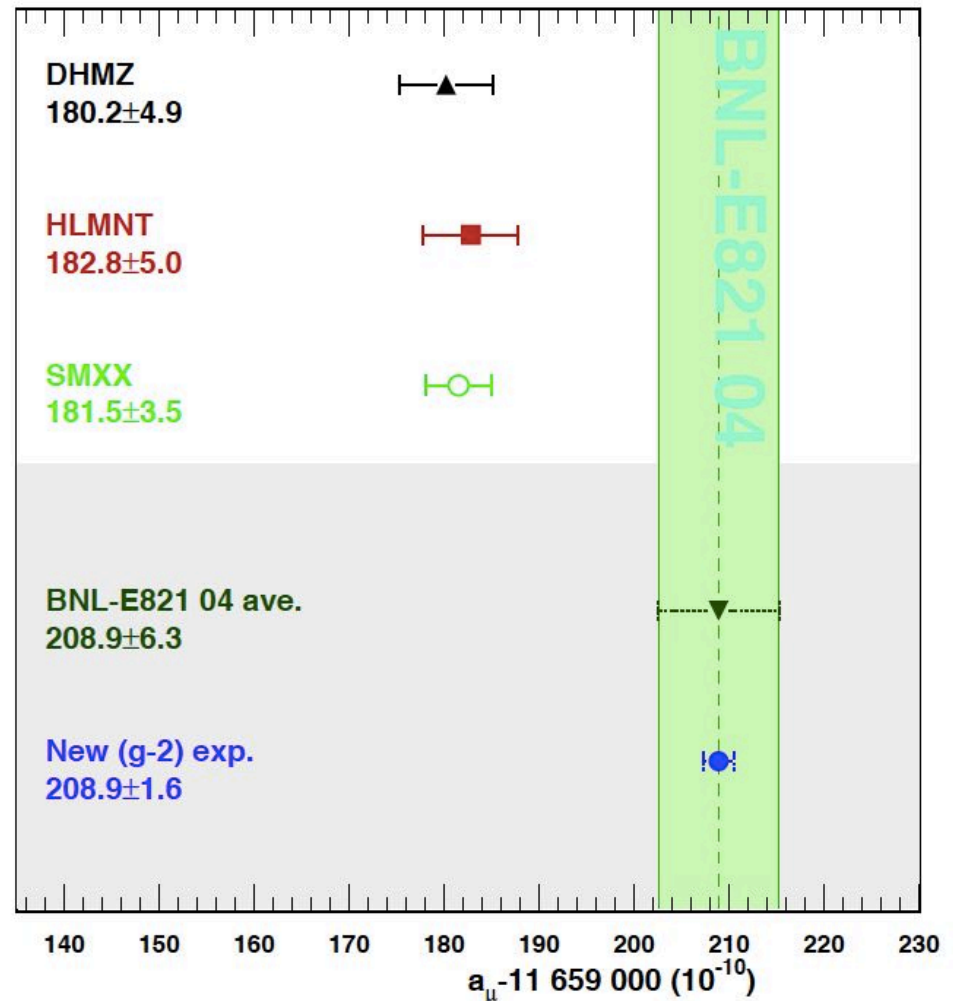
'The closer you look the more there is to see'



# $a_\mu$ : Status and future projection → charge for SM TH

$$a_\mu = a_\mu^{\text{QED}} + a_\mu^{\text{EW}} + a_\mu^{\text{hadronic}} + a_\mu^{\text{NP?}}$$

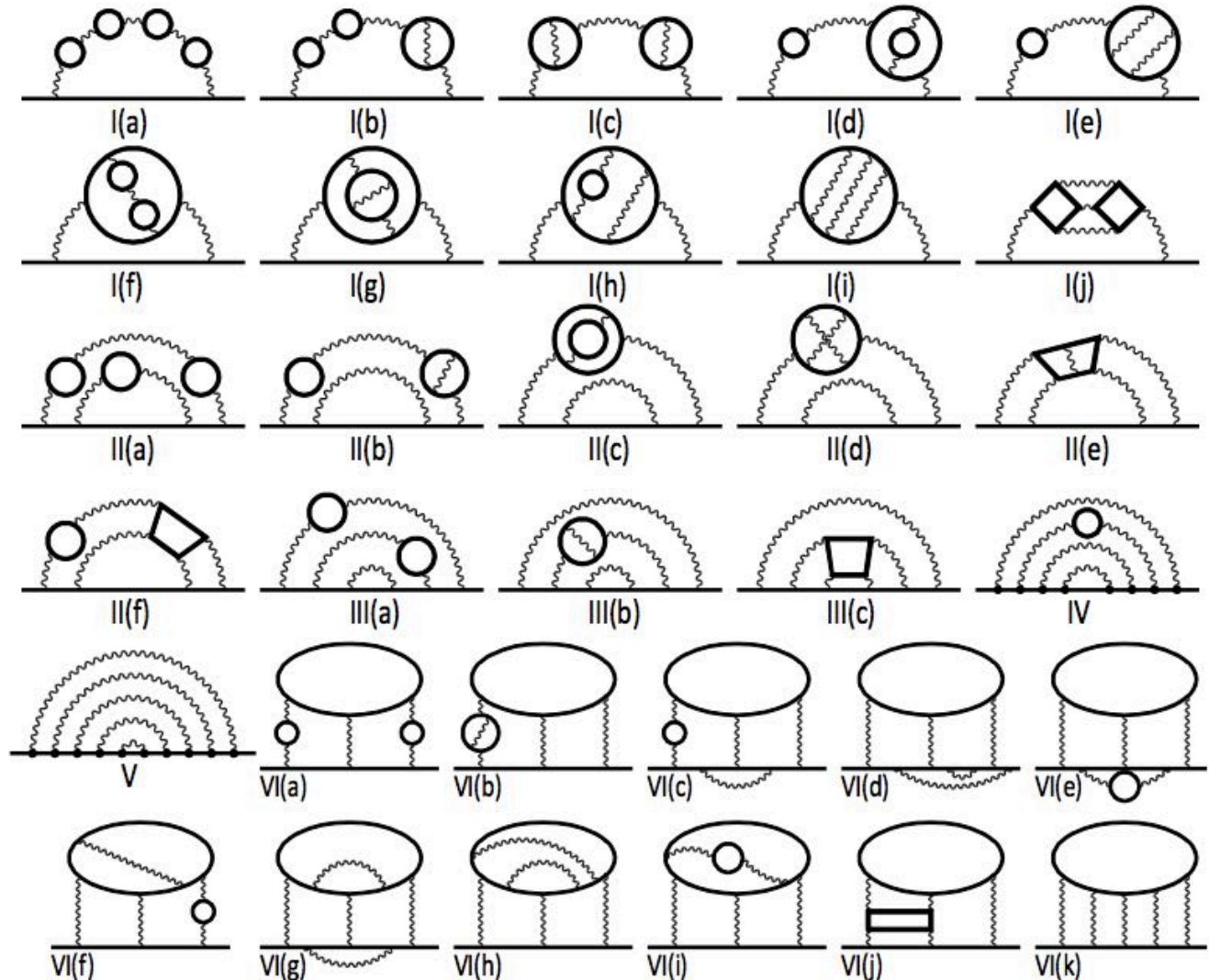
- if mean values stay and with **no**  $a_\mu^{\text{SM}}$  improvement:  
5 $\sigma$  discrepancy
- if also EXP+TH can improve  $a_\mu^{\text{SM}}$   
'as expected' (consolidation of L-by-L on level of Glasgow consensus, about factor 2 for HVP): NP at 7-8 $\sigma$
- or, if mean values get closer, very strong exclusion limits on many NP models (extra dims, new dark sector, xxxSSSM)...



T. Aoyama, M. Hayakawa,  
T. Kinoshita, M. Nio (PRLs, 2012)

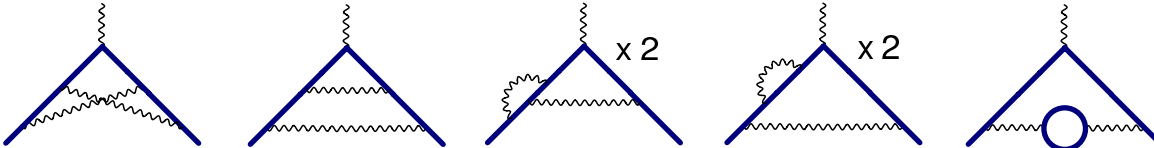
A triumph for perturbative QFT and computing!

10<sup>th</sup>  
12672  
diagrams



- code-generating code, including renormalisation
- multi-dim. numerical integrations

- **Schwinger 1948**: 1-loop  $a = (g-2)/2 = \alpha/(2\pi) = 116\,140\,970 \times 10^{-11}$

- 2-loop graphs:
 

- 72 3-loop and 891 4-loop diagrams ...

- **Kinoshita et al. 2012**: 5-loop completed numerically (12672 diagrams):

$$a_{\mu}^{\text{QED}} = 116\,584\,718.951 (0.009) (0.019) (0.007) (0.077) \times 10^{-11}$$

errors from: lepton masses, 4-loop, 5-loop,  $\alpha$  from  $^{87}\text{Rb}$

- QED extremely accurate, and the series is stable:  $a_{\mu}^{\text{QED}} = C_{\mu}^{2n} \sum_n \left(\frac{\alpha}{\pi}\right)^n$

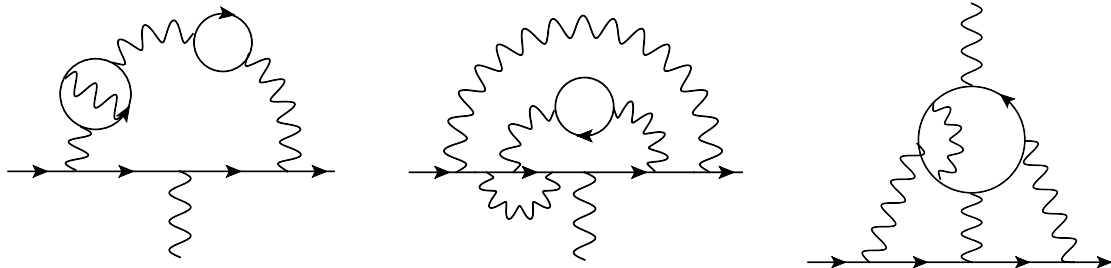
$$C_{\mu}^{2,4,6,8,10} = 0.5, 0.765857425(17), 24.05050996(32), 130.8796(63), 753.29(1.04)$$

- Could  $a_{\mu}^{\text{QED}}$  still be wrong?

Some classes of graphs known analytically ([Laporta](#); [Aguilar, Greynat, deRafael](#)),



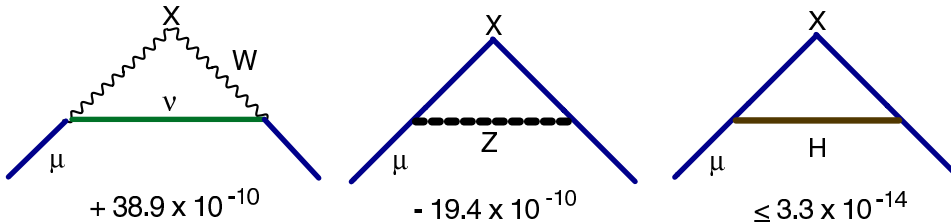
- ... but 4-loop and 5-loop rely heavily on numerical integrations
- Recently several independent checks of 4-loop and 5-loop diagrams:  
Baikov, Maier, Marquard [NPB 877 (2013) 647], Kurz, Liu, Marquard, Smirnov AV+VA, Steinhauser [NPB 879 (2014) 1, PRD 92 (2015) 073019, 93 (2016) 053017]:
- all 4-loop graphs with internal lepton loops now calculated independently, e.g.



(from Steinhauser et al., PRD 93 (2016) 053017)

- 4-loop universal (massless) term calculated semi-analytically to 1100 digits (!) by Laporta, arXiv:1704.06996, also new numerical results by Volkov, 1705.05800
- all agree with Kinoshita et al.'s results, so **QED is on safe ground** ✓

- Electro-Weak 1-loop diagrams:



$$a_\mu^{\text{EW}(1)} = 195 \times 10^{-11}$$

- known to 2-loop (1650 diagrams, the first full EW 2-loop calculation):  
Czarnecki, Krause, Marciano, Vainshtein; Knecht, Peris, Perrottet, de Rafael

- agreement,  $a_\mu^{\text{EW}}$  relatively small, 2-loop relevant:  $a_\mu^{\text{EW}(1+2 \text{ loop})} = (154 \pm 2) \times 10^{-11}$

- Higgs mass now known, update by Gneidiger, Stoeckinger, S-Kim,

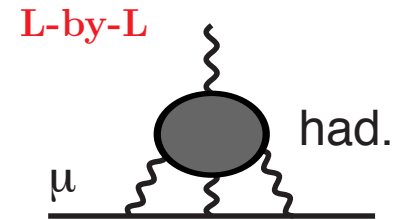
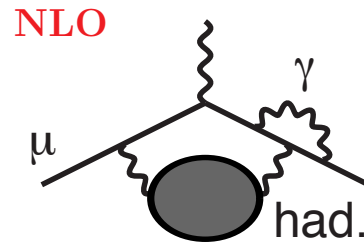
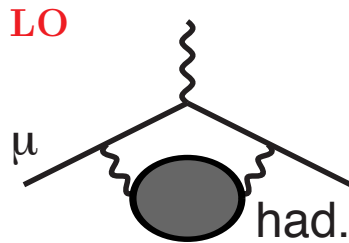
PRD 88 (2013) 053005

$$a_\mu^{\text{EW}(1+2 \text{ loop})} = (153.6 \pm 1.0) \times 10^{-11} \quad \checkmark$$

compared with  $a_\mu^{\text{QED}} = 116\,584\,718.951(80) \times 10^{-11}$

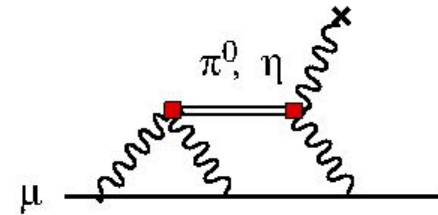
- Hadronic: **non-perturbative**, the limiting factor of the SM prediction  $\times \Rightarrow \checkmark$

$$a_\mu^{\text{had}} = a_\mu^{\text{had,VP LO}} + a_\mu^{\text{had,VP NLO}} + a_\mu^{\text{had,Light-by-Light}}$$



# $a_{\mu}^{\text{had, L-by-L}}$ : Light-by-Light

- **L-by-L**:  $\gamma \rightarrow \text{hadrons} \rightarrow \gamma^* \gamma^* \gamma^*$  non-perturbative, impossible to fully measure ✗
- so far use of **model calculations**, based on large  $N_c$  limit, Chiral Perturbation Theory, plus **short distance constraints** from OPE and pQCD
- **meson exchanges** and **loops** modified by form factor suppression, but with limited experimental information:
  - in principle off-shell form-factors ( $\pi^0, \eta, \eta', 2\pi \rightarrow \gamma^* \gamma^*$ ) needed
  - at most possible, directly experimentally:  $\pi^0, \eta, \eta', 2\pi \rightarrow \gamma \gamma^*$
  - additional quark loop, pQCD matching; theory not fully satisfying conceptually ☹️
  - several independent evaluations, different in details, but **good agreement for the leading  $N_c$  ( $\pi^0$  exchange) contribution**, differences in sub-leading bits
  - mostly used recently:
    - 'Glasgow consensus' by Prades+deRafael+Vainshtein:
 
$$a_{\mu}^{\text{had,L-by-L}} = (105 \pm 26) \times 10^{-11}$$
    - compatible with Nyffeler's  $a_{\mu}^{\text{had,L-by-L}} = (116 \pm 39) \times 10^{-11}$



## HLbL scattering: Summary of selected results for $a_\mu^{\text{HLbL}} \times 10^{11}$

Contribution	BPP	HKS, HK	KN	MV	BP, MdRR	PdRV	N, JN
$\pi^0, \eta, \eta'$	$85 \pm 13$	$82.7 \pm 6.4$	$83 \pm 12$	$114 \pm 10$	—	$114 \pm 13$	$99 \pm 16$
axial vectors	$2.5 \pm 1.0$	$1.7 \pm 1.7$	—	$22 \pm 5$	—	$15 \pm 10$	$22 \pm 5$
scalars	$-6.8 \pm 2.0$	—	—	—	—	$-7 \pm 7$	$-7 \pm 2$
$\pi, K$ loops	$-19 \pm 13$	$-4.5 \pm 8.1$	—	—	—	$-19 \pm 19$	$-19 \pm 13$
$\pi, K$ loops +subl. $N_C$	—	—	—	$0 \pm 10$	—	—	—
quark loops	$21 \pm 3$	$9.7 \pm 11.1$	—	—	—	2.3 (c-quark)	$21 \pm 3$
Total	$83 \pm 32$	$89.6 \pm 15.4$	$80 \pm 40$	$136 \pm 25$	$110 \pm 40$	$105 \pm 26$	$116 \pm 39$

BPP = Bijnsens, Pallante, Prades '95, '96, '02; HKS = Hayakawa, Kinoshita, Sanda '95, '96; HK = Hayakawa, Kinoshita '98, '02; KN = Knecht, AN '02; MV = Melnikov, Vainshtein '04; BP = Bijnsens, Prades '07; MdRR = Miller, de Rafael, Roberts '07; PdRV = Prades, de Rafael, Vainshtein '09; N = AN '09, JN = Jegerlehner, AN '09

- **Pseudoscalar-exchanges dominate numerically.** Other contributions not negligible. **Cancellation** between  $\pi, K$ -loops and quark loops !
  - Note that recent reevaluations of axial vector contribution lead to much smaller estimates than in MV:  $a_\mu^{\text{HLbL}; \text{axial}} = (8 \pm 3) \times 10^{-11}$  (Pauk, Vanderhaeghen '14; Jegerlehner '14, '15). This would shift central values of compilations downwards:  $a_\mu^{\text{HLbL}} = (98 \pm 26) \times 10^{-11}$  (PdRV) and  $a_\mu^{\text{HLbL}} = (102 \pm 39) \times 10^{-11}$  (N, JN).
- 
- **PdRV:** Analyzed results obtained by different groups with various models and suggested new estimates for some contributions (shifted central values, enlarged errors). **Do not consider dressed light quark loops as separate contribution.** Added all errors in quadrature !
  - **N, JN:** **New evaluation of pseudoscalar exchange contribution imposing new short-distance constraint on off-shell form factors.** Took over most values from BPP, except axial vectors from MV. **Added all errors linearly.**

# $a_\mu^{\text{had, L-by-L}}$ : Light-by-Light Prospects

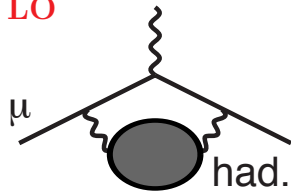
- Transition FFs can be measured by **KLOE-2** and **BESIII** using small angle taggers:  
 $e^+e^- \rightarrow e^+e^-\gamma\gamma^* \rightarrow \pi^0, \eta, \eta', 2\pi$  expected to constrain leading pole contributions from  $\pi, \eta, \eta'$  to  $\sim 15\%$  Nyffeler, arXiv:1602.03398
- or calculate on the lattice:  $\pi^0 \rightarrow \gamma^* \gamma^*$  Gerardin, Meyer, Nyffeler, arXiv:1607.08174
- Breakthrough with **new dispersive approaches**  
Pauk, Vanderhaeghen, PRD 90 (2014) 113012  
Colangelo, Hoferichter, Procura, Stoffer, JHEP 1704 (2017) 161
  - dispersion relations formulated for the general HLbL tensor or for  $a_\mu$  directly
  - allowing to constrain/calculate the HLbL contributions from data
  - e.g. Colangelo et al. have first results for the  $\pi$ -box contribution from data for  $F_V^\pi(q^2)$
- Ultimately: 'First principles' full prediction from **lattice QCD+QED**
  - several groups: **USQCD, UKQCD, ETMC, ...** much increased effort and resources
  - within  $\sim 3$  years a 10% estimate may be possible, 30% would already be useful
  - first results encouraging, **proof of principle already exists**
- We are already able to defend/confirm the error estimate of the Glasgow consensus, and probably bring it down significantly ✓

# $a_\mu^{\text{hadronic}}$ : L-by-L one-page summary

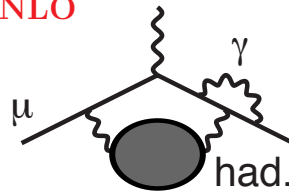
- Hadronic: **non-perturbative**, the limiting factor of the SM prediction **X**  $\Rightarrow$   $\checkmark$

$$a_\mu^{\text{had}} = a_\mu^{\text{had,VP LO}} + a_\mu^{\text{had,VP NLO}} + a_\mu^{\text{had,Light-by-Light}}$$

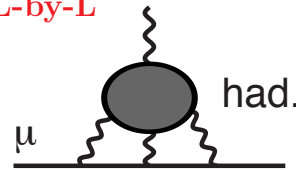
LO



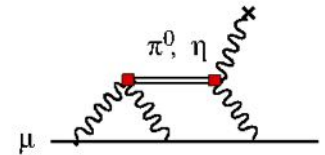
NLO



L-by-L



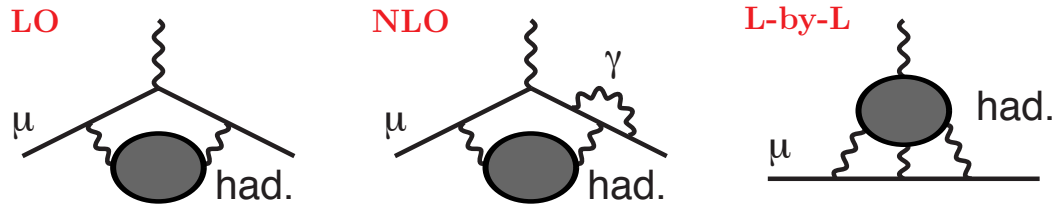
e.g.



- L-by-L**: - so far use of **model calculations** (+ form-factor data and pQCD constraints),  
- also good news from **lattice QCD**, and  
- new **dispersive** approaches
- Below I will use the '**updated Glasgow consensus**':  
(original by Prades+deRafael+Vainshtein)  $a_\mu^{\text{had,L-by-L}} = (98 \pm 26) \times 10^{-11}$
- so far no indication for a big surprise
- expect that L-by-L prediction can be improved further
- with new results & progress, tell politicians/sceptics: L-by-L \_can\_ be predicted!**

# $a_\mu^{\text{had, VP}}$ : Hadronic Vacuum Polarisation

$$a_\mu^{\text{had}} = a_\mu^{\text{had, VP LO}} + a_\mu^{\text{had, VP NLO}} + a_\mu^{\text{had, Light-by-Light}}$$

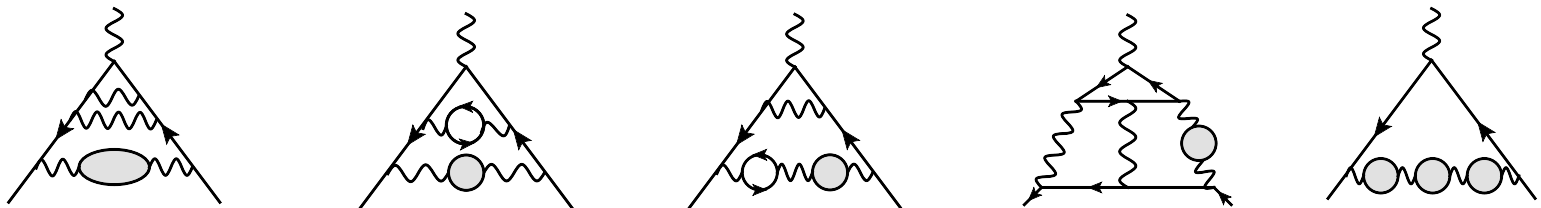


**HVP**: - most precise prediction by using  $e^+e^-$  hadronic cross section (+ tau) data and well known dispersion integrals

- done at LO and NLO (see graphs)

- and recently at NNLO [Steinhauser et al., PLB 734 (2014) 144, also F. Jegerlehner]

$a_\mu^{\text{HVP, NNLO}} = + 1.24 \times 10^{-10}$  not so small, from e.g.:

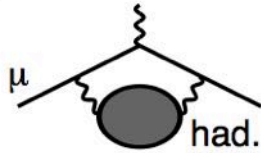


- Alternative: lattice QCD, but need QED and iso-spin breaking corrections  
Lots of activity by several groups, errors coming down, QCD+QED started



# Hadronic Vacuum Polarisation, essentials:

Use of data compilation for HVP:



pQCD not useful. Use the **dispersion relation** and the **optical theorem**.

$$\text{had.} = \int \frac{ds}{\pi(s-q^2)} \text{Im had.}$$

$$2 \text{Im had.} = \sum_{\text{had.}} \int d\Phi \left| \text{had.} \right|^2$$

$$a_{\mu}^{\text{had,LO}} = \frac{m_{\mu}^2}{12\pi^3} \int_{s_{\text{th}}}^{\infty} ds \frac{1}{s} \hat{K}(s) \sigma_{\text{had}}(s)$$

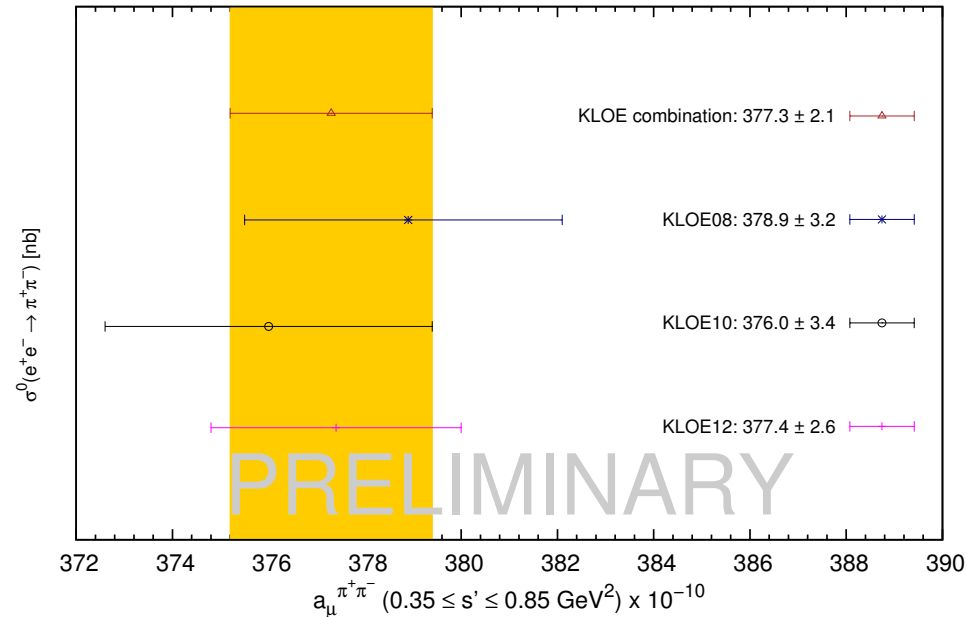
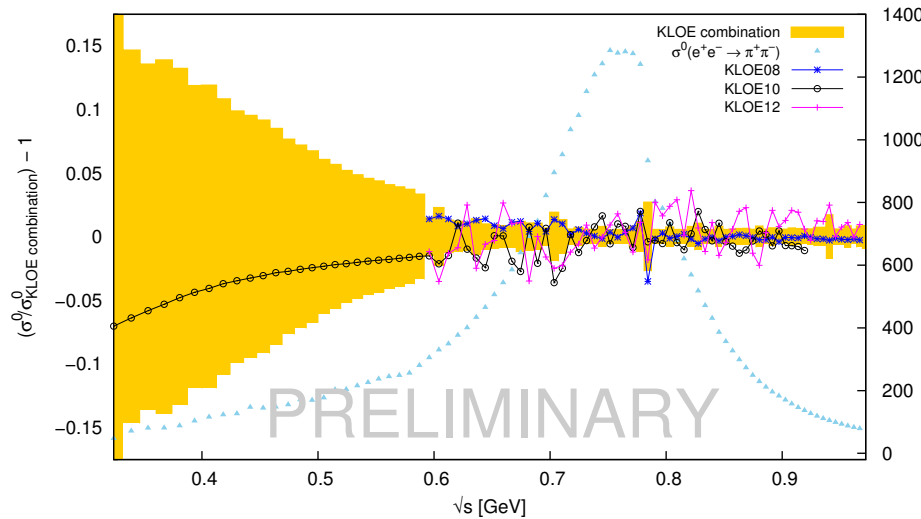
- Weight function  $\hat{K}(s)/s = \mathcal{O}(1)/s$   
 $\Rightarrow$  **Lower** energies **more important**  
 $\Rightarrow \pi^+\pi^-$  channel: 73% of total  $a_{\mu}^{\text{had,LO}}$

How to get the most precise  $\sigma_{\text{had}}^0$ ?  **$e^+e^-$  data**:

- Low energies: **sum  $\sim 30$  exclusive channels**,  $2\pi, 3\pi, 4\pi, 5\pi, 6\pi, KK, KK\pi, KK\pi\pi, \eta\pi, \dots$ , use iso-spin relations for missing channels
- Above  $\sim 1.8$  GeV: can start to use **pQCD** (away from flavour thresholds), supplemented by narrow resonances ( $J/\psi, \Upsilon$ )
- Challenge of **data combination (locally in  $\sqrt{s}$ )**: many experiments, different energy bins, stat+sys errors from different sources, **correlations**; must avoid **inconsistencies/bias**
- traditional '**direct scan**' (tunable  $e^+e^-$  beams) vs. '**Radiative Return**' [+  $\tau$  spectral functions]
- $\sigma_{\text{had}}^0$  means 'bare'  $\sigma$ , but WITH FSR: **RadCorrs** [HLMNT '11:  $\delta a_{\mu}^{\text{had, RadCor VP+FSR}} = 2 \times 10^{-10}$  !]

# HVP: KLOE 2 $\pi$ combination [on arXiv in next days]

⇒ Combination of KLOE08, KLOE10 and KLOE12 gives 85 distinct bins between  $0.1 \leq s \leq 0.95 \text{ GeV}^2$



→ Covariance matrix now correctly constructed

⇒ a **positive semi-definite matrix**

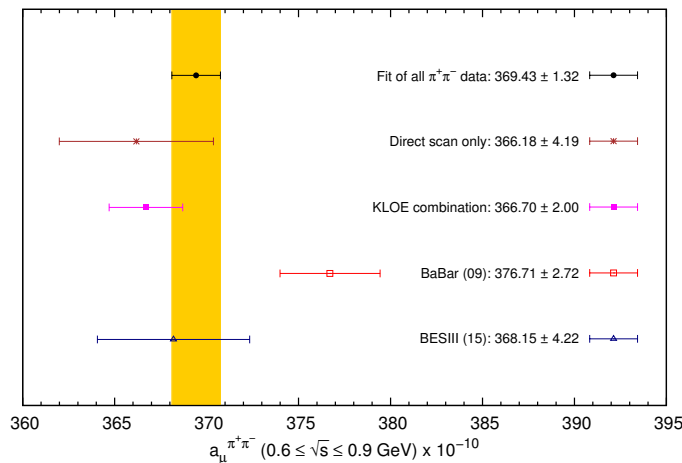
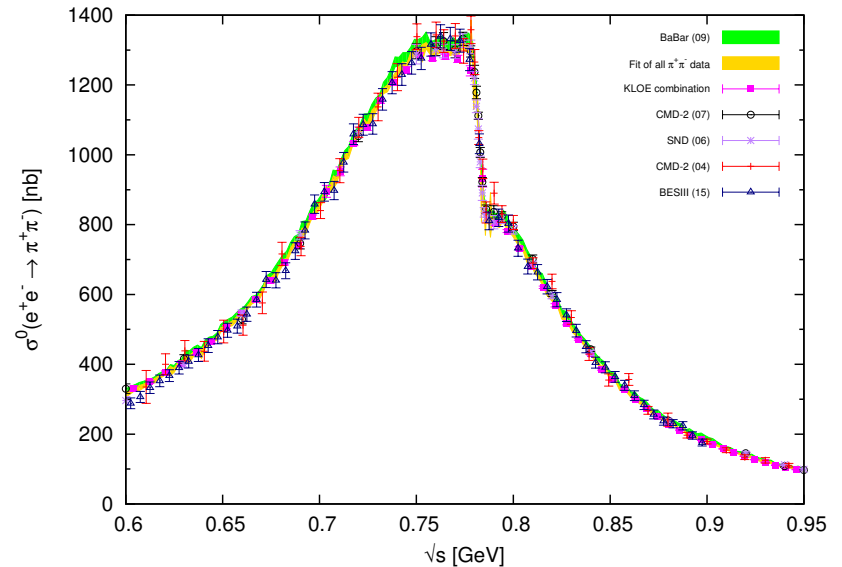
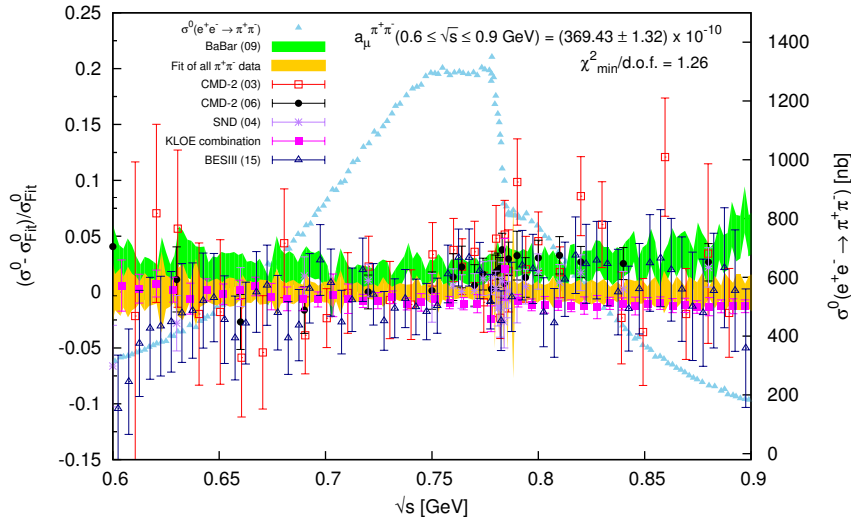
→ **Non-trivial influence of correlated uncertainties** on resulting mean value

$$a_{\mu}^{\pi^{+}\pi^{-}}(0.1 \leq s' \leq 0.95 \text{ GeV}^2) = (489.9 \pm 2.0_{\text{stat}} \pm 4.3_{\text{sys}}) \times 10^{-10}$$

# HVP: complete $2\pi$ combination by Keshavarzi+Nomura+T

⇒ Large improvement for  $2\pi$  estimate

→ BESIII [Phys.Lett. B753 (2016) 629-638] and KLOE combination provide **downward influence** to mean value



⇒ **Correlated** & experimentally corrected  $\sigma_{\pi\pi}^0(\gamma)$  data now entirely **dominant**

$a_\mu \pi^+\pi^- (0.305 \leq \sqrt{s} \leq 2.00 \text{ GeV})$ :

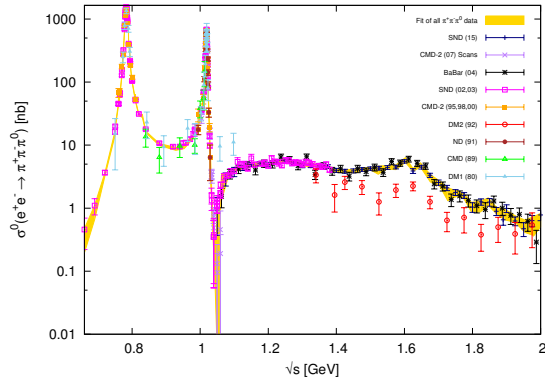
HLMNT11:  $505.77 \pm 3.09$

KNT17:  $502.85 \pm 1.93$  (!!)

(no radiative correction uncertainties)

# HVP: other notable exclusive channels [status June 2017]

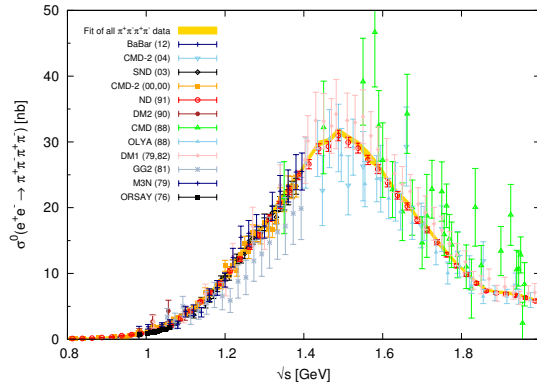
$$\pi^+ \pi^- \pi^0$$



HLMNT11:  $47.51 \pm 0.99$

KNT17:  $47.68 \pm 0.70$

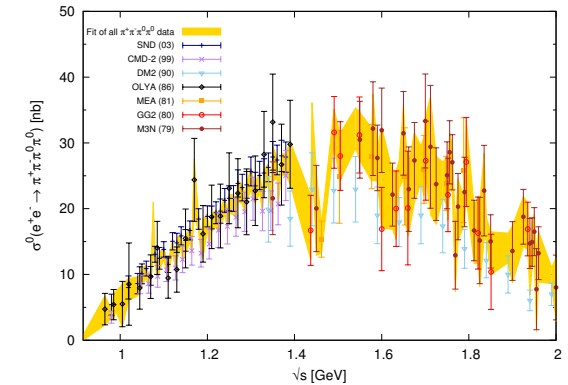
$$\pi^+ \pi^- \pi^+ \pi^-$$



HLMNT11:  $14.65 \pm 0.47$

KNT17:  $15.18 \pm 0.14$

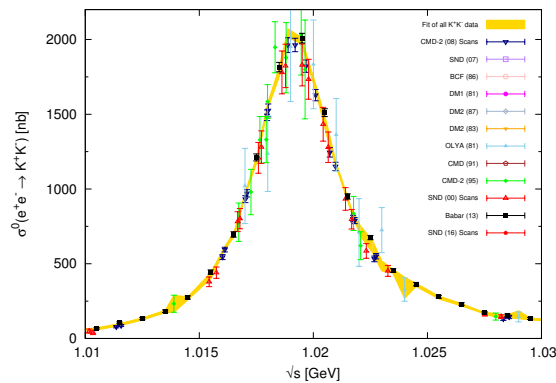
$$\pi^+ \pi^- \pi^0 \pi^0$$



HLMNT11:  $20.37 \pm 1.26$

KNT17:  $20.07 \pm 1.19$

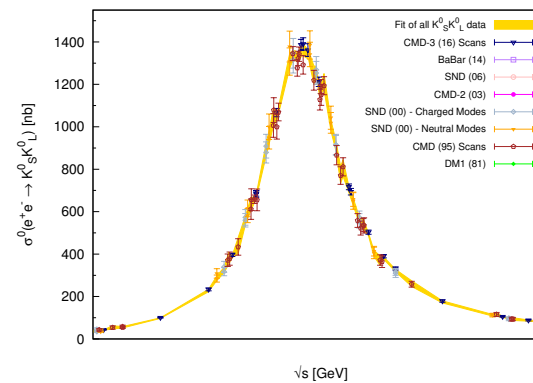
$$K^+ K^-$$



HLMNT11:  $22.15 \pm 0.46$

KNT17:  $22.76 \pm 0.22$

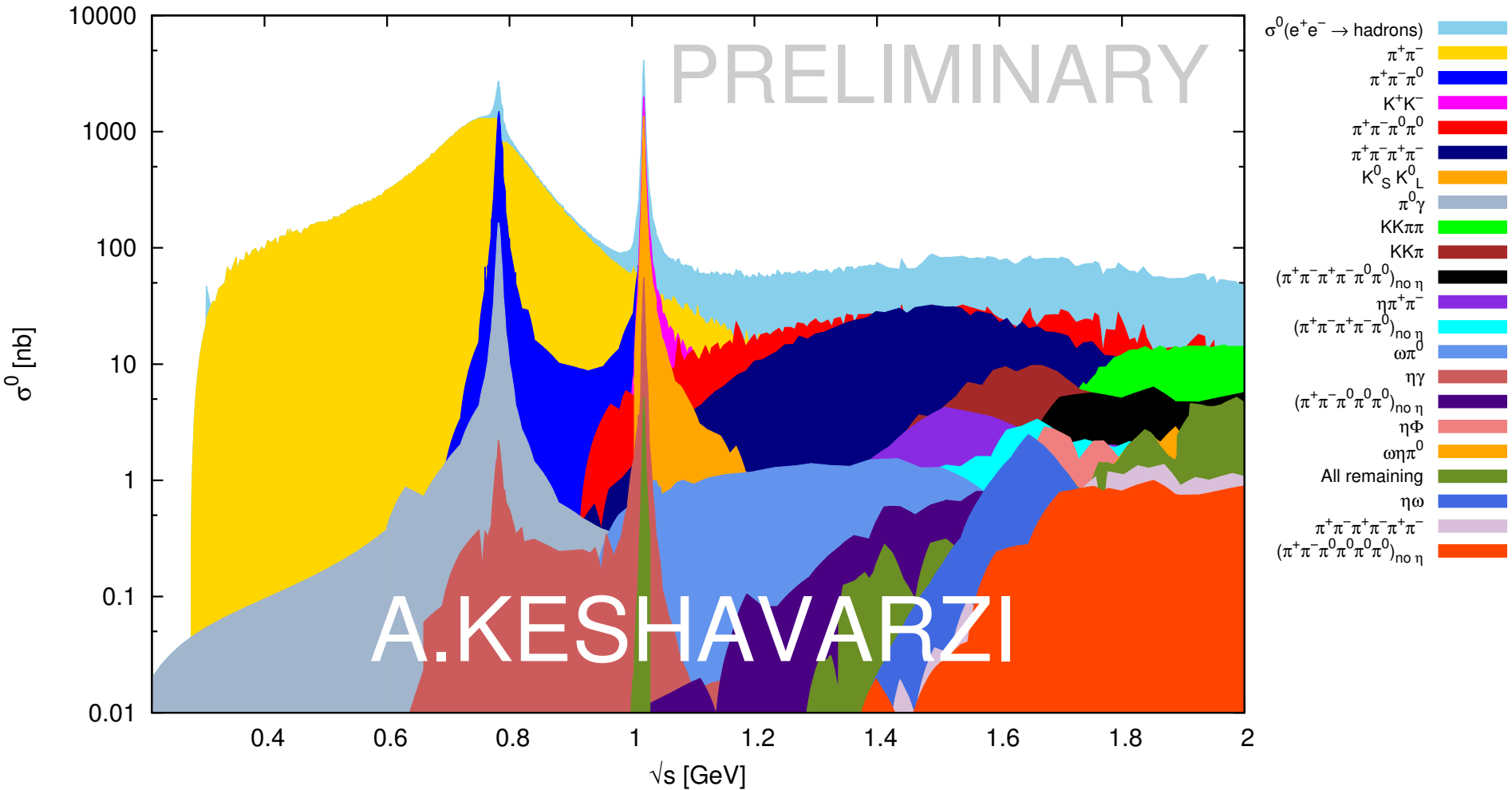
$$K_S^0 K_L^0$$



HLMNT11:  $13.33 \pm 0.16$

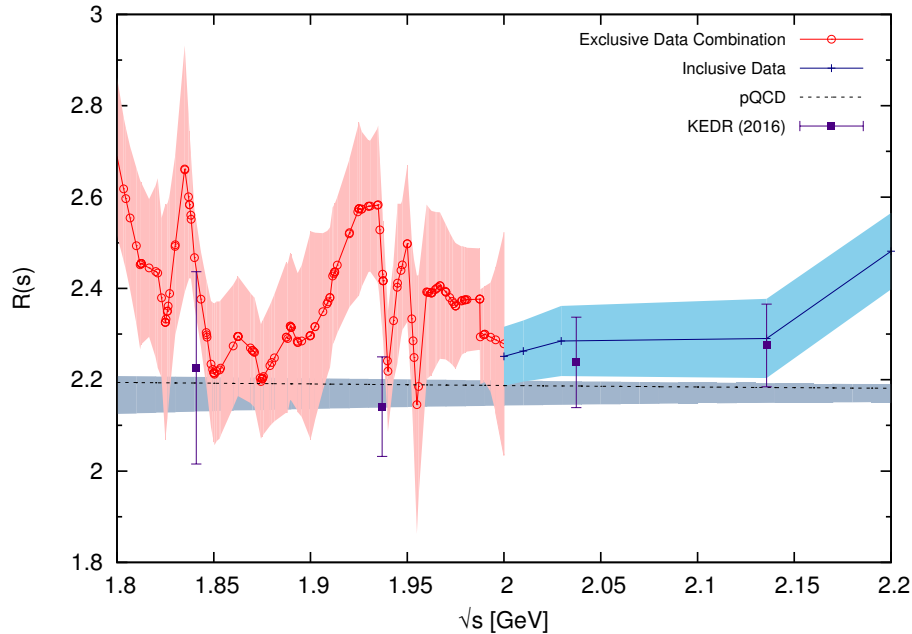
KNT17:  $13.09 \pm 0.12$

# HVP: the channel landscape (by Alex Keshavarzi)



# HVP: region of inclusive data/pQCD

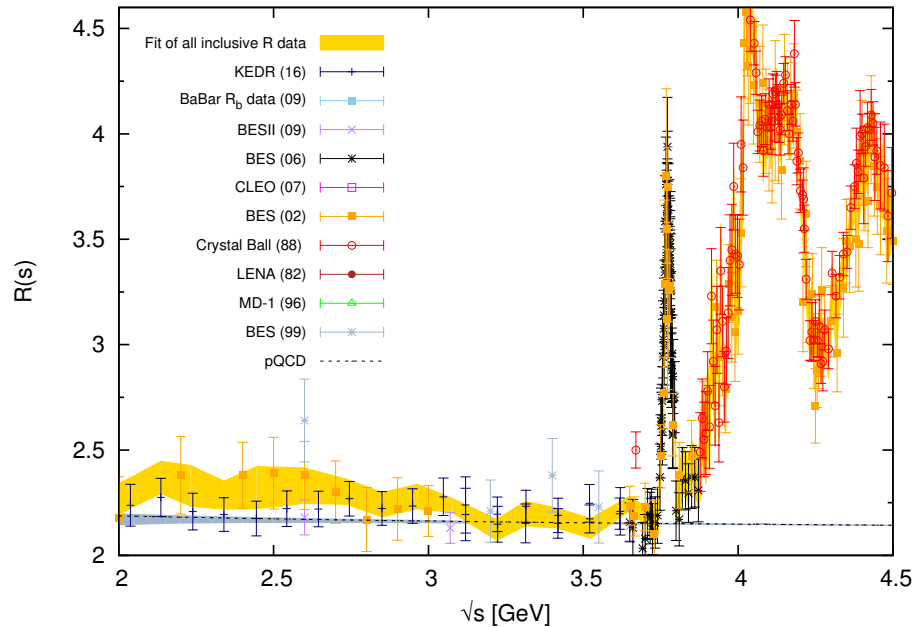
⇒ **New KEDR inclusive  $R$  data** ranging  $1.84 \leq \sqrt{s} \leq 3.05$  GeV [Phys.Lett. B770 (2017) 174-181]  
and  $3.12 \leq \sqrt{s} \leq 3.72$  GeV [Phys.Lett. B753 (2016) 533-541]



$a_{\mu}^{\text{had, LOVP}} (1.84 \leq \sqrt{s} \leq 2.00 \text{ GeV})$ :

pQCD :  $6.42 \pm 0.03$

Data :  $6.88 \pm 0.25$



$a_{\mu}^{\text{had, LOVP}} (2.60 \leq \sqrt{s} \leq 3.73 \text{ GeV})$ :

pQCD (inflated errors) :  $10.82 \pm 0.38$

Data :  $11.20 \pm 0.14$

⇒ **Choose to adopt entirely data driven estimate from threshold to 11.2 GeV**

# $a_\mu^{\text{SM}}$ : update HLMNT11 $\rightarrow$ KNT17 (prel.) as presented @ TGM2

	<u>2011</u>	$\rightarrow$	<u>2017</u>	<b>*to be discussed</b>
QED	11658471.81 (0.02)	$\rightarrow$	11658471.90 (0.01) [Phys. Rev. Lett. 109 (2012) 111808]	
EW	15.40 (0.20)	$\rightarrow$	15.36 (0.10) [Phys. Rev. D 88 (2013) 053005]	
LO HLbL	10.50 (2.60)	$\rightarrow$	9.80 (2.60) [EPJ Web Conf. 118 (2016) 01016]*	
NLO HLbL			0.30 (0.20) [Phys. Lett. B 735 (2014) 90]*	
<hr/>				
	<u>HLMNT11</u>	$\rightarrow$	<u>KNT17</u>	
LO HVP	694.91 (4.27)	$\rightarrow$	692.23 (2.54) this work*	
NLO HVP	-9.84 (0.07)	$\rightarrow$	-9.83 (0.04) this work*	
<hr/>				
NNLO HVP			1.24 (0.01) [Phys. Lett. B 734 (2014) 144] *	
<hr/>				
Theory total	11659182.80 (4.94)	$\rightarrow$	11659181.00 (3.62) this work	
Experiment			11659209.10 (6.33) world avg	
Exp - Theory	26.1 (8.0)	$\rightarrow$	28.1 (7.3) this work	
<hr/>				
$\Delta a_\mu$	3.3 $\sigma$	$\rightarrow$	3.9 $\sigma$ this work	

# $a_\mu^{\text{LO HVP}}$ : comparison of the most recent results

## KNT17 vs. DHMZ17 vs. FJ17 [preliminary]

⇒ Different data treatment/methods produce **very different results**

Channel $\sqrt{s} \leq 1.8$ GeV	KNT17	DHMZ17	FJ17
$\pi^+ \pi^-$	$502.73 \pm 1.94$	$507.14 \pm 2.58$	
$\pi^+ \pi^- 2\pi^0$	$17.82 \pm 0.99$	$18.03 \pm 0.54$	
$2\pi^+ 2\pi^-$	$14.00 \pm 0.20$	$13.68 \pm 0.31$	
$K^+ K^-$	$22.75 \pm 0.26$	$22.81 \pm 0.41$	
$K_S^0 K_L^0$	$13.03 \pm 0.20$	$12.82 \pm 0.24$	
Total HVP $\sqrt{s} < \infty$ GeV	$692.23 \pm 2.54$	$693.1 \pm 3.4$	$689.43 \pm 3.25$

⇒ Between  $1.8 \leq \sqrt{s} \leq 2$  GeV, KNT use **data**, DHMZ use **pQCD**

BUT, **pQCD** =  $8.30 \pm 0.09$ , **KNT data** =  $8.42 \pm 0.29$ , **DHMZ data** =  $7.71 \pm 0.32$

⇒ DHMZ17 use correlated systematics differently in determination of the mean value

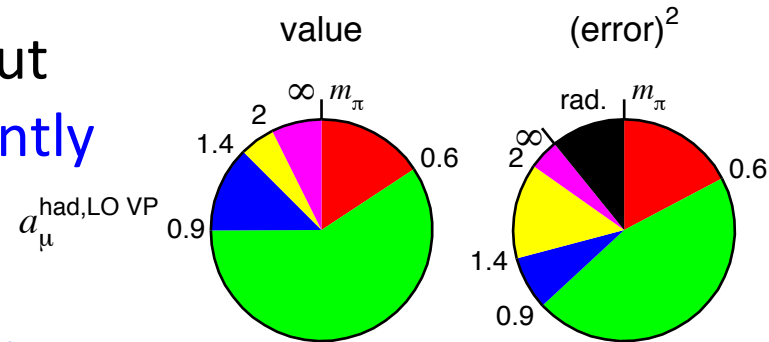
→ Determining  $\pi^+ \pi^-$  **using only local weighted average** gives  $508.91 \pm 2.84$

→ **Much better agreement** when neglecting the effect of correlated uncertainties on the mean value



# SM prediction: Summary

- All sectors of the **Standard Model prediction of  $g-2$**  have been **scrutinised** a lot in recent years
- The basic picture has not changed, but **recent data**, many from ISR, **significantly improve the prediction for  $a_\mu^{\text{HVP}}$**
- **Discrepancy  $\sim 3 \rightarrow 4 \sigma$  is consolidated**
- With **further hadronic data** in the pipeline, also on FFs for HLbL, and **efforts from lattice**, the goal of **squeezing  $\Delta a_\mu^{\text{SM}}$  by a factor of two is in reach**
- Push for the community to compare and challenge results:



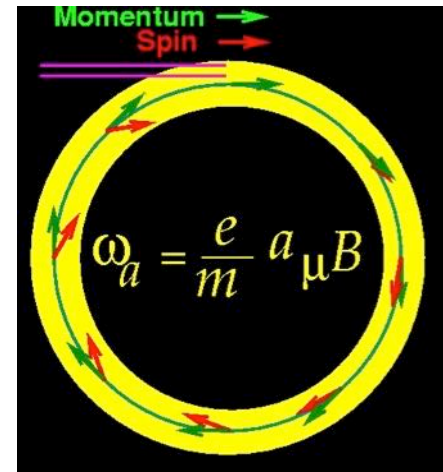
# “Muon g-2 theory initiative” formed in June 2017



“map out strategies for obtaining the **best theoretical predictions for these hadronic corrections** in advance of the experimental results”

# g-2 experiments slides thanks to Tsutomu Mibe and Lee Roberts

In uniform magnetic field, muon spin rotates ahead of momentum due to  $g-2 \neq 0$



general form of spin precession vector:

$$\vec{\omega} = -\frac{e}{m} \left[ a_\mu \vec{B} - \left( a_\mu - \frac{1}{\gamma^2 - 1} \right) \frac{\vec{\beta} \times \vec{E}}{c} + \frac{\eta}{2} \left( \vec{\beta} \times \vec{B} + \frac{\vec{E}}{c} \right) \right]$$

BNL E821 approach  
 $\gamma=30$  ( $P=3$  GeV/c)

$$\vec{\omega} = -\frac{e}{m} \left[ a_\mu \vec{B} + \frac{\eta}{2} \left( \vec{\beta} \times \vec{B} + \frac{\vec{E}}{c} \right) \right]$$

FNAL E989

J-PARC approach  
 $E = 0$  at any  $\gamma$

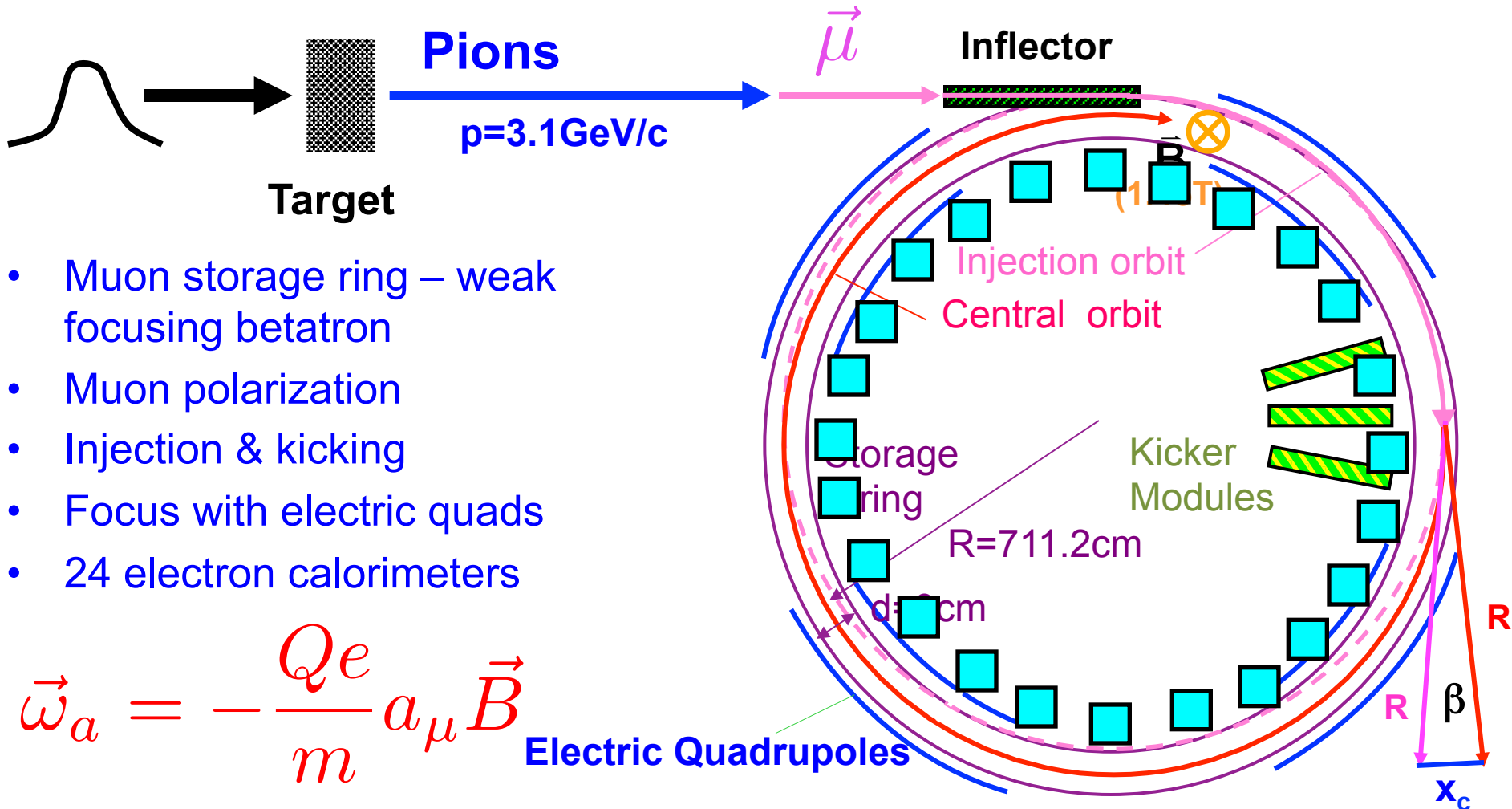
$$\vec{\omega} = -\frac{e}{m} \left[ a_\mu \vec{B} + \frac{\eta}{2} \left( \vec{\beta} \times \vec{B} \right) \right]$$

J-PARC E34

# BNL&FNAL: Experimental Technique

narrow time  
bunch of protons

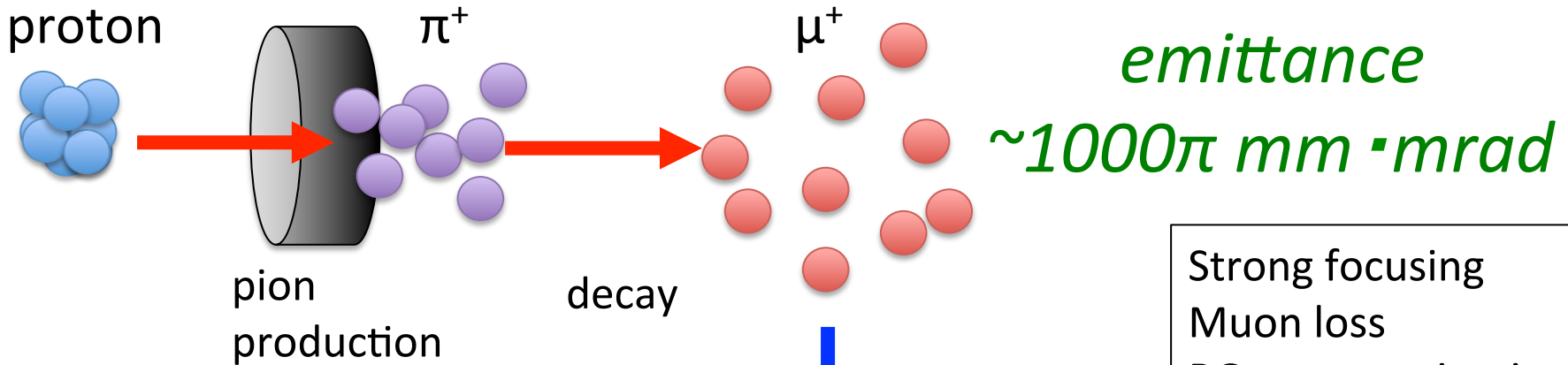
$x_c \approx 77$  mm  
 $\beta \approx 10$  mrad  
 $B \cdot dl \approx 0.1$  Tm



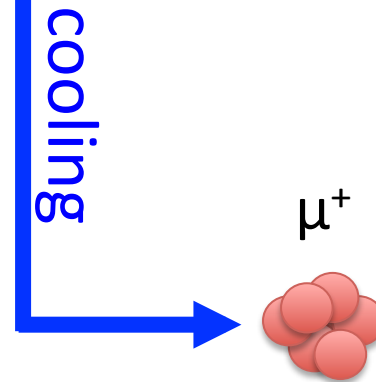
- Muon storage ring – weak focusing betatron
- Muon polarization
- Injection & kicking
- Focus with electric quads
- 24 electron calorimeters

# Muon beam

## Conventional muon beam



Strong focusing  
Muon loss  
BG  $\pi$  contamination



## Ultra-cold muon beam

*emittance*  
 $1\pi \text{ mm} \cdot \text{mrad}$

Free from any of these

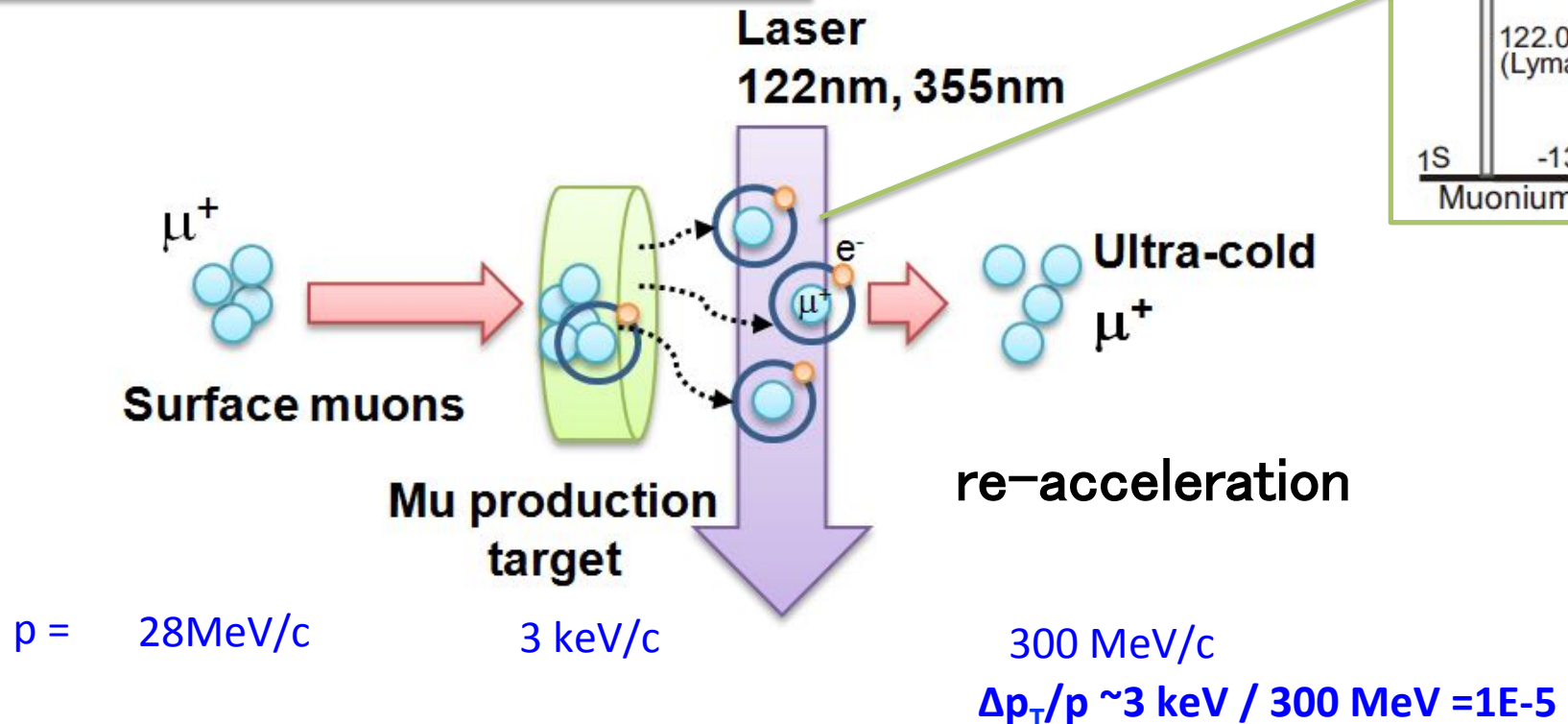
# Ultra-cold Muon

Requirement for zero E-field:

Muons should be kept stored without E-focusing

→ Beam with ultra-small transverse dispersion,  
i.e.  $\Delta p_T/p \sim 0$

Laser resonant ionization of Mu ( $\mu^+e^-$ )



# Muon g-2/EDM Experiment at J-PARC with Ultra-Cold Muon Beam

3 GeV proton beam  
(333  $\mu$ A)

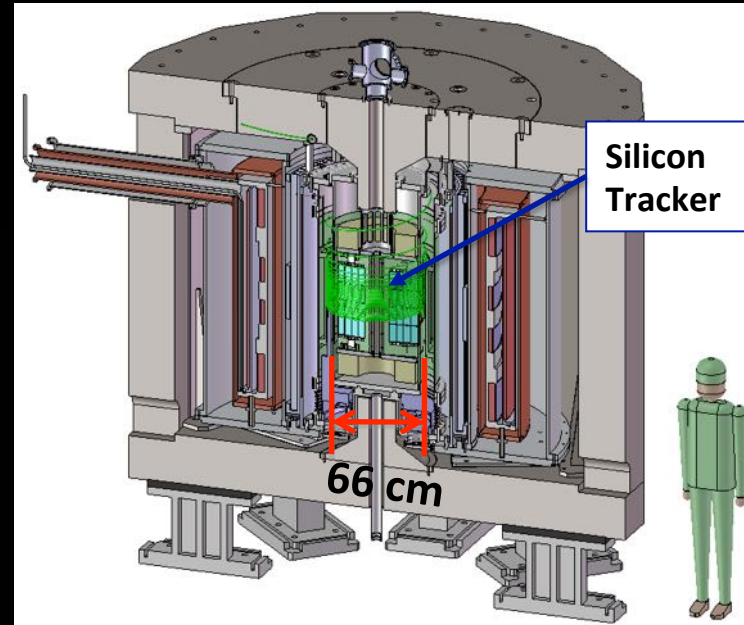
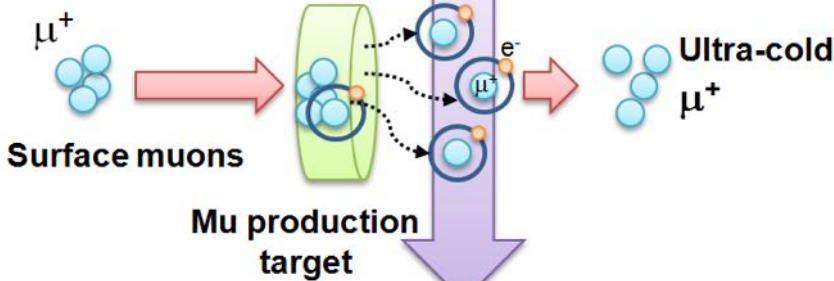
Production target  
(20 mm)

Surface muon beam  
(28 MeV/c)

Muonium Production  
(300 K  $\sim$  25 meV  $\Rightarrow$  2.3 keV/c)

Resonant Laser Ionization of Muonium

Laser  
122nm, 355nm

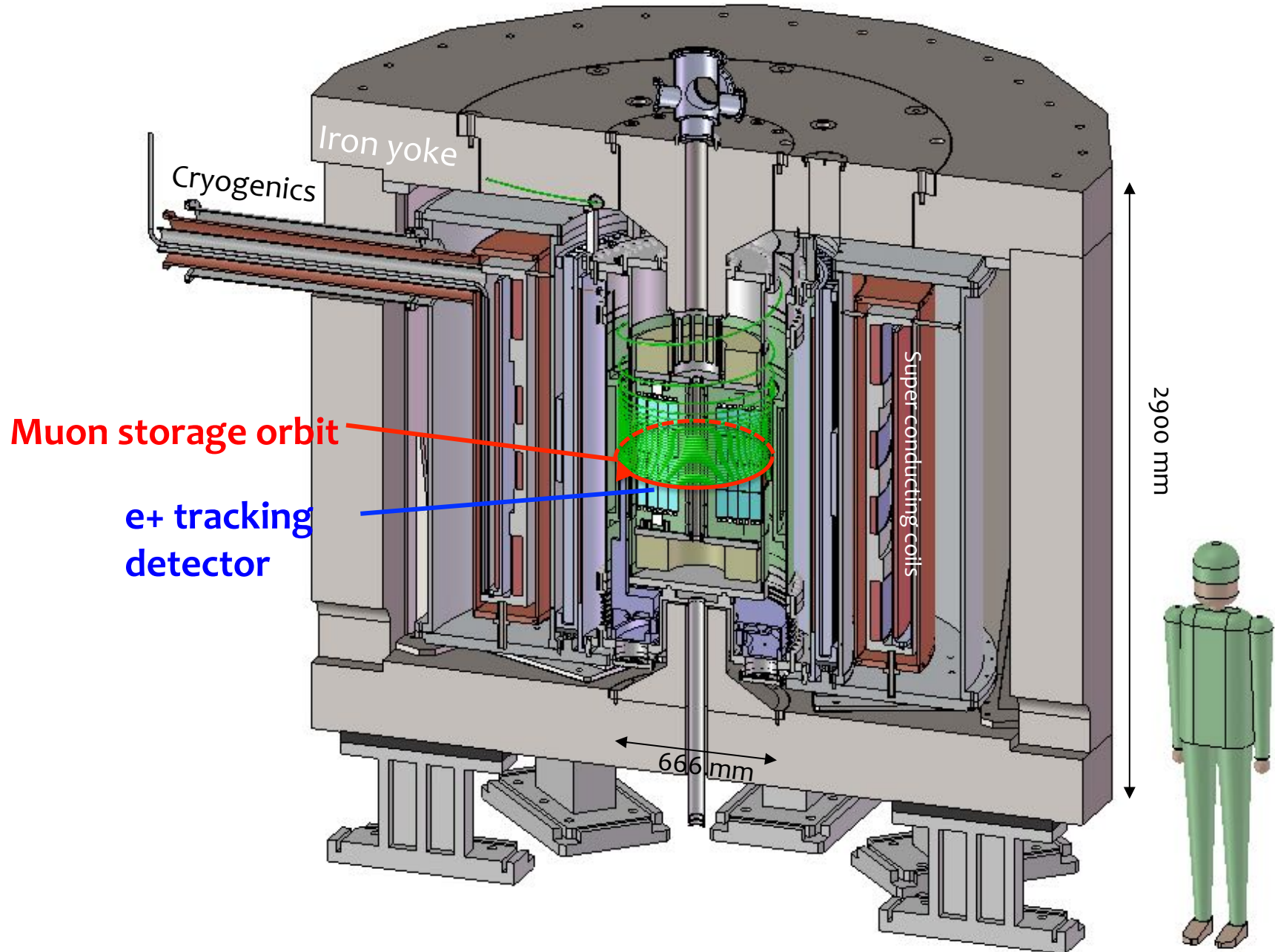


Super Precision Storage Magnet  
(3T,  $\sim$ 1ppm local precision)

Muon LINAC (300 MeV/c)

Muon storage

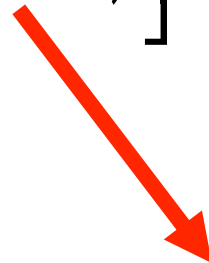
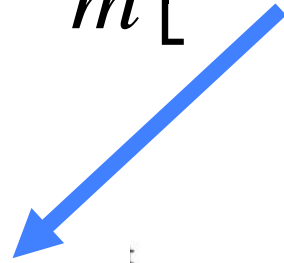
# Muon storage magnet and detector



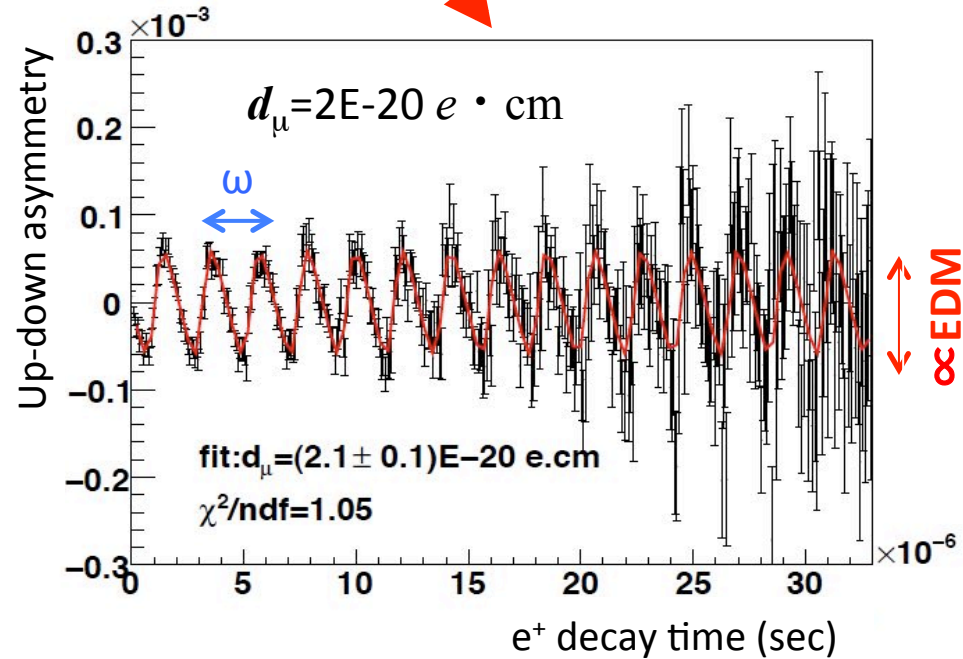
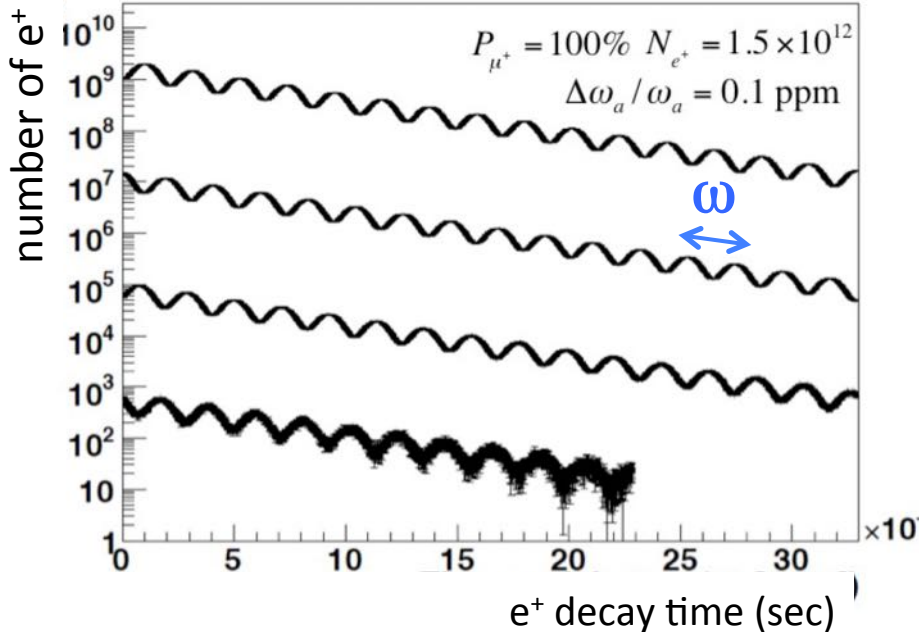


# Expected time spectrum of $e^+$ in $\mu \rightarrow e^+ \nu \nu$ decay

$$\vec{\omega} = -\frac{e}{m} \left[ a_\mu \vec{B} + \frac{\eta}{2} (\vec{\beta} \times \vec{B}) \right]$$



$p > 200 \text{ MeV}/c$



**J-PARC Facility  
(KEK/JAEA)**

**LINAC**

**3 GeV  
Synchrotron**

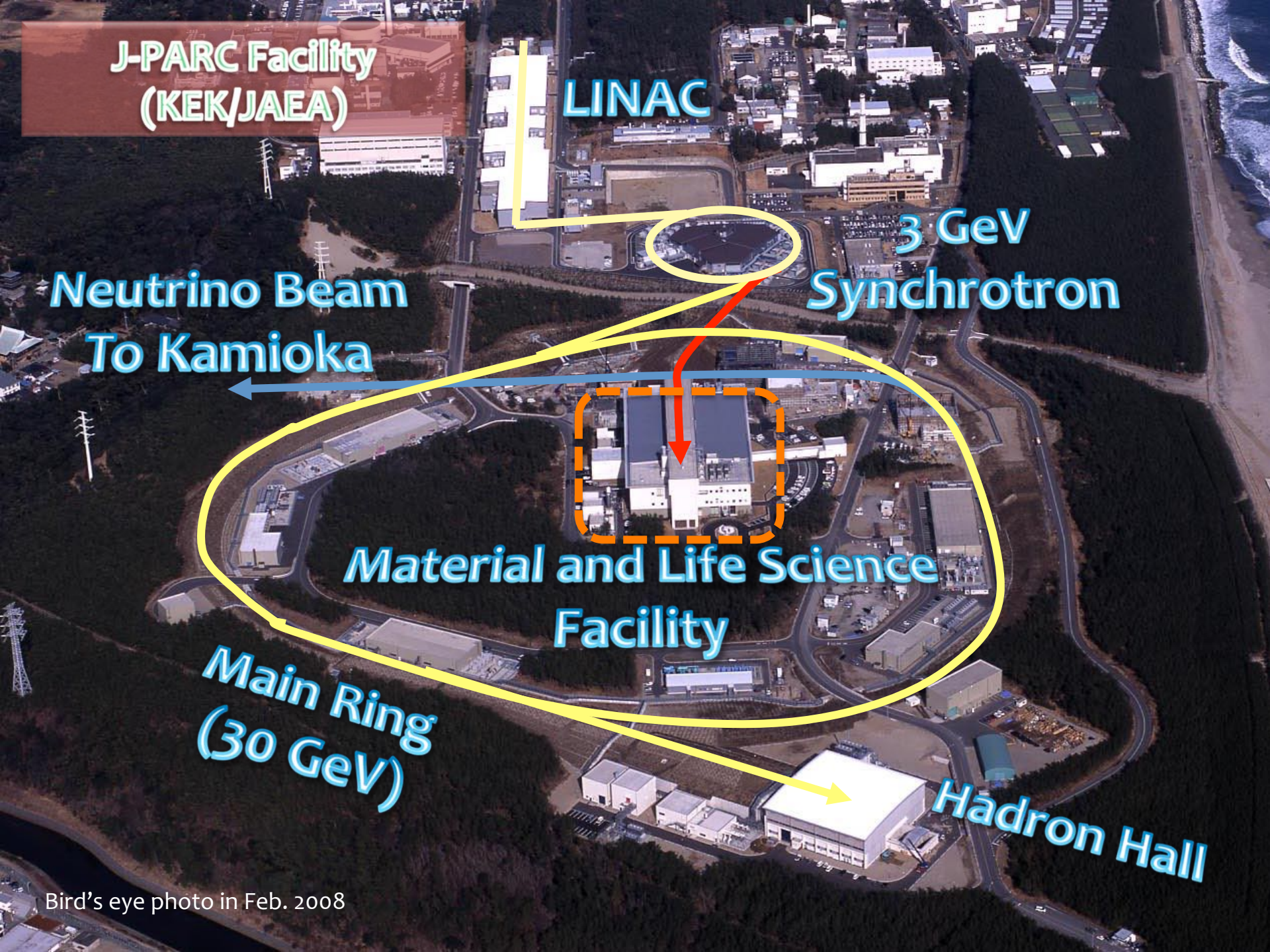
**Neutrino Beam  
To Kamioka**

**Material and Life Science  
Facility**

**Main Ring  
(30 GeV)**

**Hadron Hall**

Bird's eye photo in Feb. 2008



2016.8.17



# Summary J-PARC

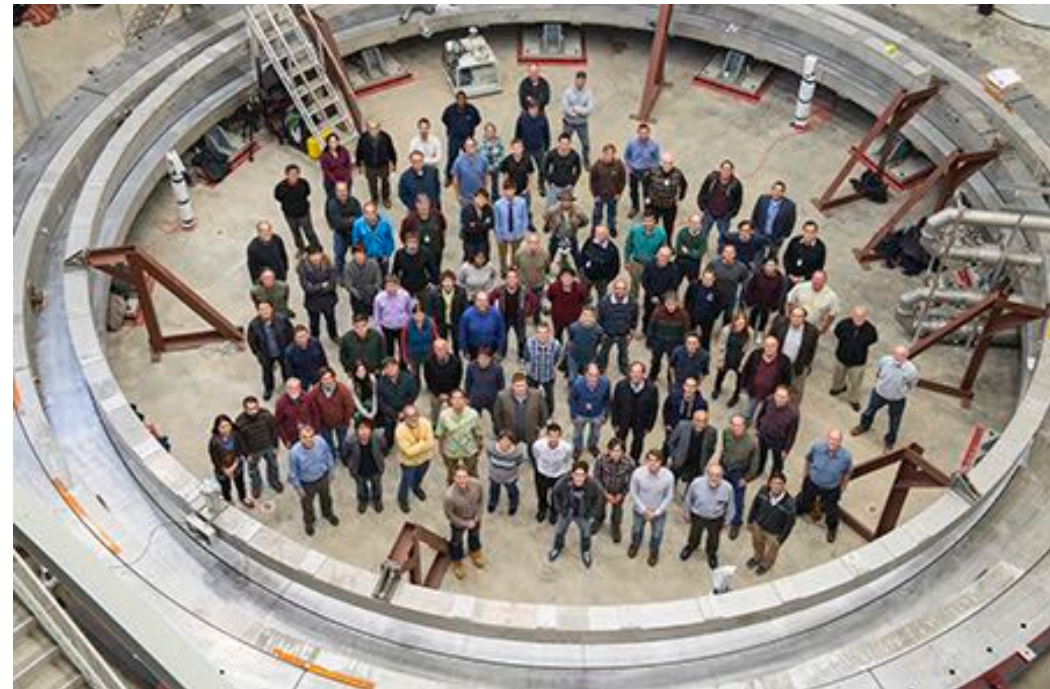
- **New g-2/EDM experiment at J-PARC**
  - Ultra-cold muon beam
  - Compact storage ring
- **R&D phase is ending.**
  - The TDR was reviewed by the focused review committee in Nov, 2016.
- **Construction phase is starting.**
  - Surface muon beamline under construction.
  - ~3-3.5 years to start data taking when full funding is provided.

# Comparison of experiments

	BNL E821	J-PARC E34
muon momentum	3.09 GeV/c	0.3 GeV/c
storage ring radius	7 m	0.33 m
storage field	1.5 T	3.0 T
focusing field (n-index)	0.14 (electric)	1.5 E-4 (magnetic)
average field uniformity	≈1 ppm	<< 1ppm
(local uniformity)	≈50 ppm	≈1ppm
Injection	inflector + kick	spiral + kick
Injection efficiency	3-5%	80%
muon spin reversal	--	pulse-to-pulse
positron measurement	calorimeters	tracking
positron acceptance*	65%	≈100%
muon polarization	≈100%	≈50%
events to 0.46 ppm	$9 \times 10^9$	$5 \times 10^{11}$

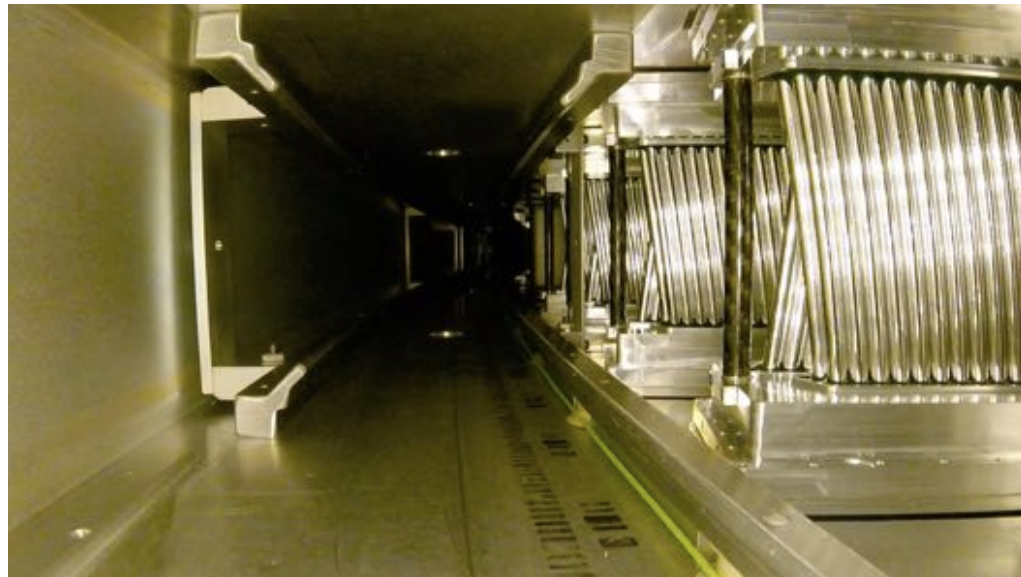
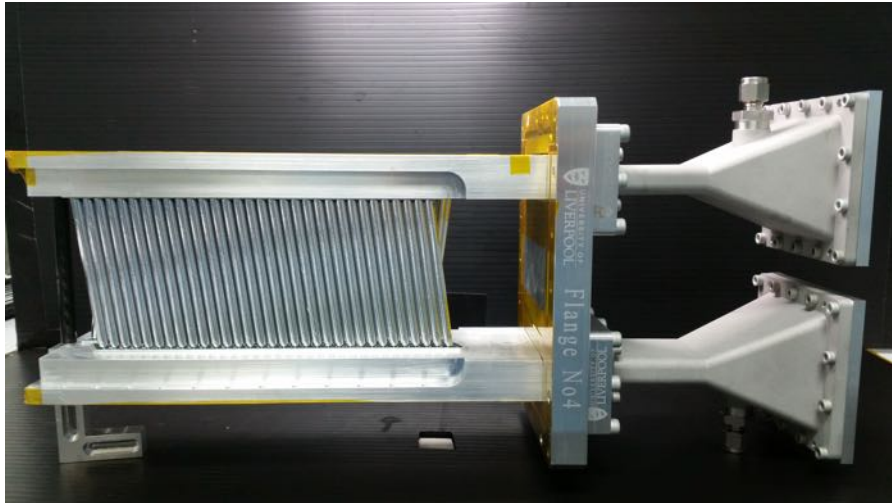
\* in the energy region of interest

# E989: Ring arrived after a long journey in one piece



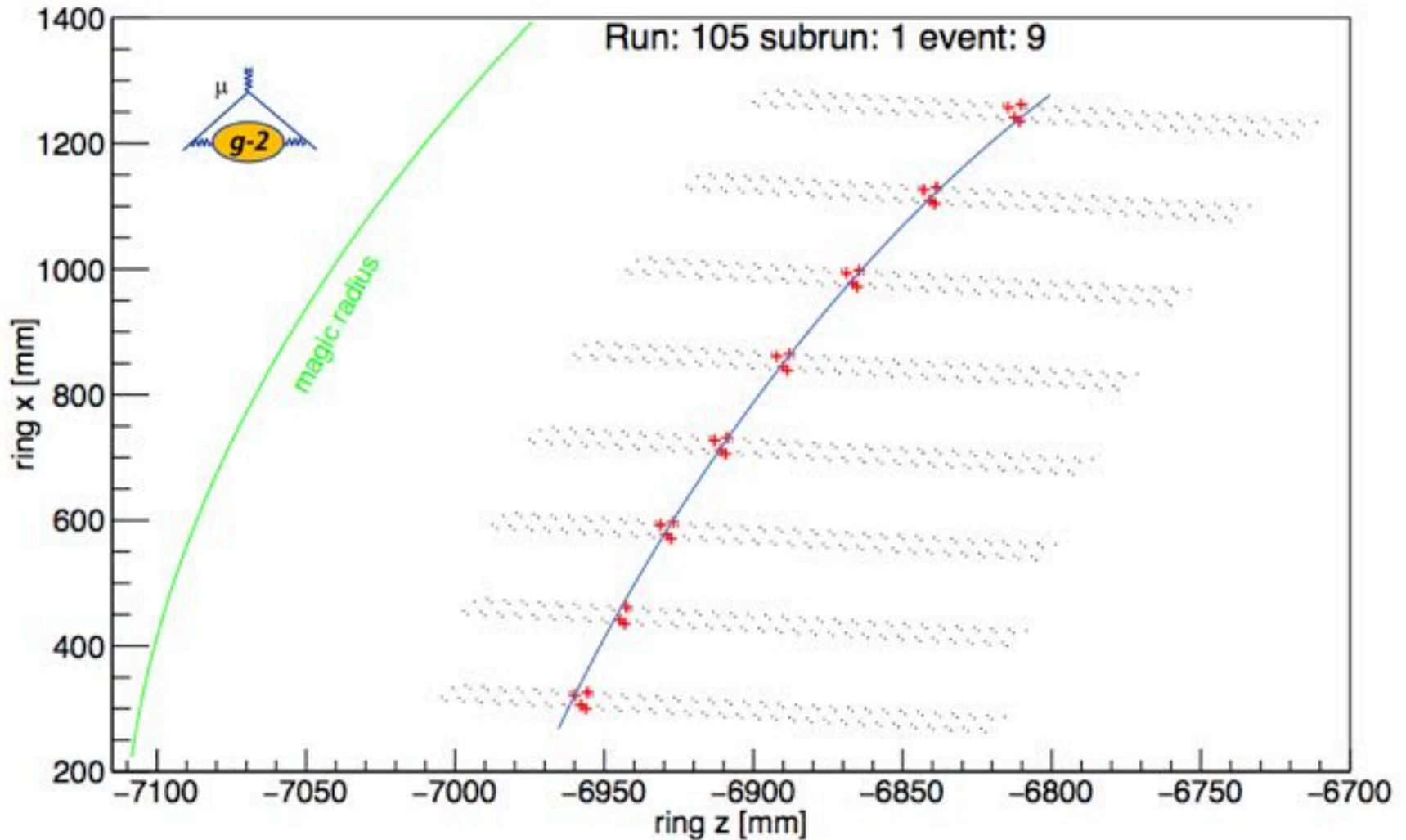
and the collaboration has been growing further since then (2014 ->)

# E989 Liverpool: design and building of trackers



- 3 stations in ring, each 8 modules with straw trackers
- tool for monitoring beam dynamics
- very important for systematics and EDM measurement
- ← photo taken in ring from trolley for NMR probes for B-mapping

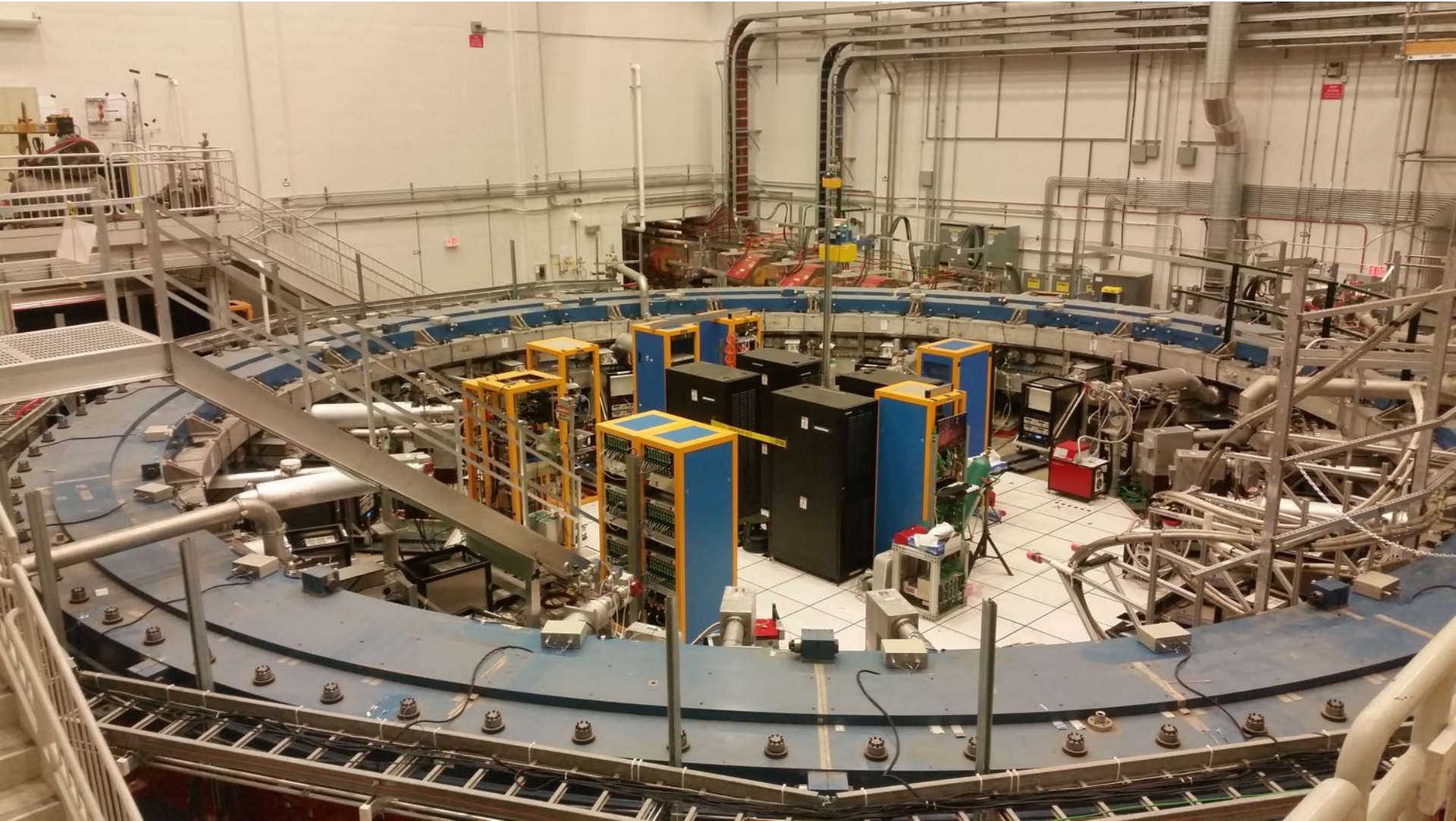
# E989 Liverpool: design and building of trackers



One of the first tracks recorded by the tracker showing the hits from a single charged particle (likely a proton) through the straw trackers and the (wire)-track fit and the magic radius

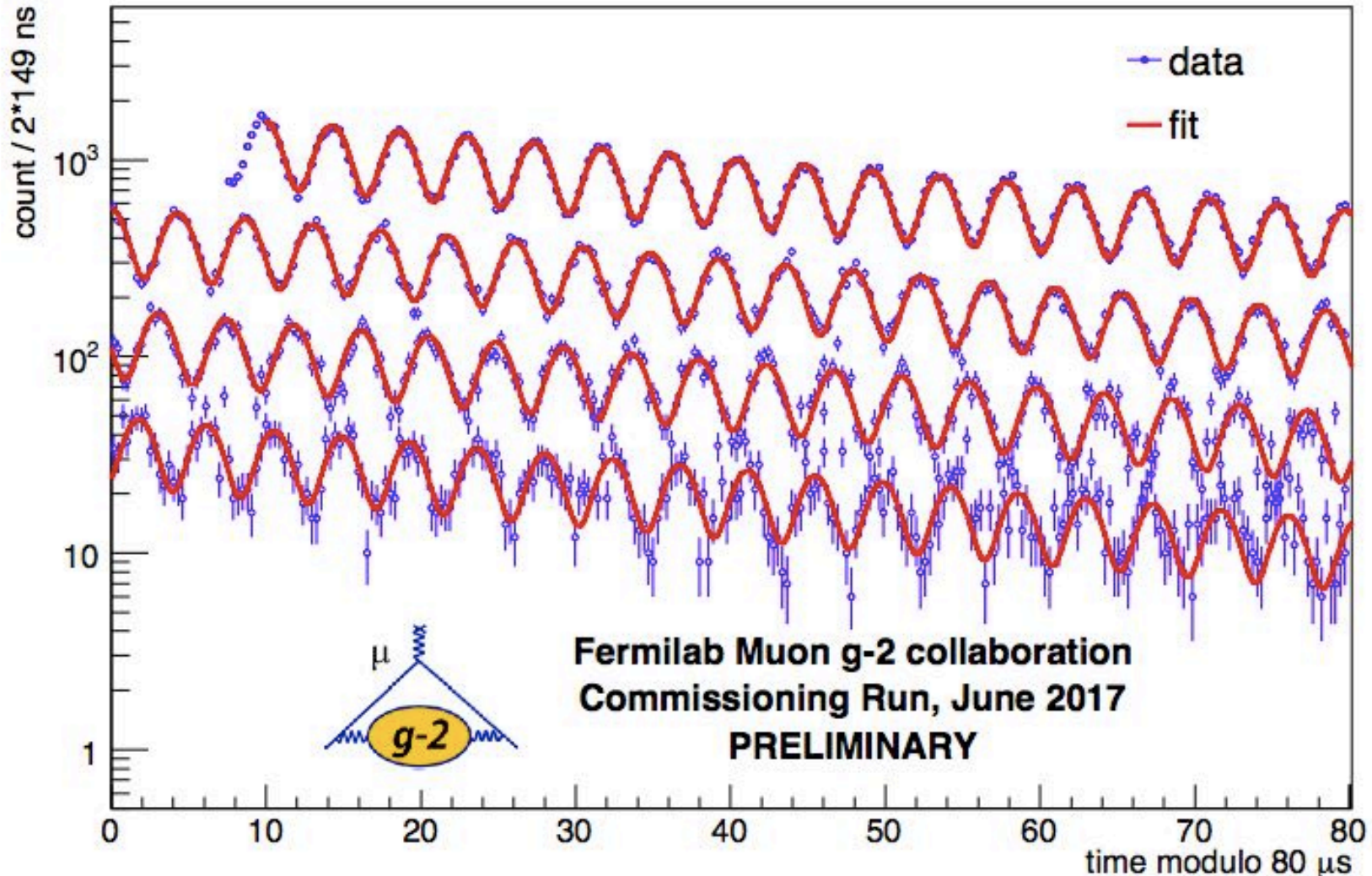


# E989: ring ready for action soon [data taking starts Nov. 2017]



# E989: the first new wiggle plot. **More soon**

Number of high energy positrons as a function of time



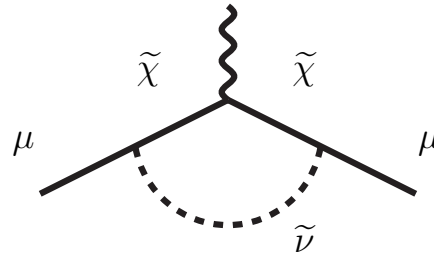
- Data accumulated during two weeks in June 2017, approximately 700k positrons
- The number of wiggles is somewhere between that achieved by CERN-II and CERN-III

# $a_\mu$ : New Physics?

- Many BSM studies use  $g-2$  as constraint or even motivation

- SUSY could easily explain  $g-2$

- Main 1-loop contributions:



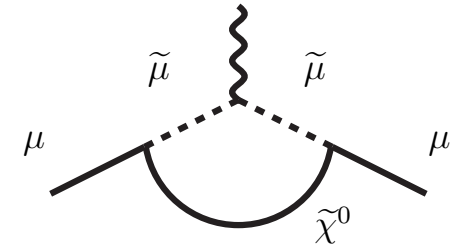
- Simplest case:

$$a_\mu^{\text{SUSY}} \simeq \text{sgn}(\mu) 130 \times 10^{-11} \tan \beta \left( \frac{100 \text{ GeV}}{\Lambda_{\text{SUSY}}} \right)^2$$

- Needs  $\mu > 0$ , 'light' SUSY-scale  $\Lambda$  and/or large  $\tan \beta$  to explain  $281 \times 10^{-11}$

- This is already excluded by LHC searches in the simplest SUSY scenarios (like CMSSM); causes large  $\chi^2$  in simultaneous SUSY-fits with LHC data and  $g-2$

- However:
  - \* SUSY does not have to be minimal (w.r.t. Higgs),
  - \* could have large mass splittings (with lighter sleptons),
  - \* be hadrophobic/leptophilic,
  - \* or not be there at all, but don't write it off yet...

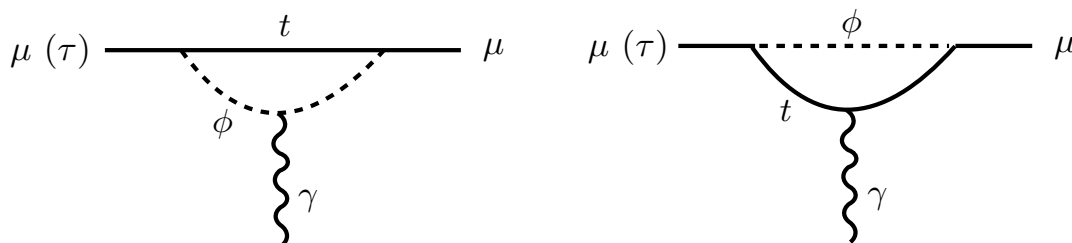


# New Physics? just a few of many recent studies

- Don't have to have full MSSM (like coded in GM2Calc [by Athron, ..., Stockinger et al., EPJC 76 (2016) 62], which includes all latest two-loop contributions), and
  - **extended Higgs sector** could do, see, e.g. Stockinger et al., JHEP 1701 (2017) 007, 'The muon magnetic moment in the 2HDM: complete two-loop result'
- lesson: 2-loop contributions can be highly relevant in both cases; one-loop analyses can be misleading

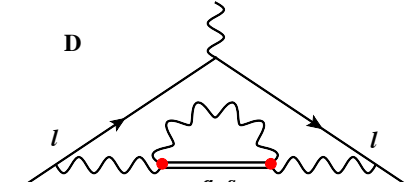
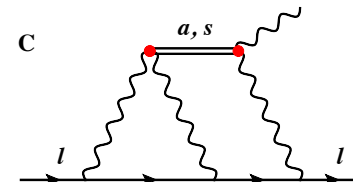
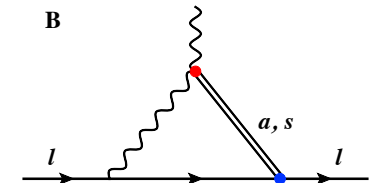
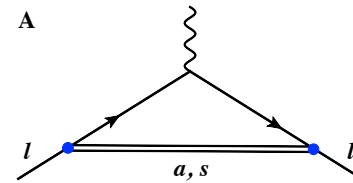
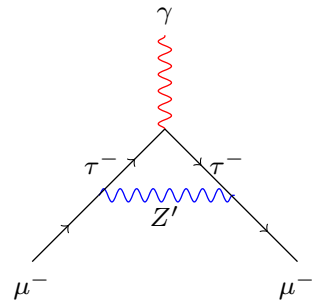
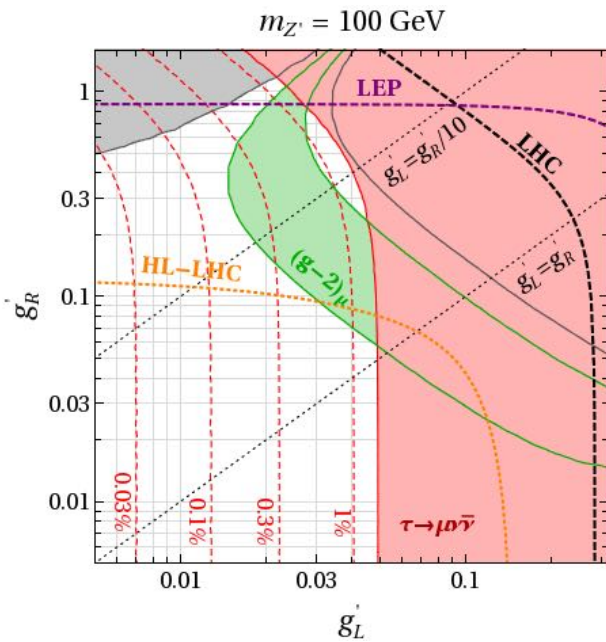
- **1 TeV Leptoquark** Bauer + Neubert, PRL 116 (2016) 141802

one new scalar could explain several anomalies seen by BaBar, Belle and LHC in the flavour sector (e.g. **violation of lepton universality** in  $B \rightarrow K\ell\ell$ , enhanced  $B \rightarrow D\tau\nu$ ) and solve  $g-2$ , while satisfying all bounds from LEP and LHC



# New Physics? just a few of many recent examples

- **light  $Z'$**  can evade many searches involving electrons by non-standard couplings preferring heavy leptons (but see BaBar's direct search limits in a wide mass range, PRD 94 (2016) 011102), or invoke flavour off-diagonal  $Z'$  to evade constraints [Altmannshofer et al., PLB 762 (2016) 389]



- **axion-like particle (ALP)**, contributing like  $\pi^0$  in HLbL [Marciano et al., PRD 94 (2016) 115033]
- **'dark photon'** - like fifth force particle [Feng et al., PRL 117 (2016) 071803]

# Conclusions/Outlook:

- The still unresolved  $g-2$  discrepancy, consolidated at about  $3 \rightarrow 4 \sigma$ , has triggered two new experiments and a lot of theory activities
- The uncertainty of the hadronic contributions will be further squeezed, with L-by-L becoming the bottleneck, but a lot of progress (lattice + new data driven approaches) is expected within the next few years
- TH will be ready for the next round
- Fermilab's  $g-2$  experiment is starting very soon, J-PARC will take a few years longer, both aiming at bringing the current exp uncertainty down by a factor of 4
- with two completely different exp's, hope to get closure
- Also expect vastly improved EDM bounds; complementarity with LFV
- Many approaches to explain the discrepancy with NP, linking  $g-2$  with other precision observables, the flavour sector, dark matter and direct searches, but so far NP is only (con)strained.

Thank you.