

HIGGS BOSON DECAY AND PRODUCTION AT HADRON COLLIDERS

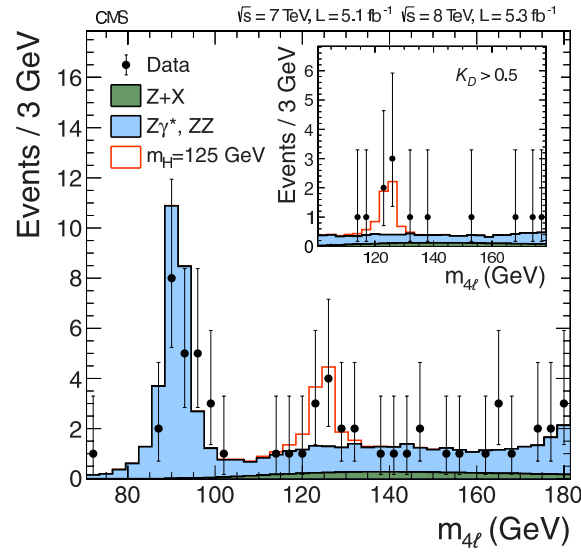
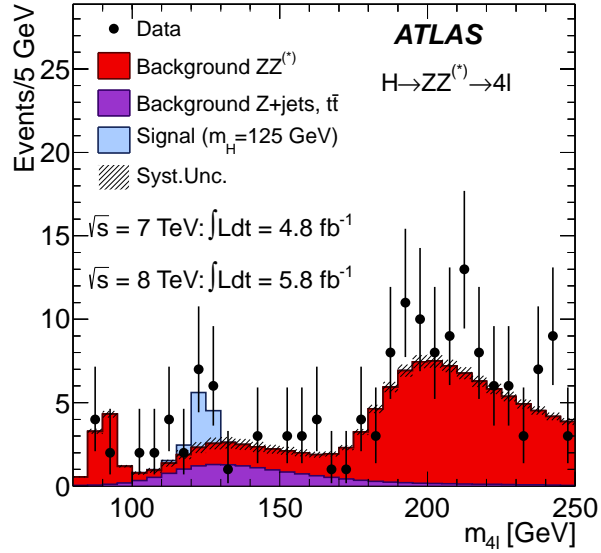
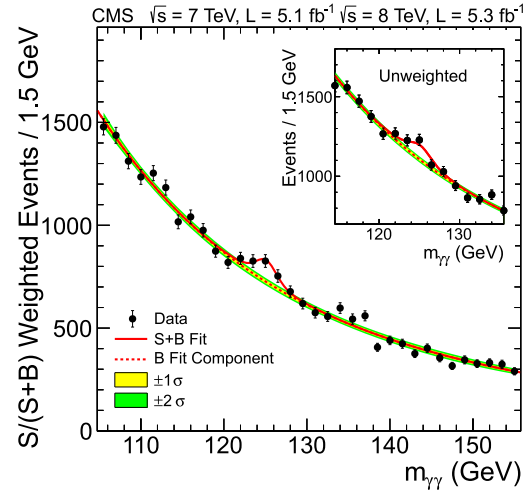
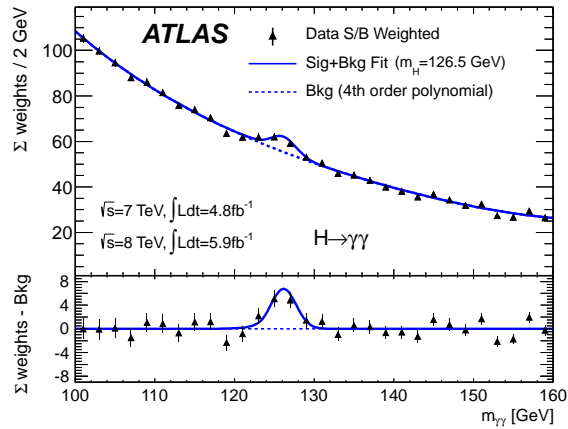
Michael Spira (PSI)

- I Introduction
- II Higgs Boson Decays
- III Higgs Boson Production
- IV Conclusions

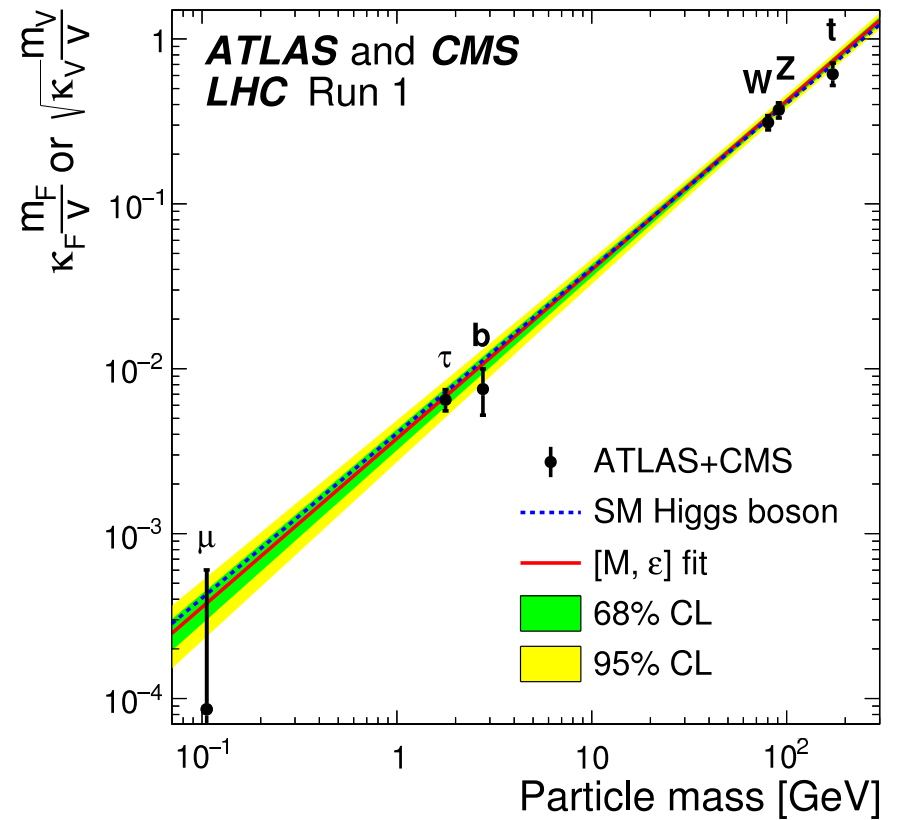
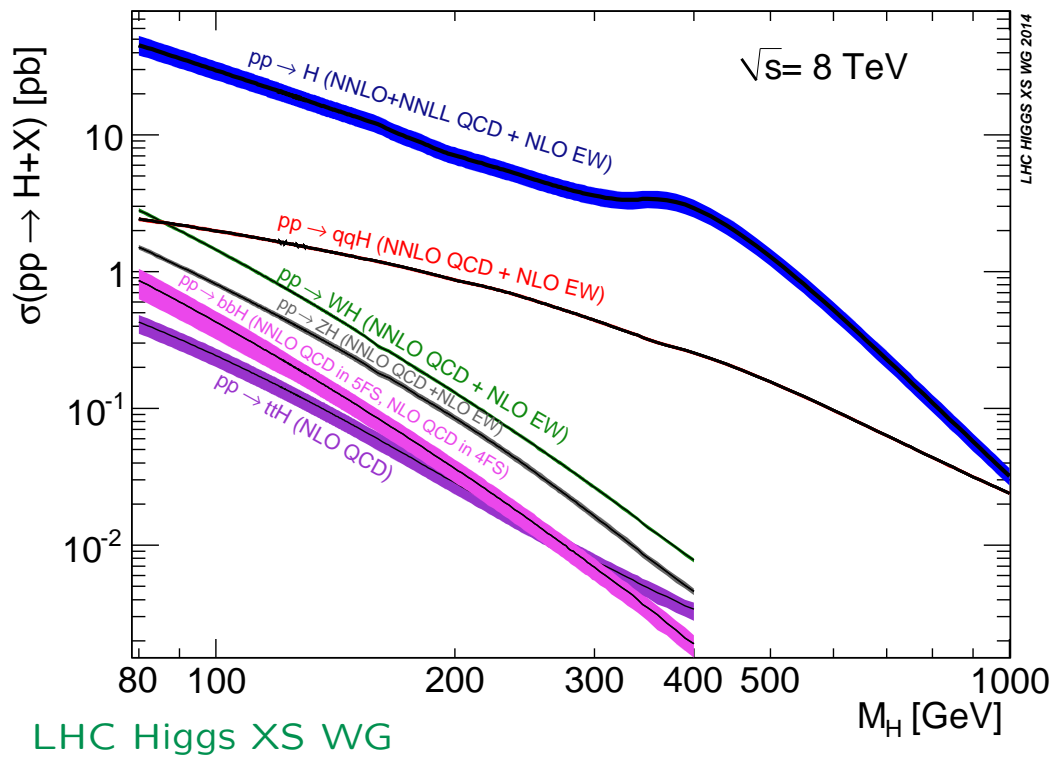
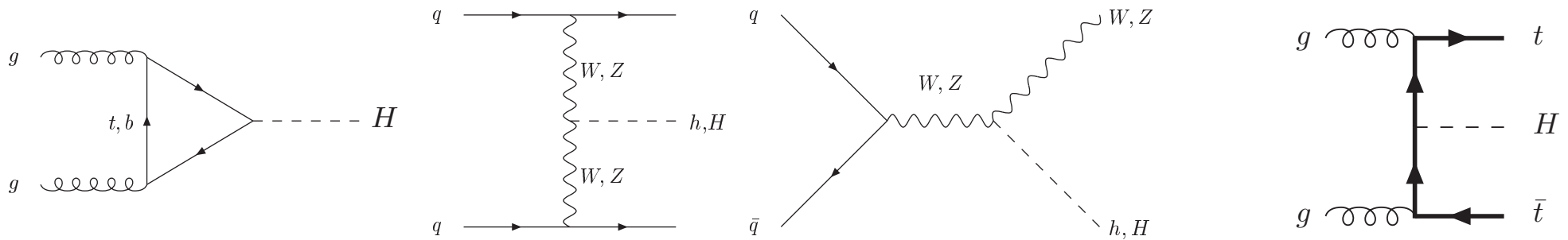
I INTRODUCTION

- SM very successful ← precision data [LEP, Tevatron, LHC]
- open problems: – mechanism of electroweak symmetry breaking
 - unification of forces
 - space-time structure @ short distances
- LHC: fundamental discoveries: Higgs boson(s?)
 - Supersymmetry ?
 - Extra space dimensions ?
- electroweak symmetry breaking: two classes of realization:
 - standard Higgs mechanism [SM, SUSY, . . .]
 - strong elw. symmetry breaking [TC, LH, Higgsless, ED, . . .]

- we have found the Higgs: $M_H \sim 125$ GeV
- $gg \rightarrow H$ dominant



• Higgs Boson Production



- Discovery: LHC [Tevatron]

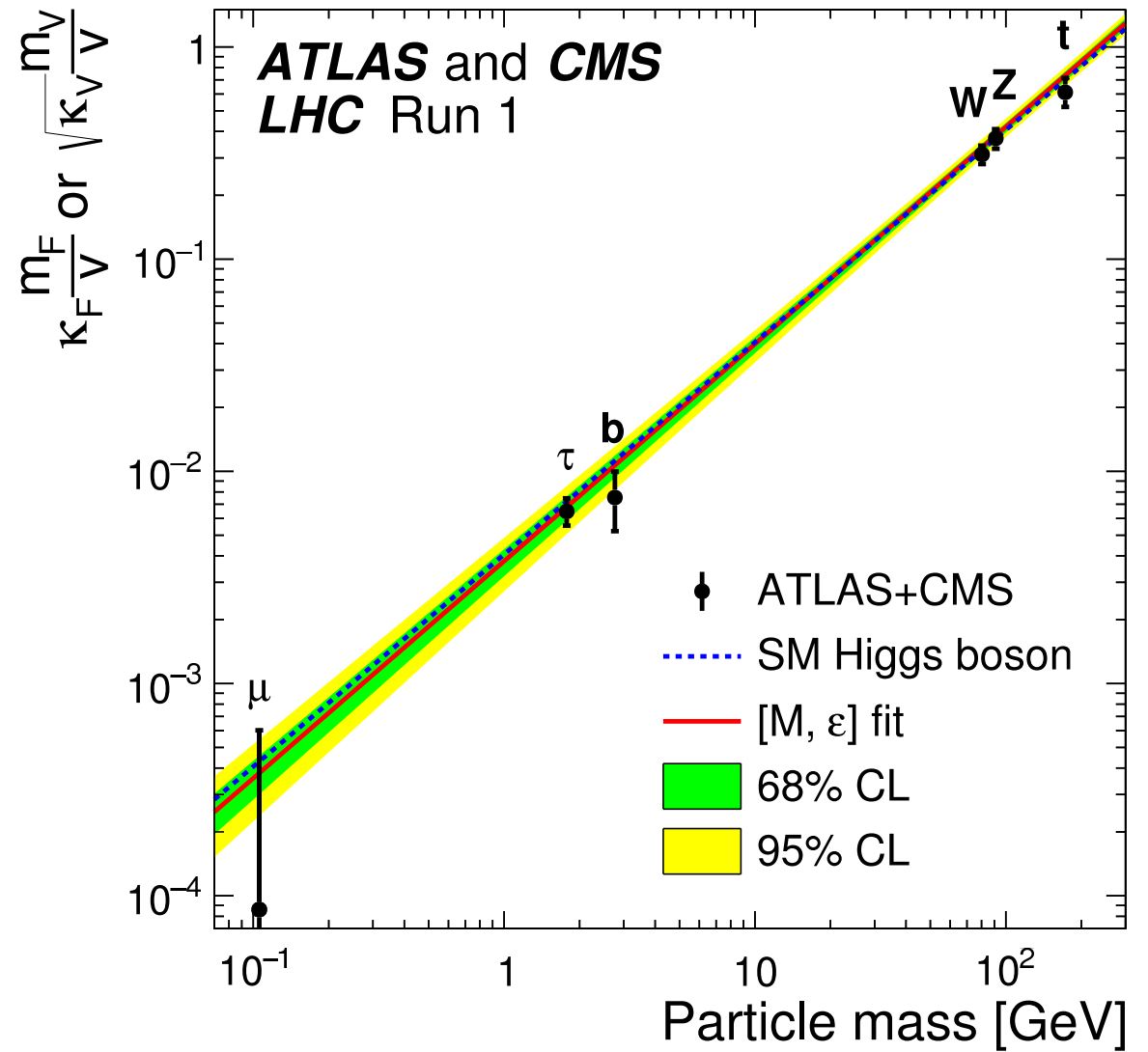
→ Higgs mass

couplings

spin

CP

$\lambda ?$



(ii) MSSM

• 2 Higgs doublets $\xrightarrow{\text{ESB}}$ 5 Higgs bosons: h, H, A, H^\pm

• LO: 2 input parameters: $M_A, \text{tg}\beta = \frac{v_2}{v_1}$

• radiative corrections $\propto m_t^4 \log \frac{m_{\tilde{t}_1} m_{\tilde{t}_2}}{m_t^2} \rightarrow \boxed{M_h \lesssim 135 \text{ GeV}}$

Haber
Carena, ...
Heinemeyer, ...
Zhang
Slavich, ...
...

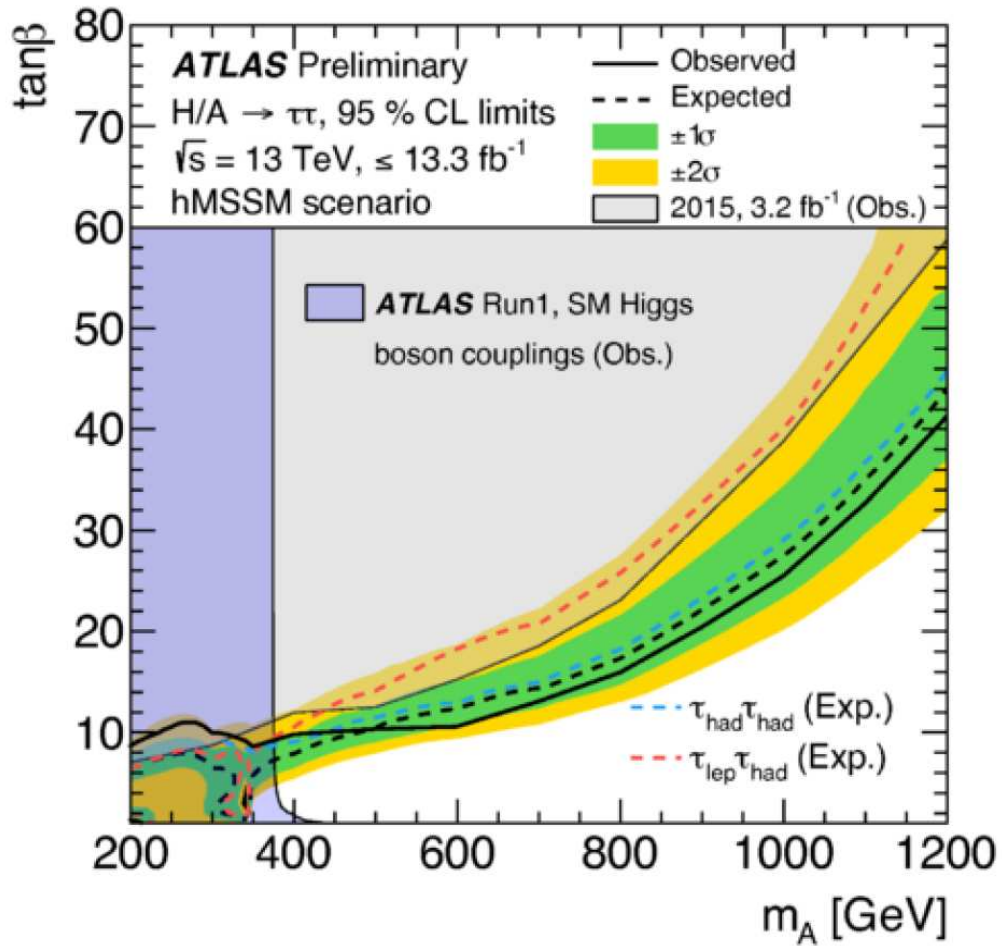
• modified couplings:

ϕ	g_u^ϕ	g_d^ϕ	g_V^ϕ
h	c_α/s_β	$-s_\alpha/c_\beta$	$s_{\beta-\alpha}$
H	s_α/s_β	c_α/c_β	$c_{\beta-\alpha}$
A	$\text{ctg}\beta$	$\text{tg}\beta$	0

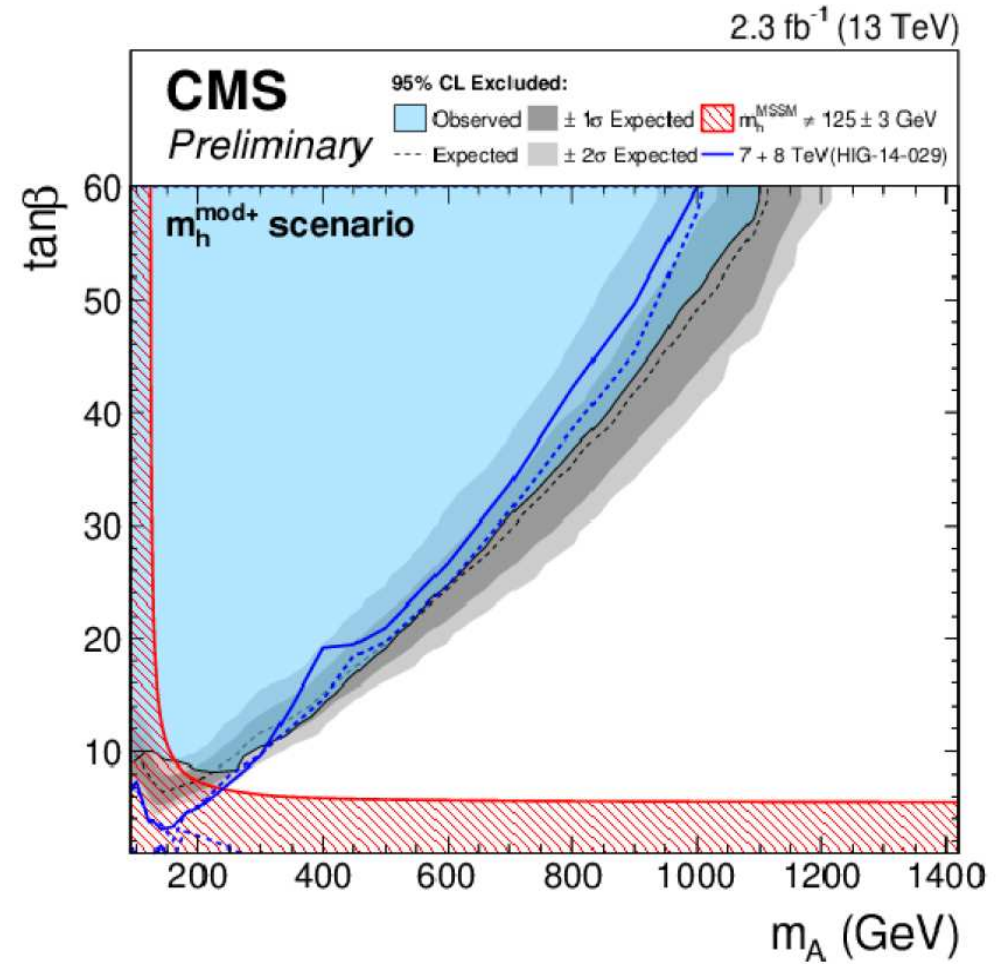
• Yukawa couplings: $\text{tg}\beta \uparrow \Rightarrow g_u^\phi \downarrow \quad g_d^\phi \uparrow \quad g_V^\phi \downarrow$

• LHC: $gg \rightarrow \phi$ dominant for $\text{tg}\beta \lesssim 10$
 $gg \rightarrow \phi b\bar{b}$ dominant for $\text{tg}\beta \gtrsim 10$

$$gg \rightarrow b\bar{b}\phi^0, \quad gg \rightarrow \phi^0$$



$$\phi^0 \rightarrow \tau^+\tau^-$$

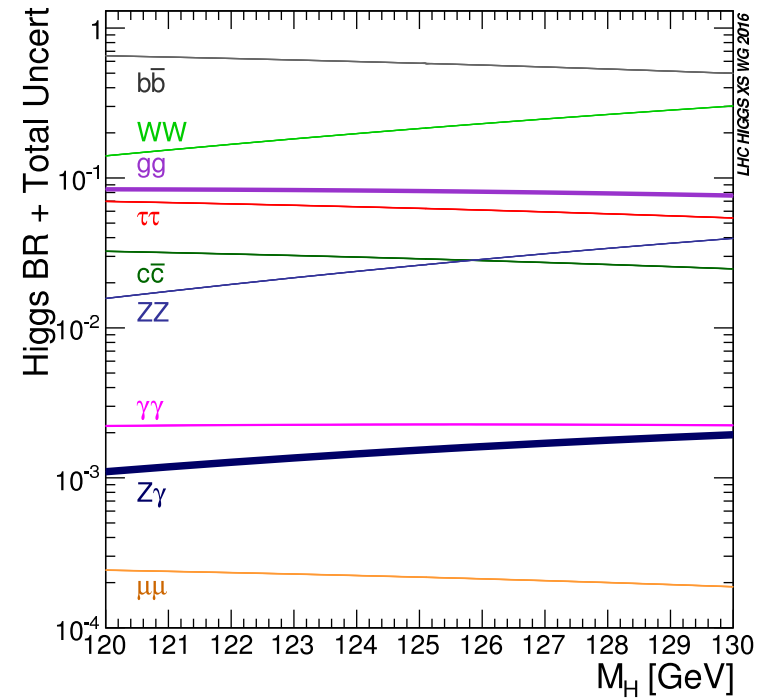
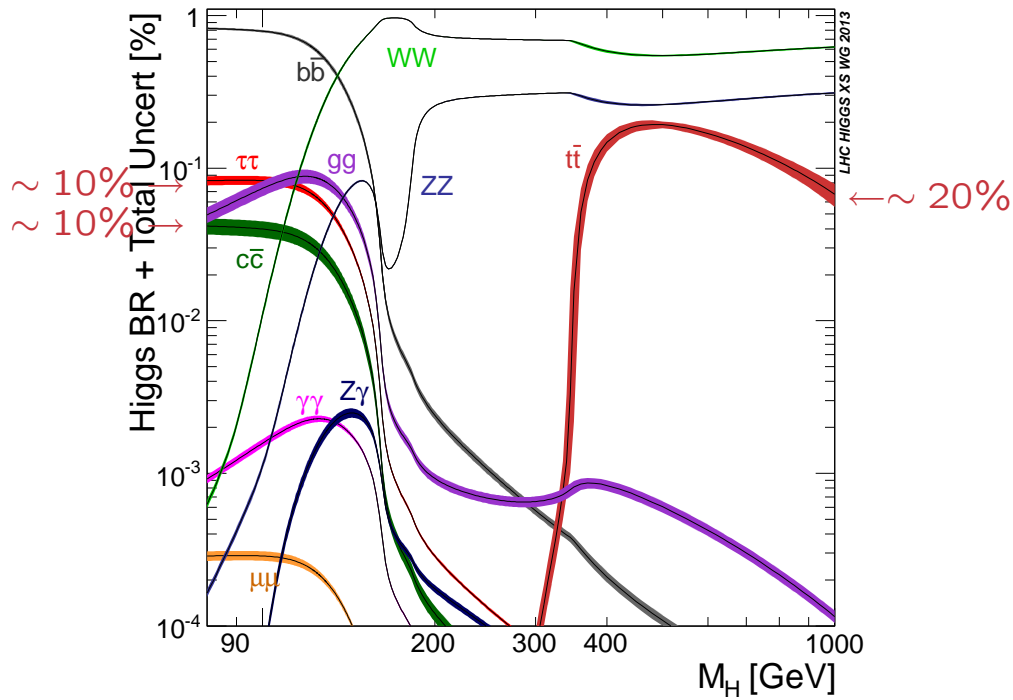


II HIGGS BOSON DECAYS

Partial Width	QCD	Electroweak	Total	on-shell Higgs
$H \rightarrow b\bar{b}/c\bar{c}$	$\sim 0.2\%$	$\sim 0.5\%$ for $M_H \lesssim 500\text{GeV}$ $\sim 0.1(\frac{M_H}{1\text{TeV}})^4$ for $M_H > 500\text{GeV}$	$\sim 0.5\%$ $\sim 0.5\text{--}10\%$	NNNNLO / NLO
$H \rightarrow \tau^+\tau^-/\mu^+\mu^-$		$\sim 0.5\%$ for $M_H \lesssim 500\text{GeV}$ $\sim 0.1(\frac{M_H}{1\text{TeV}})^4$ for $M_H > 500\text{GeV}$	$\sim 0.5\%$ $\sim 0.5\text{--}10\%$	NLO
$H \rightarrow t\bar{t}$	$\lesssim 5\%$	$\lesssim 0.5\%$ for $M_H < 500\text{GeV}$ $\sim 0.1(\frac{M_H}{1\text{TeV}})^4$ for $M_H > 500\text{GeV}$	$\sim 5\%$ $\sim 5\text{--}10\%$	(NNN)NLO / LO
$H \rightarrow gg$	$\sim 3\%$	$\sim 1\%$	$\sim 3\%$	NNNLO approx. / NLO
$H \rightarrow \gamma\gamma$	$< 1\%$	$< 1\%$	$\sim 1\%$	NLO / NLO
$H \rightarrow Z\gamma$	$< 1\%$	$\sim 5\%$	$\sim 5\%$	(N)LO / LO
$H \rightarrow WW/ZZ \rightarrow 4f$	$< 0.5\%$	$\sim 0.5\%$ for $M_H < 500\text{GeV}$ $\sim 0.17(\frac{M_H}{1\text{TeV}})^4$ for $M_H > 500\text{GeV}$	$\sim 0.5\%$ $\sim 0.5\text{--}15\%$	(N)NLO

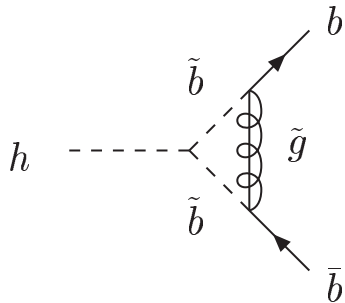
- QCD: variation of Higgs widths for scale by factor 2 and 1/2
elw: missing HO estimated from known structure at NLO
 $M_H \gtrsim 500$ GeV: Higgs self-interactions dominate error
different uncertainties added linearly for each channel
- parametric uncertainties:
 $m_t = 172.5 \pm 1$ GeV $\alpha_s(M_Z) = 0.118 \pm 0.0015$
 $m_b(m_b) = 4.18 \pm 0.03$ GeV $m_c(3\text{GeV}) = 0.986 \pm 0.025$ GeV
different uncertainties added quadratically for each channel
- total uncertainties: parametric & theor. uncertainties added linearly

HDECAY & Prophecy4f



Denner, Heinemeyer, Puljak, Rebuszi, S.

- MSSM: large SUSY–QCD corrections to $\phi^0 \rightarrow b\bar{b}$



$$\propto \frac{\alpha_s}{\pi} \frac{m_{\tilde{g}} \mu t g \beta}{M_{SUSY}^2} \sim \Delta_b$$

Hall, ...
 Carena, ...
 Nierste, ...
 Häfliger, ...
 Noth, S.
 Mihaila, Reisser
 etc.

SUSY-QCD Corrections to $b\bar{b}\phi^0$

$[\Delta \lesssim 1\%]$

$$\mathcal{L}_{eff} = -\lambda_b \bar{b}_R \left[\phi_1^0 + \frac{\Delta_b}{\text{tg}\beta} \phi_2^{0*} \right] b_L + h.c. \quad \text{valid to all orders in } \Delta_b$$

$$= -m_b \bar{b} \left[1 + i\gamma_5 \frac{G^0}{v} \right] b - \frac{m_b/v}{1 + \Delta_b} \bar{b} \left[g_b^h \left(1 - \frac{\Delta_b}{\text{tg}\alpha \text{tg}\beta} \right) h \right. \\ \left. + g_b^H \left(1 + \Delta_b \frac{\text{tg}\alpha}{\text{tg}\beta} \right) H - g_b^A \left(1 - \frac{\Delta_b}{\text{tg}^2\beta} \right) i\gamma_5 A \right] b$$

$$\Delta_b = \Delta_b^{QCD(1)} + \Delta_b^{elw(1)}$$

$$\Delta_b^{QCD(1)} = \frac{2}{3} \frac{\alpha_s(\mu_R)}{\pi} M_{\tilde{g}} \mu \text{tg}\beta I(m_{\tilde{b}_1}^2, m_{\tilde{b}_2}^2, M_{\tilde{g}}^2)$$

$$\Delta_b^{elw(1)} = \frac{\lambda_t^2(\mu_R)}{(4\pi)^2} \mu A_t \text{tg}\beta I(m_{\tilde{t}_1}^2, m_{\tilde{t}_2}^2, \mu^2)$$

$$I(a, b, c) = -\frac{ab \log \frac{a}{b} + bc \log \frac{b}{c} + ca \log \frac{c}{a}}{(a-b)(b-c)(c-a)}$$

\Rightarrow resummed Yukawa couplings \tilde{g}_b^Φ

Carena, Garcia, Nierste, Wagner
Guasch, Häfliger, S.

small α_{eff} scenario [modified]

$$\text{tg}\beta = 30$$

$$M_{\tilde{Q}} = 800 \text{ GeV}$$

$$M_{\tilde{g}} = 1000 \text{ GeV} \quad \leftarrow$$

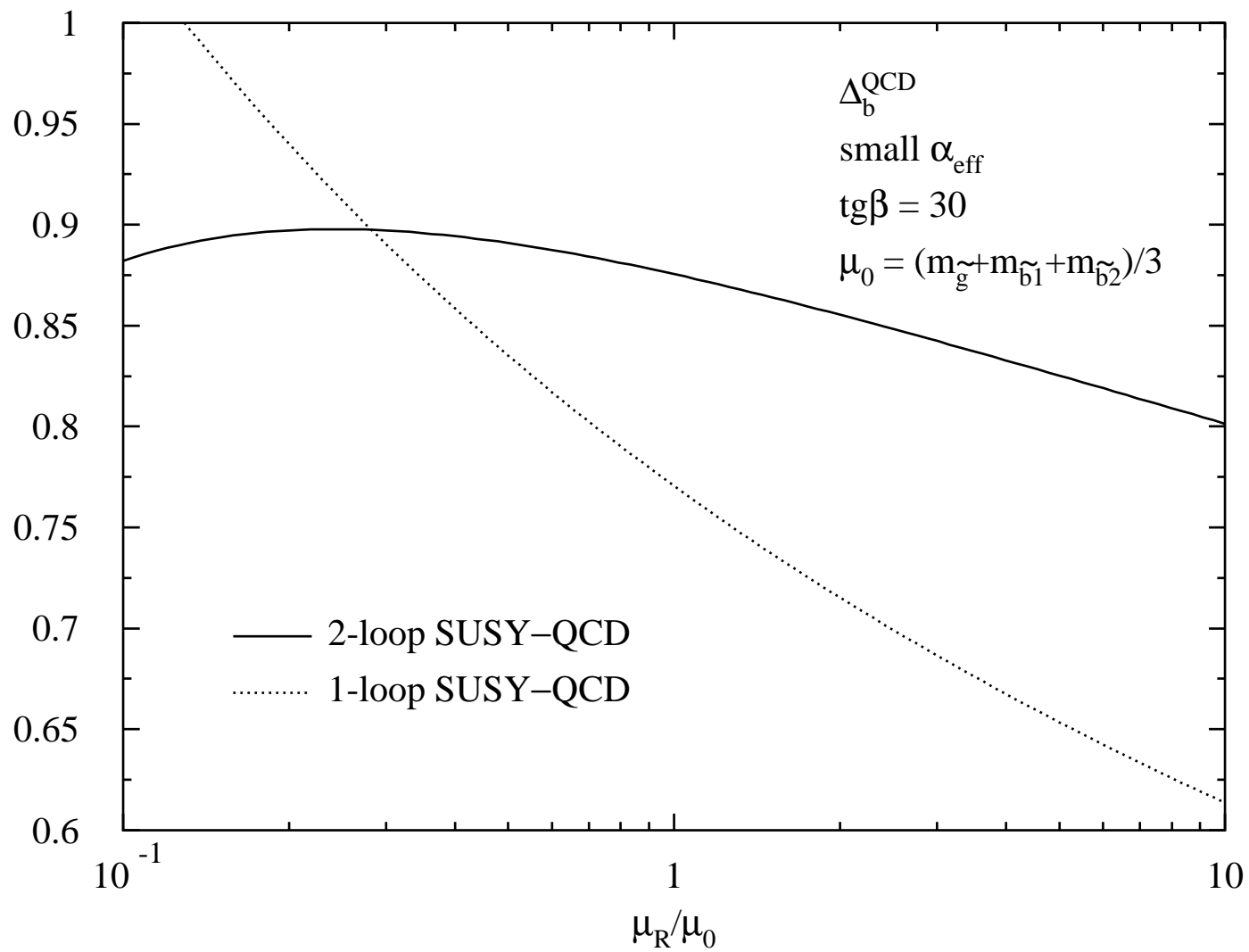
$$M_2 = 500 \text{ GeV}$$

$$A_b = A_t = -1.133 \text{ TeV}$$

$$\mu = 2 \text{ TeV}$$

$$m_{\tilde{t}_1} = 679 \text{ GeV} \quad m_{\tilde{t}_2} = 935 \text{ GeV}$$

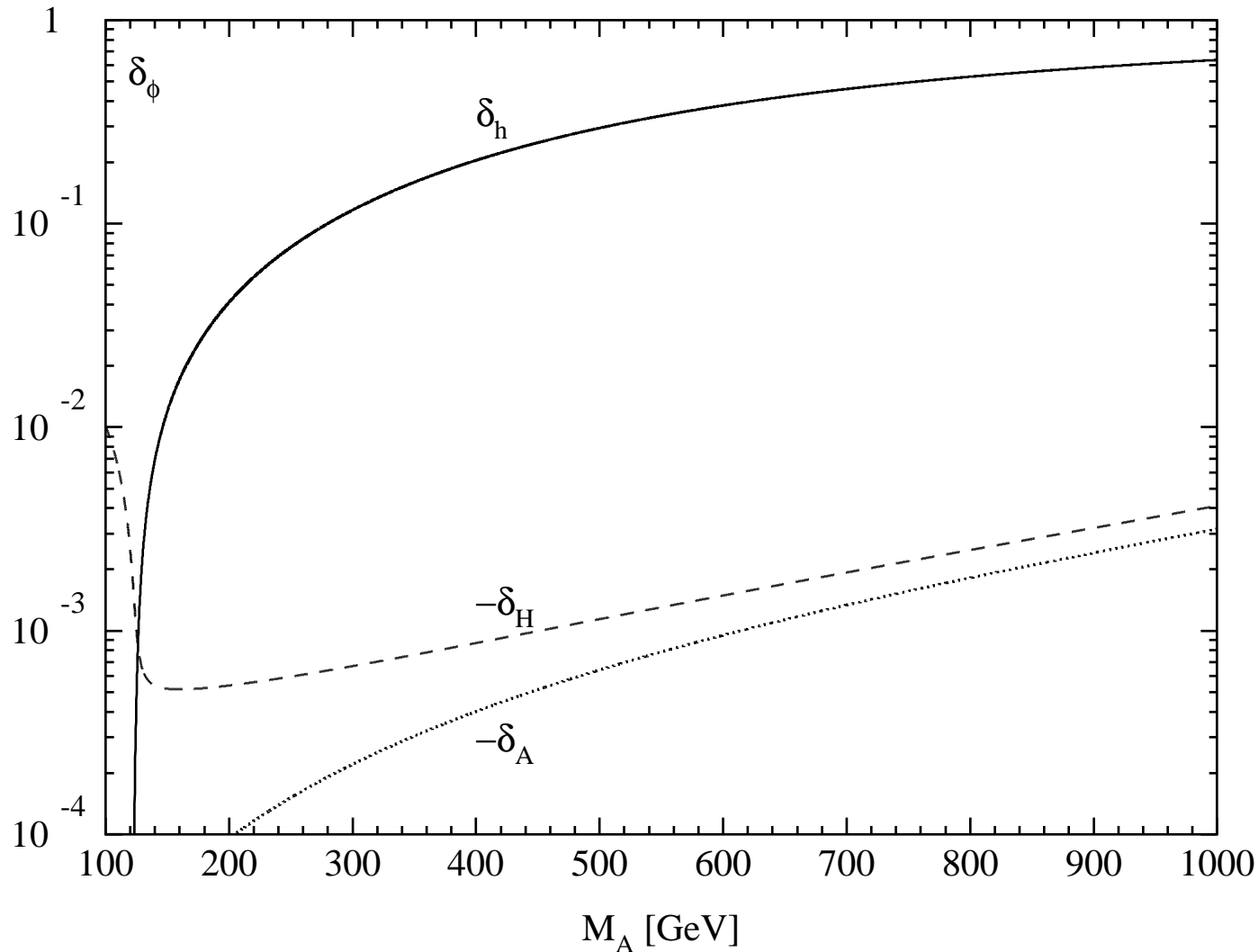
$$m_{\tilde{b}_1} = 601 \text{ GeV} \quad m_{\tilde{b}_2} = 961 \text{ GeV}$$



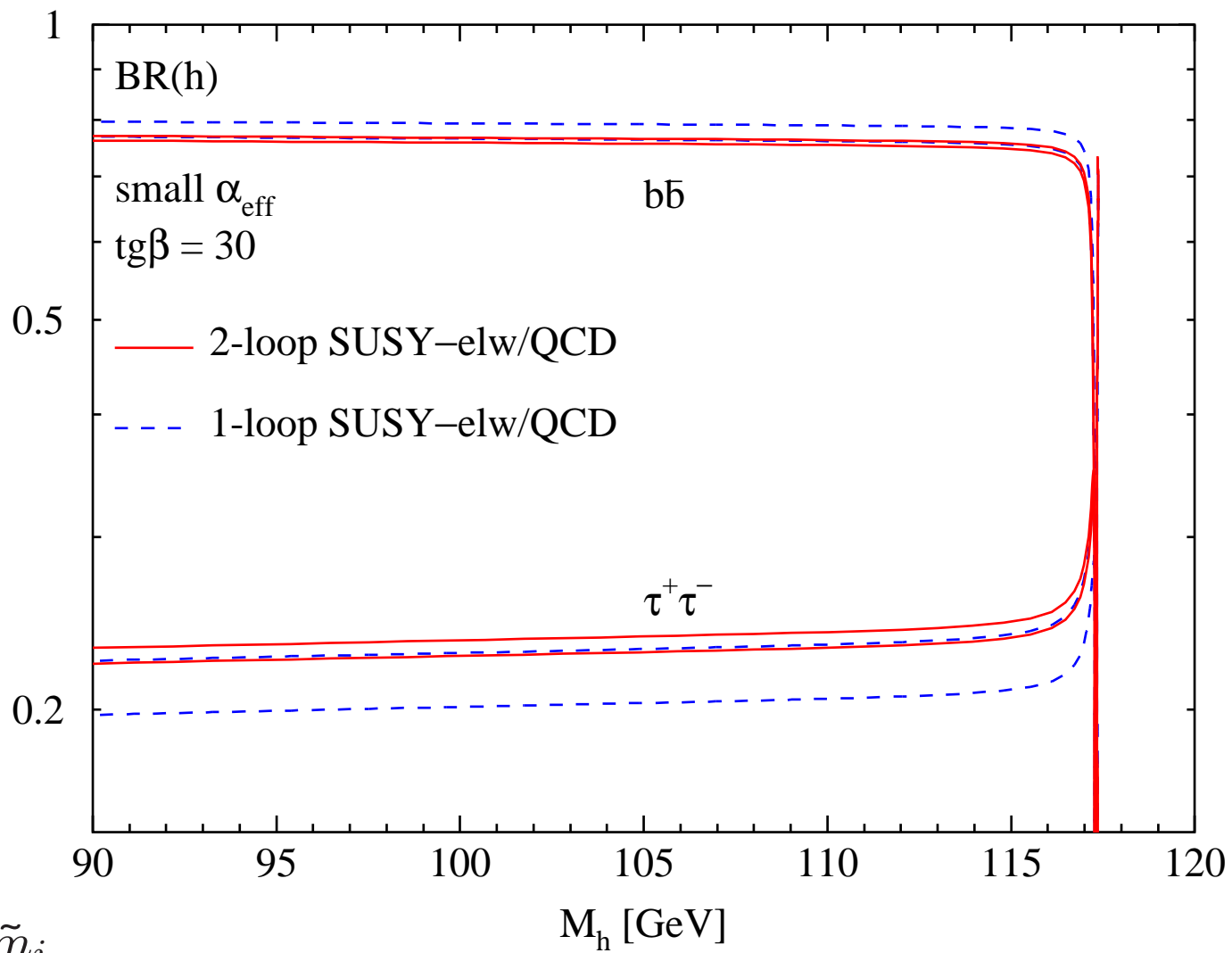
Noth, S.
(Mihaila, Reisser)

$$\Gamma[\Phi \rightarrow b\bar{b}] = \frac{3G_F M_\Phi \bar{m}_b^2(M_\Phi)}{4\sqrt{2}\pi} \Delta_{\text{QCD}} \tilde{g}_b^\Phi \left[\tilde{g}_b^\Phi + g_b^\Phi \delta_{rem} \right]$$

$$M_A^2 \gg M_Z^2 : \text{tg}\alpha \rightarrow -\frac{1}{\text{tg}\beta} \quad \Rightarrow \quad \tilde{g}_b^h \rightarrow \frac{1}{1 + \Delta_b} \left(1 - \frac{\Delta_b}{\text{tg}\alpha \text{tg}\beta} \right) \rightarrow 1$$

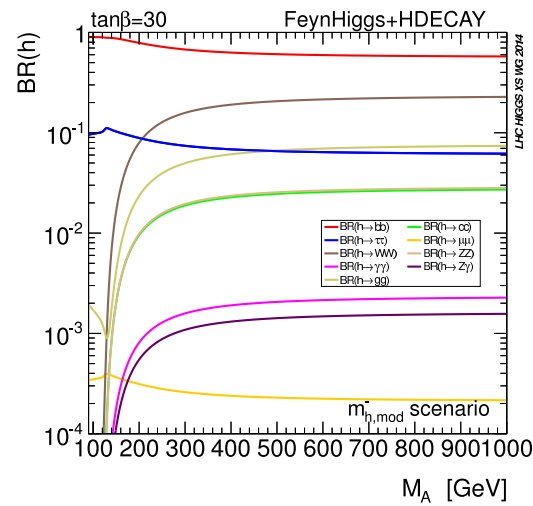
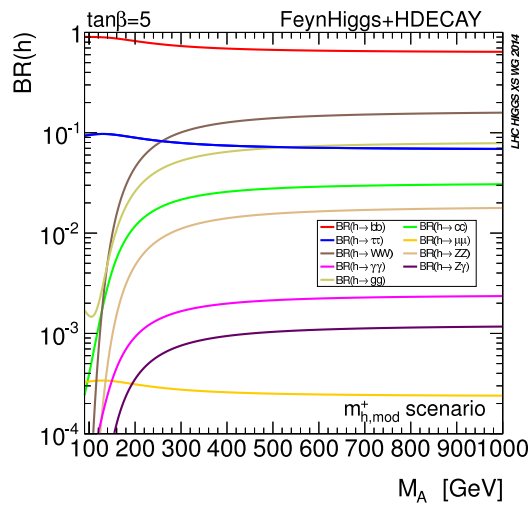
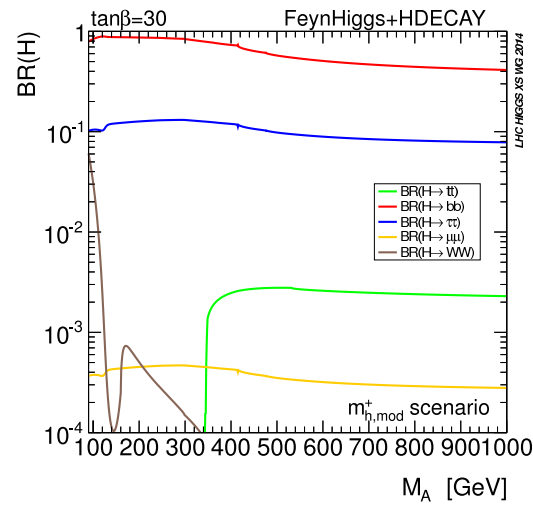
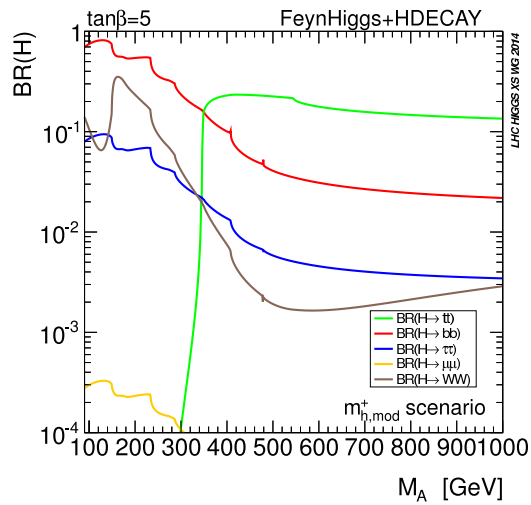
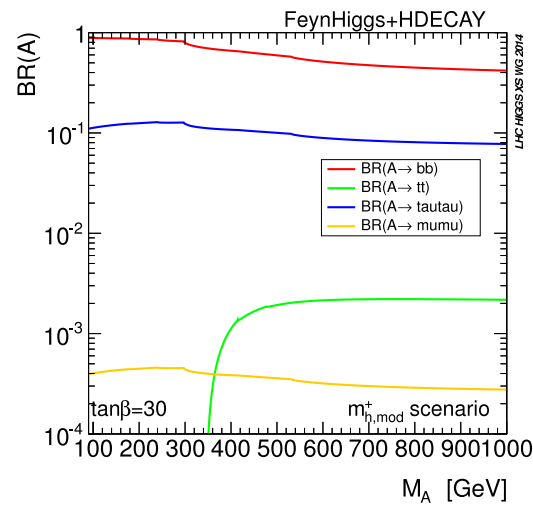
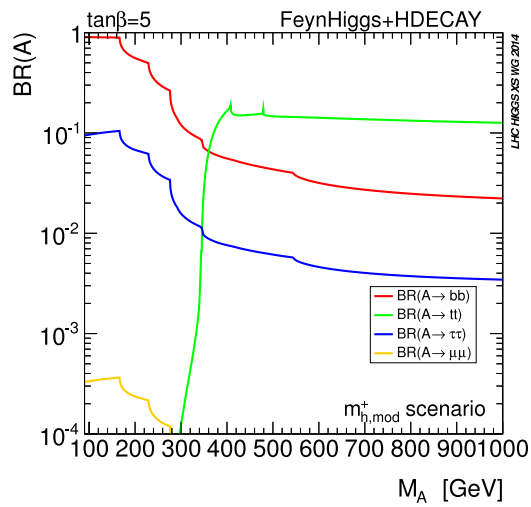


$$\delta_\phi = \frac{\delta_{rem}}{\delta_{SQCD}}$$



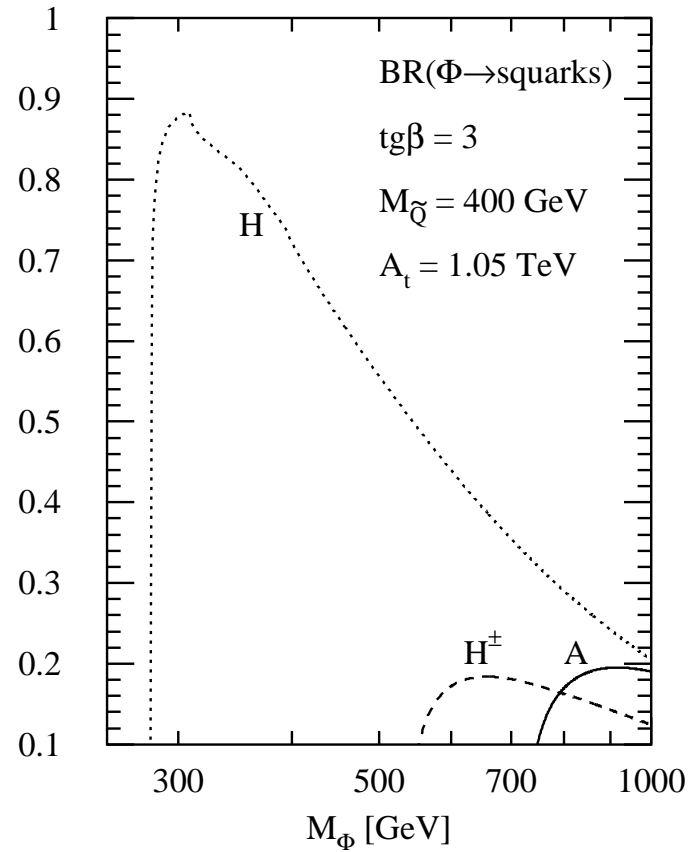
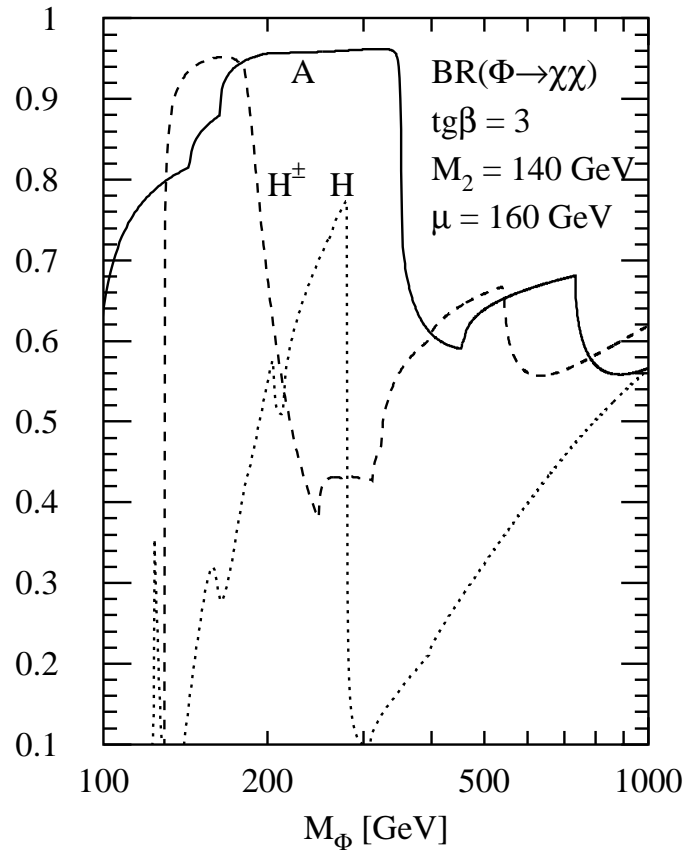
$$\mu_R = \frac{1}{3} \sum \tilde{m}_i$$

Noth, S. → HDECAY



+ charged Higgs decays

SUSY Decays

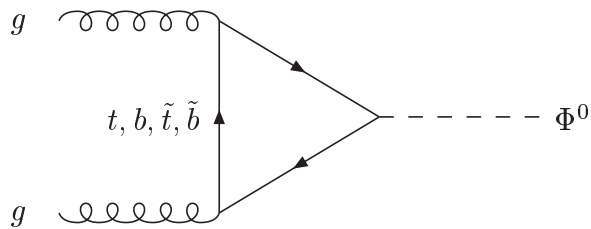


HDECAY

- if kinematically possible \rightarrow important

III HIGGS BOSON PRODUCTION

(i) $gg \rightarrow h/H/A$



Georgi,...

Gamberini,...

S., Djouadi, Graudenz, Zerwas
Dawson, Kauffman

- NLO QCD corrections: $\sim 10 \dots 100\%$

- NNLO calculated for $m_t \gg M_\phi \Rightarrow$ further increase by 20–30%
[mass effects small]

Harlander, Kilgore
Anastasiou, Melnikov

Ravindran, Smith, van Neerven

Marzani, Ball, Del Duca, Forte, Vicini
Harlander, Ozeren
Pak, Rogal, Steinhauser

- N³LO for $m_t \gg M_\phi \Rightarrow$ scale stabilization
scale dependence: $\Delta \lesssim 5\%$

Moch, Vogt
Ravindran

de Florian, Mazzitelli, Moch, Vogt
Anastasiou, Duhr, Dulat, Furlan, Gehrmann, Herzog, Mistlberger
Ball, Bonvini, Forte, Marzani, Ridolfi

- N³LL soft gluon resummation: $\lesssim 2\%$

Catani, de Florian, Grazzini, Nason
Ravindran
Ahrens, Becher, Neubert, Yang
Ball, Bonvini, Forte, Marzani, Ridolfi
Bonvini, Marzani
Schmidt, S.

- elw. corrections: $\sim 5\%$

Aglietti, . . .
Degrassi, Maltoni
Actis, Passarino, Sturm, Uccirati

- QCD corrections to squark loops: 10–100%

Mühlleitner, S.
Bonciani, Degrassi, Vicini

- genuine SUSY–QCD corrections: 10–100%
[$\leftarrow \Delta_b$ @ large $\tan\beta$]

Harlander, Steinhauser, Hofmann
Degrassi, Slavich
Anastasiou, Beerli, Daleo
Mühlleitner, Rzehak, S.

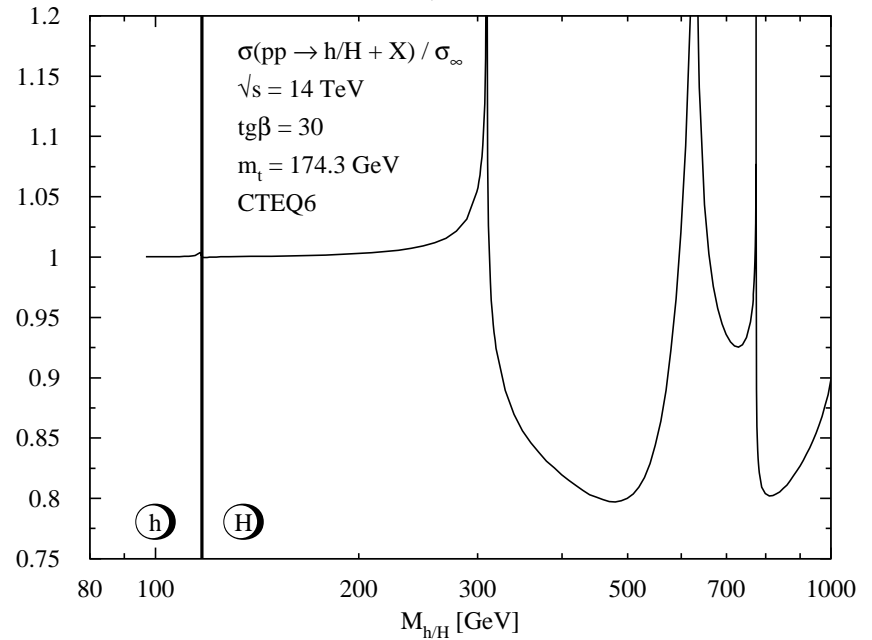
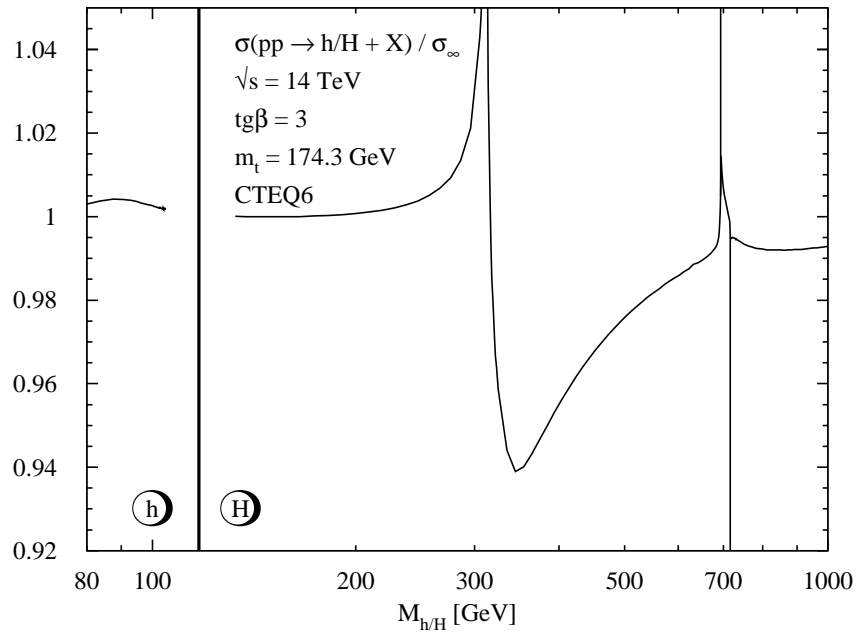
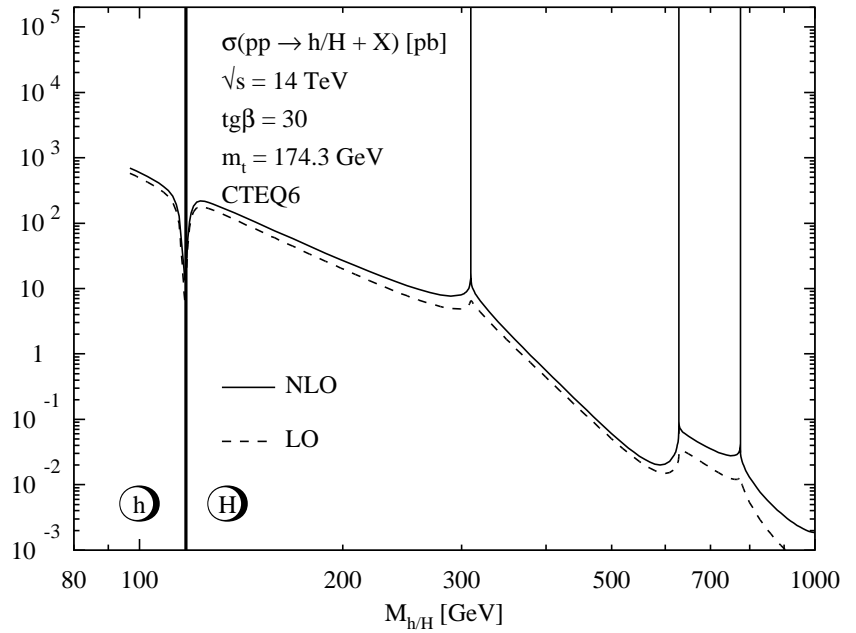
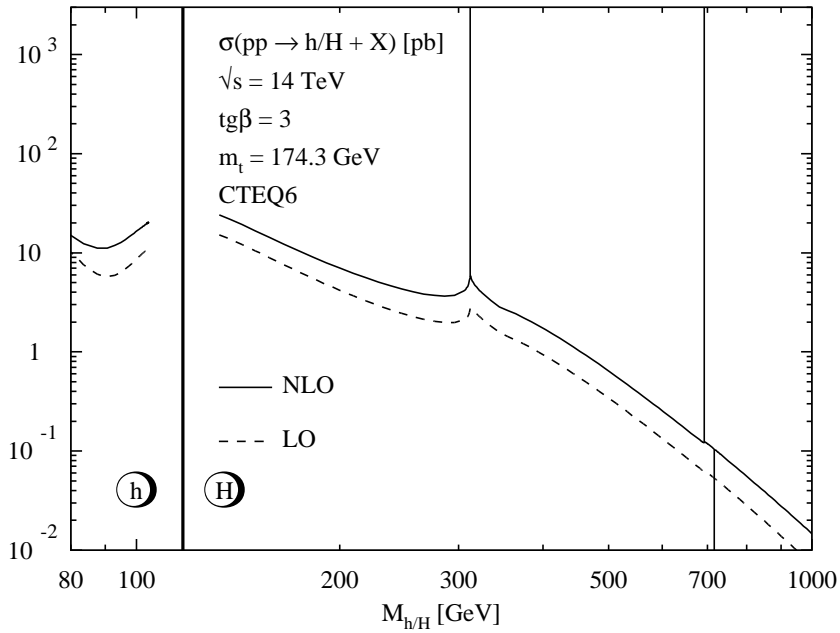
- SUSY-elw. corrections unknown

- impl. of $gg \rightarrow \phi$ in POWHEG including mass effects @ NLO

Bagnaschi, Degrassi, Slavich, Vicini

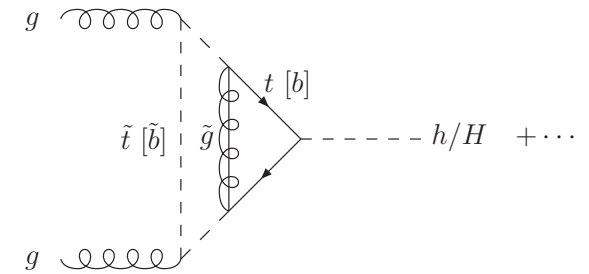
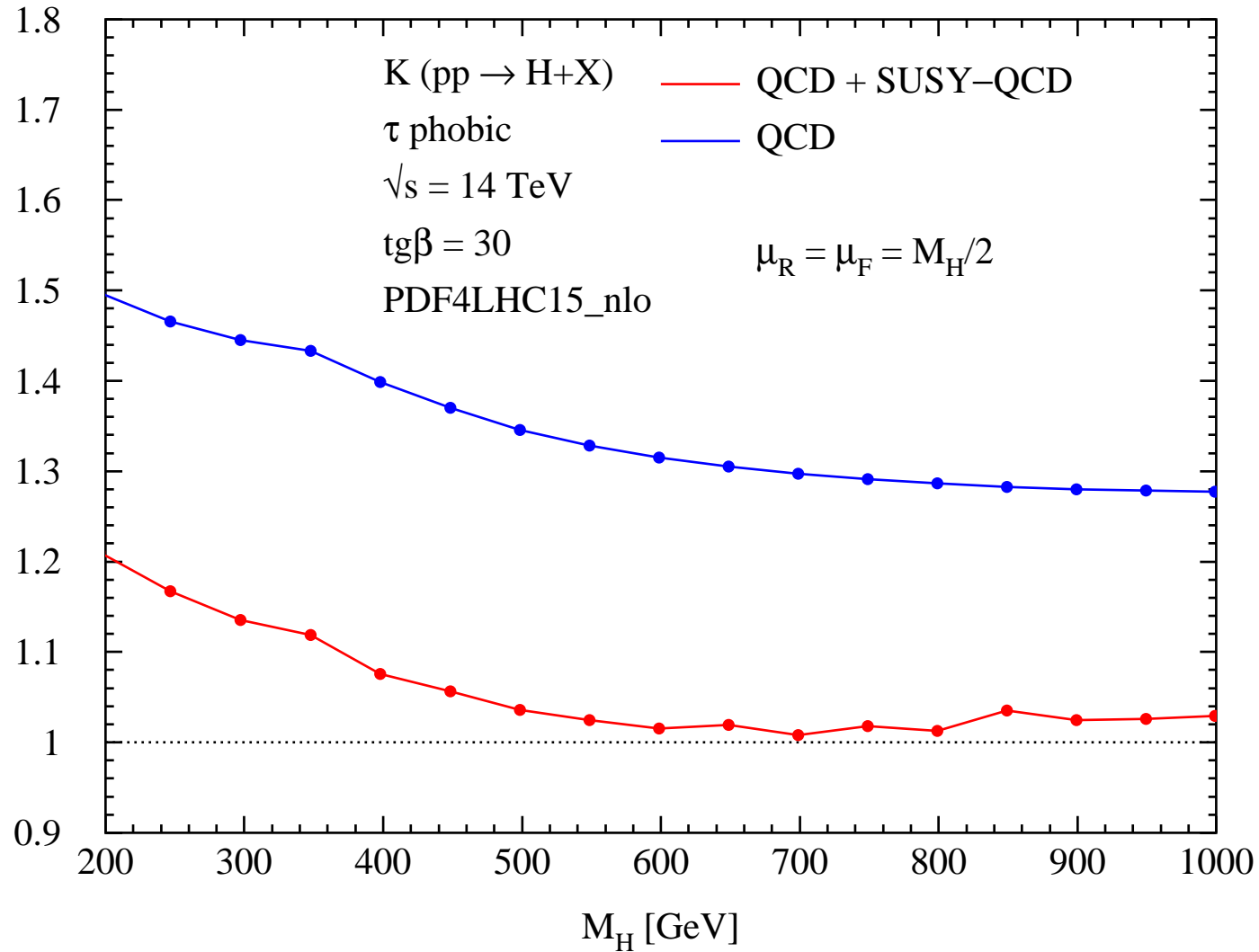
• QCD corrections to squark loops:

Mühlleitner, S.



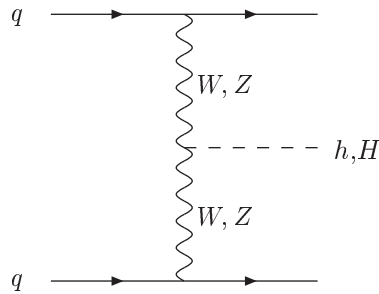
$$\sigma(gg \rightarrow \Phi) = \sigma_{LO}(g_t^\Phi, \tilde{g}_b^\Phi) [1 + \delta_{QCD} + \delta_{SQCD}]$$

PRELIMINARY



Mühlleitner, Rzehak, S.

(ii) W/Z fusion: $pp \rightarrow W^*W^*/Z^*Z^* \rightarrow h/H$



Cahn, Dawson
Hikasa
Atarelli, Mele, Pitolli

Han, Valencia,
Willenbrock
Figy, Oleari, Zeppenfeld
Berger, Campbell

Bolzano, Maltoni, Moch, Zaro
Cacciari, Dreyer, Karlberg, Salam, Zanderighi

Dreyer, Karlberg

Ciccolini, Denner, Dittmaier

Djouadi, S.

Hollik, Rzehak, Plehn, Rauch
Figy, Palmer, Weiglein

- QCD corrections \leftarrow DIS: $\sim 10\%$

[approx] 2-loop: $\lesssim 1\%$

[approx] 3-loop: $\lesssim 0.3\%$

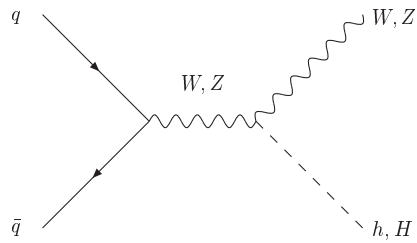
- elw. corrections: $\sim 10\%$

- genuine SUSY-QCD corrections small

- genuine SUSY-elw. corrections: $\lesssim 5\%$

[implemented in VBFNLO]

(iii) Higgs–strahlung: $pp \rightarrow W^*/Z^* \rightarrow W/Z + h/H$



Glashow,...
Kunszt,...

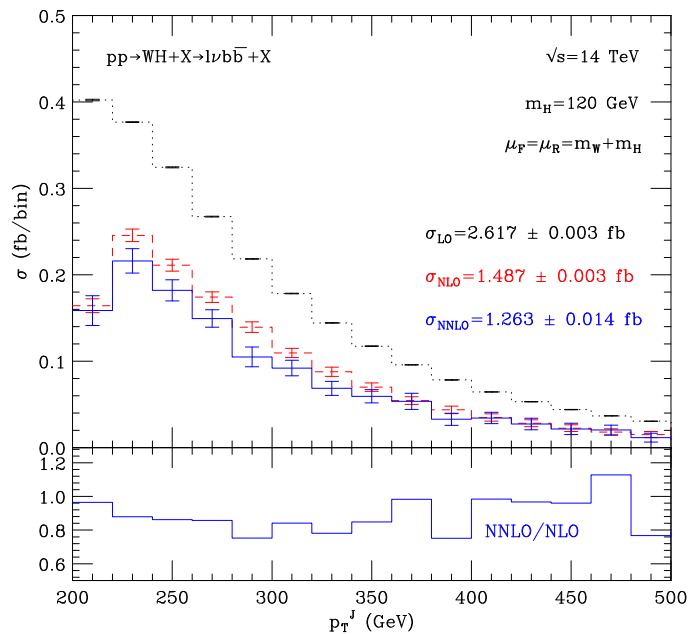
- QCD corrections \leftarrow DY: $\sim 30\%$
2-loop: $\lesssim 5\%$
- SUSY-QCD corrections small
- electroweak corrections: $\sim -10\%$
- $W/Z + H$: fully exclusive @ NNLO QCD

Han, Willenbrock
Brein, Djouadi, Harlander

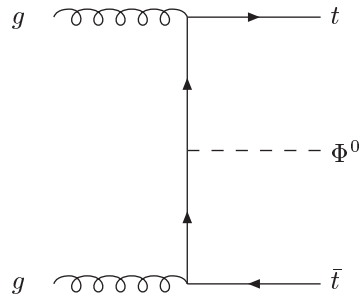
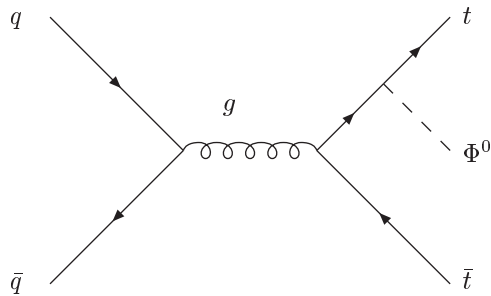
Djouadi, S.

Ciccolini, Dittmaier, Krämer

Ferrera, Grazzini, Tramantano



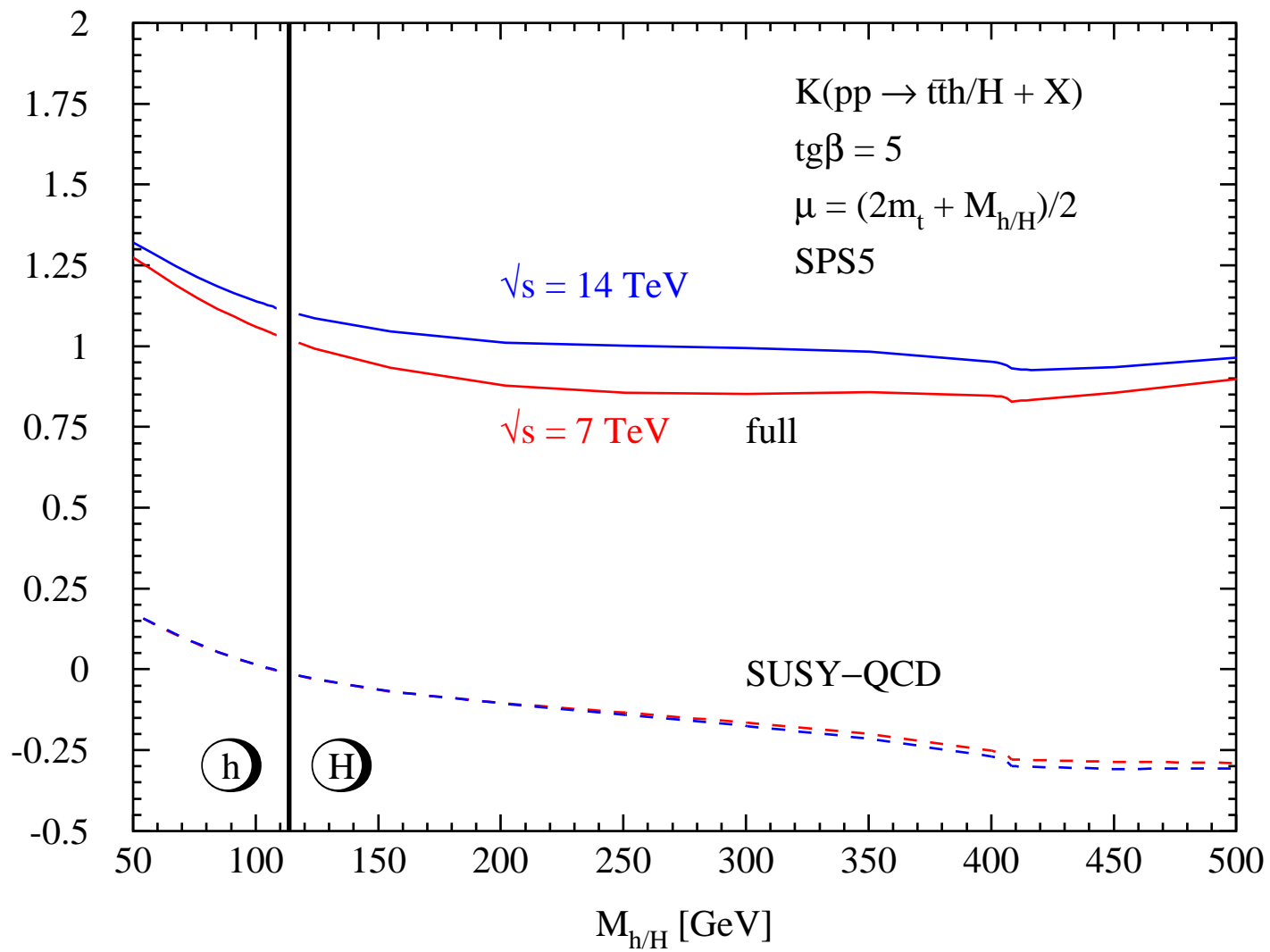
(iv) Bremsstrahlung: $pp \rightarrow t\bar{t} + h/H/A$



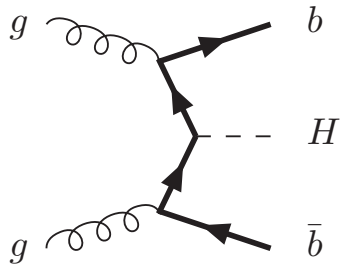
dominant

Kunszt
Gunion
Marciano, Paige

- $t\bar{t}h \rightarrow t\bar{t}b\bar{b}$ important @ LHC \rightarrow top Yukawa cplg.
- QCD corrections [SM]: $\sim 20\%$ Beenakker, Dittmaier, Krämer, Plümper, S., Zerwas
Dawson, Orr, Reina, Wackerath
Broggio, Ferroglia, Pecjak, Signer, Yang
[threshold suppressed: $\sigma_{LO} \sim \beta^4$]
- SUSY-QCD corrections: moderate Dittmaier, Häfliger, Krämer, S., Walser
- link to parton showers: aMC@NLO, PowHel Frederix et al.
Garzelli, Kardos, Papadopoulos, Trócsányi
- important work on backgrounds $t\bar{t}b\bar{b}, t\bar{t}jj$, etc. Bredenstein, Denner, Dittmaier, Pozzorini
Bevilacqua, Czakon, Papadopoulos, Pittau, Worek
Cascioli, Maierhofer, Pozzorini

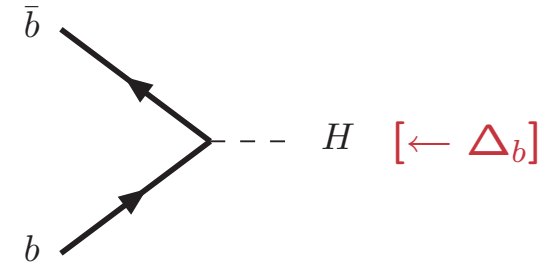


(v) $b\bar{b}$ +Higgs production



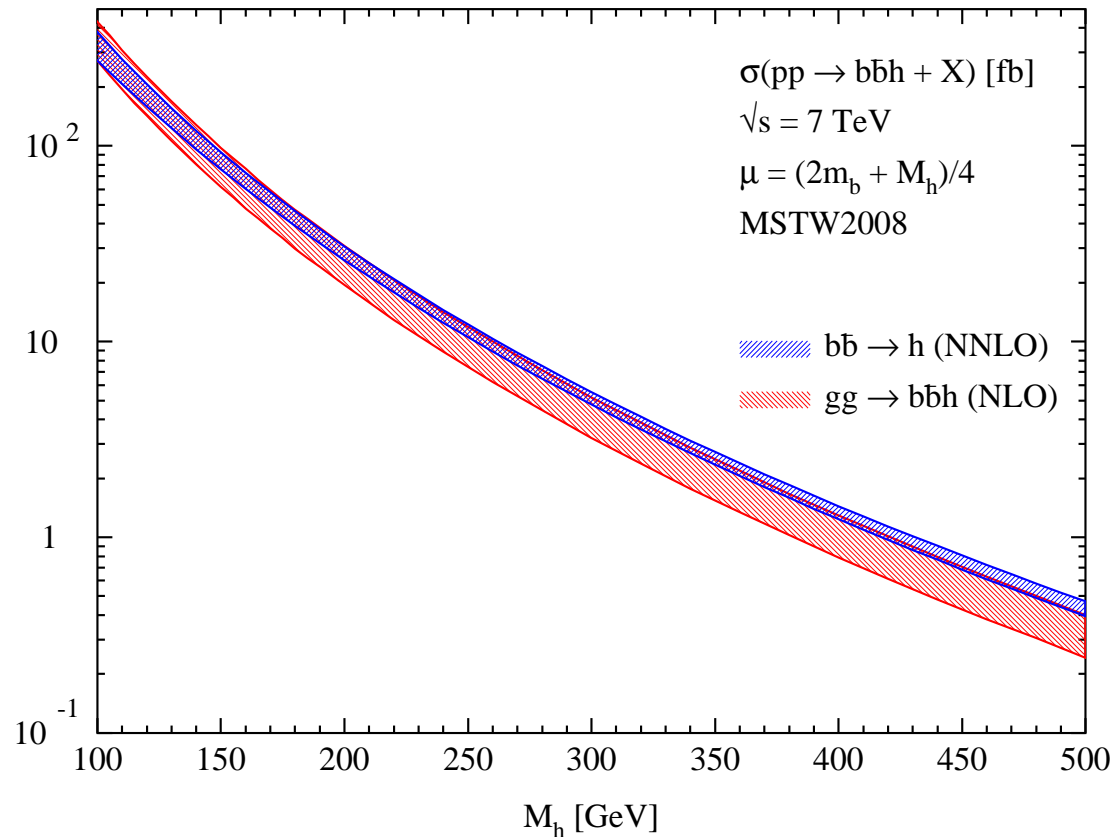
NLO

exact $g \rightarrow b\bar{b}$ splitting & mass/off-shell effects
no resummation of $\log M_H^2/m_b^2$ terms



NNLO

massless/on-shell b 's, no p_{Tb}
resummation of $\log M_H^2/m_b^2$ terms



Santander matching:

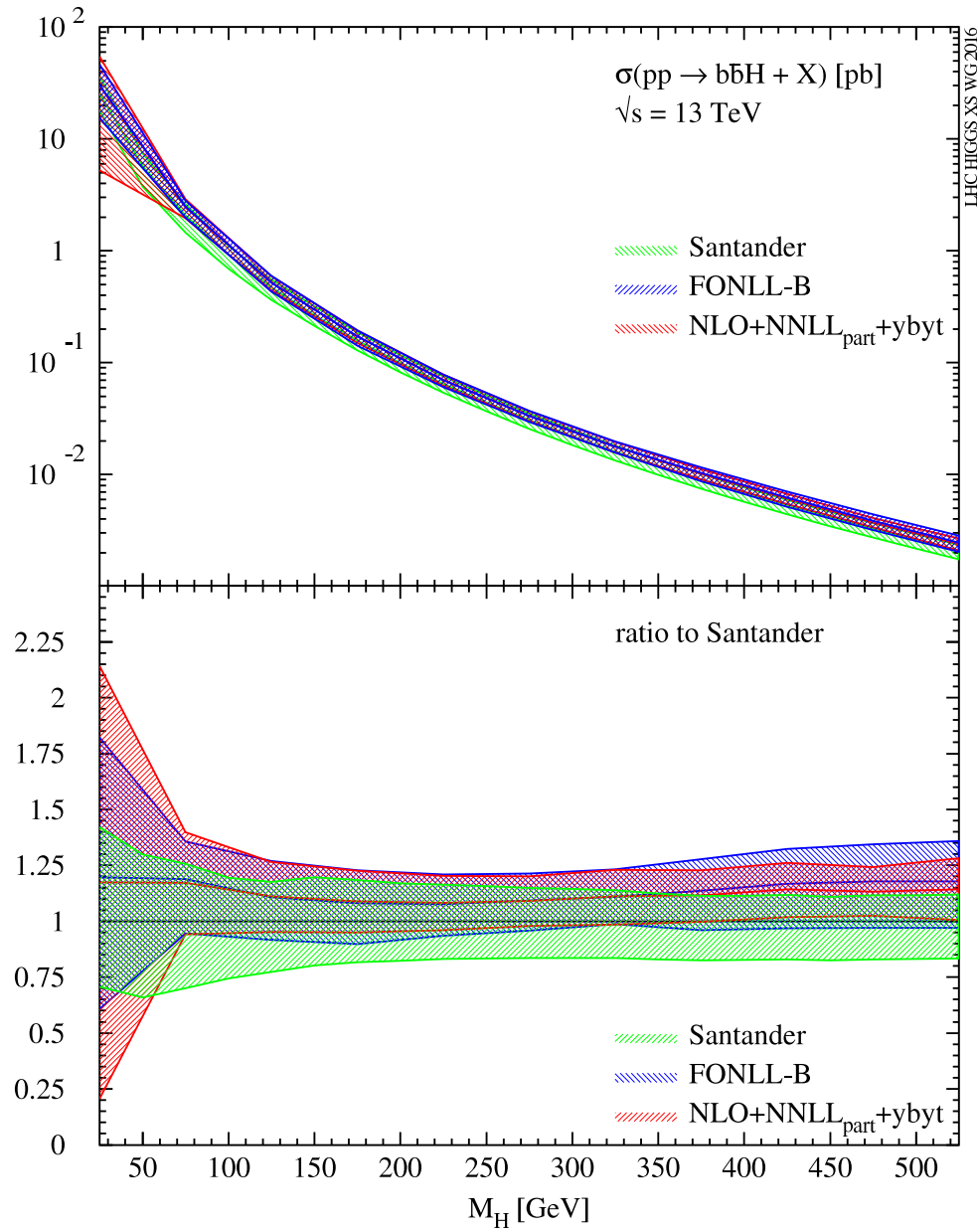
$$\sigma = \frac{\sigma^{4FS} + w\sigma^{5FS}}{1 + w}$$

$$w = \log \frac{M_H}{m_b} - 2$$

Harlander, Krämer, Schumacher

Dittmaier, Krämer, S. Dawson, Jackson, Reina, Wackerath
Harlander, Kilgore

matching



Bonvini, Papanastasiou, Tackmann

Forte, Napoletano, Ubiali

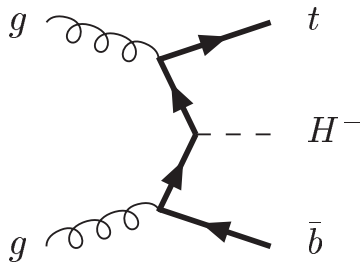
	M_A	M_H [GeV]	δ_{QCD}^A	δ_{SUSY}^A	$\delta_{SUSYrem}^A$	δ_{QCD}^H	δ_{SUSY}^H	$\delta_{SUSYrem}^H$
7 TeV	100	113.9	0.23	-0.30	0.4×10^{-4}	0.27	-0.38	0.3×10^{-4}
	200	200	0.38	-0.30	2.9×10^{-4}	0.39	-0.30	5.8×10^{-4}
	300	300	0.46	-0.30	6.7×10^{-4}	0.47	-0.30	9.3×10^{-4}
	400	400	0.53	-0.30	1.3×10^{-3}	0.53	-0.30	1.5×10^{-3}
	500	500	0.57	-0.30	2.0×10^{-3}	0.59	-0.30	2.2×10^{-3}
14 TeV	100	113.9	0.14	-0.30	0.4×10^{-4}	0.17	-0.38	0.5×10^{-4}
	200	200	0.28	-0.30	2.7×10^{-4}	0.29	-0.30	5.7×10^{-4}
	300	300	0.37	-0.30	6.5×10^{-4}	0.39	-0.30	9.3×10^{-4}
	400	400	0.45	-0.30	1.2×10^{-3}	0.45	-0.30	1.5×10^{-3}
	500	500	0.50	-0.30	2.1×10^{-3}	0.49	-0.30	2.3×10^{-3}

	$\text{tg}\beta$	M_A	M_H [GeV]	δ_{SUSY}^A	$\delta_{SUSYrem}^A$	δ_{SUSY}^H	$\delta_{SUSYrem}^H$
7 TeV	3	200	209.7	-0.04	2.1×10^{-4}	-0.04	5.7×10^{-4}
	5	200	204.0	-0.06	2.4×10^{-4}	-0.06	5.3×10^{-4}
	7	200	202.1	-0.08	2.5×10^{-4}	-0.09	3.9×10^{-4}
	10	200	200.9	-0.12	2.5×10^{-4}	-0.12	3.8×10^{-4}
	20	200	200.1	-0.21	2.6×10^{-4}	-0.21	4.4×10^{-4}
	30	200	200.0	-0.30	2.9×10^{-4}	-0.30	5.8×10^{-4}
14 TeV	3	200	209.7	-0.04	2.0×10^{-4}	-0.04	7.2×10^{-4}
	5	200	204.0	-0.06	2.2×10^{-4}	-0.06	5.0×10^{-4}
	7	200	202.1	-0.08	2.4×10^{-4}	-0.09	4.4×10^{-4}
	10	200	200.9	-0.12	2.5×10^{-4}	-0.12	4.1×10^{-4}
	20	200	200.1	-0.21	2.7×10^{-4}	-0.21	4.4×10^{-4}
	30	200	200.0	-0.30	2.7×10^{-4}	-0.30	5.7×10^{-4}

(vi) $pp \rightarrow t\bar{b}H^- + X$

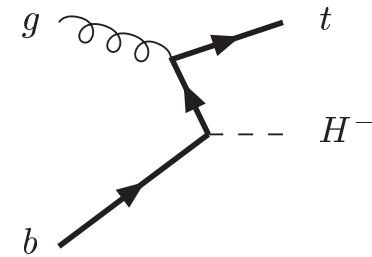
- $M_{H^\pm} < m_t - m_b$: $\sigma_{t\bar{b}H^-} = \sigma_{t\bar{t}} \times BR(\bar{t} \rightarrow \bar{b}H^-)$
- $M_{H^\pm} \sim m_t - m_b$: new NLO calculation
- $M_{H^\pm} > m_t - m_b$:

Degrande, Frederix, Wiesemann, Zaro



NLO

exact $g \rightarrow b\bar{b}$ splitting & mass/off-shell effects
no resummation of $\log M_{H^\pm}^2/m_b^2$ terms

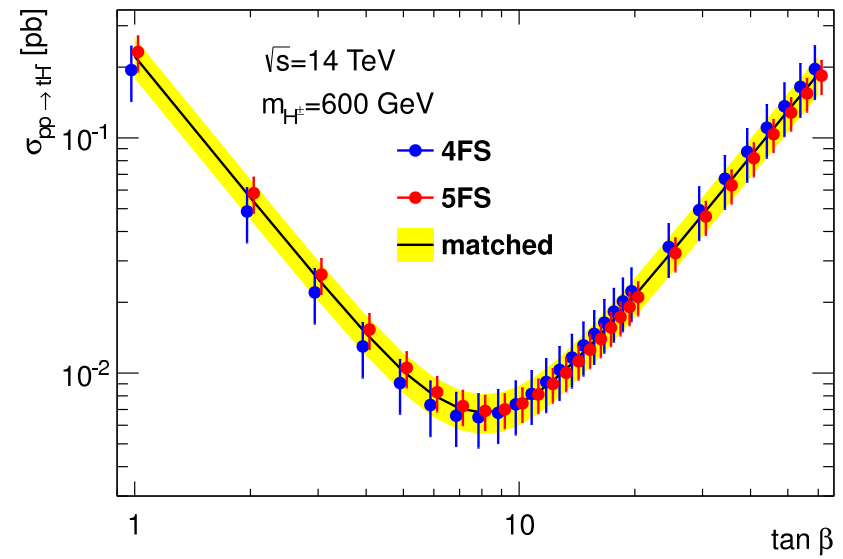
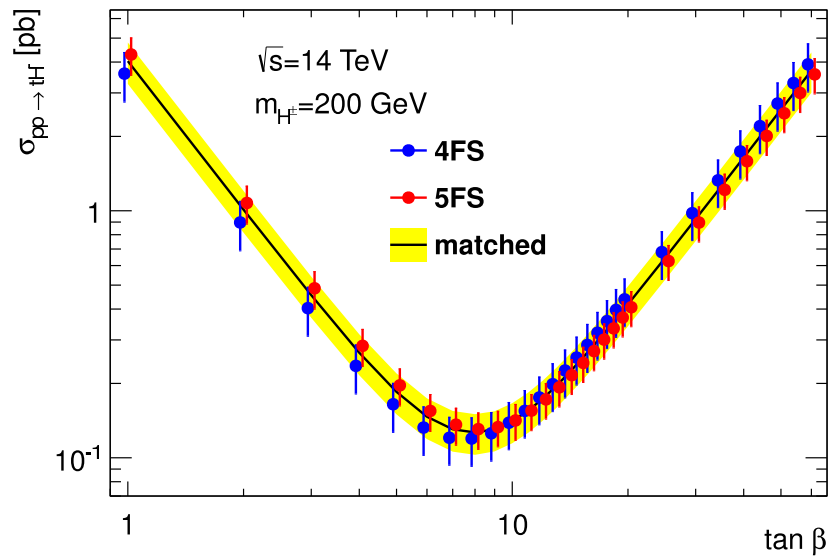


NLO

massless/on-shell b 's, no p_{Tb}
resummation of $\log M_{H^\pm}^2/m_b^2$ terms

- Santander matching

minimum: $\text{tg}\beta \sim \sqrt{\frac{m_t}{\bar{m}_b}} \sim 8$



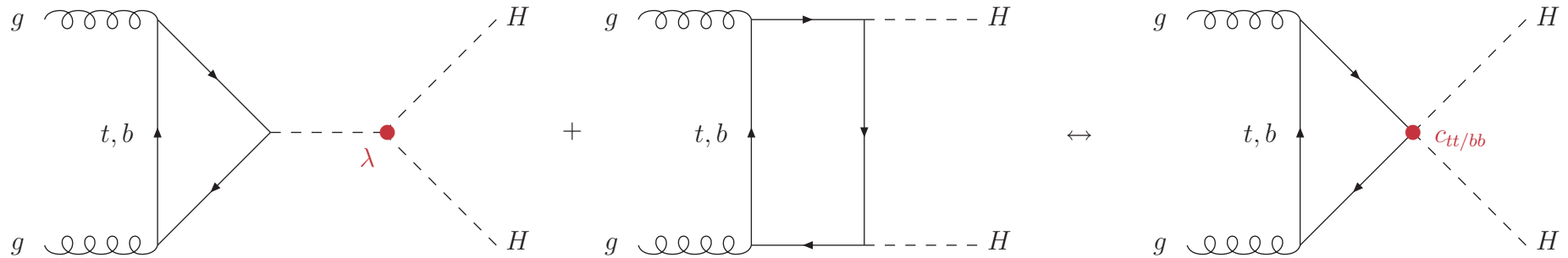
Dittmaier, Krämer, S., Walser
 Plehn
 Flechl, Klees, Krämer, Spira, Ubiali

- analogous for charged Higgs: $\tilde{g}_b^{H^\pm} = \frac{\text{tg}\beta}{1 + \Delta_b} \left(1 - \frac{\Delta_b}{\text{tg}^2\beta} \right)$

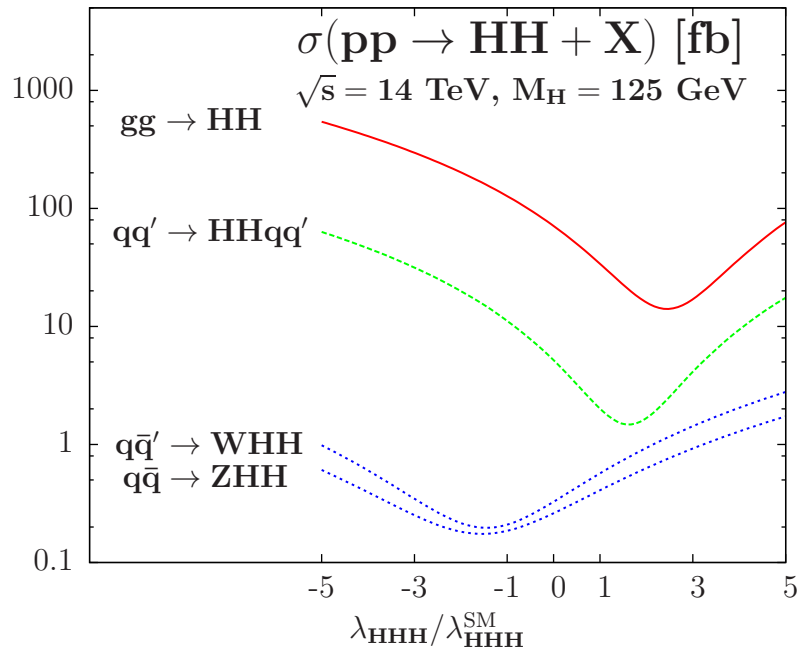
$$\sigma_{NLO} = \sigma_{LO} \Big|_{g_b^{H^\pm} \rightarrow \tilde{g}_b^{H^\pm}} \times \left\{ 1 + \delta_{QCD} + \delta_{SQCD}^{rem} \right\}$$

$\text{tg}\beta$	δ_{SUSY}^{rem} [%]
3	-5.7%
5	-7.9%
10	-4.8%
30	-0.13%

$gg \rightarrow HH$



- threshold region: sensitive to λ
- large M_{HH} : sensitive to $c_{tt/bb}$ [e.g. boosted Higgs pairs]

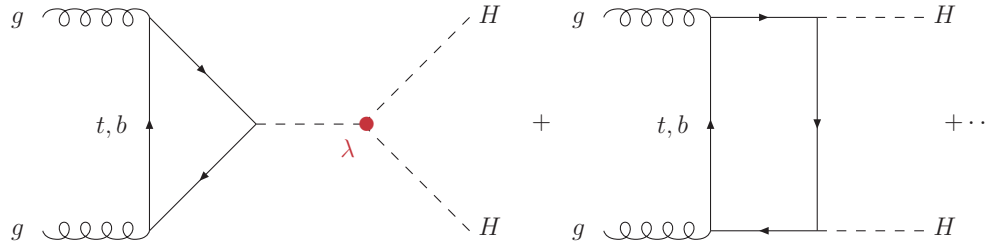


$$gg \rightarrow HH : \frac{\Delta\sigma}{\sigma} \sim -\frac{\Delta\lambda}{\lambda}$$

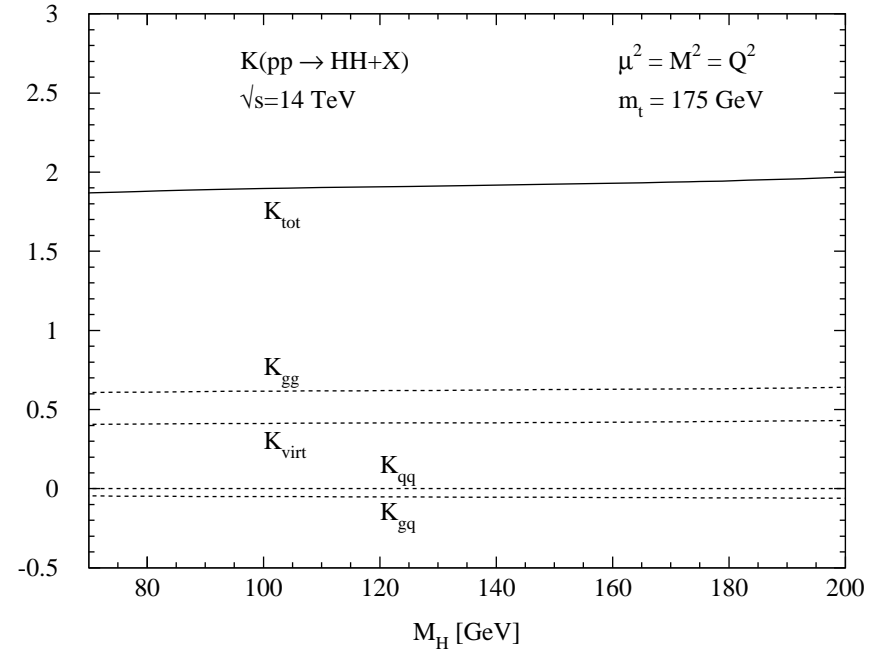
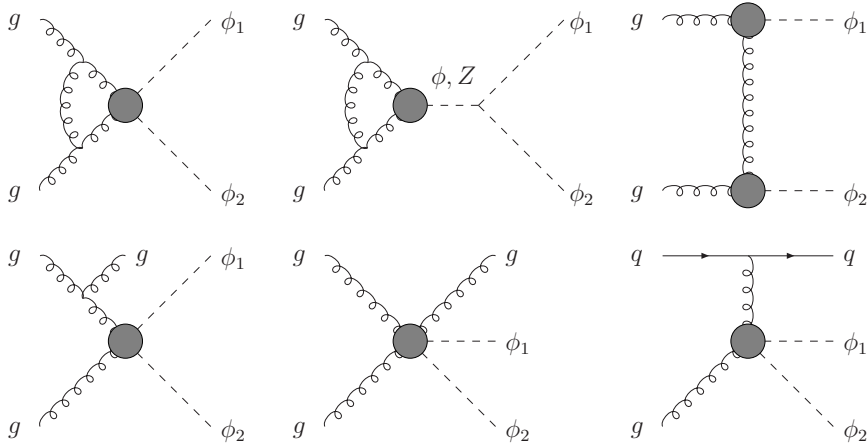
[decreasing with M_{HH}^2]

$gg \rightarrow HH$

SM



- third generation dominant $\rightarrow t, b$
- 2-loop QCD corrections: $\sim 90 - 100\%$
 $[M_H^2 \ll 4m_t^2, \quad \mu = M_{HH}]$



Dawson, Dittmaier, S.

- 2-loop QCD corrections:

$$\sigma = \sigma_0 + \frac{\sigma_1}{m_t^2} + \dots + \frac{\sigma_4}{m_t^8}$$

Grigo, Hoff, Melnikov, Steinhauser

- NLO mass effects @ NLO in real corrections: $\sim -10\%$

Frederix, Frixione, Hirschi, Maltoni, Mattelaer, Torrielli, Vryonidou, Zaro

→ sizeable virtual mass effects

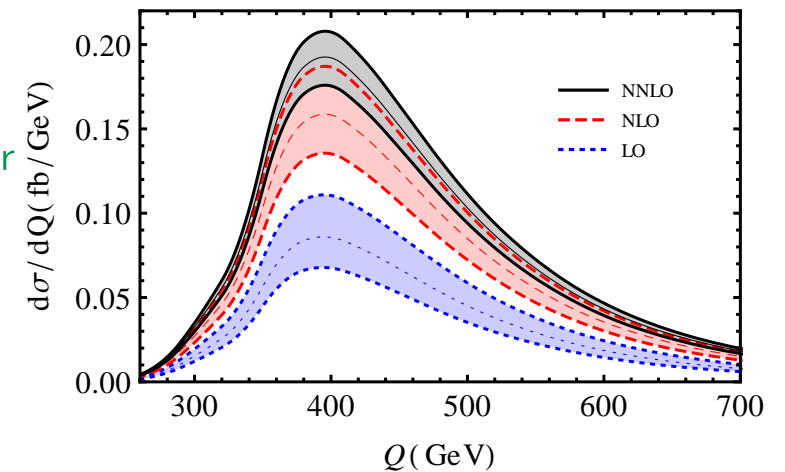
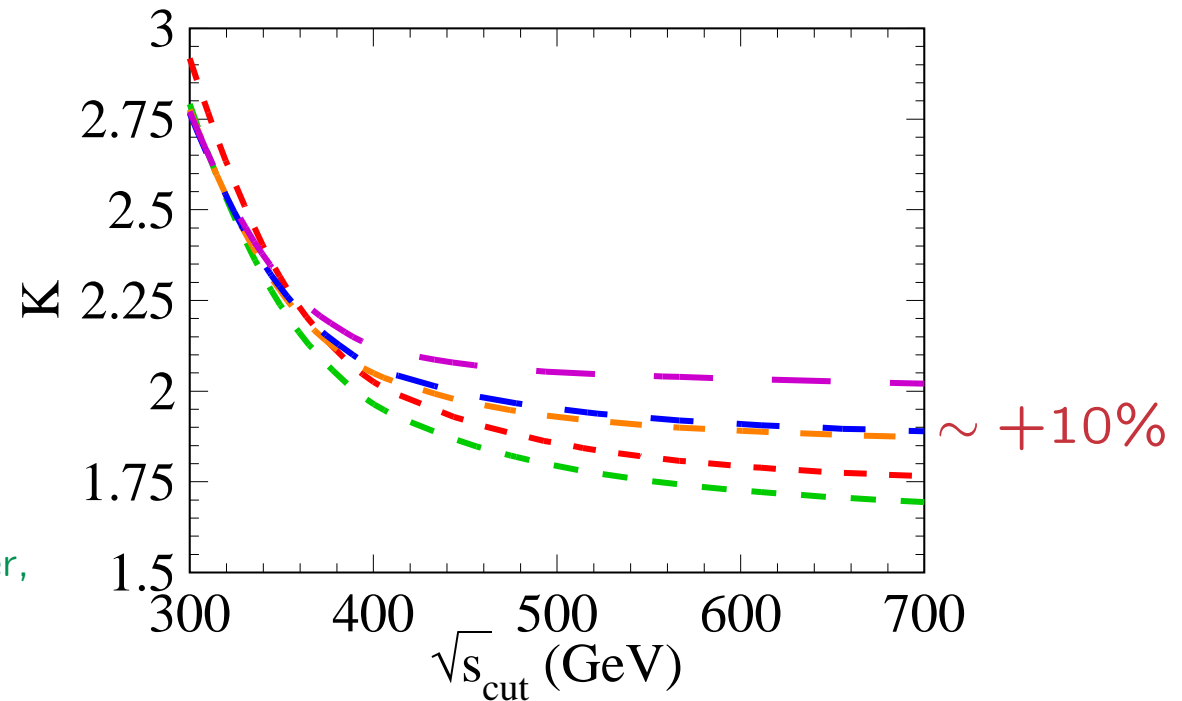
- NNLO QCD corrections: $\sim 20\%$

$$[M_H^2 \ll 4m_t^2]$$

de Florian, Mazzitelli
Grigo, Melnikov, Steinhauser

- soft gluon resummation: $\sim 10\%$

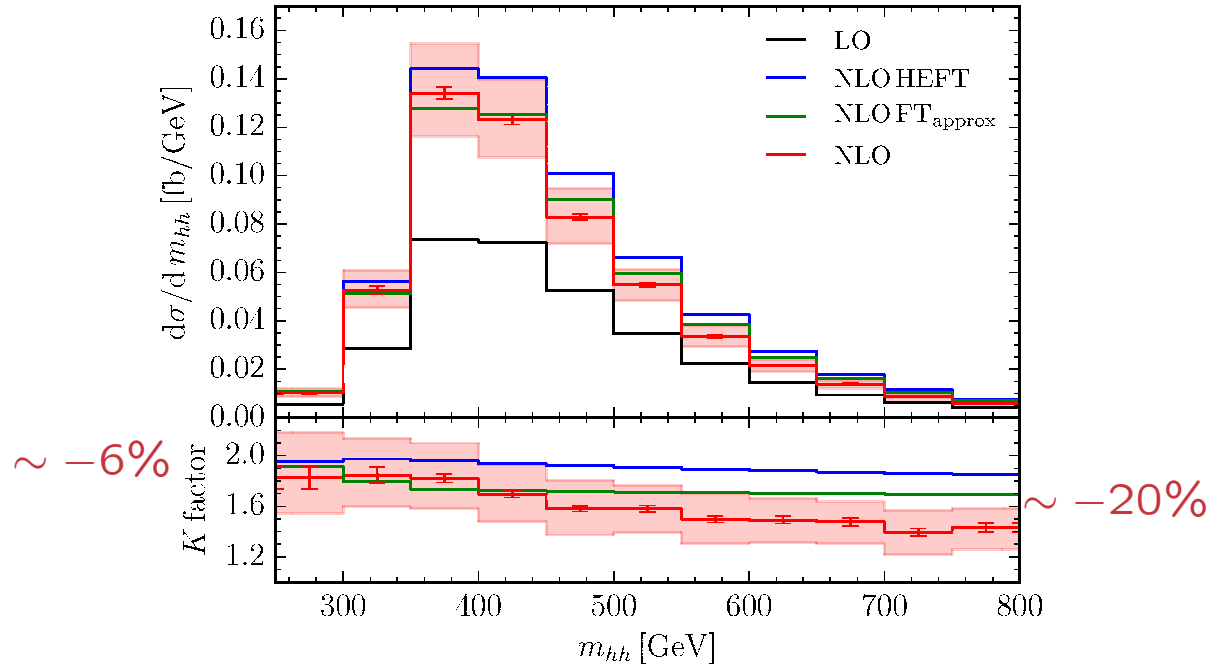
$$[M_H^2 \ll 4m_t^2]$$



Shao, Li, Li, Wang
de Florian, Mazzitelli

Full NLO calculation: top only

Numerical integration, sector decomposition, contour deformation



Borowka, Greiner, Heinrich, Jones, Kerner, Schlenk, Schubert, Zirke
Baglio, Campanario, Glaus, Mühlleitner, S., Streicher (in preparation)

• 13 TeV:

$$\sigma_{NLO} = 27.80(8)^{+13.8\%}_{-12.8\%} \text{ fb}$$
$$\sigma_{NLO}^{HEFT} = 32.22^{+18\%}_{-15\%} \text{ fb}$$

⇒ -13.7% mass effects

IV CONCLUSIONS

- Higgs boson searches/studies at LHC belong to major endeavours
- most (SUSY-)QCD and -elw. corrections known $\rightarrow \Delta \lesssim 10 - 15\%$
@ LHC
- several dedicated HO-tools available for SM, MSSM [NMSSM,...]
- important to develop NLO event generators [\leftarrow backgrounds]

BACKUP SLIDES

τ -phobic scenario

[scale = 1 TeV]

$$\begin{aligned}
 m_t &= 173.2 \text{ GeV} \\
 \text{tg}\beta &= 30 \\
 M_{\tilde{Q}} &= 1.5 \text{ TeV} \\
 M_{\tilde{g}} &= 1.5 \text{ TeV} \\
 M_2 &= 200 \text{ GeV} \\
 A_b = A_t &= 4.417 \text{ TeV} \quad [X_t = 2.9 M_{\tilde{Q}}] \\
 \mu &= 2 \text{ TeV} \\
 M_{\tilde{\ell}_3} &= 500 \text{ GeV}
 \end{aligned}$$

$$\begin{aligned}
 m_{\tilde{t}_1} &= 1.318 \text{ TeV} & m_{\tilde{t}_2} &= 1.726 \text{ TeV} \\
 m_{\tilde{b}_1} &= 1.501 \text{ TeV} & m_{\tilde{b}_2} &= 1.565 \text{ TeV}
 \end{aligned}$$

SPS 5

$$\text{tg}\beta = 5$$

$$\mu = 639.8 \text{ GeV}$$

$$A_t = -1671.4 \text{ GeV}$$

$$A_b = -905.6 \text{ GeV}$$

$$m_{\tilde{g}} = 710.3 \text{ GeV}$$

$$m_{\tilde{q}_L} = 535.2 \text{ GeV}$$

$$m_{\tilde{b}_R} = 620.5 \text{ GeV}$$

$$m_{\tilde{t}_R} = 360.5 \text{ GeV}$$

$$\longrightarrow m_{\tilde{t}_1} = 204.1 \text{ GeV}, m_{\tilde{t}_2} = 656.1 \text{ GeV}, m_{\tilde{b}_1} = 533.3 \text{ GeV}, m_{\tilde{b}_2} = 625.2 \text{ GeV}$$