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laboratory for neutron scattering



Paul Scherrer Institut

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A background image showing a water droplet on a surface, creating a colorful interference pattern of concentric rings. The colors range from blue and green to yellow and red.

**introduction to  
reflectometry  
thin films  
and  
hetero structures**

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PSI summer school on condensed matter research

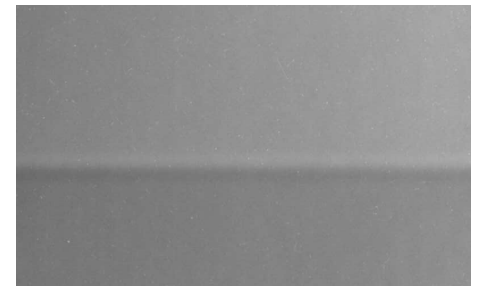
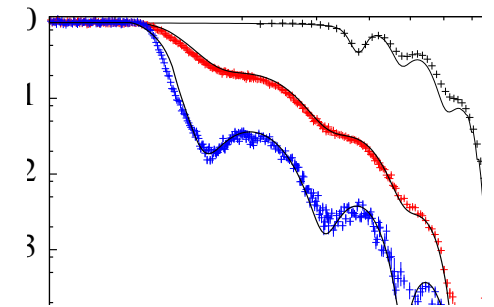
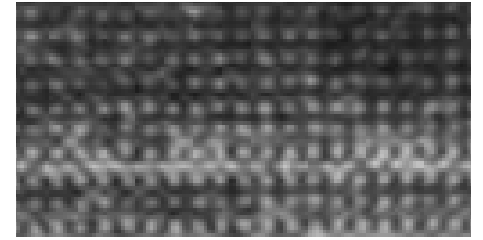
Zug, 11. – 17. August 2012

Imaging Life and Matter - using photons, neutrons and muons

## outline

- heterostructures
  - magnetic layers
  - membrane systems
- reflectometry
  - (few formulae)
- ... derivation
  - (lots of formulae)
- experimental examples
  - Fe/Si
  - FeSi/GaAs interfaces
  - bio-membrane
- relevance for imaging
  - YES, there is some!

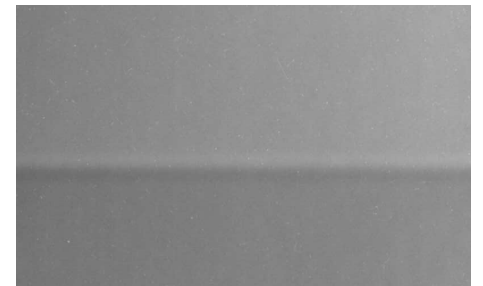
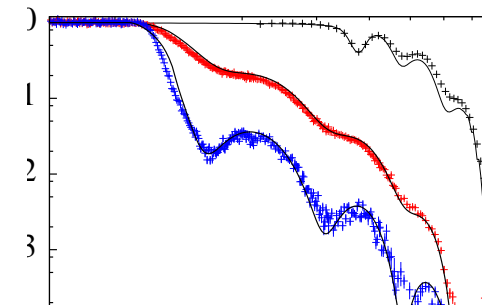
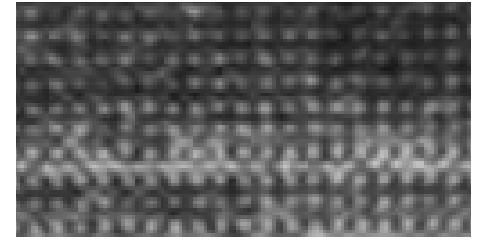
## reflectometry 1



## outline

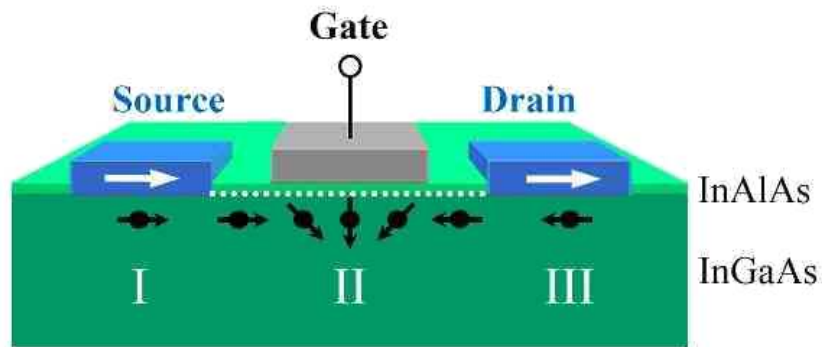
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## reflectometry 2

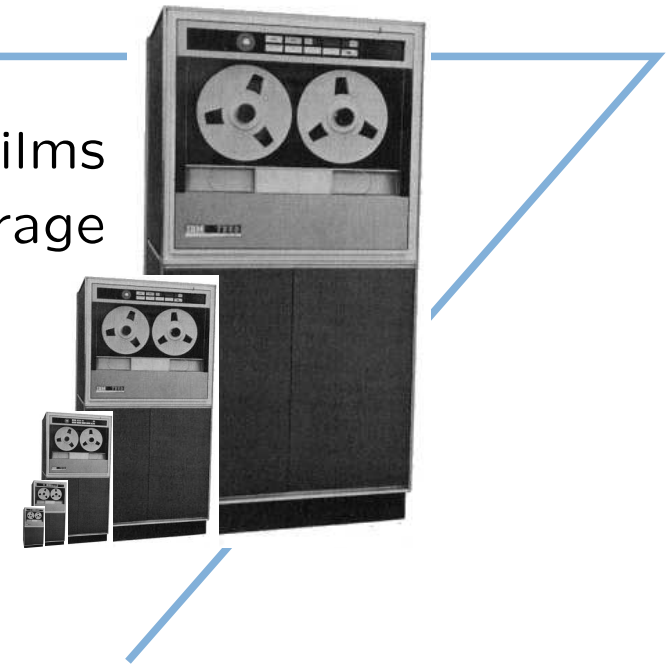


... the damn magnetically dead layers ...

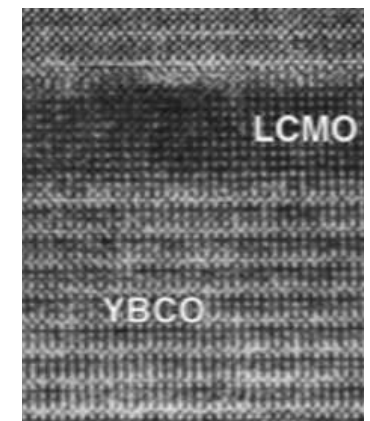
- down-scaling  $\Rightarrow$  thin magnetic films  
e.g. magnetic data storage



- spin polarised electron injection  
e.g. spin-injection in a spin-transistor

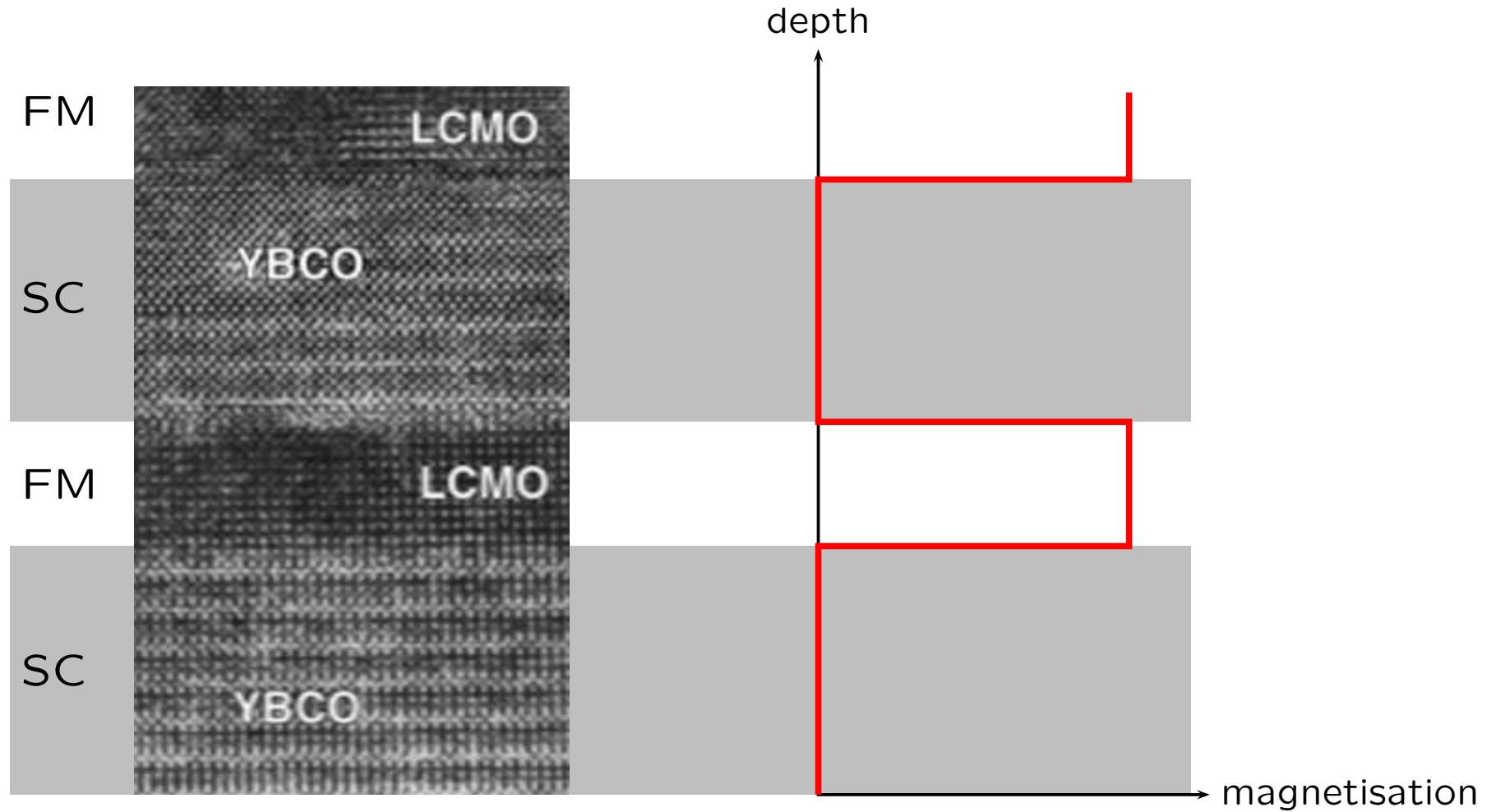


- conflicting properties at interfaces  
e.g. interface  $\frac{\text{ferro} - \text{magnet}}{\text{superconductor}}$



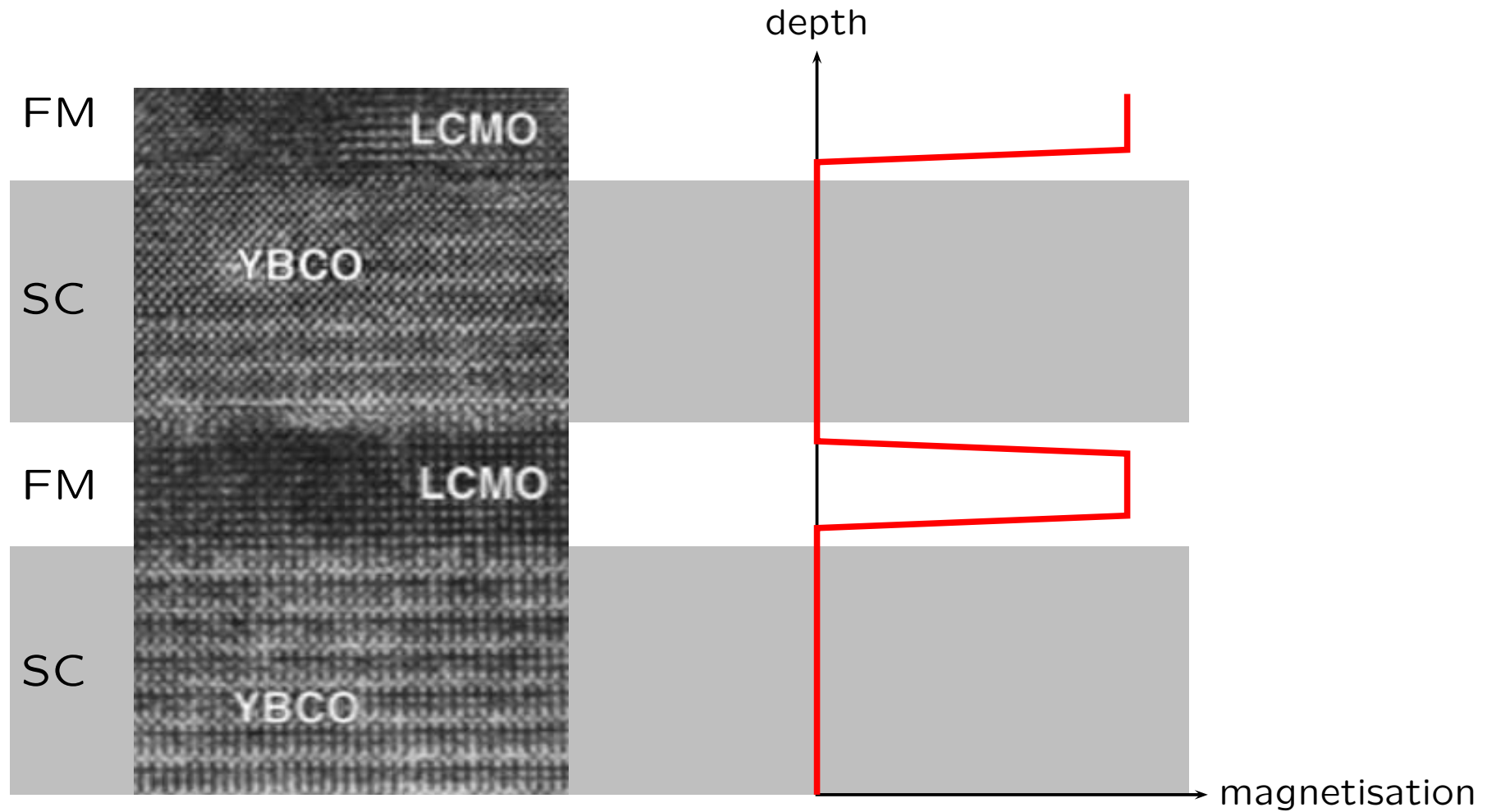
conflict of interests at superconductor / ferromagnet interfaces

(1) no interaction:



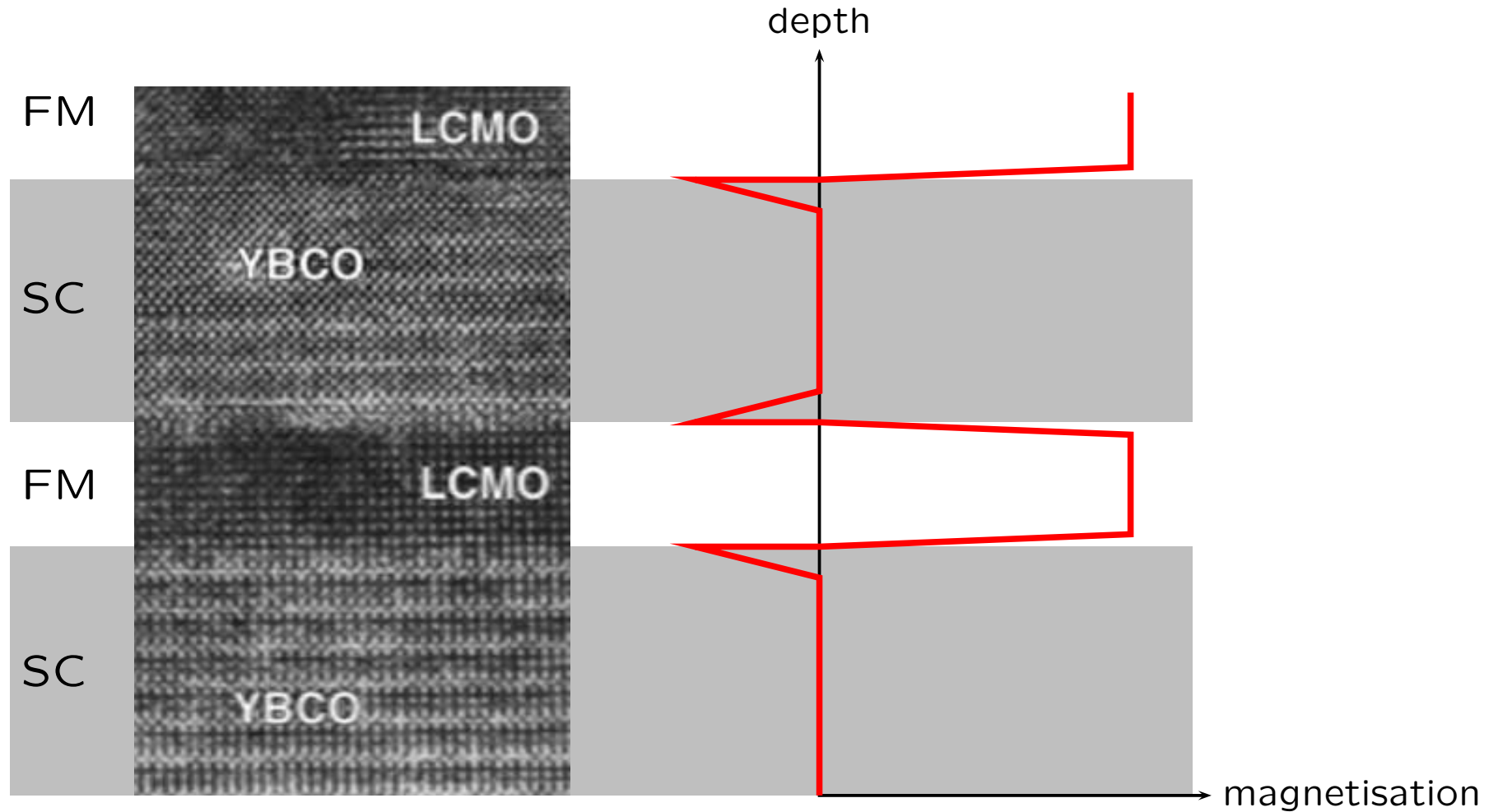
conflict of interests at superconductor / ferromagnet interfaces

(2) suppression of magnetism:



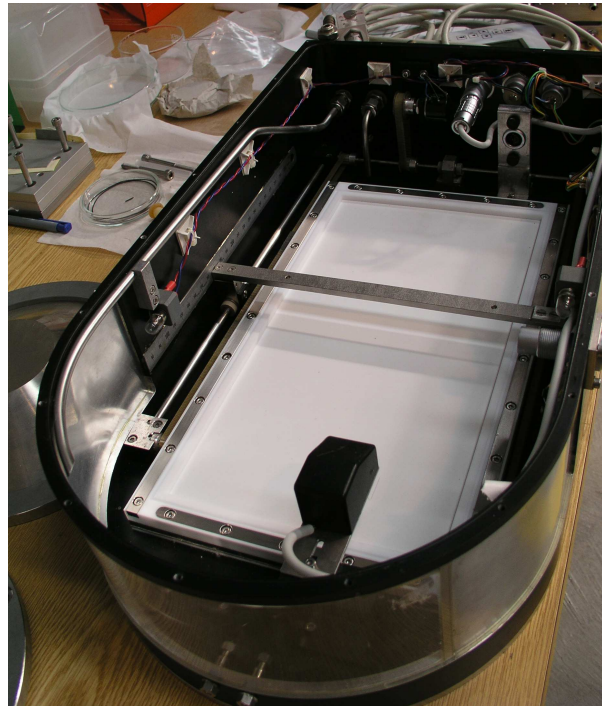
conflict of interests at superconductor / ferromagnet interfaces

(3) reality: induced magnetism within SC!

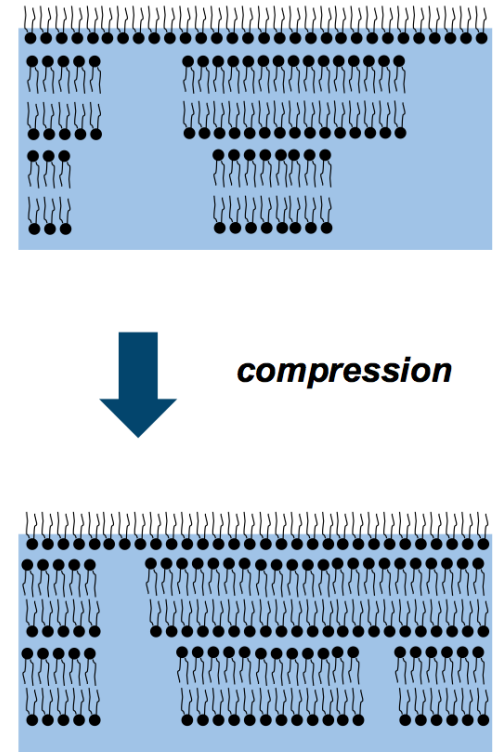


**compression of self-organising polyglycerol-ester films**

model-system for  
foams used for stabilising food products  
e.g. yogurt



trough to investigate  
membranes at the  
liquid/air interface

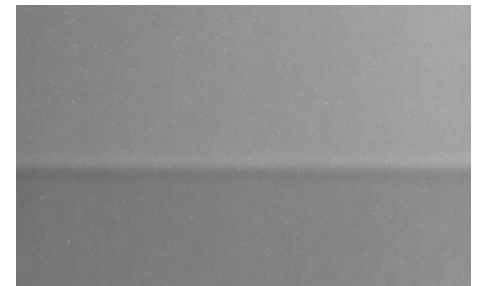
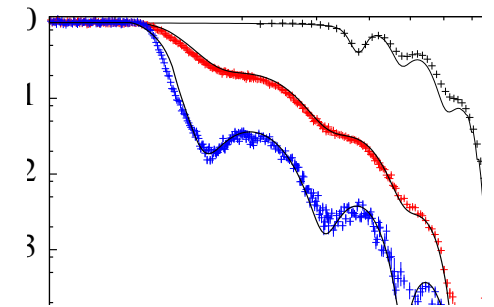
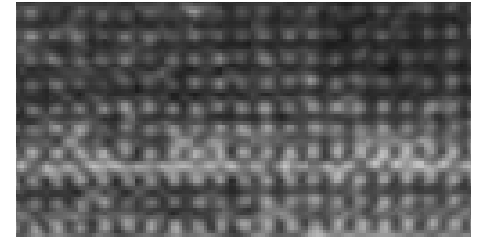




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## reflectometry 8





*flat* surfaces partly reflect light

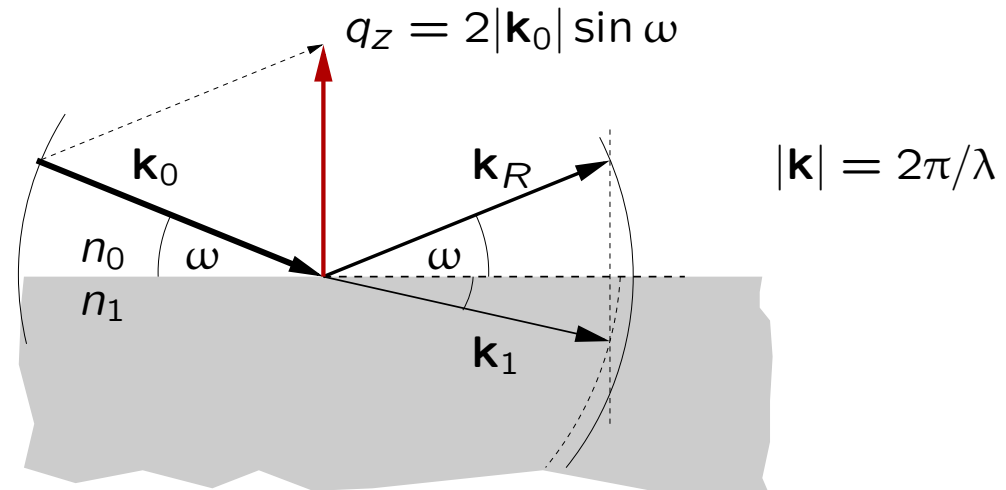
→ picture of the boot

some media also transmit light

→ ground below the water

parallel interfaces

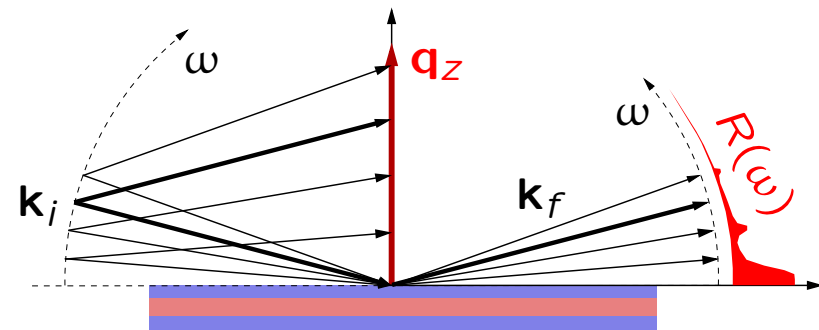
→ colourful soap bubbles



$$R = R(q_z) = R(\lambda, \omega) \quad q_z = 4\pi \frac{\sin \omega}{\lambda}$$

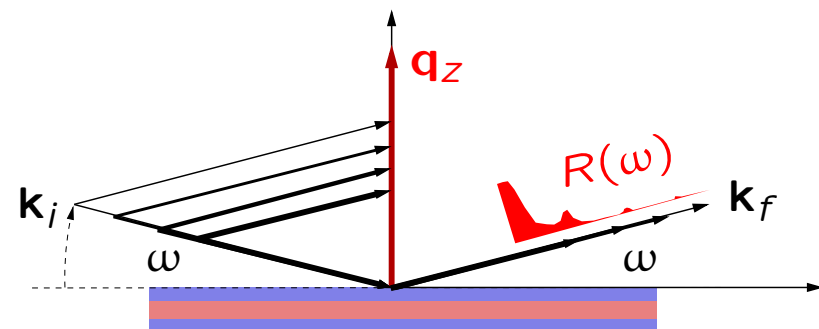
**angle-dispersive set-up**

variation of  $\omega$  with fixed  $\lambda$   
detection under  $2\omega$



**energy-dispersive set-up**

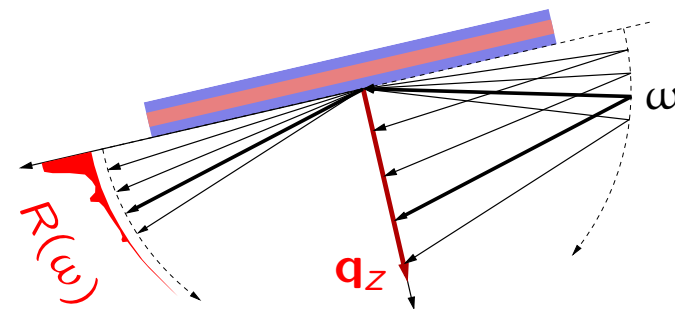
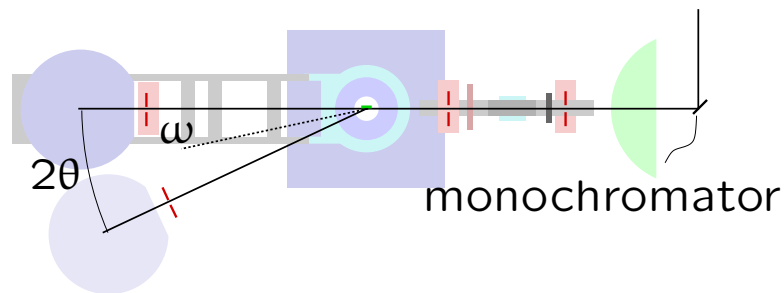
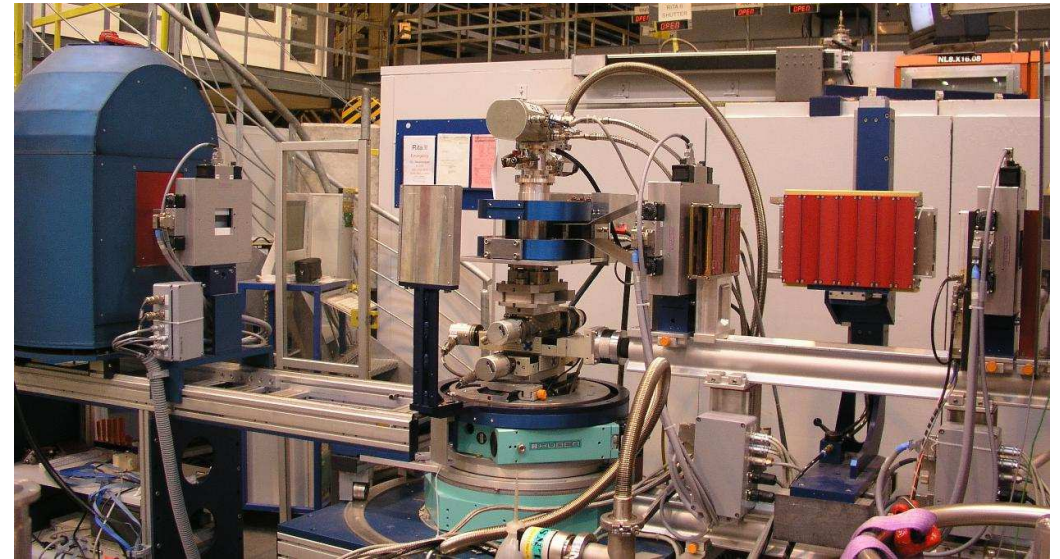
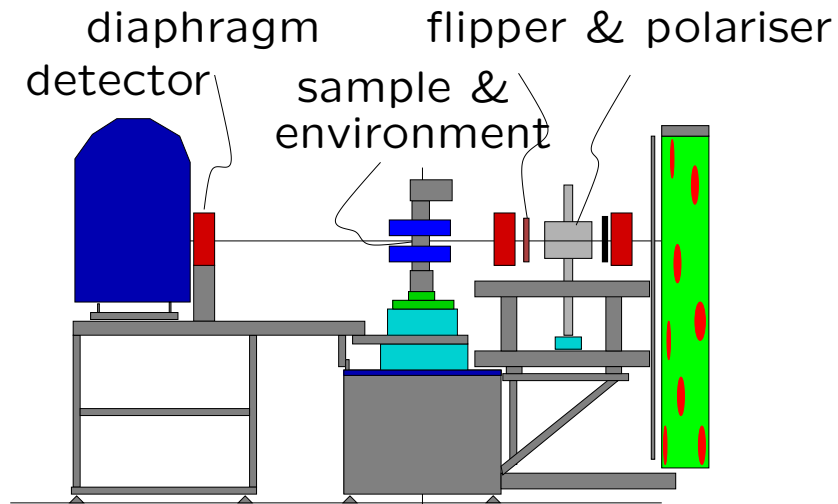
variation of  $\lambda$  with fixed  $\omega$   
detection via time-of-flight



# angle-dispersive set-up

neutron reflectometer

instrument: Morpheus at SINQ



## sample environment

cooling with a  
*closed cycle refrigerator*

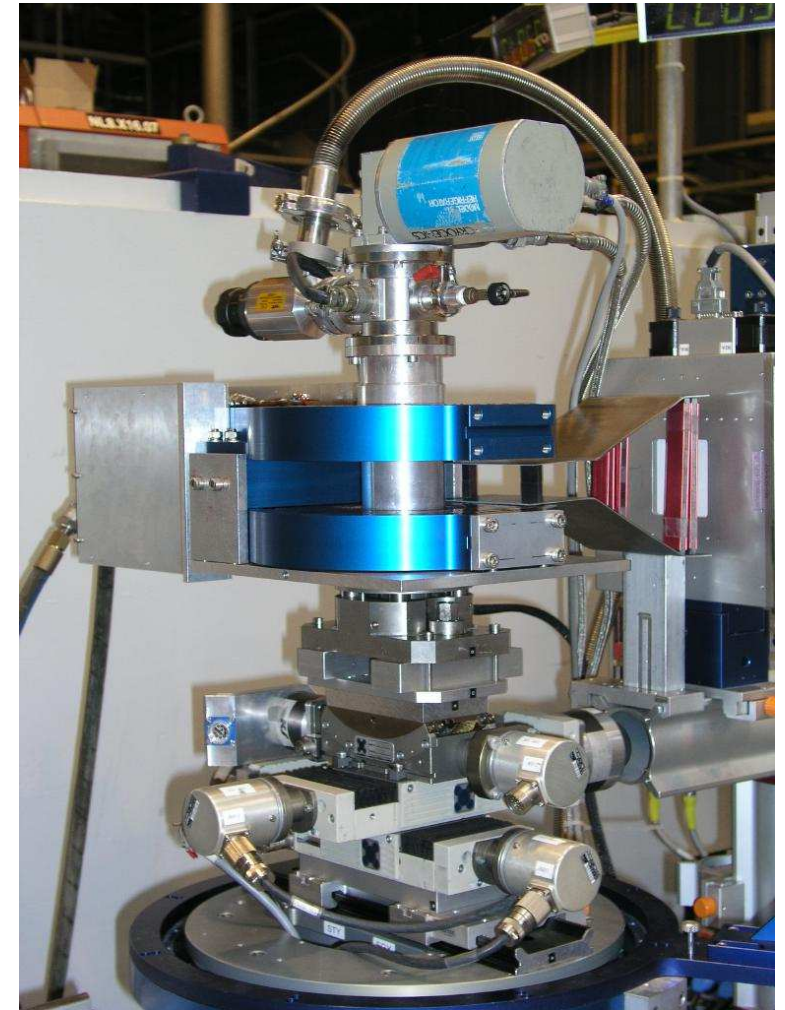
$$8 \text{ K} < T < 300 \text{ K}$$

application of an external magnetic field with  
*Helmholtz coils*       $-1000 \text{ Oe} < H < 1000 \text{ Oe}$

and sample



## reflectometry 12



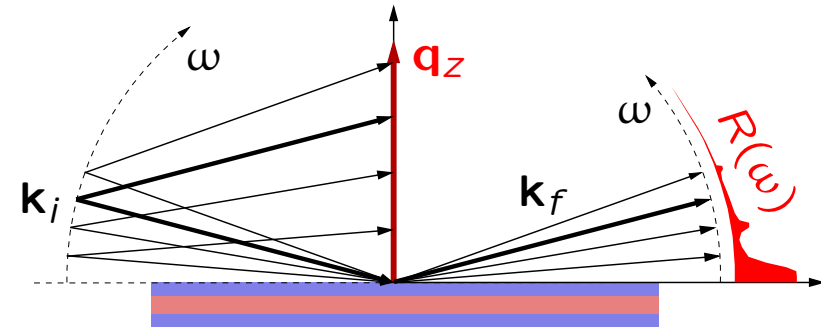
tilt- and  
translation stages  
for alignment

typical quantities:

angular range  $0^\circ \dots 10^\circ$

$\lambda$  range  $3 \text{ \AA} \dots 15 \text{ \AA}$

measurement time  $10 \text{ min} \dots 12 \text{ h}$

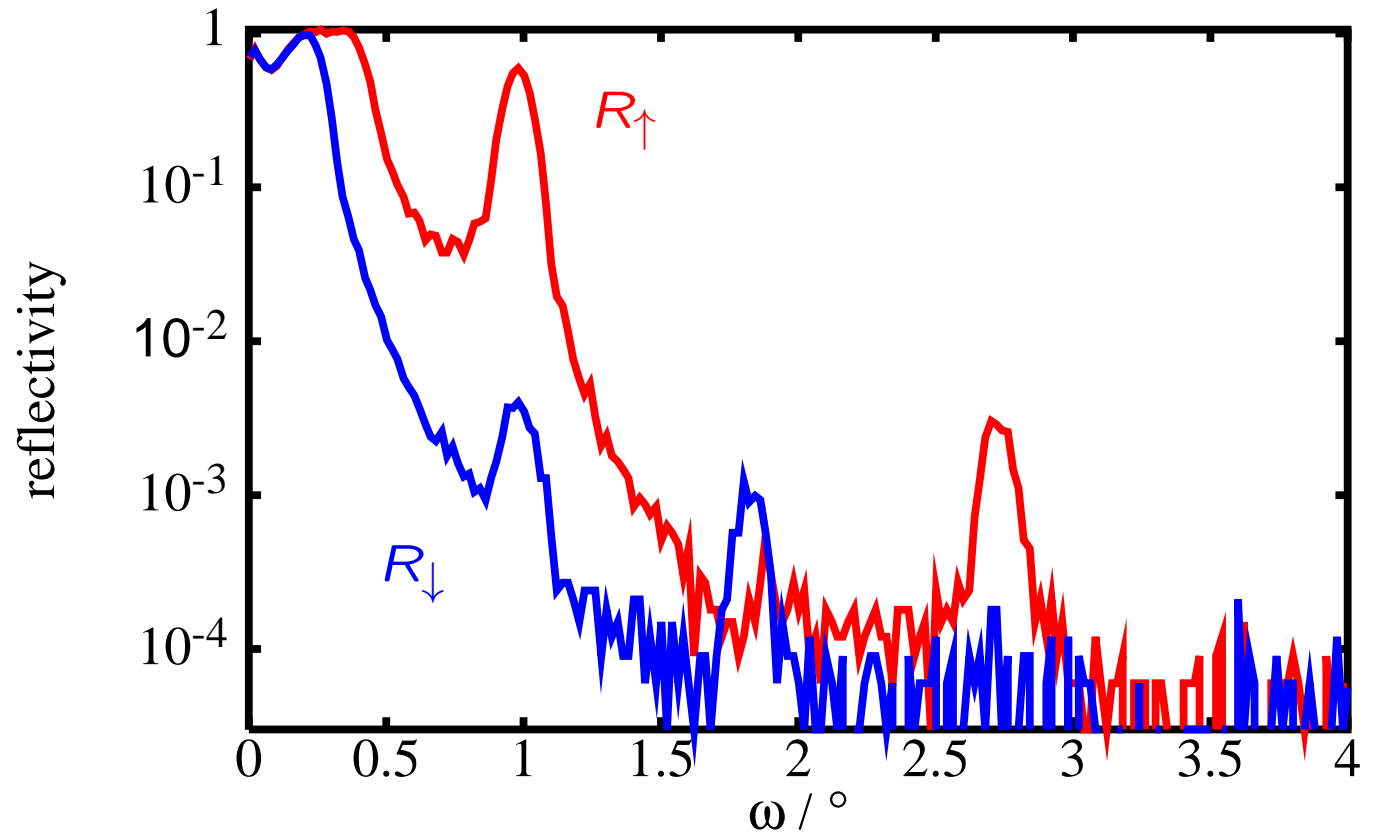


example:

Fe/Si multilayer on glass

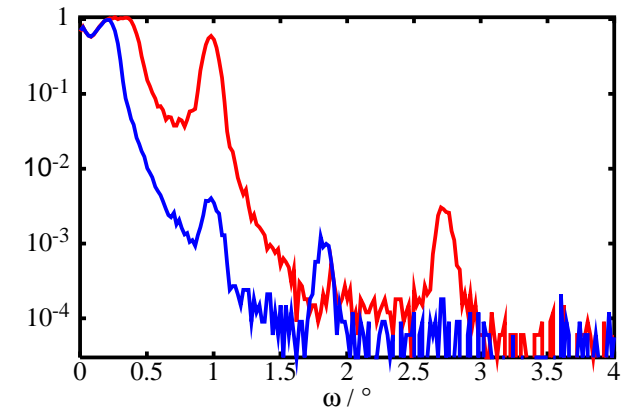
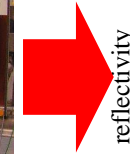
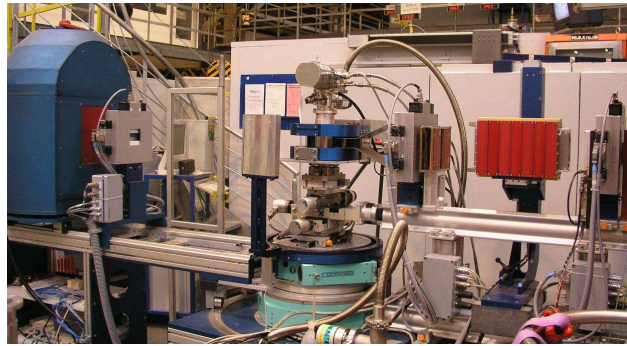
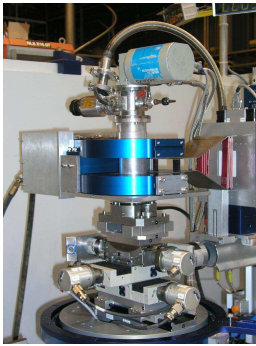
polarised neutrons

1h per spin state

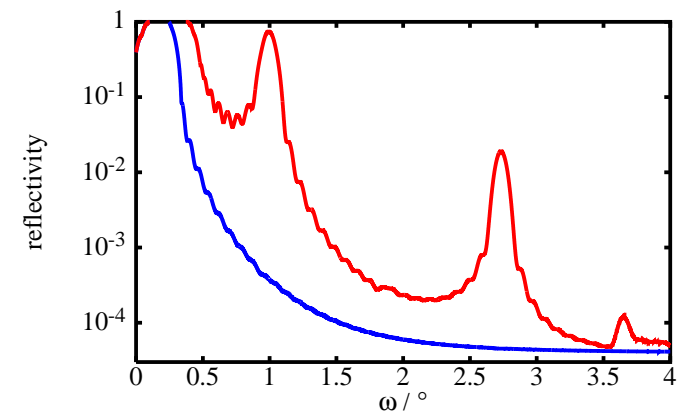
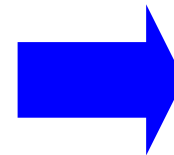
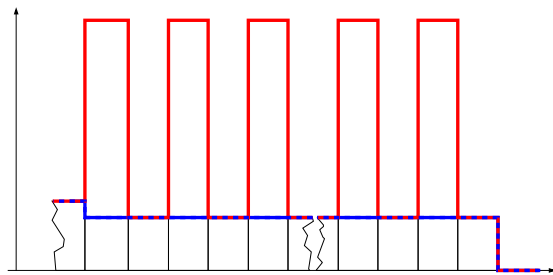


# from the sample to $\rho(z)$

# reflectometry 14



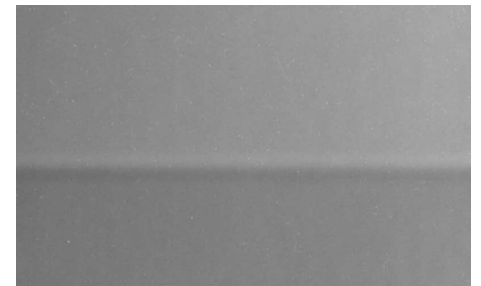
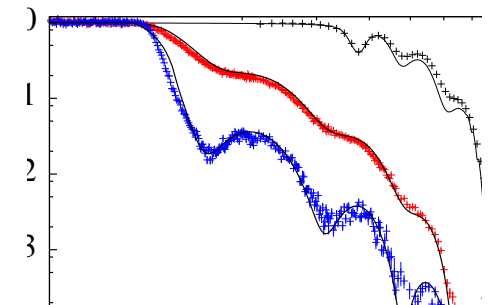
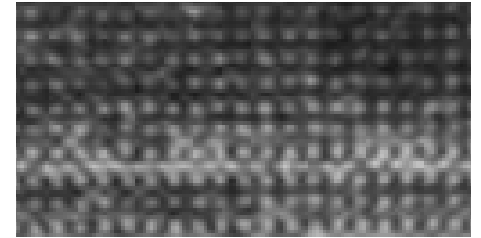
?



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## reflectometry 15







*flat* surfaces partly reflect light  
→ picture of the boot

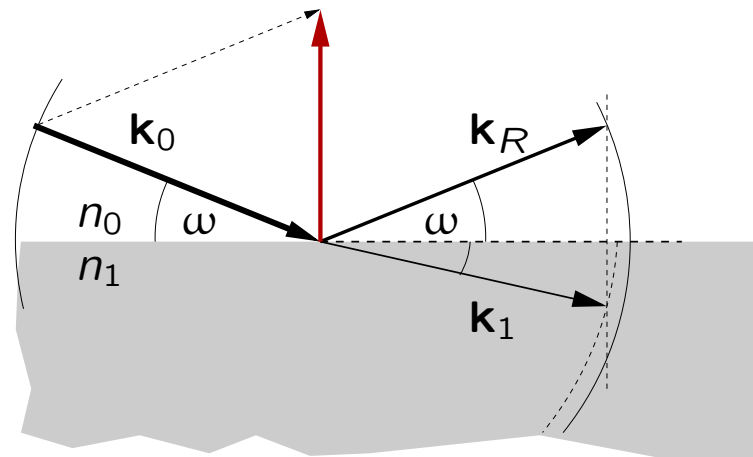
some media also transmit light  
→ ground below the water

parallel interfaces  
→ colourful soap bubbles



scientist's explanation:

- index of refraction,
- Fresnel reflectivity,
- transmittance,
- interference,
- bla bla bla ...



plane wave in a medium  $i$ :

$$\frac{\hbar^2}{2m} \frac{d^2}{dr^2} A e^{ik_i r} + (E - V_i) A e^{ik_i r} = 0$$

$$\frac{\hbar^2}{2m} (-k_i^2) e^{ik_i r} + (E - V_i) e^{ik_i r} = 0$$

$$\Rightarrow k_i^2 = (E - V_i) \frac{2m}{\hbar^2}$$

$$n_i^2 = \frac{k_i^2}{k_0^2}$$

$$= \frac{E - V_i}{E}$$

$$n_i = \sqrt{1 - V_i/E}$$

$$\approx 1 - V_i/2E$$

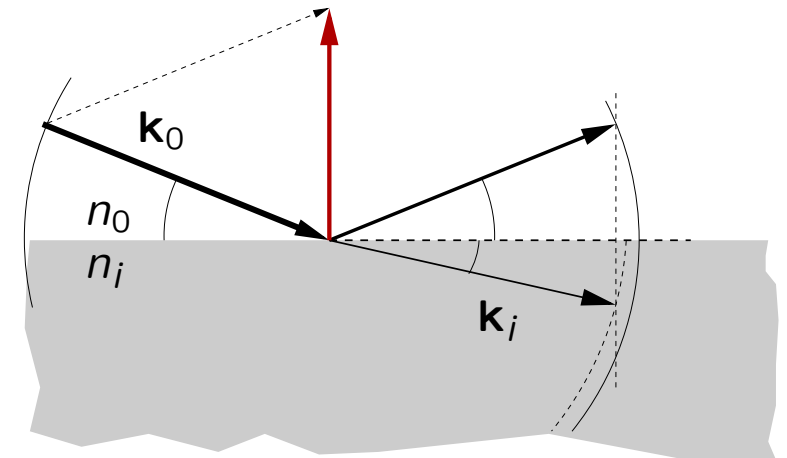
$$:= 1 - \delta$$

by definition

with  $V_0 = 0$  (vacuum)

for  $V_i \ll E$

$n_i - 1 \propto V_i \Rightarrow$  what is  $V_i$ ?



## what is $V_i$ for x-rays?

interaction  $\gamma$  / electron

(off-resonance)

$$\begin{aligned}V^e &= \frac{2\pi\hbar^2}{m_e} \frac{r_e}{\text{vol}} \sum_i Z_i \\ &= \frac{2\pi\hbar^2}{m_e} r_e \rho^e\end{aligned}$$

with

$$\begin{aligned}Z_i &= \text{electron number of atom } i \\ r_e &= \text{electron radius} \\ m_e &= \text{electron mass}\end{aligned}$$

$$\delta = \frac{\lambda^2}{2\pi} r_e \rho^e$$

with absorption: complex  $n$

$$n = 1 - \delta - i\beta$$

at resonances:

$$\delta = \delta(\mathbf{B})$$

## what is $V_j$ for neutrons?

interaction neutron / nucleus  $j$

with  $\lambda \gg r_{\text{nucleus } j}$

$$V_j^{\text{Fermi}} = b_j \frac{2\pi \hbar^2}{m_n} \delta(\mathbf{r})$$

$$V^n = \frac{1}{\text{vol}} \int_j V_j^{\text{Fermi}} d\mathbf{r}$$

$$= \frac{2\pi \hbar^2}{m_n} \frac{1}{\text{vol}} \sum_j b_j$$

$$:= \frac{2\pi \hbar^2}{m_n} \rho^b$$

interaction neutron magnetic moment  $\mu$   
/ magnetic induction  $\mathbf{B}$

$$\mu \uparrow \uparrow \mathbf{B} \Rightarrow V^m = +\mu B$$

$$\mu \uparrow \downarrow \mathbf{B} \Rightarrow V^m = -\mu B$$

$$\mu \perp \mathbf{B} \Rightarrow \text{spin-flip scattering}$$

$$V^m = \mu \mathbf{B}_\perp$$

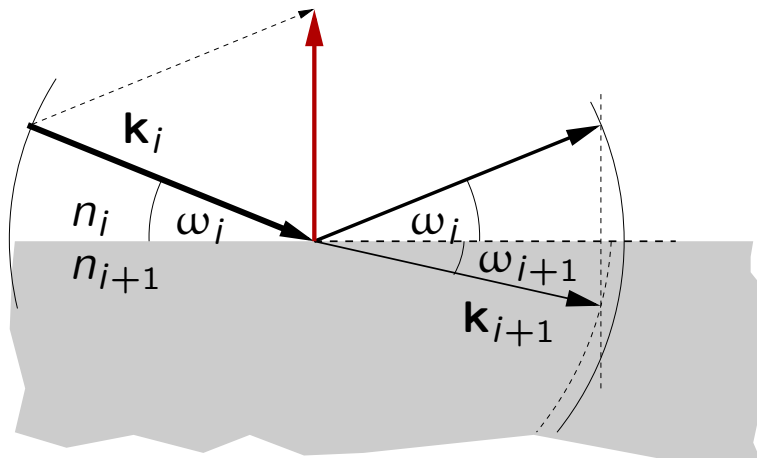
$$:= \frac{2\pi \hbar^2}{m_n} \rho^m$$

$$m_n = \text{neutron mass}$$

## what is the reflected intensity?

assumptions:

- one interface, only
- ideally flat and sharp
- homogeneous in  $x$  and  $y$   
 $\Rightarrow$  only normal ( $z$ ) components are relevant



continuity conditions for a plane wave impinging on the interface  $i, i + 1$ :

$$\Psi_{z,i} = \Psi_{z,i+1}$$

$$\frac{d}{dz}\Psi_{z,i} = \frac{d}{dz}\Psi_{z,i+1}$$

with

$$\Psi_{z,j} = A_j^\uparrow e^{ik_{z,j}z} + A_j^\downarrow e^{-ik_{z,j}z}$$

$$\begin{aligned} k_{z,j} &= k_j \sin \omega_j \\ &= n_j k_0 \sin \omega_j \end{aligned}$$

reflectance

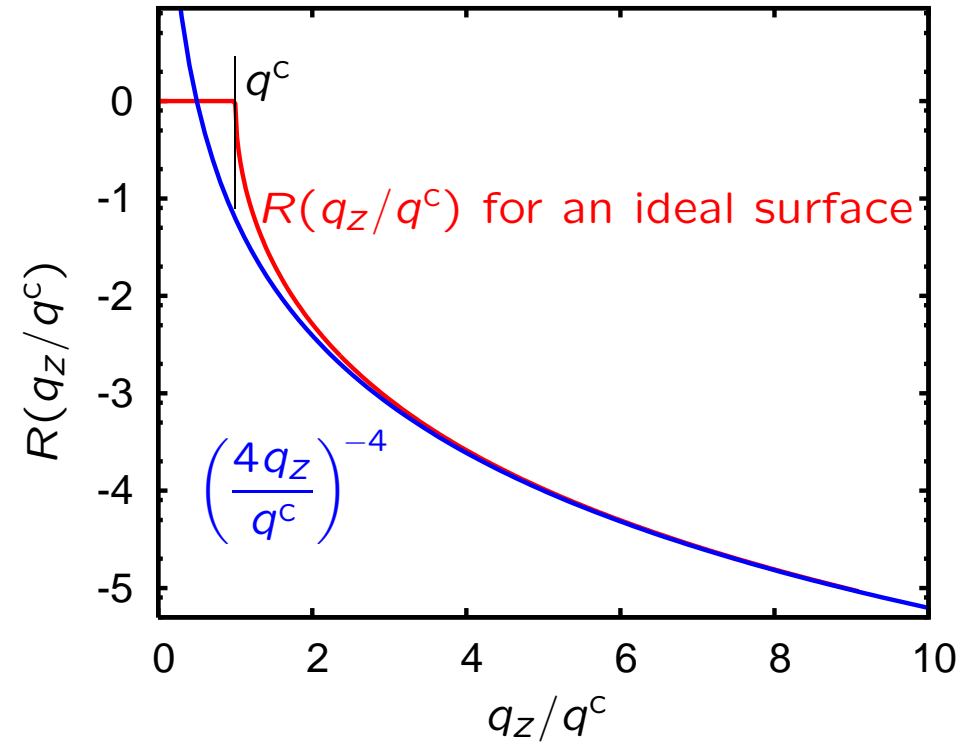
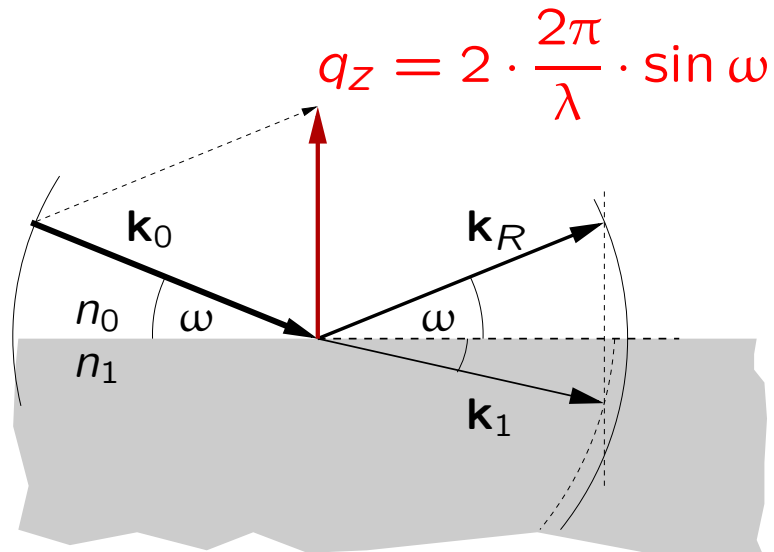
$$\begin{aligned} r_{i,i+1} &= \frac{A_i^\uparrow}{A_i^\downarrow} \\ &\vdots \\ &= \frac{n_i \sin \omega_i - n_{i+1} \sin \omega_{i+1}}{n_i \sin \omega_i + n_{i+1} \sin \omega_{i+1}} \end{aligned}$$

reflectance for  $\omega_{i+1} > 0$

$$r_{i,i+1} = \frac{n_i \sin \omega_i - n_{i+1} \sin \omega_{i+1}}{n_i \sin \omega_i + n_{i+1} \sin \omega_{i+1}}$$

transmittance for  $\omega_{i+1} > 0$

$$t_{i,i+1} = \frac{2 n_i \sin \omega_i}{n_i \sin \omega_i + n_{i+1} \sin \omega_{i+1}}$$



air/solid interface for  $q_z > q^c$

$$r_{0,1} = \frac{1 - \sqrt{1 - (q^c/q_z)^2}}{1 + \sqrt{1 - (q^c/q_z)^2}}$$

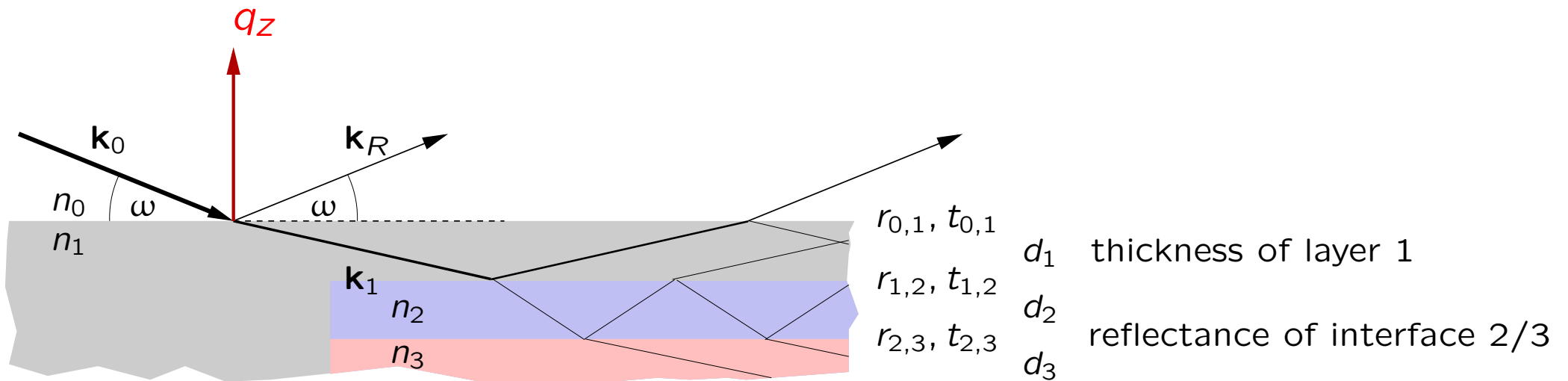
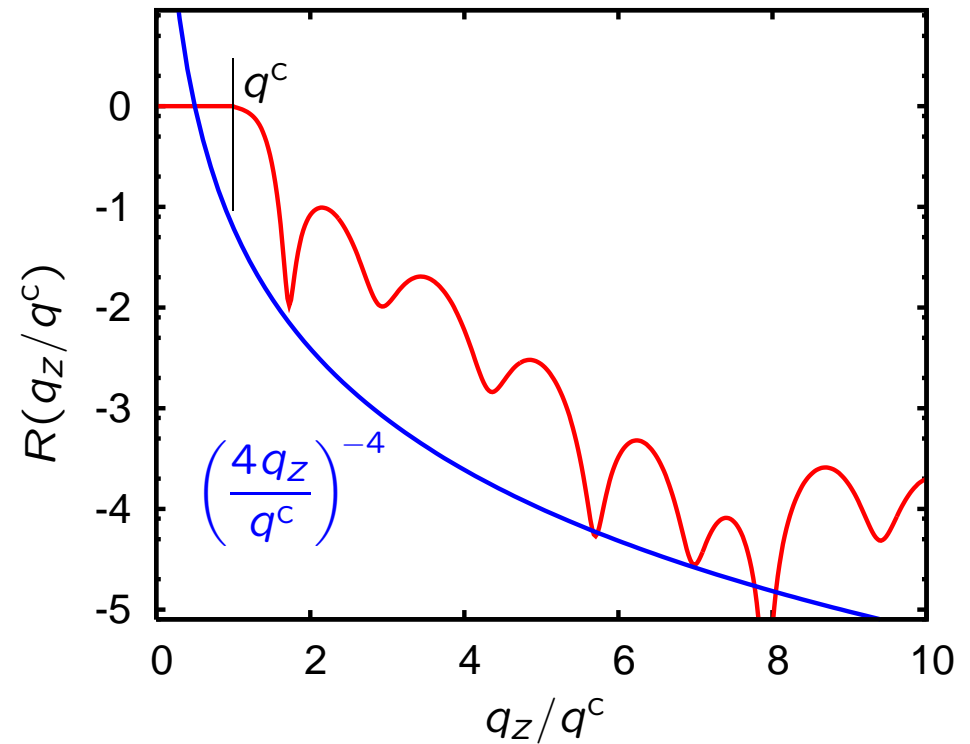
$$R(q_z) = |r_{0,1}(q_z)|^2$$

several parallel interfaces:

interference of all waves

$$R(q_z) = |r(q_z)|^2$$

what is  $r(q_z)$  of a multilayer?



$$\begin{aligned}
 \Psi_0(0) &= \begin{pmatrix} A_0^\uparrow \\ A_0^\downarrow \end{pmatrix} \quad \text{free choice of phase} \\
 &= \begin{pmatrix} 1/t_{0,1} & r_{0,1}/t_{0,1} \\ r_{0,1}/t_{0,1} & 1/t_{0,1} \end{pmatrix} \begin{pmatrix} A_1^\uparrow \\ A_1^\downarrow \end{pmatrix} \quad \text{continuity condition} \\
 &= \mathbf{I}_{0,1} \begin{pmatrix} e^{ik_{z,1}d_1} & 0 \\ 0 & e^{-ik_{z,1}d_1} \end{pmatrix} \begin{pmatrix} A_1^\uparrow e^{-ik_{z,1}d_1} \\ A_1^\downarrow e^{ik_{z,1}d_1} \end{pmatrix} \quad \text{phase factor} \\
 &= \mathbf{I}_{0,1} \mathbf{T}_1 \begin{pmatrix} 1/t_{1,2} & r_{1,2}/t_{1,2} \\ r_{1,2}/t_{1,2} & 1/t_{1,2} \end{pmatrix} \begin{pmatrix} A_2^\uparrow e^{-ik_{z,1}d_1} \\ A_2^\downarrow e^{ik_{z,1}d_1} \end{pmatrix} \\
 &= \mathbf{I}_{0,1} \mathbf{T}_1 \mathbf{I}_{1,2} \begin{pmatrix} e^{ik_{z,2}d_2} & 0 \\ 0 & e^{-ik_{z,2}d_2} \end{pmatrix} \begin{pmatrix} A_2^\uparrow e^{-ik_{z,2}(d_1+d_2)} \\ A_2^\downarrow e^{ik_{z,2}(d_1+d_2)} \end{pmatrix} \\
 &\vdots \\
 &:= \mathbf{M} \begin{pmatrix} A_{\text{substr}}^\uparrow e^{-ik_{z,\text{substr}} \sum_i d_i} \\ A_{\text{substr}}^\downarrow e^{ik_{z,\text{substr}} \sum_i d_i} \end{pmatrix}
 \end{aligned}$$



$$\Psi_0(0) = \begin{pmatrix} A_0^\uparrow \\ A_0^\downarrow \end{pmatrix}$$

$$= \mathbf{M} \begin{pmatrix} 0 \\ A_{\text{substr}}^\downarrow e^{ik_{z,\text{substr}} \sum_i d_i} \end{pmatrix}$$

$$r(q_z) = A_0^\uparrow / A_0^\downarrow$$

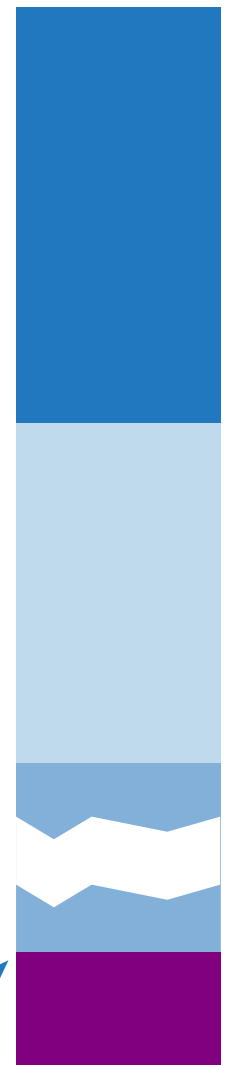
$$= \frac{M_{12} A_{\text{substr}}^\downarrow e^{ik_{z,\text{substr}} \sum_i d_i}}{M_{22} A_{\text{substr}}^\downarrow e^{ik_{z,\text{substr}} \sum_i d_i}}$$

$$= \frac{M_{12}(q_z)}{M_{22}(q_z)}$$

calculation of  $M_{12}(q_z)$  and  $M_{22}(q_z)$  is trivial ...

... if all  $n_i$  and  $d_i$  are known!

there is no  
upcoming  
wave



$$R(q_z) = |r(q_z)|^2$$

⇒ all phase information is lost

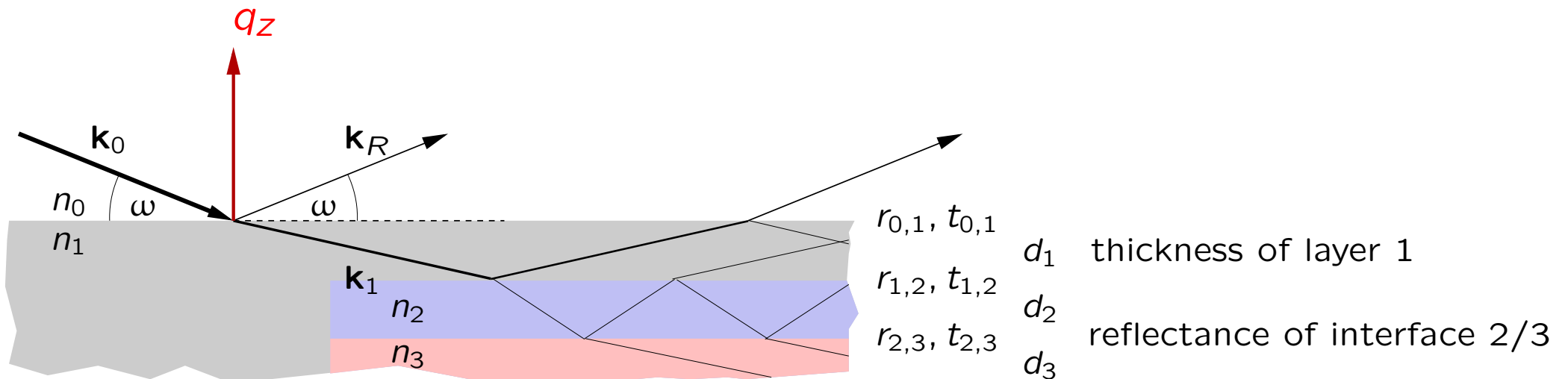
⇒ one way road:

⇒ calculation of  $R(q_z)$  using a model  
and  
comparison to measured curve(s)

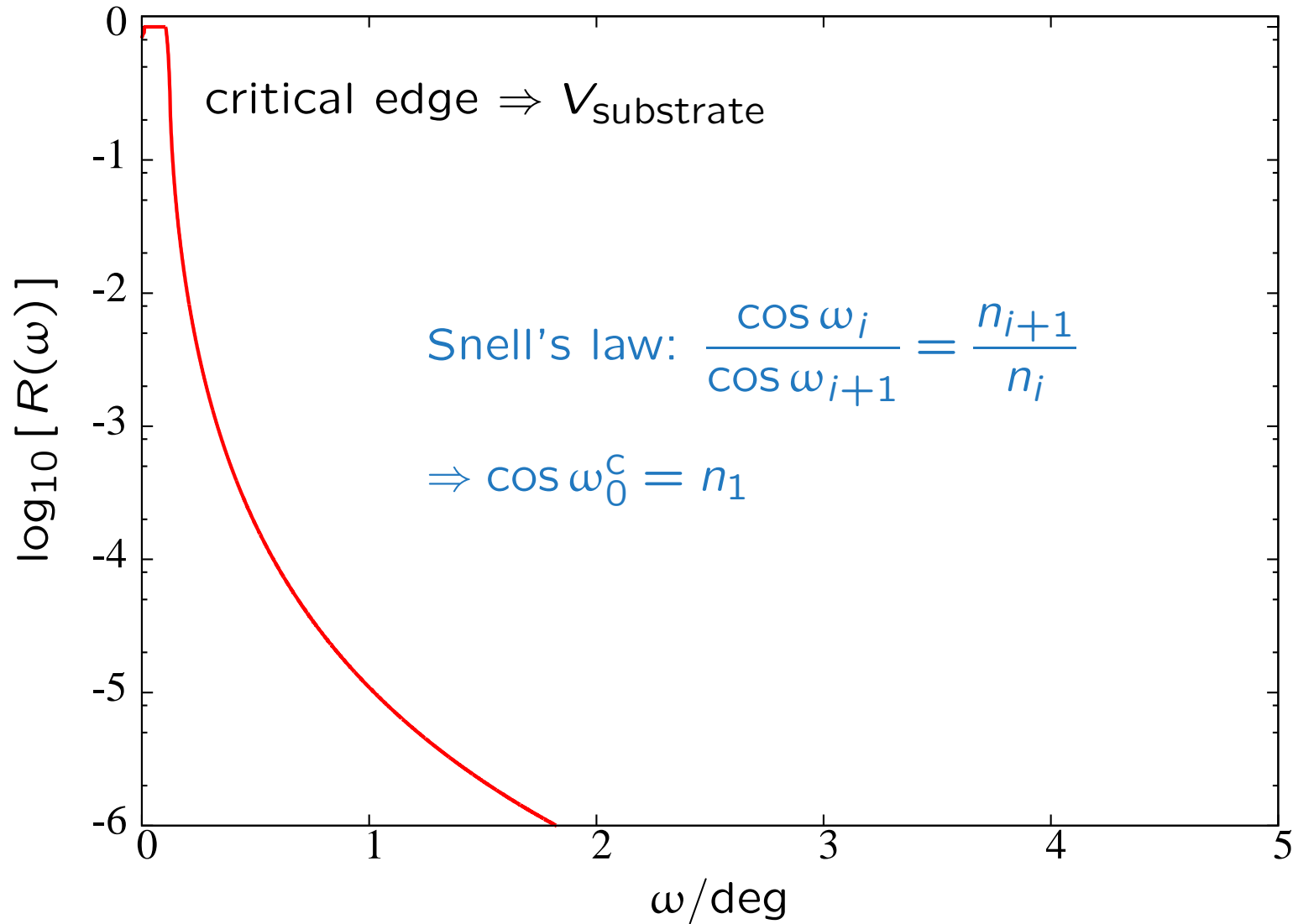
real effects

to be taken into account:

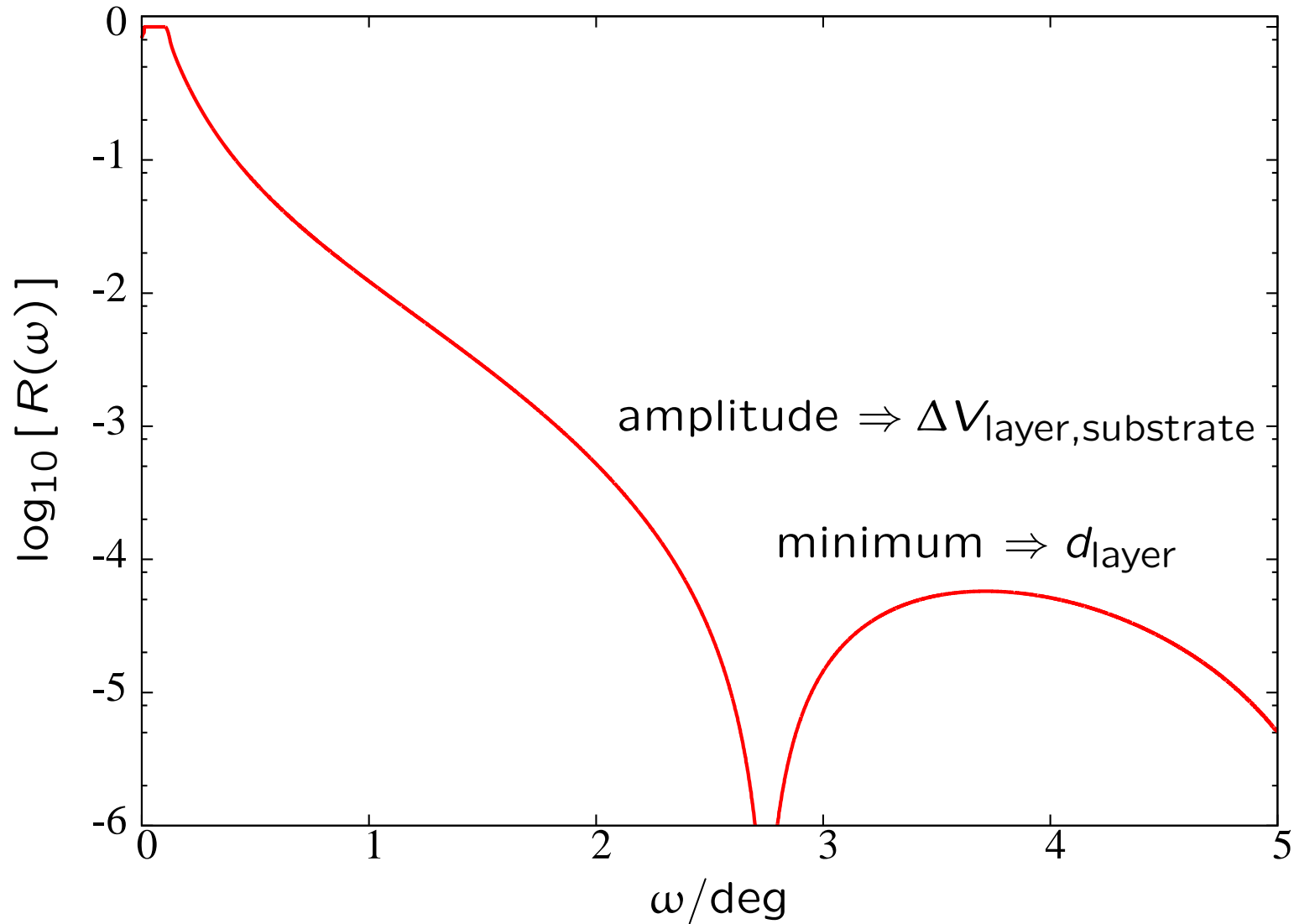
- non-sharp interfaces
- inhomogeneous layers
- illumination of the sample
- resolution of the set-up  $\Delta\omega, \Delta\lambda$



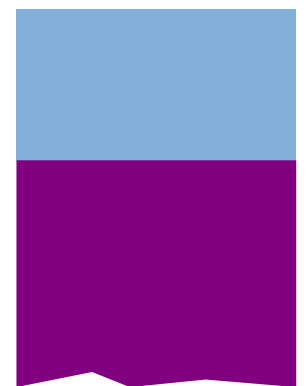
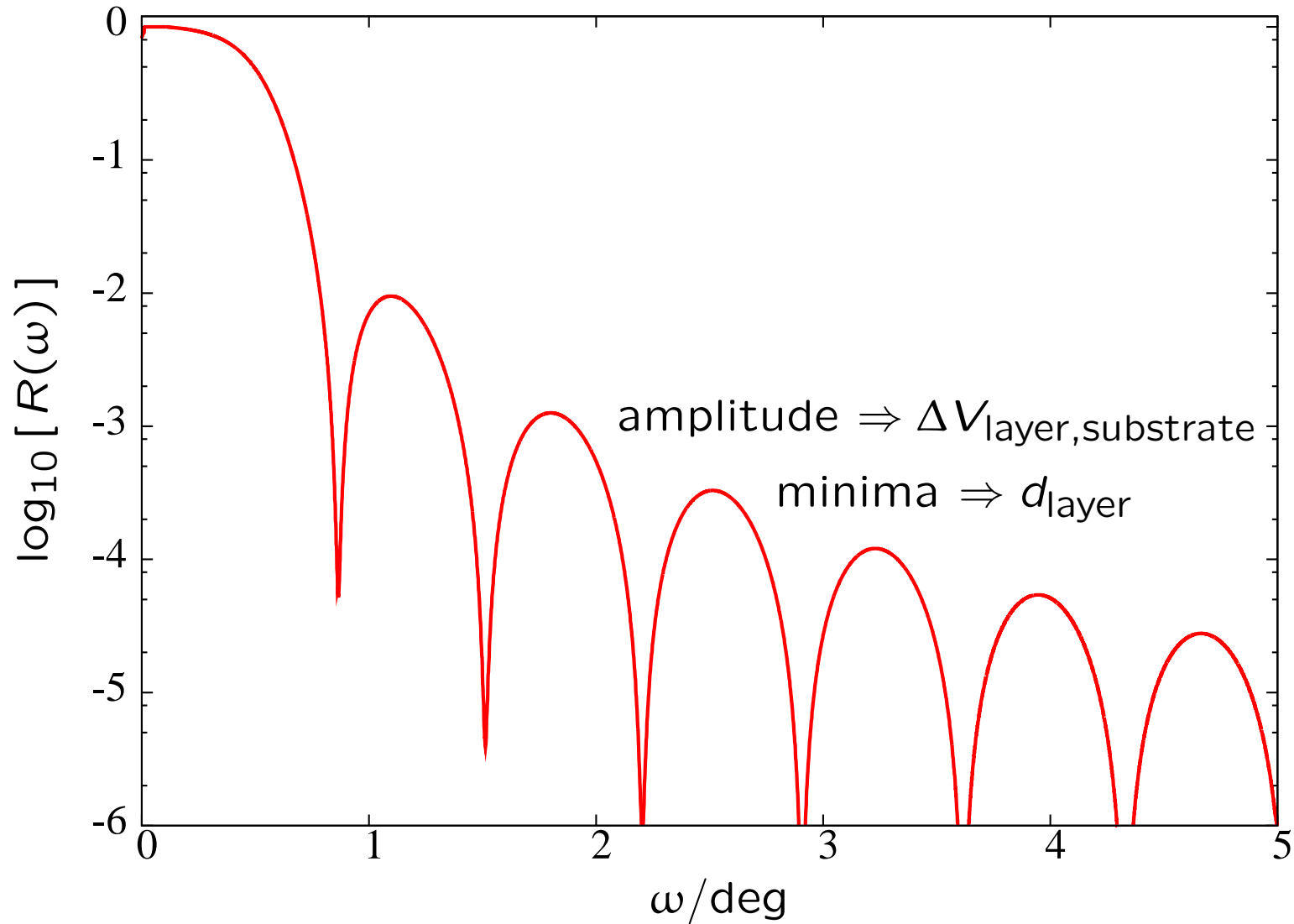
... of a surface



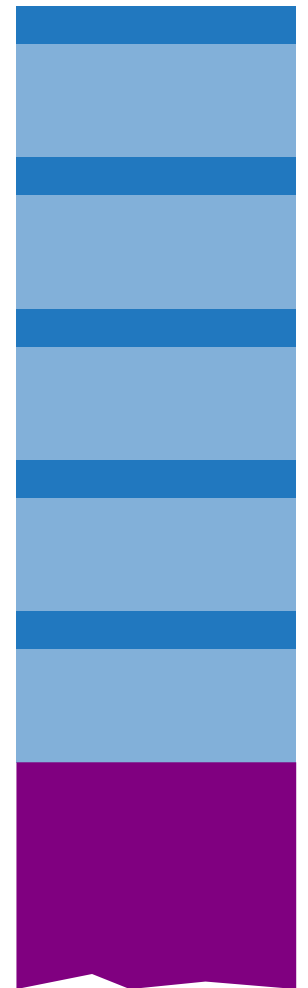
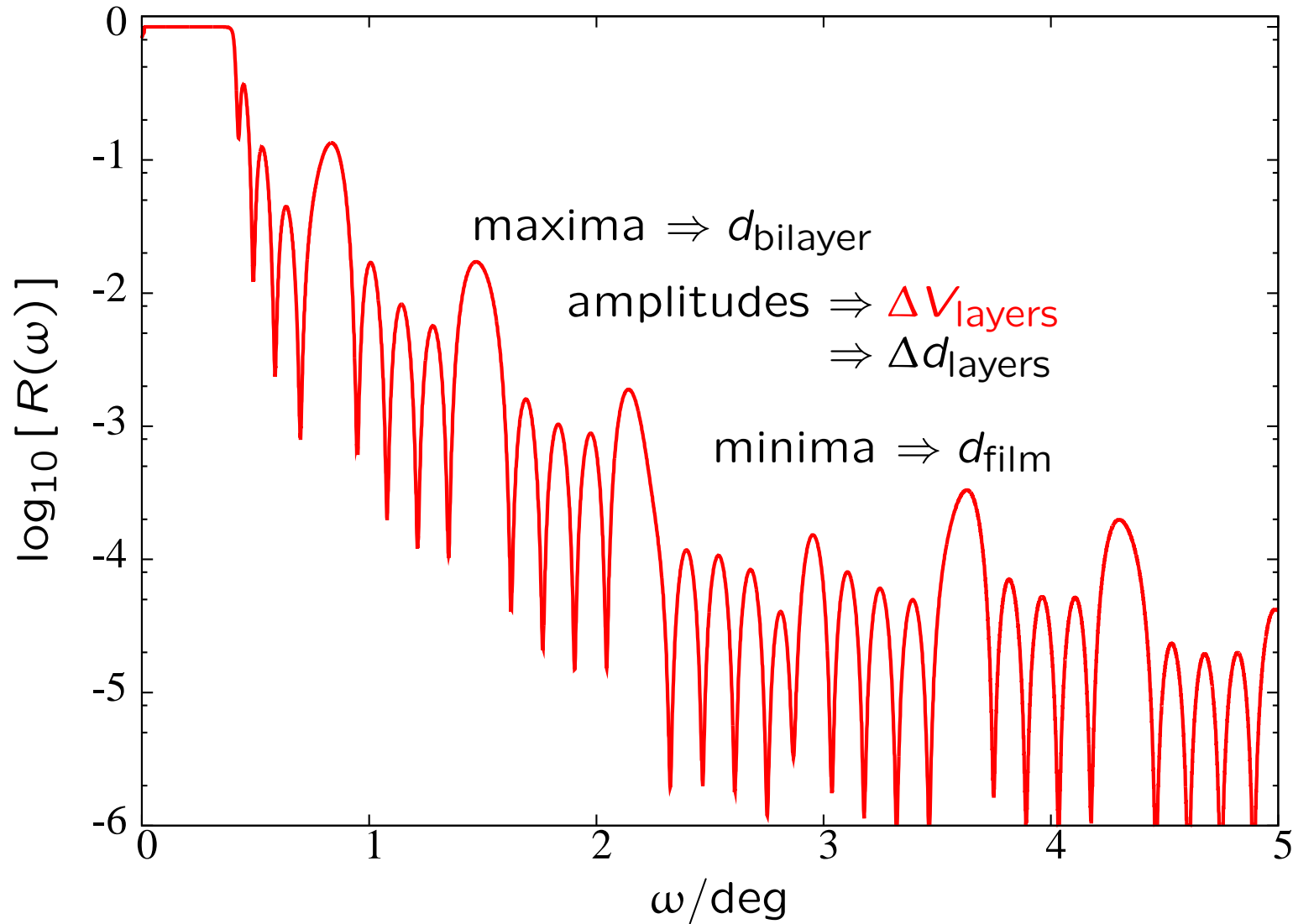
... of a thin layer



... of a thick layer



... of a periodic multilayer



$$\begin{aligned}\delta = 1 - n &= \frac{\lambda^2}{2\pi} (\rho^b + \rho^m) \text{ for neutrons} \\ &= \frac{\lambda^2}{2\pi} r_e \rho^e \text{ for x-rays}\end{aligned}$$

Ni:  $\rho^b = 9.4 \cdot 10^{-6} \text{ \AA}^{-2}$

$\Rightarrow \delta^{\text{nuc}} = 3.75 \cdot 10^{-5}, \lambda = 5 \text{ \AA}$

$\delta \ll 1$

$\Rightarrow \omega^c \approx 0.5^\circ$

small angles of incidence!

Fe:  $\rho^m \approx 6 \cdot 10^{-6} \text{ \AA}^{-2}$

$\Rightarrow \delta^m \approx 2.4 \cdot 10^{-5}, \lambda = 5 \text{ \AA}$

$\delta^m \sim \delta^b$

Al:  $r_e \rho^e = 2.2 \cdot 10^{-5} \text{ \AA}^{-2}$

$\Rightarrow \delta^e = 8.7 \cdot 10^{-5}, \lambda = 5 \text{ \AA}$

$\delta^e \sim \delta^b$

probed depth      100 nm  $\rightarrow$  1  $\mu$ m

(less for strong absorbers)

depth resolution      0.2 nm  $\rightarrow$  400 nm

strongly model dependent

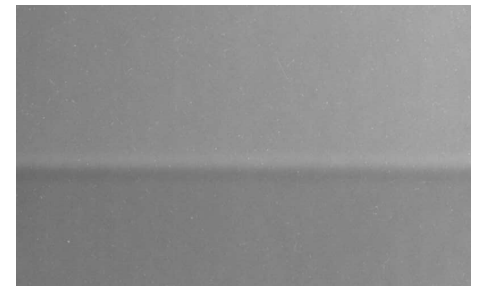
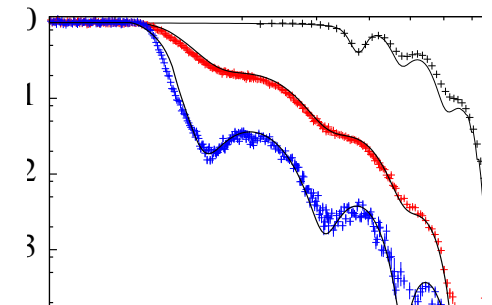
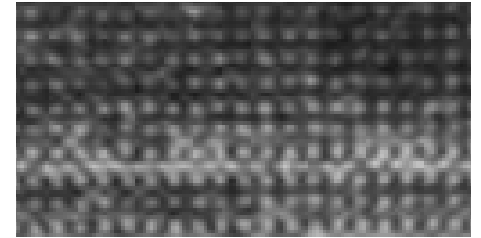
$t$  and  $\delta$  might be strongly correlated

lateral coherence      1  $\mu$ m  $\rightarrow$  100  $\mu$ m

averaging laterally over all  
*microstructures*

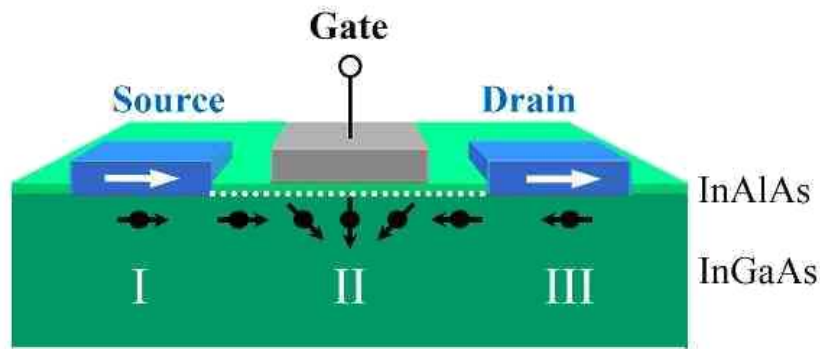


- heterostructures
  - magnetic layers
  - membrane systems
- reflectometry
  - (few formulae)
- ... derivation
  - (lots of formulae)
- experimental examples
  - Fe/Si
  - FeSi/GaAs interfaces
  - bio-membrane
- relevance for imaging
  - YES, there is some!



use not only the electron charge to carry information but also its spin

e.g. transistor based on spin / FM alignment:



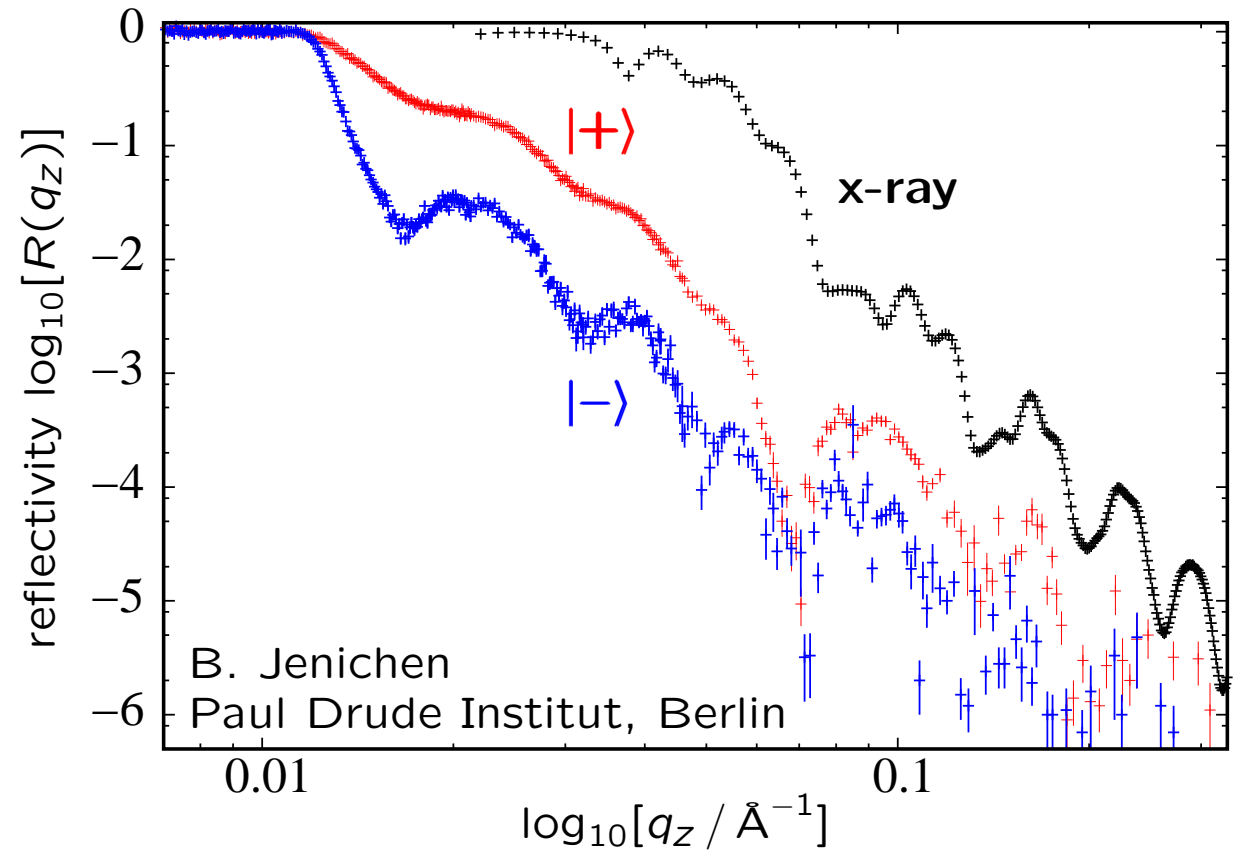
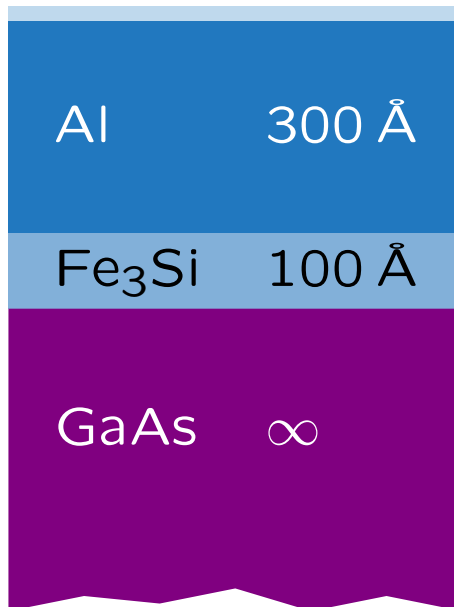
spin-polarised currents exist in *half-metals* (e.g.  $\text{Fe}_3\text{Si}$ )

but

polarised spin injection into a semiconductor (e.g. GaAs) is inefficient

⇒ what happens at the interface?

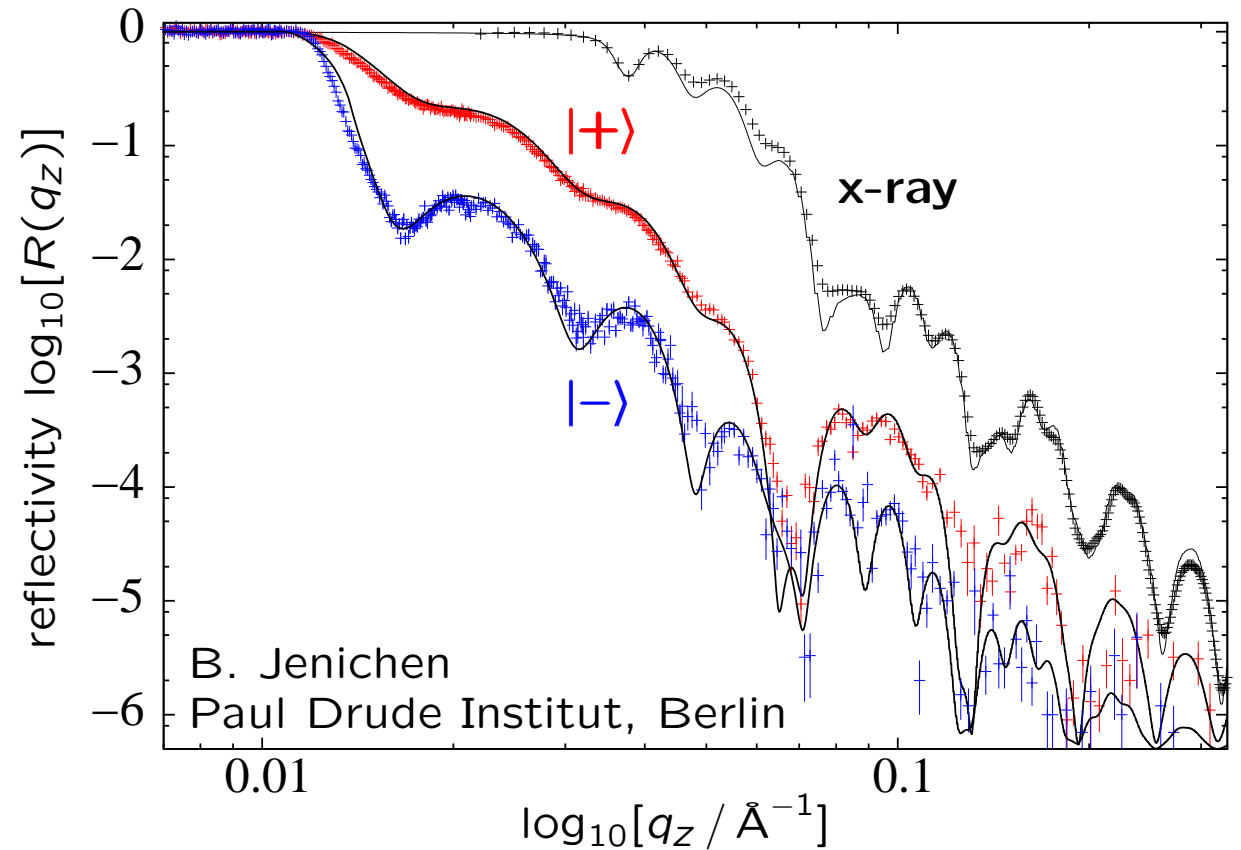
Fe<sub>3</sub>Si film on GaAs  
 search for a magnetically  
 dead layer



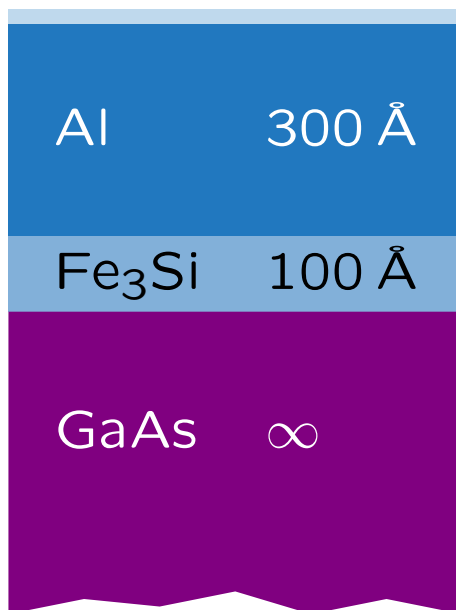
B. Jenichen  
 Paul Drude Institut, Berlin

sample size: 5 × 5 mm<sup>2</sup>  
 measurement time: 24 h neutron  
 1 h x-ray

Fe<sub>3</sub>Si film on GaAs  
 search for a magnetically  
 dead layer



B. Jenichen  
 Paul Drude Institut, Berlin



$$\delta \propto \rho^b \pm \rho^m$$

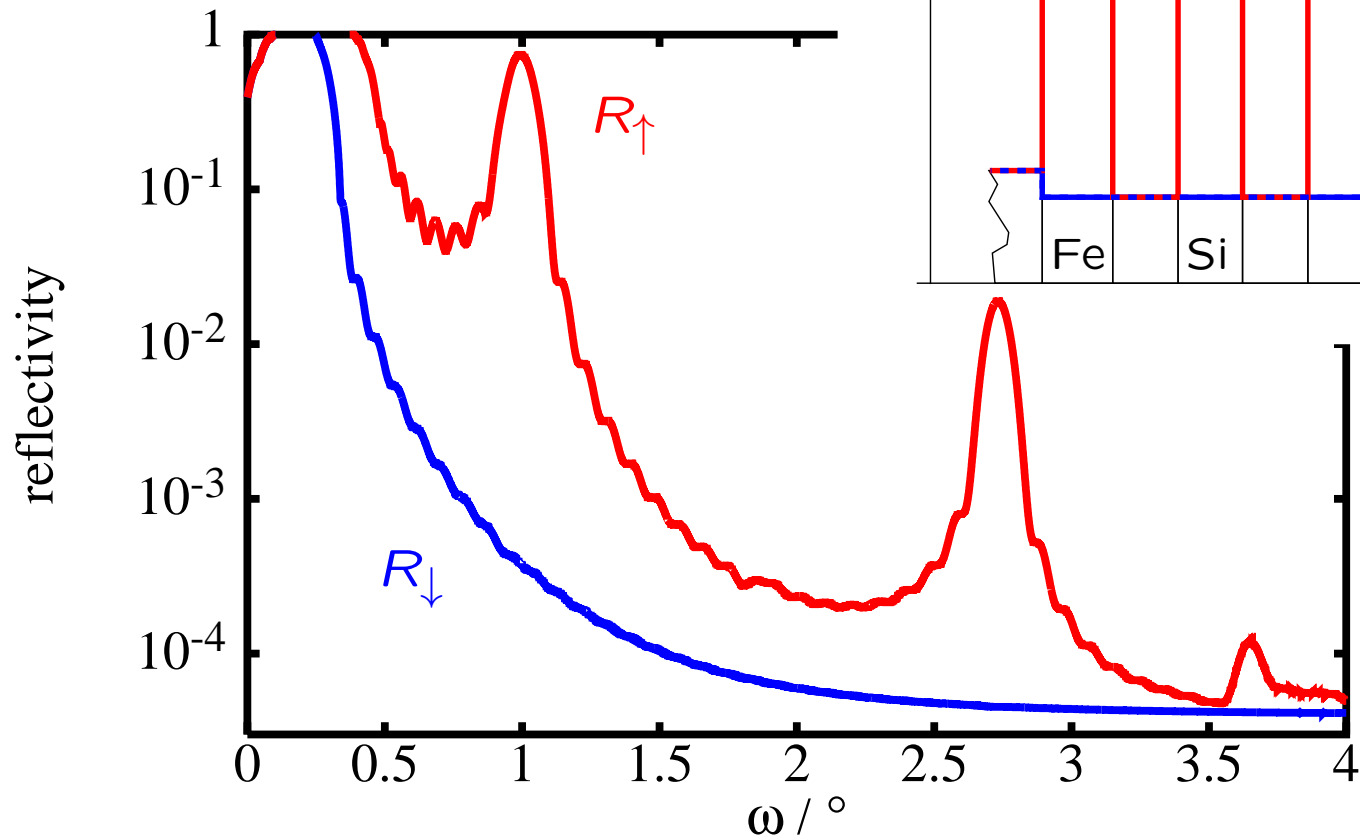
$B = 2.0(2)$  T in Fe<sub>3</sub>Si  
 no magnetically dead layer detectable

Fe/Si multilayer

ideal case:

$$\rho_{\text{Fe}}^b + \rho_{\text{Fe}}^m \gg \rho_{\text{Si}}$$

$$\rho_{\text{Fe}}^b - \rho_{\text{Fe}}^m = \rho_{\text{Si}}$$

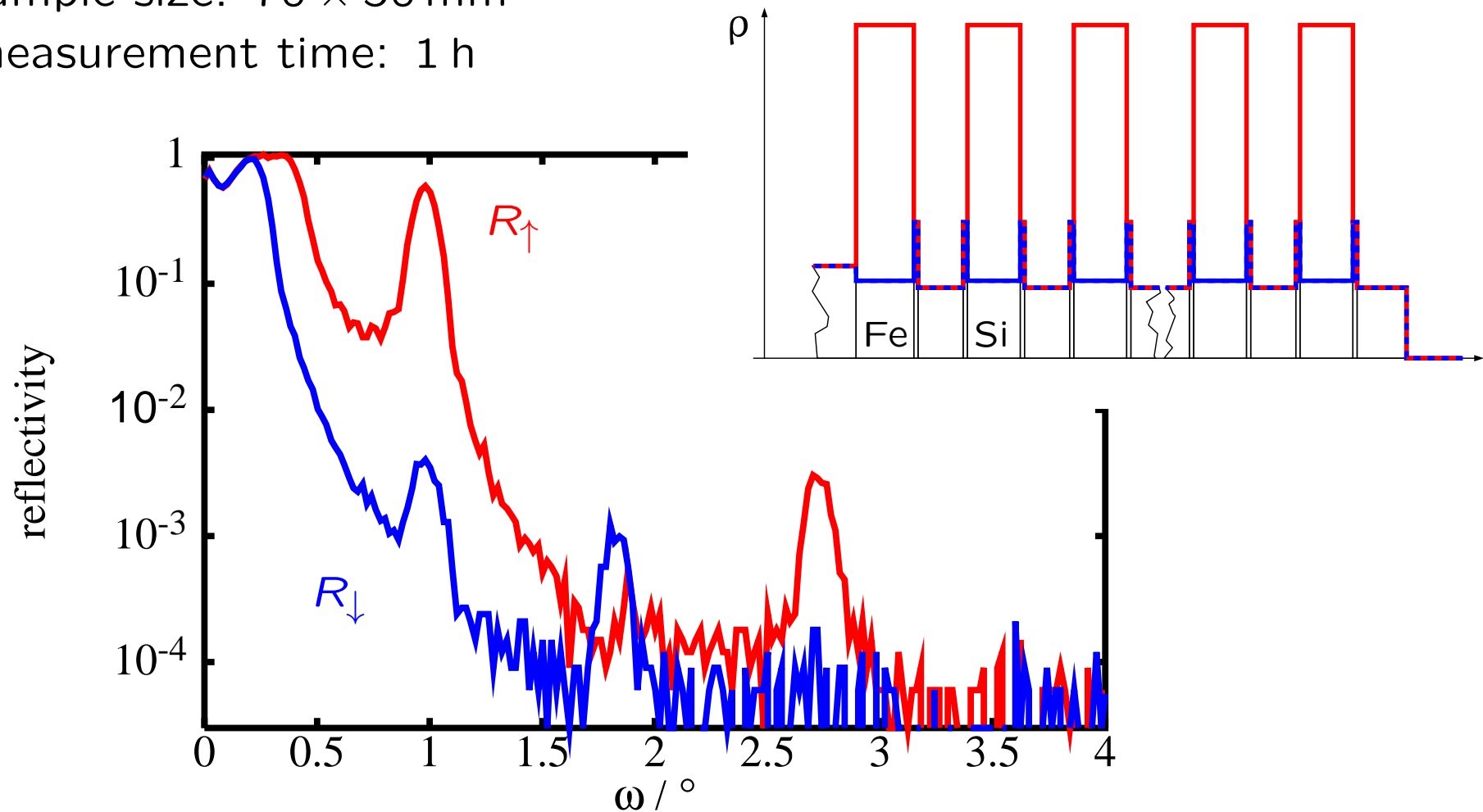


## Fe/Si multilayer

reality: interdiffusion leads to 5 Å thin magnetically dead Fe : Si layers

sample size:  $70 \times 50 \text{ mm}^2$

measurement time: 1 h

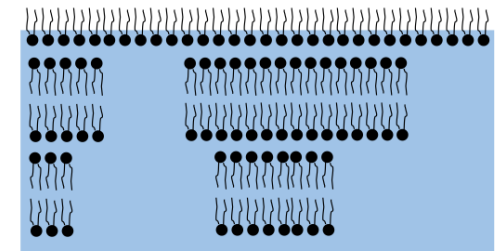
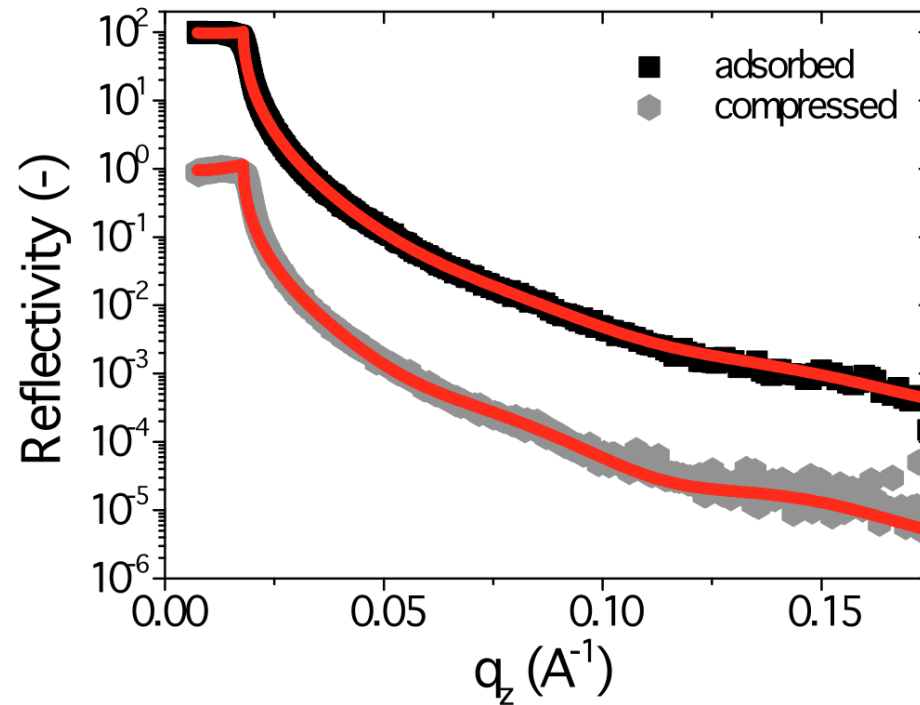


**compression of self-organising polyglycerol-ester films**

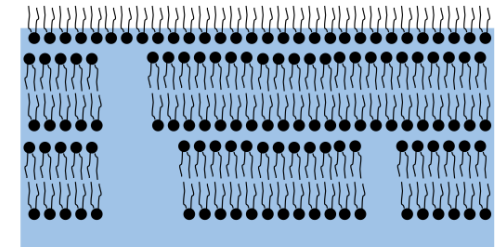
H<sub>2</sub>O substituted by D<sub>2</sub>O

⇒ strong contrast between solvent and film (essentially [CH<sub>2</sub>]<sub>n</sub>)

⇒ *high* critical edge



↓ **compression**



constant film thickness

laterally more homogeneous

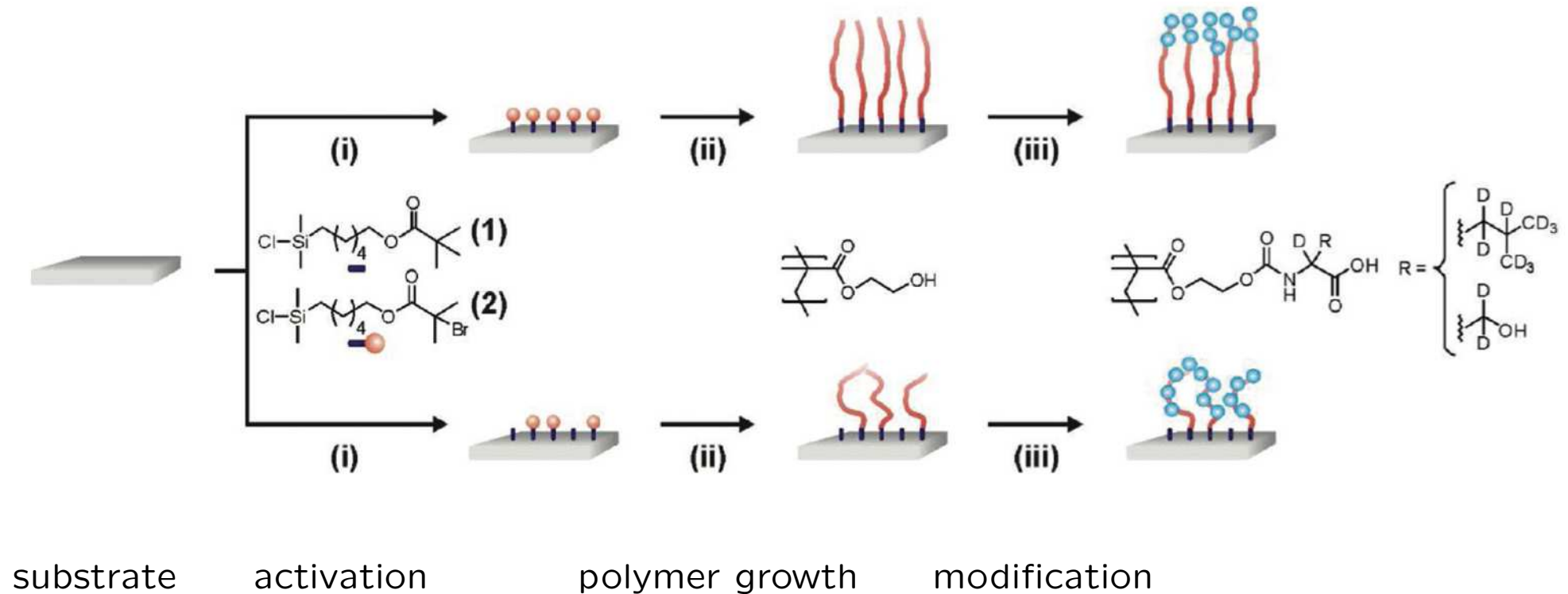
⇒ less *roughness*

⇒ lower damping of  $R(q_z)$

**polymer brushes**

- applications:
- anti-fouling color
  - coating within ball bearings
  - **matrix for chemical sensors**

where are the functional groups located?





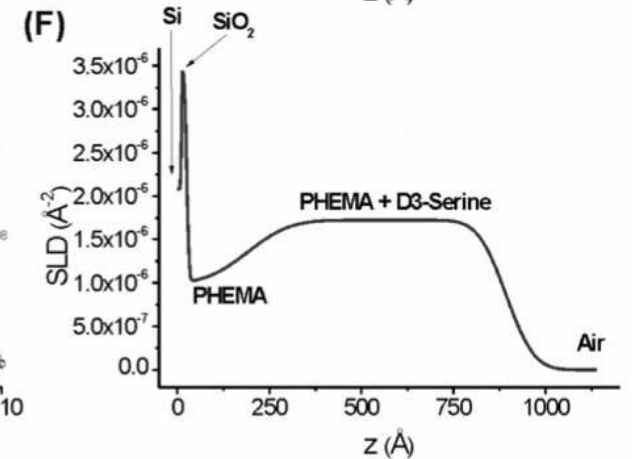
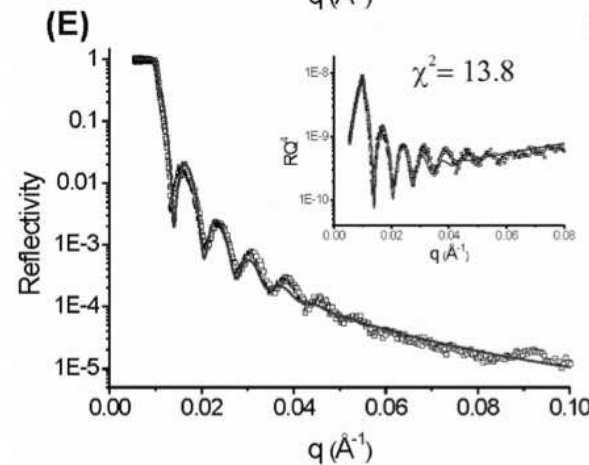
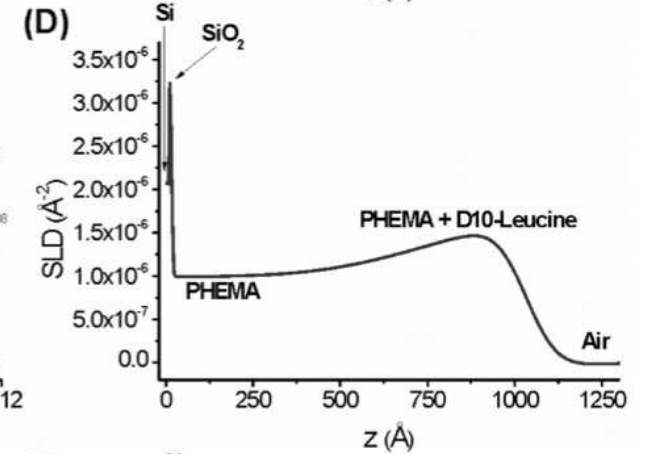
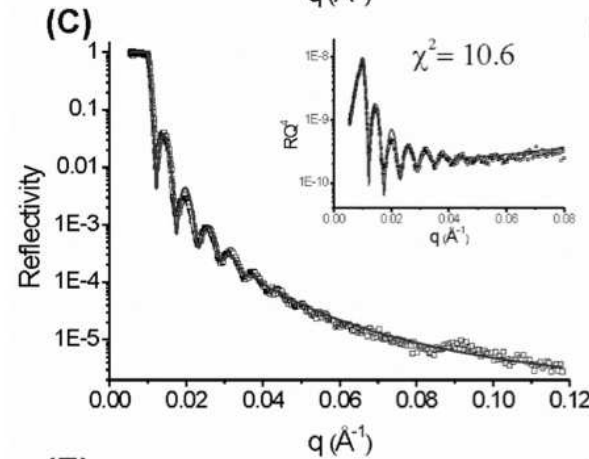
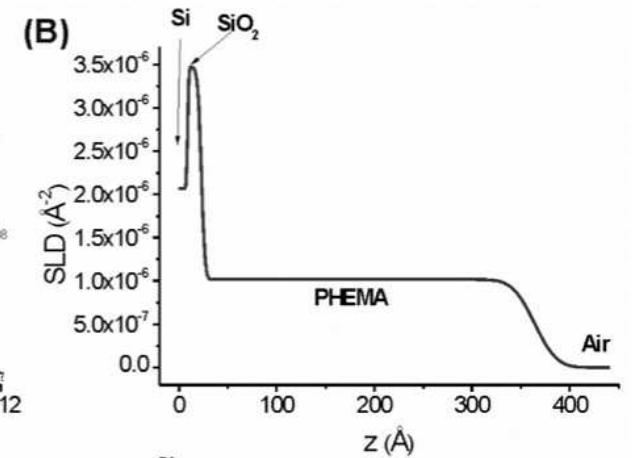
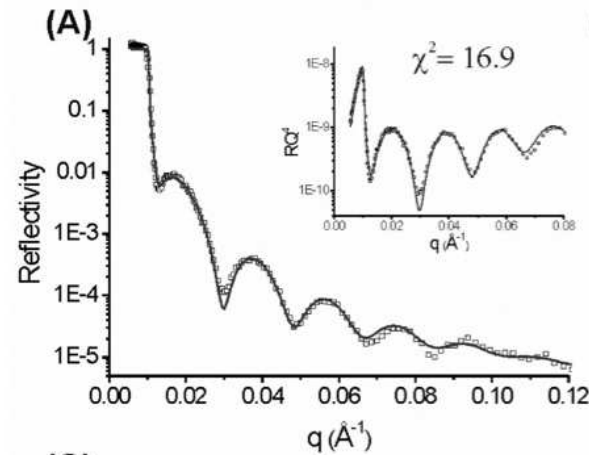
polymer brushes

location of functional groups

341 Å  
non-functionalised

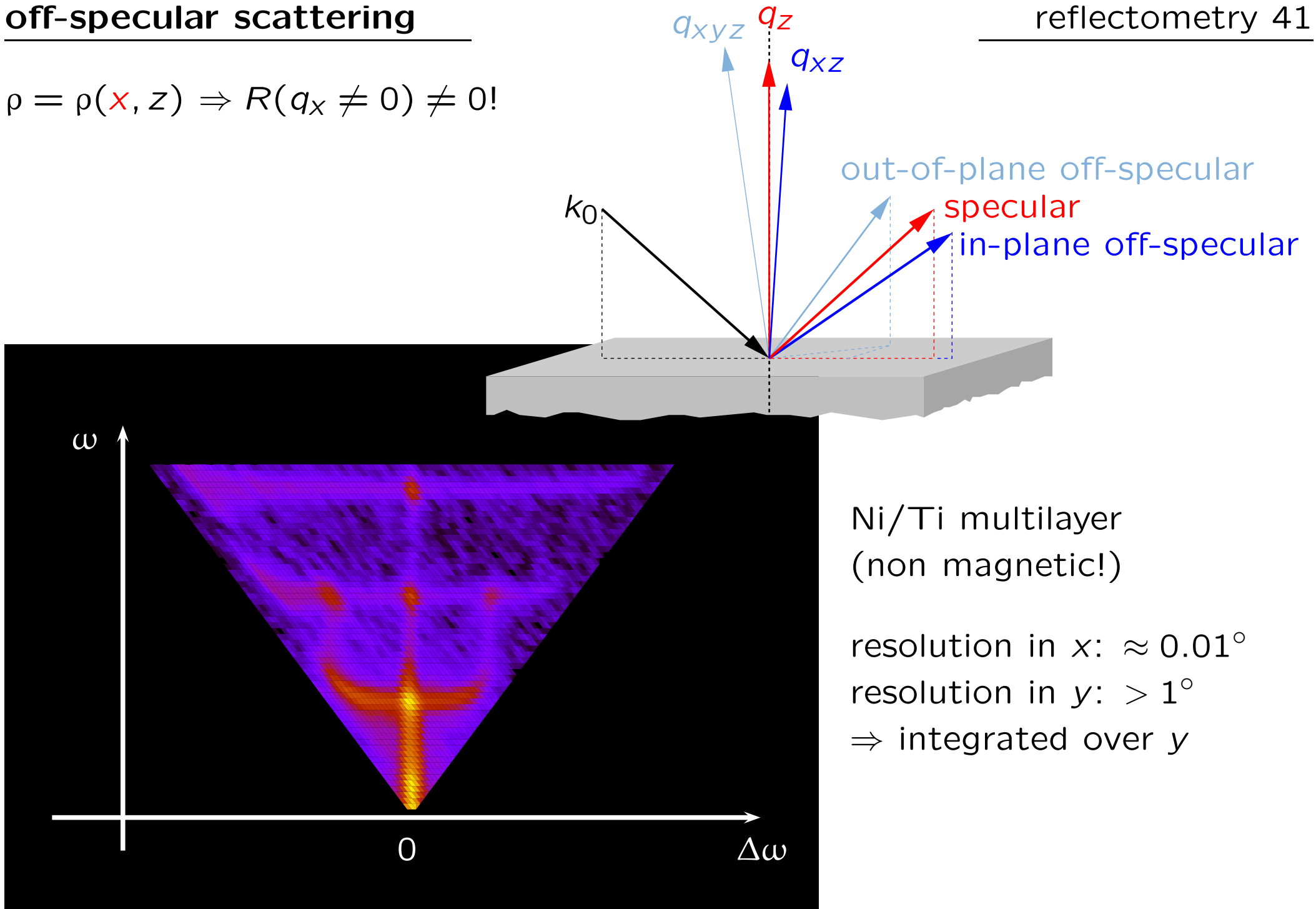
1016 Å  
leucine functionalised

867 Å  
serine functionalised



# off-specular scattering

$$\rho = \rho(x, z) \Rightarrow R(q_x \neq 0) \neq 0!$$



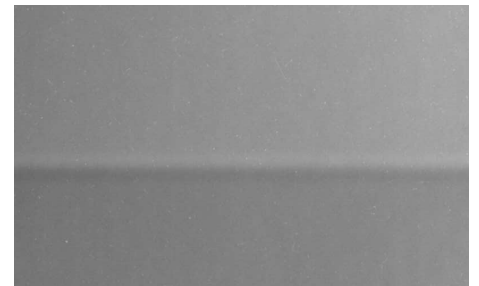
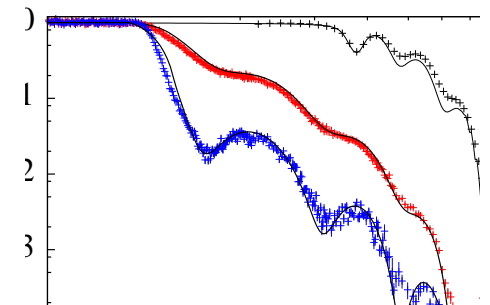
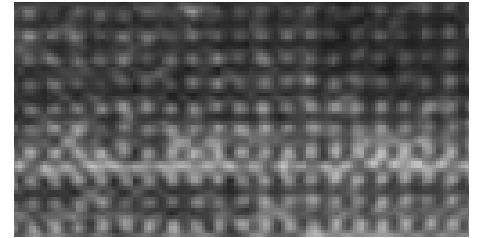
Ni/Ti multilayer  
(non magnetic!)

resolution in  $x$ :  $\approx 0.01^\circ$   
resolution in  $y$ :  $> 1^\circ$   
 $\Rightarrow$  integrated over  $y$

## outline

- heterostructures
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- reflectometry
  - (few formulae)
- ... derivation
  - (lots of formulae)
- experimental examples
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  - FeSi/GaAs interfaces
  - bio-membrane
- relevance for imaging
  - YES, there is some!

## reflectometry 42

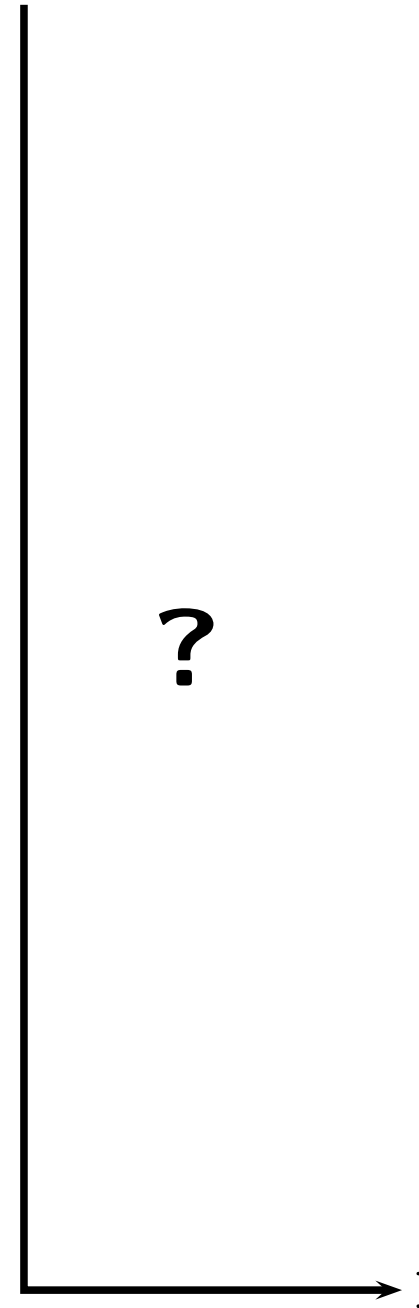
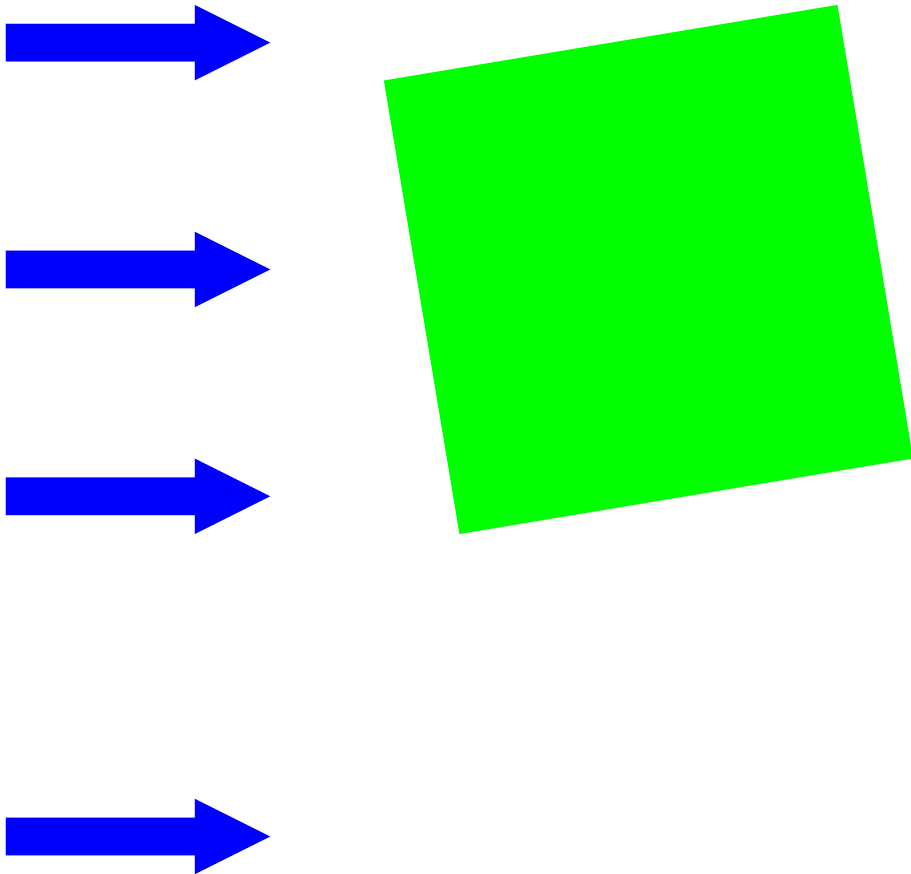


total reflection and refraction change beam direction

⇒ important for *large* sample-detector distances

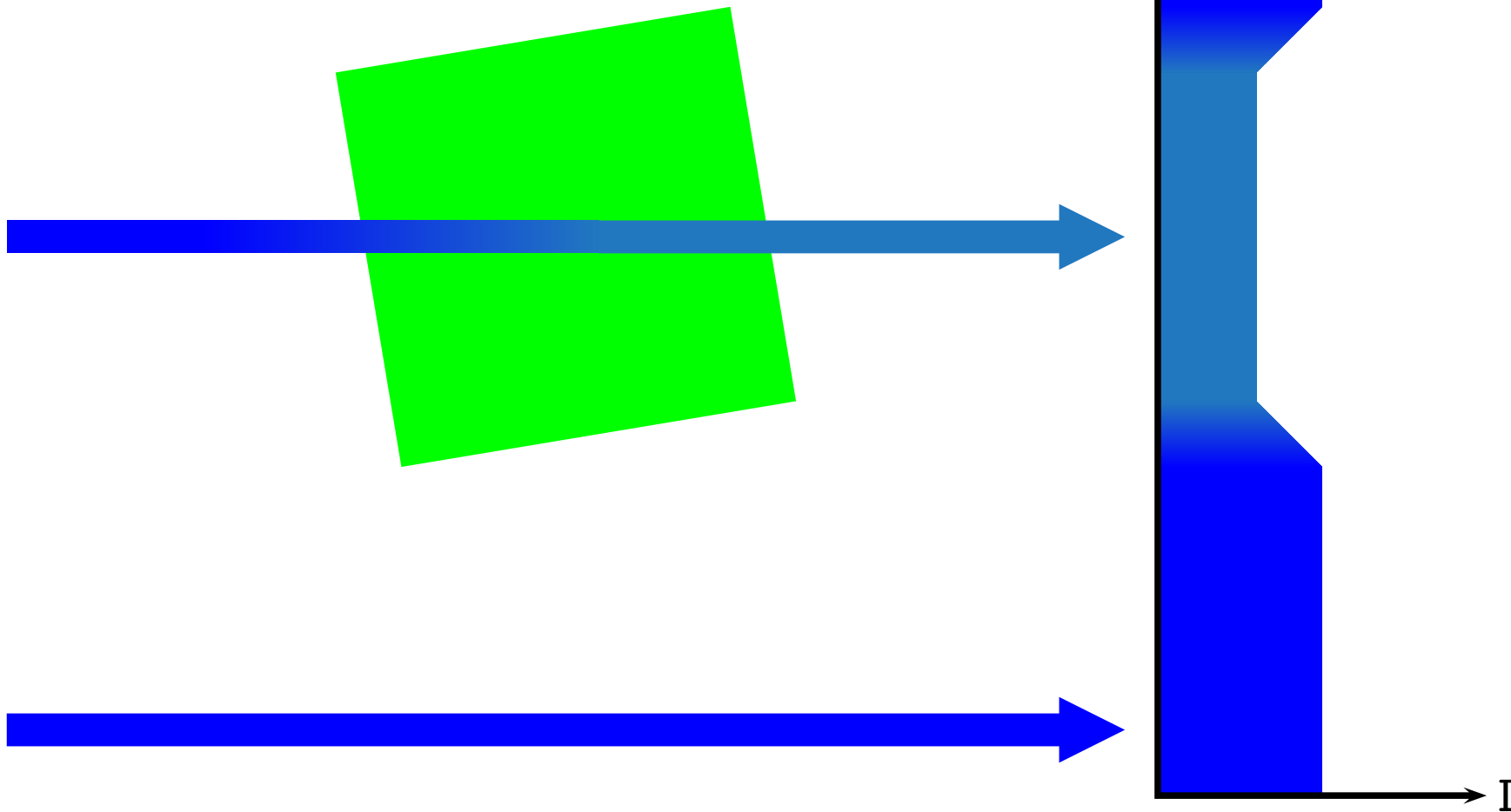
also (optically) rough interfaces show significant total reflection!

transmission of a slightly tilted square prism:  
 $n < 1 \Rightarrow$  total external reflection possible  
parallel, monochromatic beam



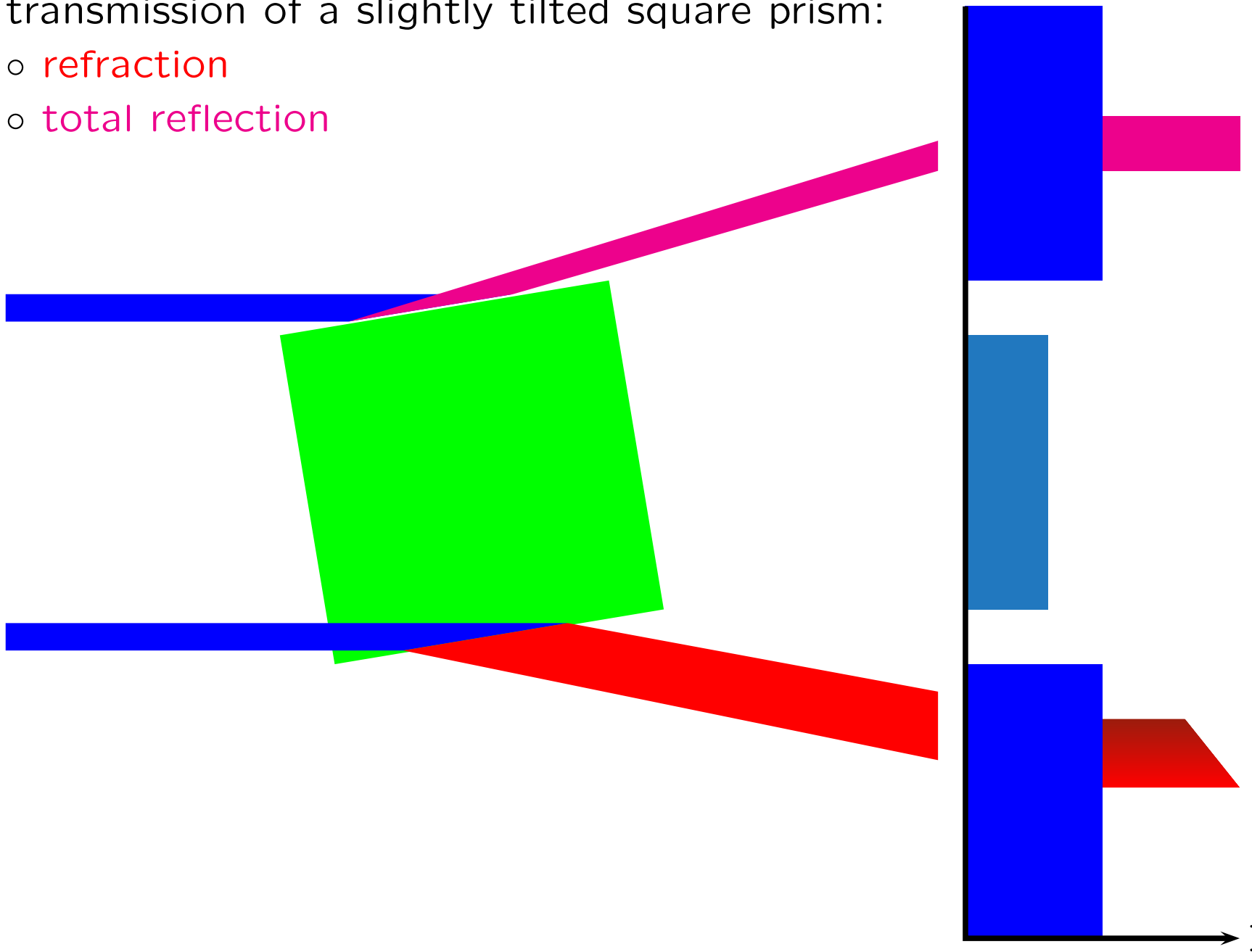
transmission of a slightly tilted square prism:

- no refraction
- no reflection



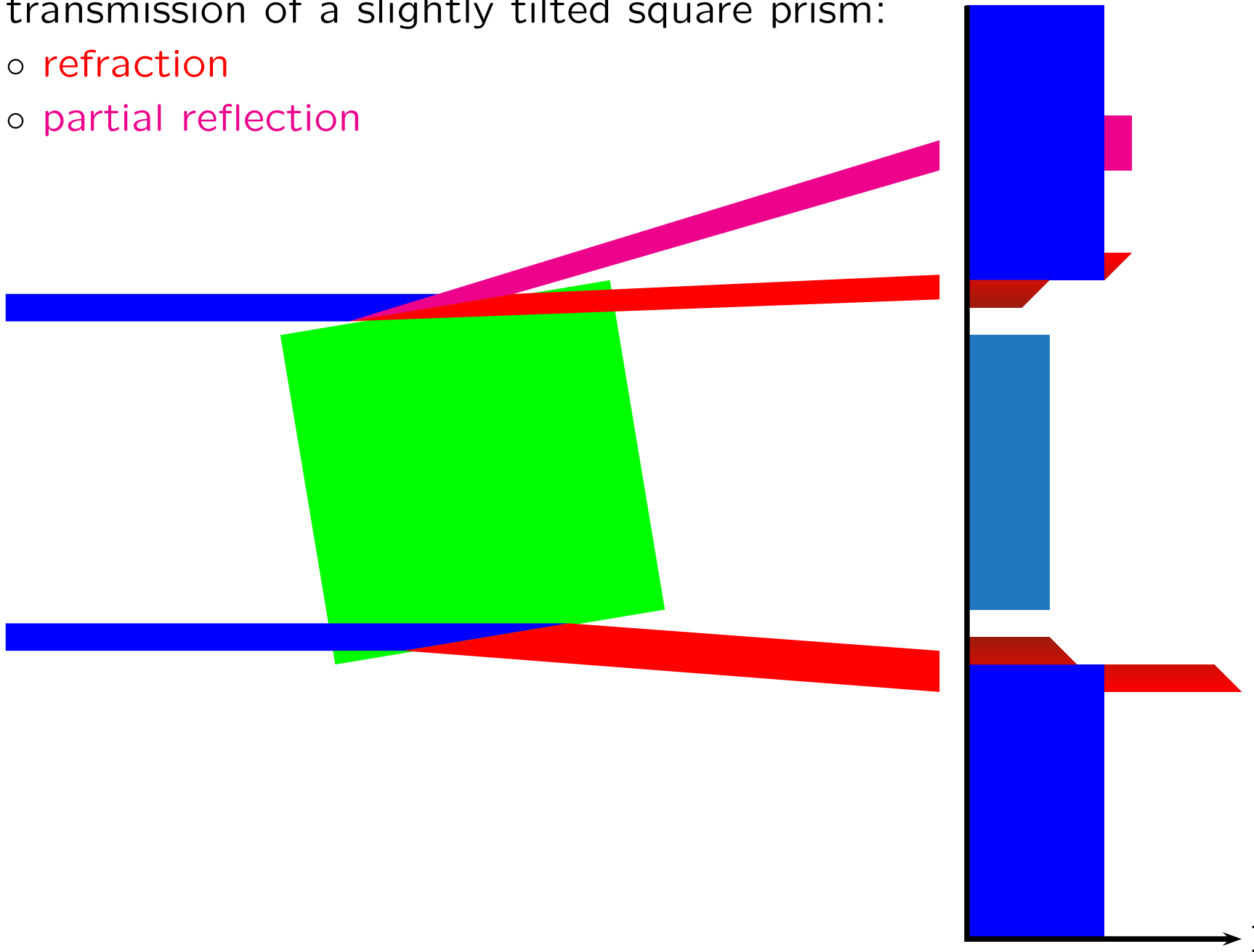
transmission of a slightly tilted square prism:

- refraction
- total reflection



transmission of a slightly tilted square prism:

- refraction
- partial reflection



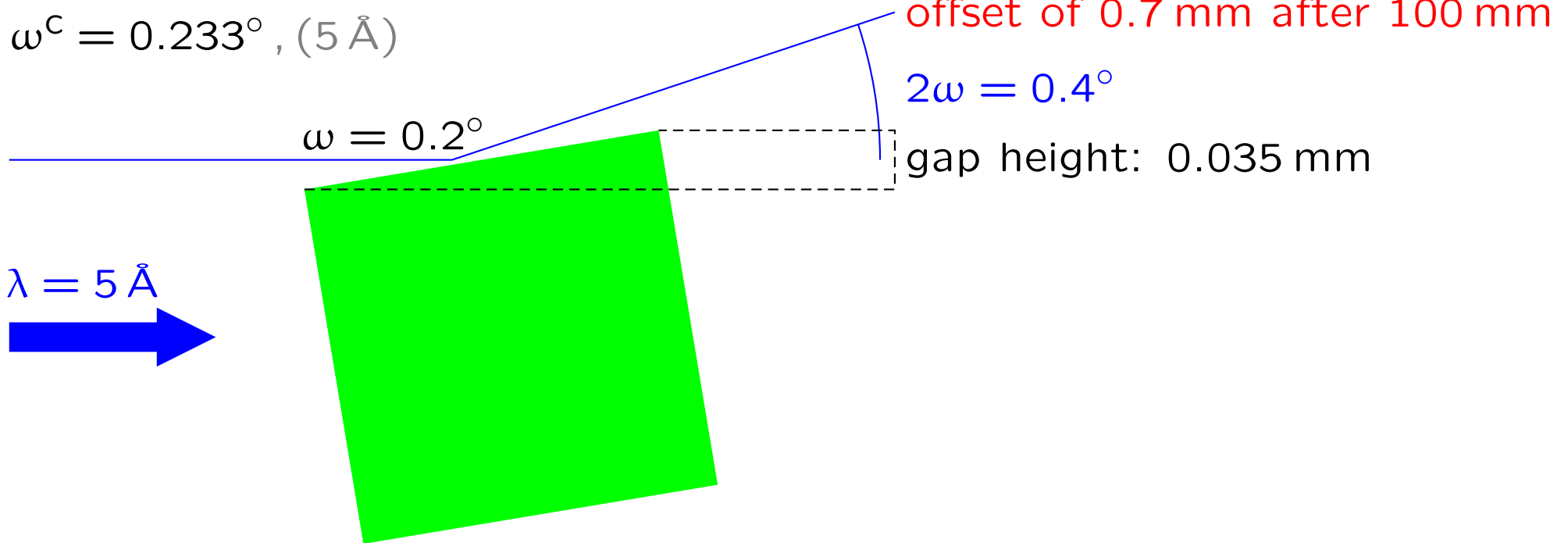


transmission of a slightly tilted square prism: some numbers

Al prism with  $\varnothing = 10 \times 10 \text{ mm}^2$

$n = 1 - 8.3 \cdot 10^{-6}$ , (5 Å)

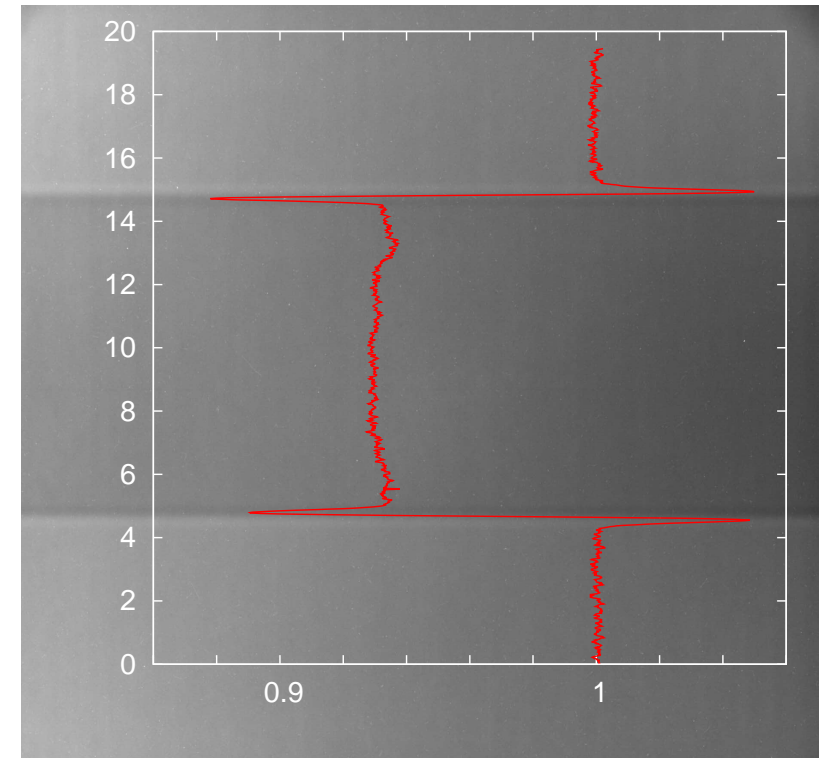
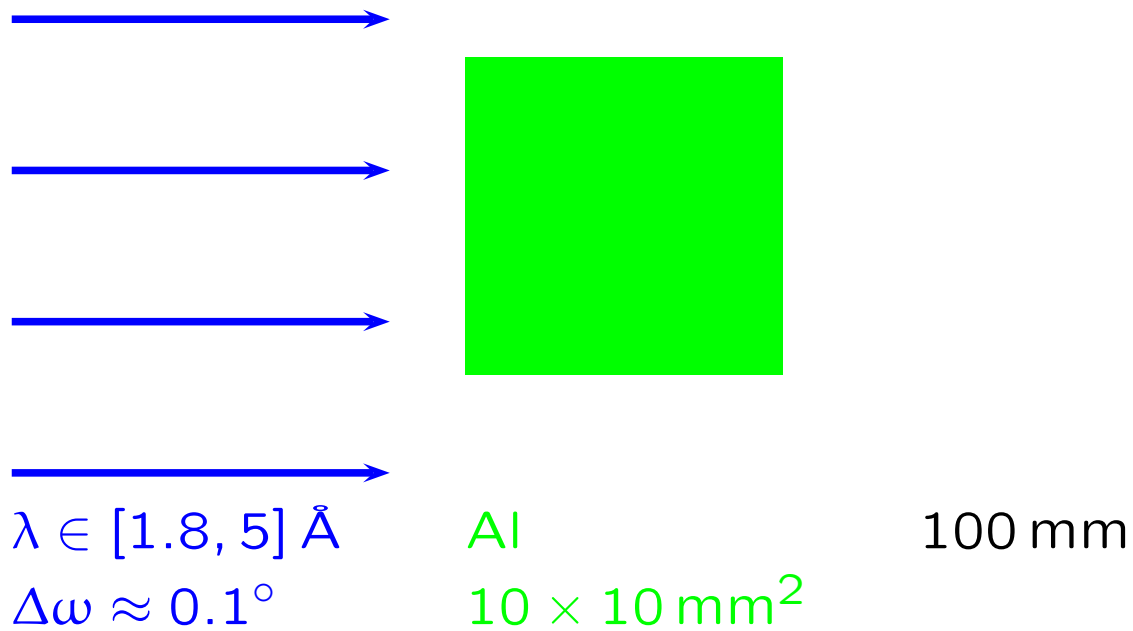
$\omega^c = 0.233^\circ$ , (5 Å)



$\Rightarrow$  reflection (and refraction) can lead to detectable features

like *halos* or *shadows*

measured transmission (Eberhard Lehmann, PSI)

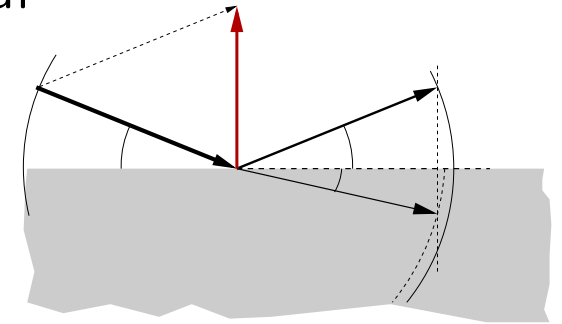


Al cube has not perfectly flat and parallel surfaces

$$\Rightarrow \omega = 0 \pm \Delta\omega_{\text{beam}} \pm \Delta\omega_{\text{surface}}$$

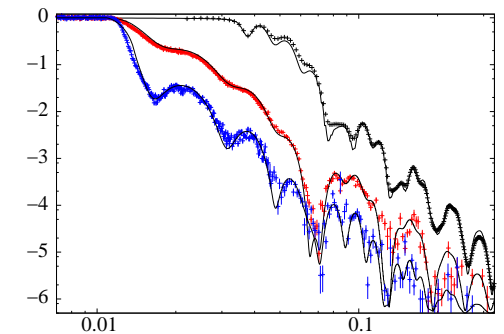
**reflectometry**

probes **depth-profile** of some potential  
averages laterally  
⇒ ideal for layered systems  
data analysis by **modelling**



**with neutrons**

resolution: atom to sub- $\mu\text{m}$   
isotope selective  
detects **in-plane magnetic induction**



**with x-rays**

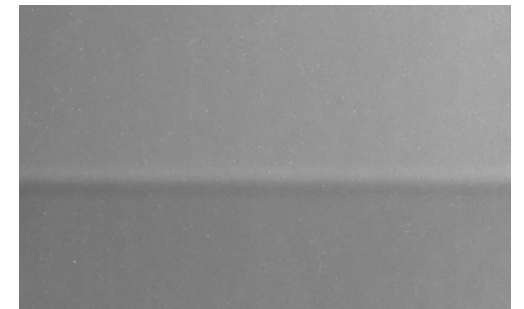
resolution: atom to sub- $\mu\text{m}$   
detects electron density

**... in resonance**

detects **magnetic states** of atoms

**radiography**

might be affected !!!



reflectometry, in general :

J. Daillant, A. Gibaud:

*X-ray and Neutron Reflectivity*

Lect. Notes Phys. 770 (Springer 2009)

U. Pietsch, V. Holý, T. Baumbach:

*High-Resolution X-Ray Scattering*

(Springer 2004)

... on magnetic systems

F. Ott:

*Neutron scattering on magnetic surfaces*

C. R. Physique **8**, 763-776 (2007)

... using resonant x-rays

S. Brück:

*Magnetic Resonant Reflectometry on Exchange Bias Systems*

Dissertation, Stuttgart 2009