

## Theory and Practice of Consequence Analysis using MACCS

## A.J. Nosek, PhD US Nuclear Regulatory Commission

## Outline

- Code Overview
- Atmospheric Dispersion and Deposition
- Dosimetry
- Protective Actions
- Social and Economic Impacts
- Radiogenic Health Effects



## CODE OVERVIEW Outline

- Computational framework
- Spatial grid
- Population cohorts
- MACCS outputs



#### CODE OVERVIEW Computational Framework





#### CODE OVERVIEW Spatial Grid

- Calculations are performed on a radial polar grid
- The user specifies the number of compass sectors and radial intervals, and the outer distance of each radial interval
- MACCS calculates results for each spatial element



Example of MACCS polar coordinate grid with 16 sectors and 3 radial divisions. (reproduced from Fig. 2-1 of NUREG/CR-6613 Vol. 1



### CODE OVERVIEW Population Cohorts

- User can divide the regional population into population cohorts that have similar characteristics during an emergency response
  - Cohorts can have different protection factors, breathing rates, evacuation timelines, evacuation regions, and other factors.
  - In the intermediate and long-term phases, MACCS treats all survivors as a single population cohort.
- For each cohort, MACCS runs a separate simulation
- Many outputs report both summary results from all cohorts and cohort-specific results



## CODE OVERVIEW

#### MACCS outputs

Output Name	ATMOS	EARLY	CHRONC
Type 0: Atmospheric Results for Specified Downwind Distances	X		
Type 1: Health Effect Cases		Х	Х
Type 2: Early Fatality Distance		Х	
Type 3: Population Exceeding Early Dose Threshold		Х	
Type 4: Average Individual Risk		Х	Х
Type 5: Population Dose		Х	Х
Type 6: Centerline Dose		Х	Х
Type 7: Centerline Risk		Х	Х
Type 8: Population-Weighted Individual Risk		Х	Х
Type A: Peak Dose for Specified Distances		Х	Х
Type B: Peak Dose for Specified Spatial Elements		Х	Х
Type C: Land Area Exceeding Dose		Х	
Type D: Land Area Exceeding Concentration		Х	
Type E: Population Movement Across Radius		Х	
Type 9: Breakdown of Long-term Population Dose			Х
Type 10: Economic Cost Measures			Х
Type 11: Maximum Distance for Protective Actions			Х
Type 12: Impacted Area / Population			X
Type 13: Maximum Annual Food Ingestion Dose			X
Type 14: Evacuated and Relocated Population			X



### ATMOSPHERIC DISPERSION AND DEPOSITION Outline

- Meteorological data
- Gaussian plume equations
- Virtual source calculation
- Diffusion parameters
- Plume rise
- Wet and dry deposition
- Off-centerline correction factors
- Atmospheric source term
- Weather sampling
- Plume meander
- Various other models (wind rotation, mixing height model, boundary weather, radioactive decay and ingrowth, weather and source term alignment)





# ATMOSPHERIC DISPERSION

#### Meteorological Data

- User supplies one year's worth of hourly meteorological data in an external file
- Windspeeds generally based on 10 m observations
- Wind directions are defined by the compass sectors of the spatial grid and is given as the direction towards which the wind is blowing
- The plume segment direction is based on observed wind direction at time of release.
- After release, plume segments do not change direction.
- After release, plume segment dispersion changes with observed changes in weather
  - Plume speed changes with windspeed
  - Plume diffusion rate changes with stability class
  - Wet deposition rate changes with rain rate

WINDIR	VINDSPD			
Met Inpt 2012- Added column day hr dispds # 12345678901234 1 1 37 137 1 2 6 147	-3/ srn IST 567 0 # 1	AB RNMM		
1 23 25 305 1 24 26 305	0 0	WINDIR	Wind direction sector #	
5 10 45 85	5 0	WINDSPD	Wind speed	
5 11 45 114	4 0 ISTAB		Stability Class	
5 13 8 274	i o	RNMM	Rain Rate	
5 14 7 253 5 15 5 214 5 16 4 174 5 17 63 109 5 18 9 109	0 4 0 4 0 5 0			



## ATMOSPHERIC DISPERSION

**Gaussian Plume Equations** 

$$\chi(x, y, z) = \frac{Q}{u} \cdot f_G(y) \cdot \psi(z) \quad for \quad z \in [0, H]$$

where

- $\chi(x, y, z)$  is the time-integrated air concentration ( $Bq \cdot s/m^3$ ) at downwind location (x, y, z),
- $Q_0$  is the released activity (*Bq*),
- *u* is the windspeed (*m/s*), as given by the weather data,
- $f_G(y)$  is the Gaussian distribution  $(m^{-1})$  representing lateral dispersion,
- $\psi(z)$  is the vertical distribution ( $m^{-1}$ )
- *H* is the height (*m*) of the capping inversion layer, i.e., the height of the mixing layer



Figure adapted from Figure 3-1 of Turner (1970)



### ATMOSPHERIC DISPERSION Lateral and Vertical Distribution

#### Lateral distribution function

 $f_{G}(y)$ 

All distances:

 $\frac{1}{\sqrt{2\pi}\sigma_{y}}exp\left[-\frac{1}{2}\left(\frac{y}{\sigma_{y}}\right)^{2}\right]$ 

# Vertical distribution function $\psi(z)$

Incomplete vertical mixing, i.e., shorter distances:

$$\frac{1}{\sqrt{2\pi}\sigma_z}\sum_{n=-100}^{100} \left\{ exp\left[ -\frac{1}{2} \left( \frac{z-h+2nH}{\sigma_z} \right)^2 \right] + exp\left[ -\frac{1}{2} \left( \frac{z+h+2nH}{\sigma_z} \right)^2 \right] \right\}$$

Complete vertical mixing, e.g., longer distances  $\psi(z) = \frac{1}{H}$ 

#### Where

 σ<sub>y</sub>(x) is the lateral dispersion parameter representing one standard deviation of the Gaussian distribution (m)

#### Where

- $\sigma_z(x)$  is the vertical dispersion parameter representing one standard deviation of the Gaussian distribution (*m*).
- *h* is the height of the plume centerline (*m*)
- *H* is the height (*m*) of the capping inversion layer, i.e., the height of the mixing layer



### ATMOSPHERIC DISPERSION Virtual Sources

- Basic Gaussian equations assume a point source
- To represent an area source (e.g., to account for initial dispersion due to turbulent wake effects), MACCS computes a "virtual source" distance as shown below:



(reproduced from Fig. 2.2 of NUREG/CR-4691 Vol. 2)

• Also used to ensure continuity of the plume during changes in meteorological conditions, i.e., stability class.



### ATMOSPHERIC DISPERSION Diffusion Parameters

- Diffusion is represented as a function of downwind distance rather than plume travel time
- Diffusion curves may be represented in MACCS by a either power law or by a lookup table.



• Values based on Pasquill-Gifford diffusion curves are commonly used, but user may enter any desired set of diffusion parameter data



### ATMOSPHERIC DISPERSION Surface Roughness Effects on Vertical Scaling

- Users can specify scaling factors, YSCALE and ZSCALE, that act as multipliers on diffusion parameters,  $\sigma_y$  and  $\sigma_z$ , respectively.
- Scaling factors can reflect increased or decreased plume expansion.
- Users commonly use ZSCALE to model increased vertical dispersion  $\sigma_z$  due to surface roughness of terrain:

$$ZSCALE = \left(\frac{z_0}{z_{0,ref}}\right)^q = \left(\frac{z_0}{3 \ cm}\right)^{0.2}$$



# ATMOSPHERIC DISPERSION

#### Plume Rise

- Liftoff criterion
- Plume rise equations calculate:
  - Plume trajectory,  $\Delta h(x)$
  - Total plume rise,  $\Delta h_f$
- Calculated factors that affect plume rise:
  - Buoyancy flux, F
  - Average windspeed,  $\overline{u}$
  - Stability parameter, S
  - Downwind distance where the plume reaches its final rise height, x<sub>f</sub>





## ATMOSPHERIC DISPERSION Buoyant Plume Trapping/Liftoff

- Based on model proposed by Briggs (1973b)
- Plume rise occurs only when the wind speed upon release of the segment is less than a critical wind speed  $u_c$ , which is calculated using the following formula:

$$u_c = \left(\frac{9.09F}{H_b}\right)^{\frac{1}{3}}$$

where

- *H<sub>b</sub>* is the height (*m*) of the building from which the plume escapes (BUILDH), and
- *F* is the buoyancy flux  $(m^4/s^3)$  of the plume segment



### **ATMOSPHERIC DISPERSION** *Plume Trajectory* $\Delta h(x)$

For bent-over plume trajectory  $\Delta h(x)$ , MACCS uses the Briggs "two-thirds law" (Hanna, Briggs, & Hosker, 1982):

$$\Delta h(x) = \frac{1.6F^{\frac{1}{3}}x^{\frac{2}{3}}}{\overline{u}}$$

Where

- $\Delta h(x)$  is the plume rise (*m*), as measured from the initial release height (PLHITE),
- *x* is downwind distance (*m*),
- F is the buoyancy flux  $(m^4/s^3)$  of the plume segment, and
- $\overline{u}$  is the wind speed (*m/s*) averaged between the initial release height and the final plume height ( $h_f$ )



#### ATMOSPHERIC DISPERSION Final Plume Rise $\Delta h_f$

lf

#### Unstable or neutral conditions

(stability classes A through D)

Final plume rise  $\Delta h_f$  based on the work of Briggs (1970):

$$\Delta h_f = \begin{cases} \frac{38.7 \cdot F^{0.6}}{\overline{u}} & if \quad F \ge 55 \, m^4 / s^3 \\ \frac{21.4 \cdot F^{0.75}}{\overline{u}} & if \quad F < 55 \, m^4 / s^3 \end{cases}$$

#### **Stable conditions** (stability classes E or F)

Final plume rise  $\Delta h_f$  depends on the downwind distance  $x_f$  where the plume reaches its final rise height. If  $x_f \leq 1.84 \frac{\bar{u}}{\sqrt{s}}$ ,  $\Delta h_f$  is identical to the formulae used for unstable conditions (stability class A through D)

$$x_f > 1.84 \frac{\bar{u}}{\sqrt{S}}$$
, then:  
 $\Delta h_f = 2.4 \left(\frac{F}{\overline{u}S}\right)^{\frac{1}{3}}$ 

Stability parameters S for classes E and F are  $5.04 \times 10^{-4}$  s<sup>-2</sup> and  $1.27 \times 10^{-3}$  s<sup>-2</sup>, respectively.



## ATMOSPHERIC DEPOSITION

- Radioactivity is removed from plume segments by decay and by deposition of radioactive materials onto the ground. MACCS considers decay and ingrowth in a separate step.
- The amount of material  $\Delta Q_j$  of a given radionuclide that is deposited onto the ground during transport of a plume segment across radial interval *j* is given by the following:

$$\Delta Q_j = Q_j \big( 1 - f_{dj} \cdot f_{wj} \big)$$

#### Where

- $Q_j$  is the amount of radioactive material (*Bq*) that is transported into radial interval *j* by the plume segment,
- $f_{dj}$  is the fraction of material (dimensionless) that would remain in the plume after transport across radial interval *j* if only dry deposition occurred, and
- $f_{wj}$  is the fraction of material (dimensionless) that would remain in the plume after transport across radial interval *j* if only wet deposition occurred.



### ATMOSPHERIC DEPOSITION Dry Deposition

The fraction  $f_d$  of material not removed by dry deposition from transport across a radial interval is a weighted average of each particle size bin *i* (i.e.,  $f_d = \sum_i p_i \cdot f_{di}$ ), where  $f_{di}$  is the following:

$$f_{di} = exp\left[-v_{di} \cdot \psi_0 \cdot \Delta t_{ref}\right]$$

where

- $p_i$  is the fraction of all aerosol materials in particle size bin *i* (PSDIST)
- $v_{di}$  is the dry deposition velocity (*m/s;* VDEPOS)
- $\psi_0^{-1}$  is the ground-level value of the plume distribution in the vertical direction ( $m^{-1}$ ), and
- $\Delta t_{ref}$  is the time (s) required for the reference location (REFTIM) of a plume segment to transverse the radial interval.

The material removed by dry deposition is uniformly deposited along the length of the radial interval.



#### ATMOSPHERIC DEPOSITION Wet Deposition

Wet deposition depends on both precipitation duration and intensity (Brenk and Vogt 1981).

The total fraction  $f_w$  of material not removed by wet deposition from transport across a radial interval is the product of the fractions not removed during period  $\Delta t_1$ ,  $\Delta t_2$ ,  $\Delta t_3$ , ... (i.e.,  $f_w = \prod_i f_{wi}$ ), where  $f_{wi}$  is the following:

$$f_{wi} = 1 - f_{av,i} \cdot \left( 1 - exp\left[ -C_1 \left( \frac{I_i}{I_0} \right)^{C_2} \Delta t_i \right] \right)$$

where

- $f_{av,i}$  is the average fraction (dimensionless) of the plume segment within the radial interval during  $\Delta t_i$ ,
- $\Delta t_i$  is a period (s) during which the plume segment is crossing the radial interval (where  $\sum_i \Delta t_i$  is the duration for the full plume segment to cross both ends of the radial interval),
- $C_1$  is the linear wet deposition coefficient (1/s), as given by the parameter CWASH1
- $C_2^{-}$  is the exponential wet deposition coefficient (dimensionless), as given by the parameter CWASH2,
- $I_i$  is the intensity of precipitation (*mm/hr*), as specified by the weather data, and
- $I_0$  is the unit rain intensity, 1 mm/hr

The material removed by wet deposition is uniformly deposited along the length of the radial interval



### ATMOSPHERIC DISPERSION Standard Off-Centerline Corrections

- ATMOS calculates air and ground concentrations directly along and / or directly under the plume centerline
- Off-centerline correction factors are adjustments to calculate the concentrations in the spatial elements
- EARLY calculations for stationary individuals use fine spatial elements
- CHRONC calculations use coarse spatial elements
- Correction factors are computed for all fine or coarse grid sectors within 2.15 standard deviations of the plume centerline
- MACCS uses special correction factors for evacuees and for cloudshine



Approximation of a Gaussian Distribution by fine grid histogram. (reproduced from Fig. 3.2 of NUREG/CR-4691 Vol. 2)



#### ATMOSPHERIC DISPERSION AND DEPOSITION

#### **QUESTIONS?**

