

Track reconstruction for the Mu3e experiment

DPG Dresden

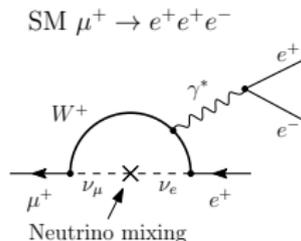
T 127.5 2023-03-23 @ WIL/C129 15:50-16:05

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Mu3e Experiment

Search for charged Lepton Flavor Violation

- Through a decay $\mu^+ \rightarrow e^+e^+e^-$
- Allowed in the Standard Model but not observable ($\text{Br} < 10^{-54}$)
- *Any observation will point to New Physics*



Current experimental status:

- SINDRUM (1988) [Nucl.Phys.B299\(1988\)1](#)
- $\text{Br} < 10^{-12}$ at 90% c.l

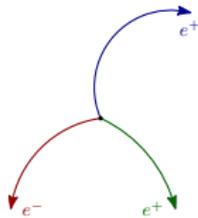
Mu3e aims for sensitivity of $2 \cdot 10^{-15}$ (Phase 1)

- Under construction at Paul Scherrer Institute using existing beam line ($\pi\text{E}5$, $10^8 \mu/\text{s}$)
- Further improve to 10^{-16} (Phase 2) with new beam line (HIMB)

Signal

Signal ($\mu \rightarrow 3e$):

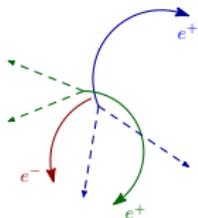
- Decay at rest to two positrons and one electron
 - Common vertex & time
 - Invariant mass: $M_{e^+e^+e^-} = m_\mu$
 - Total (missing) momentum: $\sum \mathbf{p}_e = 0$
- Require good momentum, vertex and time resolution
- Tracks with maximum momentum of 53 MeV/c
 - Large Multiple Scattering (MS) \rightarrow minimize material budget



Background sources

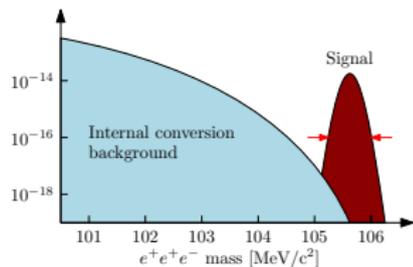
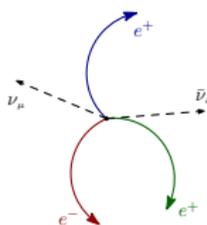
1st - random combinations:

- Overlap of several $\mu^+ \rightarrow e^+ + 2\nu$ and/or e^\pm scattering
- Contribution from *fake* tracks
- Signature: not same vertex, time, etc.

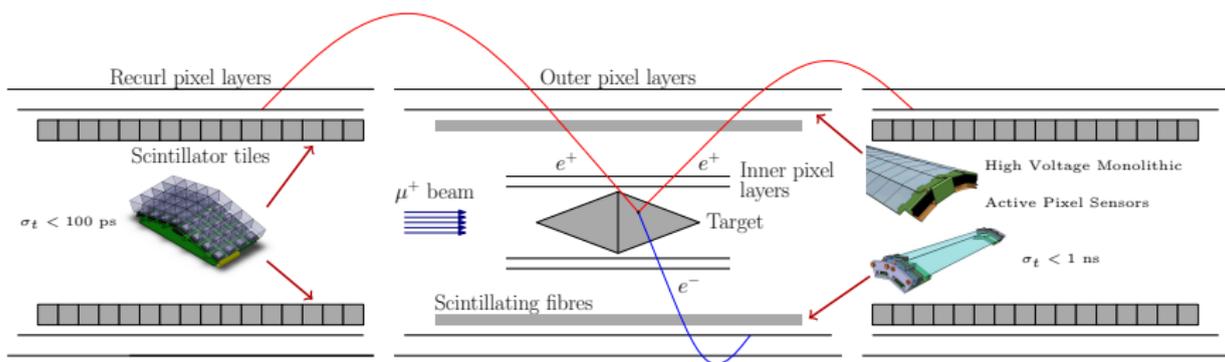


2nd - internal conversion:

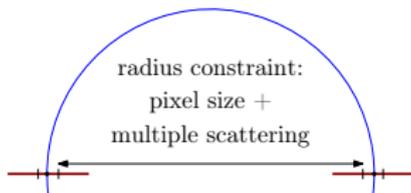
- $\mu^+ \rightarrow e^+e^+e^- + 2\nu$
- Signature: missing momentum & energy



Detector - recurl stations

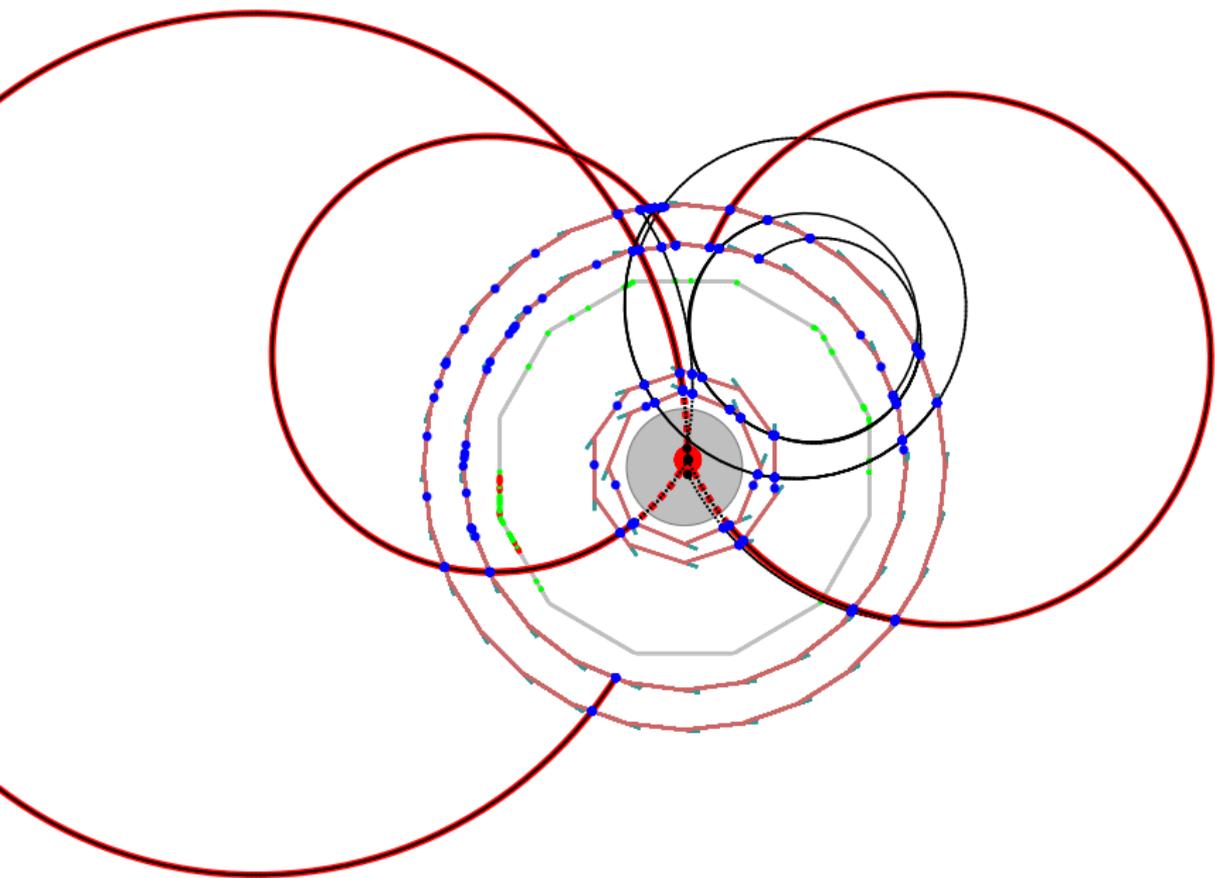


- Muons stop on target and decay at rest
- 4 pixel layers provide hits for track reconstruction
- Particles bend back in magnetic field and measured again, improving momentum resolution



- Two recurl stations to improve acceptance for such particles

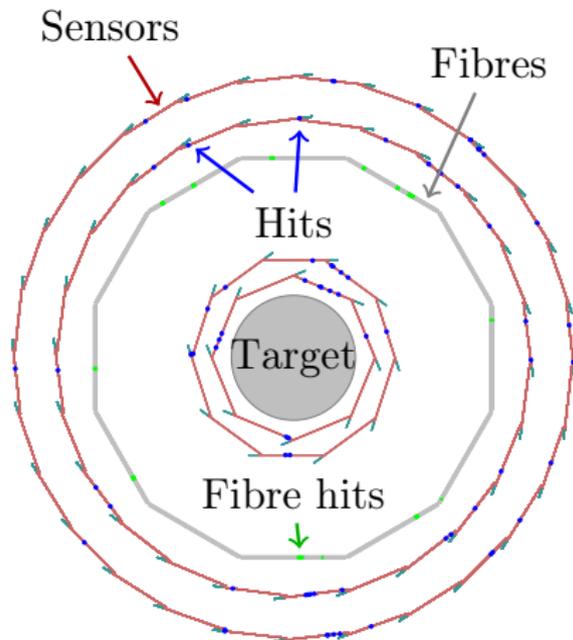
Track reconstruction



Event

$10^8 \mu/s$ stop and decay on target

- Hit rate of 10^9 per second + fibre and & tile hits
- Continuous readout: use time slices of 64 ns as events
- 10-20 hits per layer per event
→ $O(10^3)$ track fits per event
→ 10^{10} track fits each second
- Need fast and efficient track reconstruction

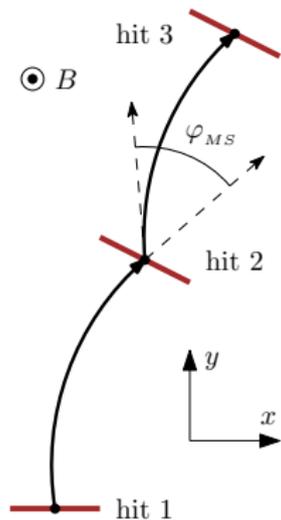


Transverse view (xy-plane)

Triplet fit

Track in magnetic field:

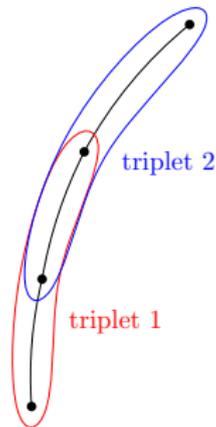
- Described by helical trajectory
- Minimum 3 hits to reconstruct track (triplet)
- Multiple Scattering (MS) in middle point
- One parameter: 3D curvature
→ fit: minimize MS



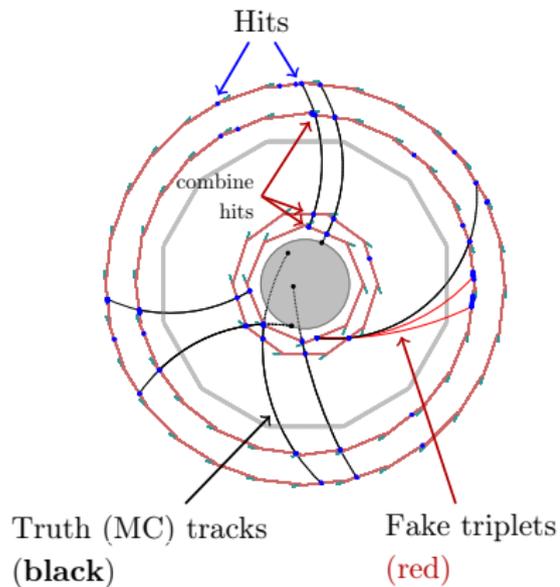
NIM A844(2017)135

Track ($n_{hit} \geq 4$):

- Sequence of triplets
- Minimize combined χ^2
→ weighted average of individual triplets



Reconstruction: from triplets to short tracks

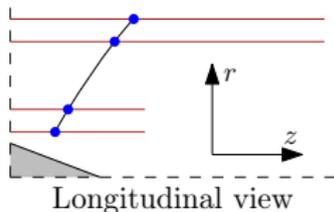


Triplet (3 hits) seeds:

- Combine hits from first 3 layers
- Fake rate $\approx O(1)$ (1 per truth track)

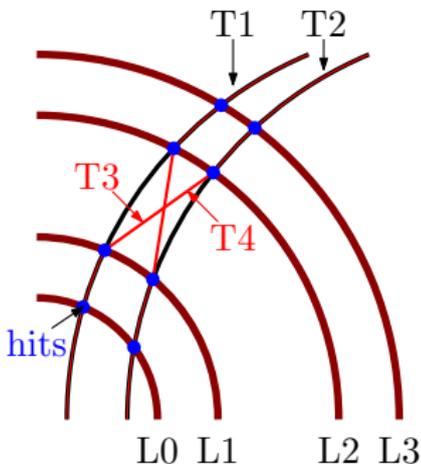
Short (4 hits) tracks:

- Combination of triplet and hit in outer layer
- Fake rate $\approx O(0.1)$



Reconstruction: resolve algorithm

- Some particles can recur several times (10 and more) in central station
- These particles produce a large number of closely packed hits that result in a large number of reconstructed short tracks (**true** and **fake** combinations)
- Need a way to disentangle (resolve) these groups of tracks, otherwise these events/tracks would be unusable



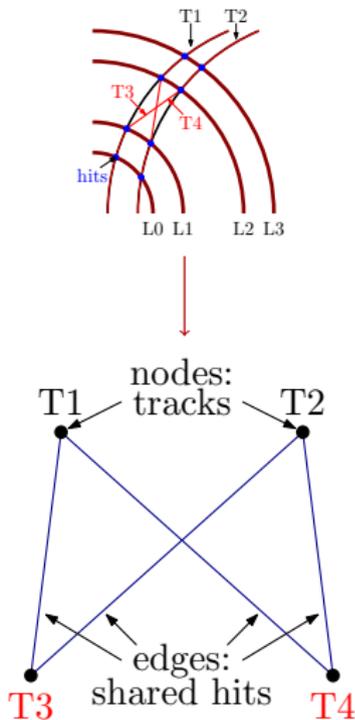
T1 - first recur of particle

T2 - second recur of same particle

T3/T4 - are fake tracks

Reconstruction: resolve algorithm

- The idea is to create graph of connected tracks,
- where each node is a track and edges connect tracks that share hits (intersecting tracks),
- and find largest subset of disconnected nodes (tracks) → standard graph theory exercise

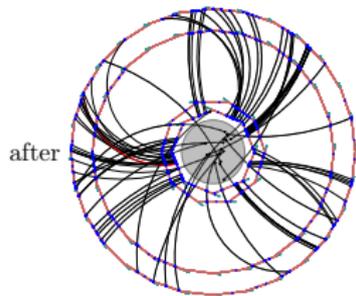
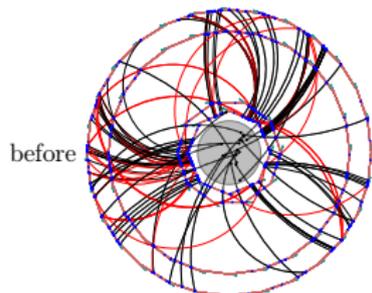


Reconstruction: resolve algorithm

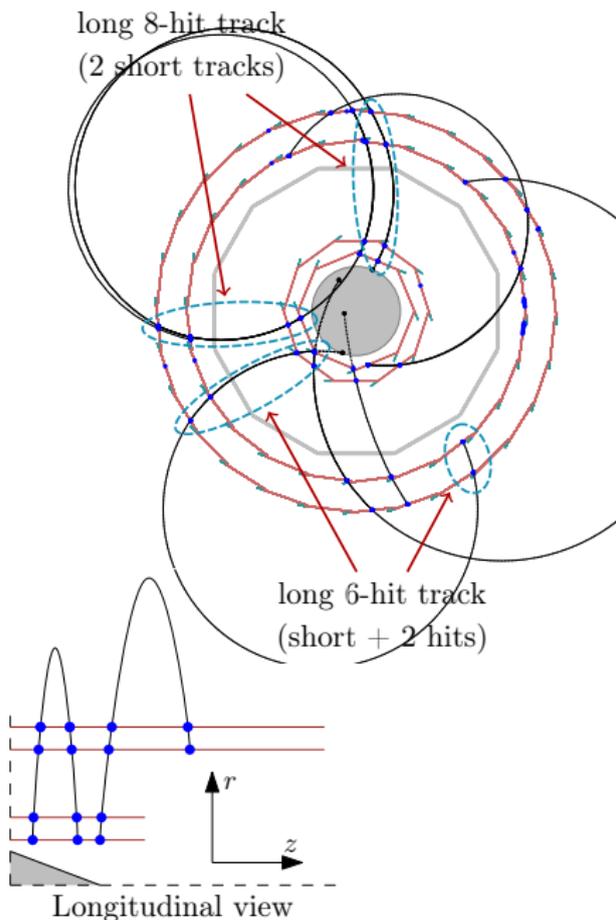
- Exponentially hard algorithm, partially due to unknown number true tracks
- High granularity and efficiency, low noise \rightarrow estimate number of tracks as $N_{hit}/4$

Short track performance:

- Factor 5 reduction in fake rate (from 0.16 to 0.03)
- No efficiency loss (select several sets within distance to minimum χ^2)



Reconstruction: long tracks



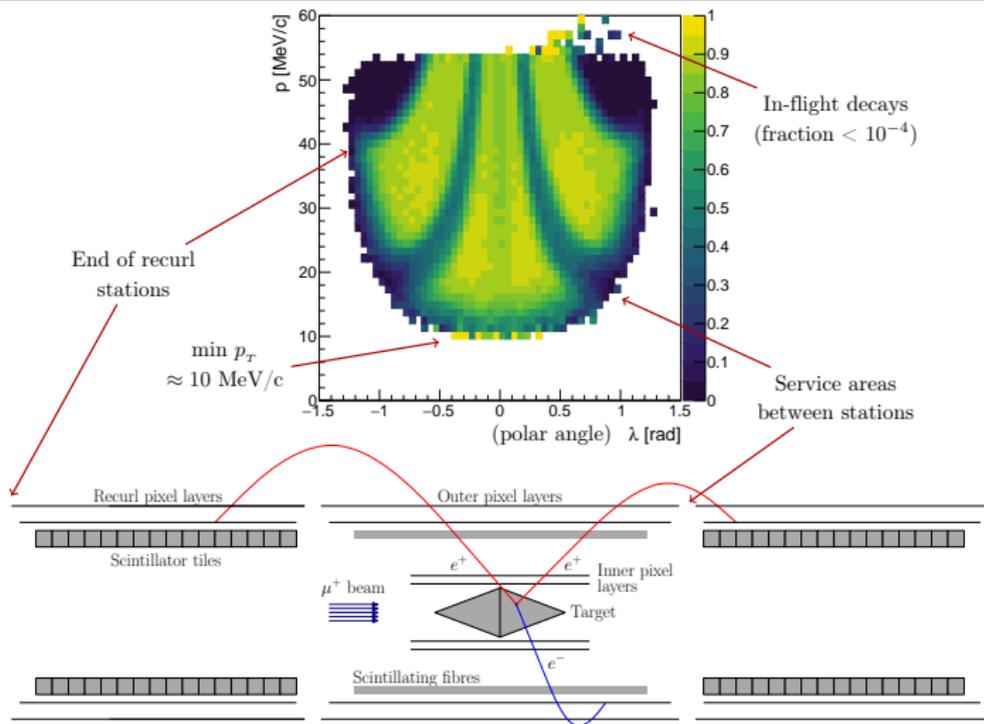
Long 6-hit tracks:

- Combine short track with pair of hits in outer layers

Long 8-hit tracks:

- Combine 2 short tracks with opposite curvature
- Fake rate $\approx O(0.1) - O(1)$ - combination of short tracks from wrong turns
- Direction (charge) ambiguity \rightarrow reconstruct recurl chain

Acceptance and efficiency



- Acceptance: $\epsilon_{acc} \approx 70\%$ (1 hit per layer, $\min p_T$, etc.)
- Short tracks: $\epsilon_{short} \approx 90\% \cdot \epsilon_{acc}$ (χ^2 cut)
- Long tracks: $\epsilon_{long} \approx 70\% \cdot \epsilon_{short}$ (gaps, etc.) \rightarrow analysis

Summary

- Efficient and fast tracks reconstruction is necessary to reach design sensitivity of $2 \cdot 10^{-15}$
- Track reconstruction handles high occupancy and large MS by utilizing knowledge of high efficiency and low noise of the detector, allowing to reconstruct above 90% of particles within detector acceptance with about 2.5% of the fake tracks (at Phase 1)
- For more information see TDR [NIMA 1014 \(2021\), 165679](#)

Backup

Momentum resolution

Short tracks (4 hits)

- $\langle \sigma_p \rangle \approx 1.4 \text{ MeV/c}$
- Depends linearly on momentum

Long tracks (6 and 8 hits)

- $\langle \sigma_p \rangle \approx 0.2 \text{ MeV/c}$ (**min 100 KeV/c**)
 - ($\times 10$ better than short tracks)
- Allows to separate signal from internal conversion decays

