

# Decision making in electricity markets: Bi-level games and stochastic programming

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# Outline

Two decision problems of power producers:

## I. Strategic: Investment & production decision

- Bi-level game with several producers
- Numerical solutions

## II. Operational: Dispatch of pumped-storage hydropower

- Stochastic programming problem
- Exact solution

# Scope of the bi-level game model

- Project for Swiss Federal Office of Energy (2015–2017)
- Aim for the policy maker: Anticipate investment, production and trading decisions of producers in the European electricity market, and especially for Switzerland
- Focus on producers (and not consumers)
- Oligopolistic market (producers can influence prices):
  - Producers can withhold production, or limit investment to drive prices up
  - Producers can invest more what is demanded to deter market entry of other players
  - Market power may be exerted only in some sub-markets (e.g. during peak-hours)
- Complements PSI's energy-system cost-optimization models

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## Is there market power?

“Yes”: EEX market, Jan+Feb 2006, especially at peak-load (Willems, Rumiantesva & Weigt, 2009)

“No”: EEX market, 2007–2010, peak- and base-load (Graf & Wozabal, 2013)

“Less over time”: Spanish market (Moutinho, 2014) Dutch market (Mulder, 2015)

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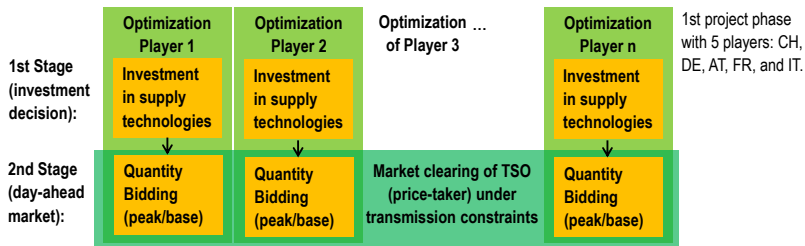
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→ Assumption (first project phase): **Players are countries (CH, DE, AT, IT, FR)**

# Game of investment and of subsequent production

Multi-leader–follower game (Murphy & Smeers, 2005):



i.e., producers first invest (lock-in), then they play Nash-Cournot production game together



# Mean-risk bi-level optimization for each player (producer)

For each player  $i$ :

max expected total profit =

$$\begin{array}{l} \left( \text{profit from selling power} - \text{capital costs} \right) \\ \left. \begin{array}{l} \bullet \text{ capacity} \leq \text{max-capacity,} \\ \bullet \text{ constraint on risk,} \\ \bullet \text{ production-, import-amounts, and prices are given by:} \end{array} \right\} \text{s.t.} \end{array} \quad \begin{array}{l} \text{summed over load-} \\ \text{periods and scenarios} \\ \text{for each technology, e.g.} \\ \text{maximum potential for player } i \\ \text{on total profit} \\ \text{for each load period,} \\ \text{scenario, and player } i' \\ \text{for each technology,} \\ \text{load period, and scenario} \\ \text{for each load period,} \\ \text{and scenario} \end{array}$$

$\left. \begin{array}{l} \text{max total profit of player } i' \\ \text{s.t.} \left\{ \begin{array}{l} \bullet \text{ production}_{i'} \leq \text{capacity}_{i'}, \\ \bullet \text{ price}_{i'} = f_{i'}(\text{production}_{i'} + \text{import}_{i'}) \end{array} \right. \end{array} \right\}$

Currently implemented:

- Financial constraint on risk is relaxed
- Stochastics: 16 demand scenarios (level and elasticity variation)

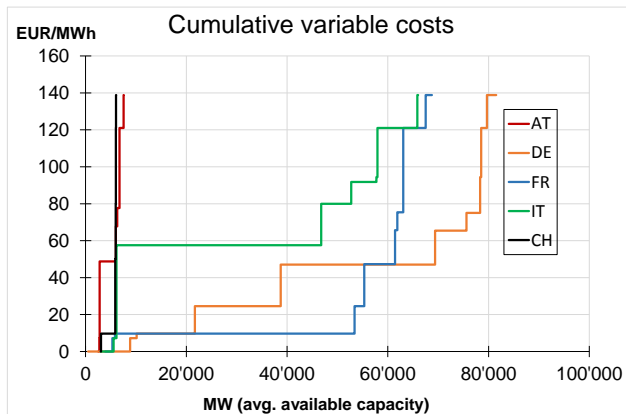
# Optimization for each player $i$ (producer)

- $i \in \mathcal{I}$ : player,  $l \in \mathcal{L}$ : load period,  $\xi \in \Xi$ : scenario,  $|\Xi| < \infty$
- Variables:  $x_i \in \mathbb{R}_+^n$ : investment in  $n$  different technologies,  $y_{il\xi} \in \mathbb{R}$ : total profit,  $q_{il\xi} \in \mathbb{R}_+^n$ : production,  $a_{il\xi} \in \mathbb{R}$ : import,  $p_{il\xi} \in \mathbb{R}$ : price
- $\delta_l$ : length load period,  $x_i^0/x_i^{\max}$ : initial/maximal capacity,  $\beta_i$ : capital costs
- Inverse linear demand function:  $p_{il\xi}^0, b_{il\xi}$ : intercept and slope
- Risk measure Average-Value-at-Risk AVaR $_\alpha$  at level  $\alpha$  and lower bound  $\rho_i$ ;  $\mathbb{E}[\cdot]$ : expected value over the scenarios;  $e := (1 \dots, 1)^\top \in \mathbb{R}^n$

$$\begin{aligned} \max_{x_i} \quad & \sum_{l \in \mathcal{L}} \delta_l \mathbb{E}[y_{il\xi}] \\ \text{s.t.} \quad & \left\{ \begin{array}{l} y_{il\xi} = q_{il\xi}^\top (p_{il\xi} e - c_i) - \beta_i^\top x_i, \\ x_i^0 + x_i \leq x_i^{\max}, \\ \text{AVaR}_\alpha \left[ \sum_{l \in \mathcal{L}} \delta_l y_{il\xi} \right] \geq \rho_i, \\ q_{il\xi}, a_{il\xi}, p_{il\xi} \in \arg \max_{q_{i'l\xi}, a_{i'l\xi}} y_{i'l\xi} \\ \text{s.t.} \quad \left\{ \begin{array}{l} q_{i'l\xi} \leq x_{i'}^0 + x_{i'}, \\ p_{i'l\xi} = p_{i'l\xi}^0 + b_{i'l\xi} \left( q_{i'l\xi}^\top e + a_{i'l\xi} \right), \quad \forall i', l, \xi. \end{array} \right. \end{array} \right. \end{array} \quad \begin{array}{l} e := (1 \dots, 1)^\top \in \mathbb{R}^n \\ \text{market power: } p'_{il\xi}(q_{il\xi}) = b_{il\xi} \end{array}$$

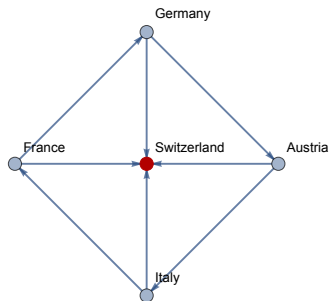
## Assumptions: Price-demand, costs

- Price is linear in demand (data EPEX/GME; 2015, 0h+12h)
- All demand is traded (today: DE/AT 45%, CH 35%, FR 20%)
- New capacity has same costs as existing



- Solar/wind with average availability

# Simple transmission model between countries



- DC flow model (lines have same reactances)
- Aggregated transmission capacity between countries
- No fringe region; no endogenous transmission expansion
- TSO (price-taker) maximizes profit of redistributing electricity; producers are paid locational price
  - Metzler, Hobbs & Pang (2003): (Producers sell to TSO at locational prices)  $\Leftrightarrow$  (Bilateral trading & TSO/arbitrageur is price-taker).

Players may base investment decisions on such simplifications

## Solution method: Players' + TSO's optimizations

In steps 1.→2.→3. because of non-convexities:

1. Social Welfare (SW) maximization problem

- Convex quadratic problem (CPLEX solver)

2. Simplified problem: Investment & production decided together

- Start with solution from 1.
- Linear mixed-complementarity problem (PATH solver)

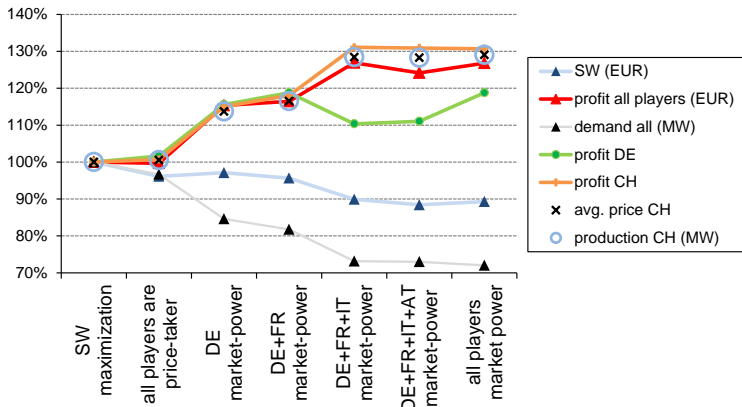
3. Bi-level problem formulated as EPEC (Equilibrium problem with equilibrium constraints)

- Start with solution from 2.
- Solve MPEC (Mathematical program with equilibrium constraints) for each player (MPEC solver of GAMS)
- Diagonalization over the players (Hu & Ralph, 2007): Each MPEC is solved with first-stage decision of other players fixed.  
STOP: numerical convergence in 1st stage decisions

# Preliminary result: Influence of market power

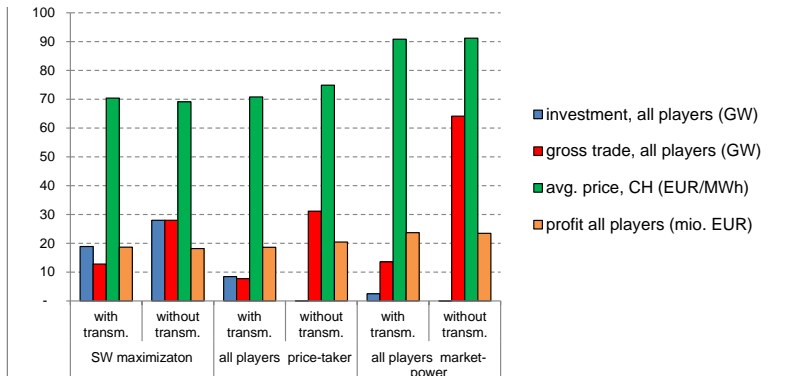
## Assumptions:

- Same price-elasticity scenarios for players
- Existing capacity scaled down to 50% (because of today's overcapacity in Europe)



FR cannot exert market power; if DE/IT has market-power, CH exports

# Preliminary result: Influence of transmission constraints



- Investments: SW > price-taker > market-power
- Removable of transmission constraints:
  - Case SW: Production where cheapest (DE lignite)
  - Case market-power: More trade, but not higher profits

## II: Operational decisions of producers

- Usually much more focused: Exogenous electricity prices, single player etc.
- Easier problem formulations possible? For example: **Is there a simple dispatch problem with an analytical solution?**



## Single-period (steady-state) pumped-storage

- $S$ : electricity spot price (EUR/MWh), random variable
- $U^\pm$ : control function of turbined/pumped water (MWh)
- $c \in (0, 1)$ : efficiency of pumping
- Capacity, usable expected water in reservoir:  $u_{\max}^+ > l > 0$
- Constraint on water-level is in expectation, and a lower reservoir is neglected

$$\begin{aligned} \max_{u^\pm} \quad & \mathbb{E} \left[ SU^+ - \frac{1}{c} SU^- \right] \\ \text{s.t.} \quad & \begin{cases} \mathbb{E}[U^+ - U^-] \geq l, \\ 0 \leq U^\pm \leq u_{\max}^\pm. \end{cases} \end{aligned}$$

Optimal solution:

$$U^+ = u_{\max}^+ 1_{\{S \geq q\}}, \quad U^- = u_{\max}^- 1_{\{S \leq cq\}},$$

$$q \text{ given by: } u_{\max}^+ \mathbb{P}[S \geq q] - u_{\max}^- \mathbb{P}[S \leq cq] = l$$

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# Conclusions

## I. Game-theoretic investment & market model





- Solution procedures (MPEC solver of GAMS; diagonalization over the players) yields economically reasonable local solutions
- Preliminary results: Player 'Switzerland' profits
  - from market power of other players,
  - not much from a removal of transmission constraints
- More careful evaluation of assumptions and of data needed

## II. Exact solutions of simple problems

- May serve as building blocks in large-scale models
- Help to understand the basic mechanisms

**Collaboration is very welcome!**

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